

# Applied Econometric Time Series – Problem Set 4

Dominik R. Wehr  
Due: Mar 6th 3:15PM

February 12, 2024

## 1 Error correction

### Preliminaries

Consider the bivariate error correction system

$$\Delta r_{St} = \alpha_S(r_{Lt-1} - \beta r_{St-1} - \mu) + a_{1,11}\Delta r_{St-1} + a_{1,12}\Delta r_{Lt-1} + \epsilon_{St} \quad (1.1)$$

$$\Delta r_{Lt} = \alpha_L(r_{Lt-1} - \beta r_{St-1} - \mu) + a_{1,21}\Delta r_{St-1} + a_{1,22}\Delta r_{Lt-1} + \epsilon_{Lt} \quad (1.2)$$

where  $r_{St} \sim I(1)$  and  $r_{Lt} \sim I(1)$ , and  $\epsilon_{St}$  and  $\epsilon_{Lt}$  are white noise processes.

**Question (1a)** Argue why  $r_{St}$  and  $r_{Lt}$  must be co-integrated. What is the co-integrating vector? What is the long-run equilibrium? Why is an intercept  $\mu$  included in the co-integrating relationship? In which case should the restrictions  $\alpha_S\mu = 0$  and  $\alpha_L\mu = 0$  be imposed?

**Question (1b)** Formulate the null hypothesis that  $r_{Lt}$  does not Granger cause  $r_{St}$ .

**Question (1c)** Describe the adjustment mechanisms towards the long-run equilibrium. Also, describe the adjustment mechanisms toward the long-run equilibrium assuming that  $r_{Lt}$  is weakly exogenous. What is the role of  $\Delta r_{St-1}$  and  $\Delta r_{Lt-1}$  terms?

**Question (1d)** Assume that  $r_{St} \sim I(1)$  and  $r_{Lt} \sim I(1)$  (as before) but not cointegrated. Why is it a problem to run the regression  $r_{St} = \mu + \beta_1 r_{Lt} + \epsilon_t$ ? Are there any cures for spurious regressions?

## 2 Empirical exercise

Do Exercise 4 (but not 4f) in the textbook (page 402).