# Modely farieb

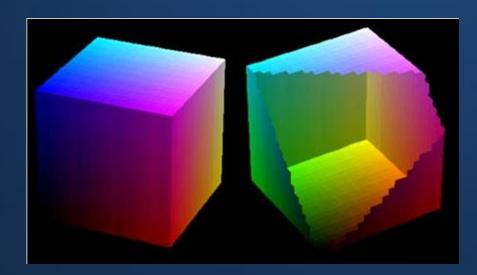
#### **MODELY FARIEB**

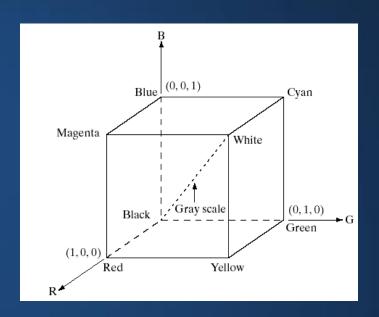
- HW orientované:
- RGB, CMYK, televízne normy
- Užívateľsky orientované:
- HLS, HSV, HSI
- Vnemovo rovnomerné (perceptually uniform):
- CIE Lab, Luv, WUV
- Iné:
- XYZ, oponent, TSV, LUX, YES, ...

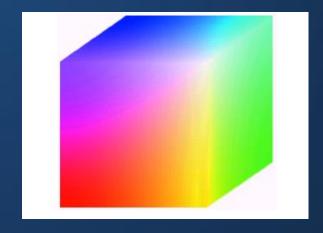
# **RGB**

Najznámejší model Používaný v monitoroch Farebné svetlá

Hodnoty R,G,B  $\in \langle 0, 1 \rangle$ Kocka



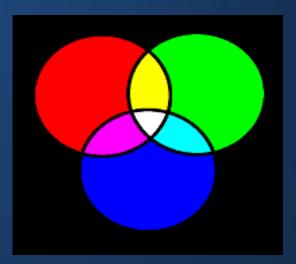




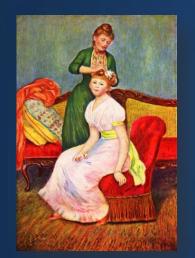
# **RGB**

Aditívne skladanie farieb: čím viac farieb zložíme, tým je výsledok svetlejší (spočítava sa ich intenzita).

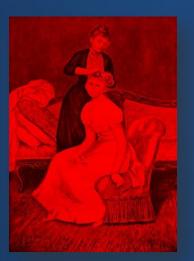
- Veľa rôznych modelov RGB
- Každý ma iné hodnoty základných farieb užívateľovi obvykle nedostupné
- TV spoločnosti si určili hodnoty základných farieb RGB podľa použitých technológií



# RGB PRÍKLAD



Original



Red Band



Green Band



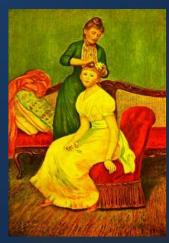
Blue Band



No Red



No Green



No Blue

### **MODELY RGB**

CIE RGB – E

NTSC – pôvodne C, teraz D65

EBU (European Broadcast Union) – Calebo D65

CCIR (Comité Consultatif International des Radiocommunications) – D65 ITU-R BT.709 standard

SMPTE (Society of Motion Picture and Television Engineers) – D65

Medzinárodná dohoda pre HDTV ITU-R BT.709 standard

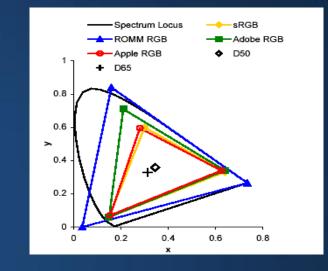


TABLE 3.5-2. XYZ Chromaticity Coordinates of Standard Primaries

| Standard |                  | х        | у        | Z        |
|----------|------------------|----------|----------|----------|
| CIE      | $R_C$            | 0.640000 | 0.330000 | 0.030000 |
|          | $G_{\mathbb{C}}$ | 0.300000 | 0.600000 | 0.100000 |
|          | $B_C$            | 0.150000 | 0.06000  | 0.790000 |
| NTSC     | $R_N$            | 0.670000 | 0.330000 | 0.000000 |
|          | $G_N$            | 0.210000 | 0.710000 | 0.080000 |
|          | $B_{\mathbf{N}}$ | 0.140000 | 0.080000 | 0.780000 |
| SMPTE    | $R_S$            | 0.630000 | 0.340000 | 0.030000 |
|          | $G_{\mathbb{S}}$ | 0.310000 | 0.595000 | 0.095000 |
|          | $B_{\mathbf{S}}$ | 0.155000 | 0.070000 | 0.775000 |
| EBU      | $R_E$            | 0.640000 | 0.330000 | 0.030000 |
|          | $G_E$            | 0.290000 | 0.60000  | 0.110000 |
|          | $B_{\mathrm{E}}$ | 0.150000 | 0.060000 | 0.790000 |
| CCIR     | $R_R$            | 0.640000 | 0.330000 | 0.030000 |
|          | $G_R$            | 0.30000  | 0.600000 | 0.100000 |
|          | $B_R$            | 0.150000 | 0.060000 | 0.790000 |

### $RGB \rightarrow XYZ$

# Lineárna transformácia

Súradnice základných farieb

Súradnice bieleho bodu

$$\begin{bmatrix} a(1) \\ a(2) \\ a(3) \end{bmatrix} = \begin{bmatrix} x_R & x_G \\ y_R & y_G \\ z_R & z_G \end{bmatrix} \begin{bmatrix} x_W/y_W \\ 1 \\ z_W/y_W \end{bmatrix}$$

$$\begin{bmatrix} M(1,1) & M(1,2) & M(1,3) \\ M(2,1) & M(2,2) & M(2,3) \\ M(3,1) & M(3,2) & M(3,3) \end{bmatrix} = \begin{bmatrix} x_R & x_G & x_B \\ y_R & y_G & y_B \\ z_R & z_G & z_B \end{bmatrix} \begin{bmatrix} a(1) & 0 & 0 \\ 0 & a(2) & 0 \\ 0 & 0 & a(3) \end{bmatrix}$$

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} M_{1,1} & M_{1,2} & M_{1,3} \\ M_{2,1} & M_{2,2} & M_{2,3} \\ M_{3,1} & M_{3,2} & M_{3,3} \end{bmatrix} \cdot \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$





RGB R

G

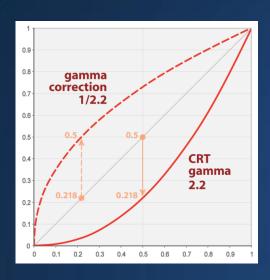
B





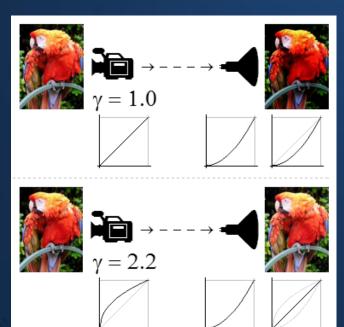


- Lineárne RGB
  - lineárna transformácia z XYZ
  - vnemovo neuniformný
  - Device independent
- Nelineárne RGB
  - lineárne RGB pomocou gamma korekcie -> nelineárne RGB
  - Obrazovky CRT
  - Device dependent



### **GAMA KOREKCIA**

- γ reprezentuje numerický parameter vyjadrujúci nelinearitu reprodukcie intenzity svetla
- CRT nelineárne
  - Intenzita svetla reprodukovaného na monitore je nelineárna funkcia napätia



NTSC  $\gamma = 2.2$ 



### **RGBA**

RGBA- α kanál, informácia o priehľadnosti, akým pomerom sa farba mieša s pozadím.

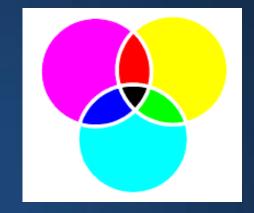
Používa sa napríklad v OpenGL

 $\alpha$  = 1 perfektne nepriesvitné  $\alpha$  = 0 úplne priehľadné  $0 < \alpha < 1$  rôzne úrovne priesvitnosti

Blending je miešanie rôznych farieb: zdroja a miesta určenia

Priesvitný – čiastočne prepúšťajúci svetlo

### **CMY**



Farebné filtre

Farba telies - farby sa ukladajú na seba, svetlo musí prejsť vrstvami (filtrami) a odraziť sa od podkladu

Komplementárny model k RGB:

$$C = 1 - R$$

$$M = 1 - G$$

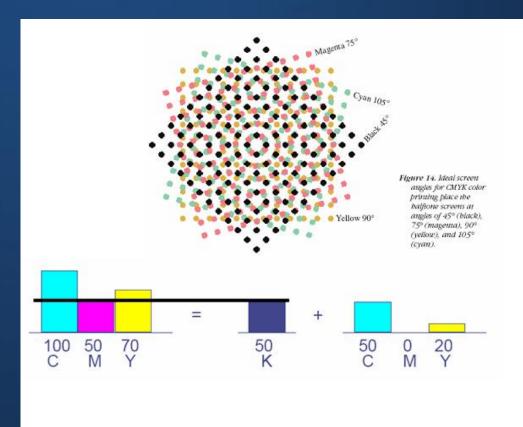
$$Y = 1 - B$$

Subtraktívne skladanie farieb pridávaním pigmentu tvorí tmavšiu farbu

#### **CMYK**

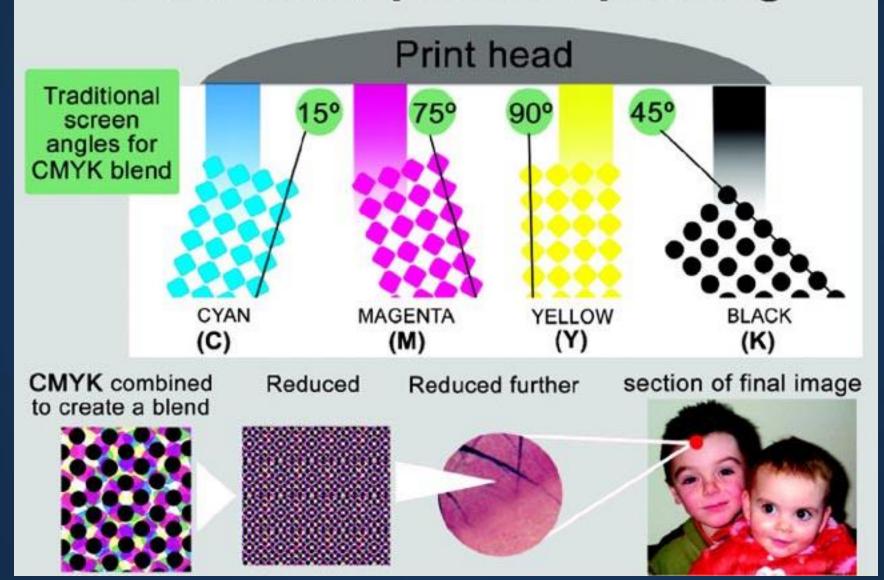
Pri tlači sa používa CMYK (blacK)
Nemusia sa tlačiť 3 farby na seba - ušetrí sa na drahých farebných náplniach
Čierna sa tlačí samostatne

CMYK (K, blacK)  $K^* = min(1-R, 1-G, 1-B)$   $C = 1 - R - uK^*$   $M = 1 - G - uK^*$   $Y = 1 - B - uK^*$   $K = bK^*$  $0 \le u, b \le 1$ 





# Four color process printing



# Four color process separations

Separating an image into the four process colors



#### **MODELY FARIEB "TRIEDY Y"**

Televízne a video štandardy

YIQ - NTSC

YUV - PAL

YCbCr – digital video

YPbPr – analógová TV

YCC – Kodak



Farebná zložka oddelená od jasovej (Y) Farebná zložka: zeleno/červený kanál modro/žltý kanál

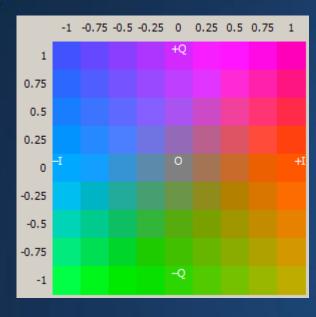
Vo všeobecnosti:

$$Y' = 0.299R' + 0.587G' + 0.114B'$$

$$C_1 = a_1(R' - Y') + b_1(B' - Y')$$

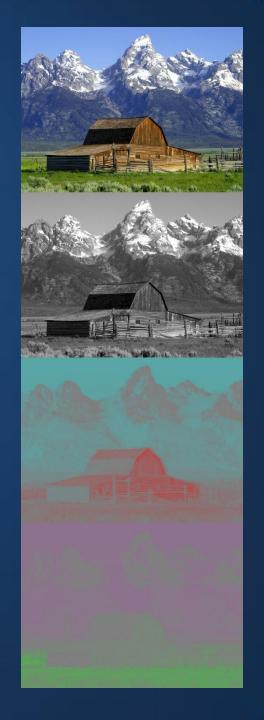
$$C_2 = a_2(R' - Y') + b_2(B' - Y'),$$

$$\begin{bmatrix} Y' \\ C_1 \\ C_2 \end{bmatrix} = M * \begin{bmatrix} R' \\ G' \\ B' \end{bmatrix}$$



### YIQ

- Y luma
- I in-phase, (orange-blue range)
- Q quadrature (purple-green range)
- 1950 NTSC štandard
- kompatibilita s jednofarebným TV
- väčšia šírka pásma pre Y ako pre I Q.
- oddelená jasová zložka manipulácia bez ovplyvnenia farebnej zložky (histogram equalization)
- vnemovo neuniformné Euklidovská vzdialenosť nefunguje
- Gama korekcia aplikovaná na lineárny RGB, vážený súčet nelineárnych komponentov RGB -> luma Y



#### **YUV - PAL**

Podobne ako YIQ YUV vzorkovacie formáty 4:4:4, 4:2:2, and 4:2:0

### Y U V – vypočítané z RGB s gama korekciou (R G B)

Y'= 0.299\*R' + 0.587\*G' + 0.114\*B'

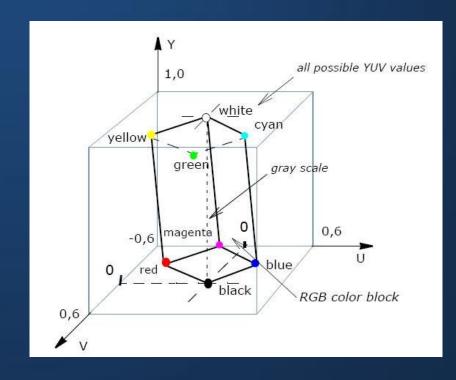
U'=0.492\*(B'-Y')

V'=0.877\*(R'-Y')

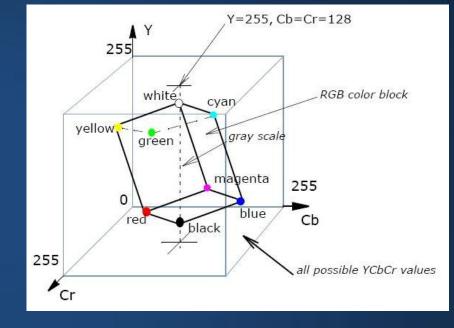
R' = Y' + 1.140\*V'

G' = Y' - 0.394\*U' - 0.581\*V'

B' = Y' + 2.032\*U'



# YCbC, a YCCK



- YCbCr component digital video
- Popísané v štandarde ITU-R BT.601
- YCbCr je škálovaná a posunutá verzia YUV
- Y'Cb'Cr' vypočítané z RGB s gama korekciou (R G B)
- YCCK špeciálne pre JPEG kompresiu obrazu
- Je variáciou YCrCb modelu s pridaným K (black) kanálom

# LINEÁRNE VZŤAHY

| Color space | Matrix/cefficients   |  |  |  |  |
|-------------|--|--|--|--|--|
| $YC_bC_r$   | $\begin{bmatrix} 0.299 & 0.587 & 0.114 \\ -0.168736 & -0.331264 & 0.5 \\ 0.5 & -0.418668 & -0.081312 \end{bmatrix}$                      |  |  |  |  |
| YCC         | $\begin{bmatrix} 0.299 & 0.587 & 0.114 \\ -0.299 & -0.587 & 0.886 \\ 0.701 & -0.587 & -0.114 \end{bmatrix}$                              |  |  |  |  |
| YIQ         | $\begin{bmatrix} 0.299 & 0.587 & 0.114 \\ 0.59597799 & -0.27417610 & -0.32180189 \\ 0.21147017 & -0.52261711 & 0.31114694 \end{bmatrix}$ |  |  |  |  |
| YUV         | $a_1 = 0$ $b_1 = 1/2.03$<br>$a_2 = 1/1.14$ $b_2 = 0$   |  |  |  |  |

Polárne súradnice

$$Hue = \tan^{-1}\left(\frac{C_2}{C_1}\right)$$

$$Saturation = \sqrt{C_1^2 + C_2^2}.$$

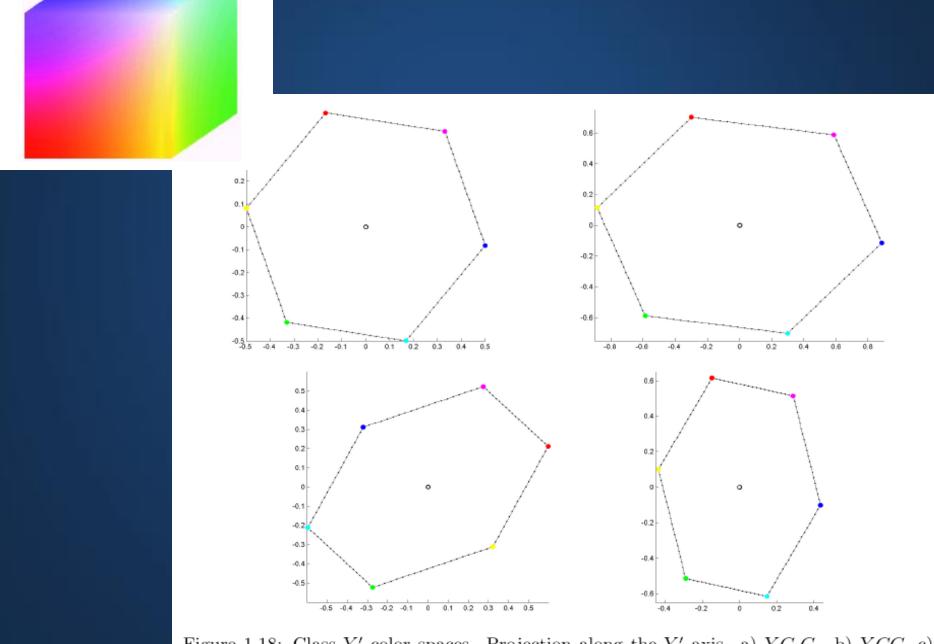


Figure 1.18: Class Y' color spaces. Projection along the Y' axis. a)  $YC_bC_r$ , b) YCC, c) YIQ, d) YUV.

# YIQ



| Color space    | Color<br>mixing | Primary parameters                                       | Used for                                  | Pros and cons              |
|----------------|-----------------|--|---|----------------------------|
| RGB            | Additive        | Red,<br>Green, Blue                                      |   | Easy but wasting bandwidth |
| СМҮК           | Subtractive     | Cyan, Magenta,<br>Yellow, Black                          | Printer                                   | Works in pigment mixing    |
| YCbCr<br>YPbPr | additive        | Y(luminance),<br>Cb(blue chroma),<br>Cr(red chroma)      | Video encoding,<br>digital camera         | Bandwidth efficient        |
| YUV            | additive        | Y(luminance),<br>U(blue chroma),<br>V(red chroma)        | Video encoding<br>for NTSC, PAL,<br>SECAM | Bandwidth efficient        |
| YIQ            | additive        | Y(luminance),<br>I(rotated from U),<br>Q(rotated from V) | Video encoding<br>for NTSC                | Bandwidth efficient        |

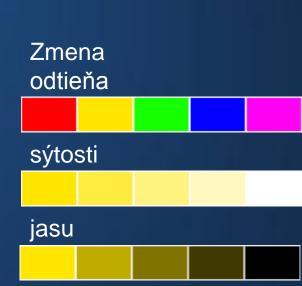
## **UŽÍVATEĽSKY ORIENTOVANÉ MODELY**

Analógia s maliarskym pohľadom (odtieň, sýtosť, jas)

Vhodné pre vizualizáciu (color maps)

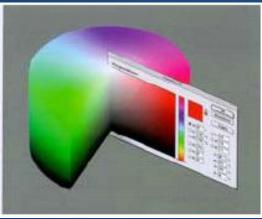
Nelineárny prevod z/do RGB

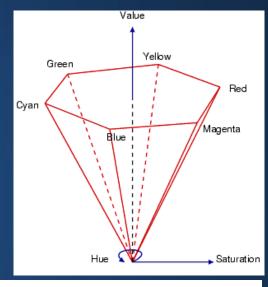
Tvar: kužeľ (aj dvojitý), ihlan, niekedy valec

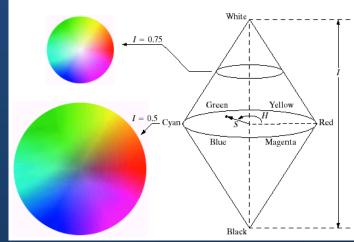


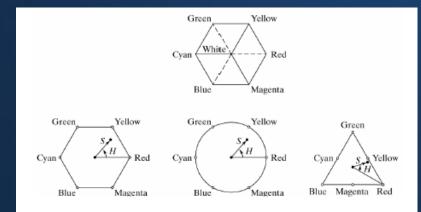
### **TVARY**

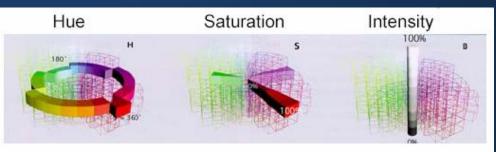












### $RGB \rightarrow HSV$

max(R,G,B)min(R,G,B)

V = max

S = (max-min)/max  $A = \pi/3(max-min)$ 

H = (G-B)A

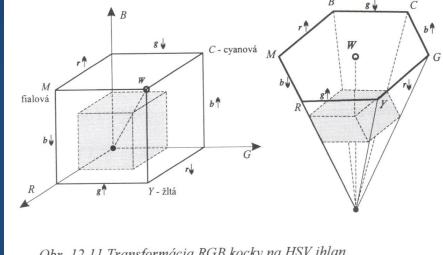
(B-R)A

(R-G)A

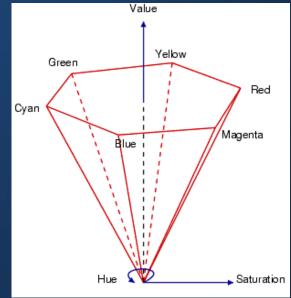
ak max = R

ak max = G

ak max = B



Obr. 12.11 Transformácia RGB kocky na HSV ihlan



ak max = 0, S nie je definovaná ak R = G = B, H nie je definovaná

### **HSV** → **RGB**

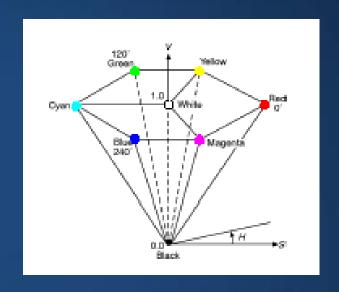
```
I = floor(3H/\pi)

f = H-I

p = V(1-S)

q = V(1-Sf)

t = = V(1-S(1-f))
```



[R G B] = [V t p] 
$$ak I = 0$$
  
[q V p]  $ak I = 1$   
[p V t]  $ak I = 2$   
[p q V]  $ak I = 3$   
[t p V]  $ak I = 4$   
[V p q]  $ak I = 5$   
[0 0 0]  $ak S = 0$ 

# **HSV PLANES**



### $RGB \rightarrow HSI$

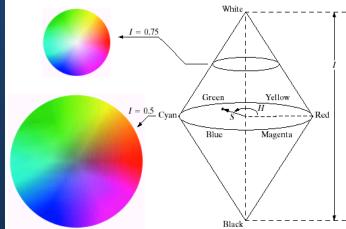








H – normalizácia do  $\langle 0,1 \rangle$ : H/360 ak R = G = B, H nie je definovaná ak I = 0, S nie je definovaná



### **HSI** → **RGB**

### Záleží na tom, v ktorom sektore leží H

RG sektor  $(0^0 \le H \le 120^0)$ :

$$b = \frac{1}{3}(1 - S)$$

$$r = \frac{1}{3}\left[1 + \frac{S\cos(H)}{\cos(6\theta^0 - H)}\right]$$

$$g = 1 - (r + b)$$

*GB* sektor  $(120^{0} \le H \le 240^{0})$ :

$$H = H - 120^{0}$$

$$g = \frac{1}{3} \left[ 1 + \frac{S \cos(H)}{\cos(60^{0} - H)} \right]$$

$$r = \frac{1}{3} (1 - S)$$

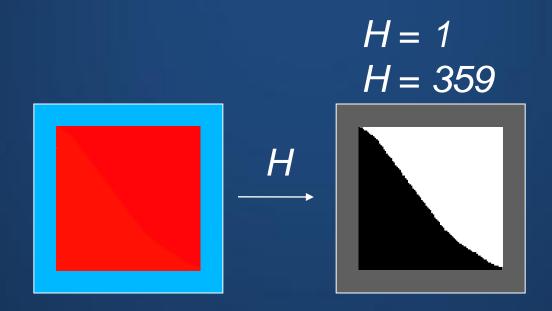
$$b = 1 - (r + b)$$



*BR* sektor  $(240^{0} \le H \le 360^{0})$ :

$$g=rac{1-S}{3}, \qquad b=rac{1}{3}\left[1+rac{S\cos H}{\cos(60-H)}
ight], \qquad r=1-g-b$$

# PROBLÉM?



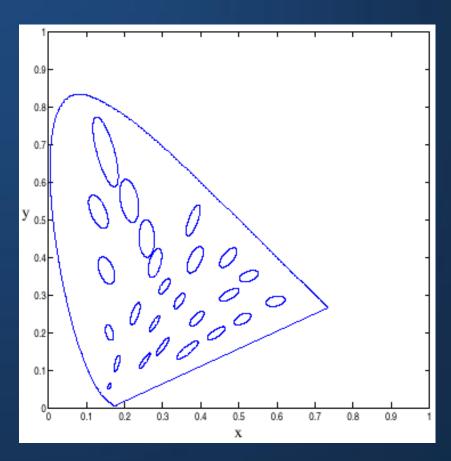
### McAdamove elipsy

V doteraz spomínaných modeloch:

Euklidovská vzdialenosť farieb nezodpovedá

vizuálnej "vzdialenosti"

McAdamove elipsy v xy – pre pozorovateľa nerozlíšiteľné farby



## **CIE UVW**

Lineárna aproximácia vnemovo rovnomerného priestoru

$$\begin{bmatrix} \mathsf{U} \\ \mathsf{V} \\ \mathsf{W} \end{bmatrix} = \begin{bmatrix} 0.66 & 0 & 0 \\ 0 & 1 & 0 \\ -0.5 & 1.5 & 0.5 \end{bmatrix} \begin{bmatrix} \mathsf{X} \\ \mathsf{Y} \\ \mathsf{Z} \end{bmatrix}$$

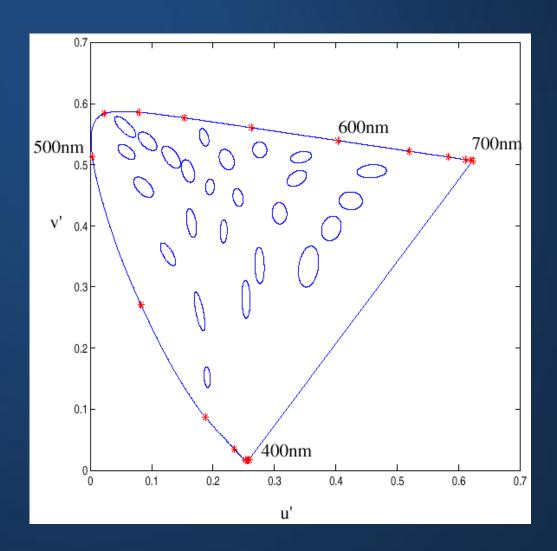
Nerieši problém úplne

→ nelineárne transformácie

# CIE YU'V'

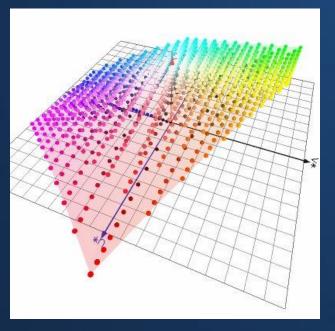
$$u' = \frac{4X}{X+15Y+3Z}$$

$$v' = \frac{9Y}{X+15Y+3Z}$$



### CIE L\*U\*V\*

L\* - jas u\*, v\* - farebné súradnice n – súradnice bieleho bodu



$$L^* = \begin{cases} 116 \left(\frac{Y}{Y_n}\right)^{\frac{1}{3}} - 16 & \text{ak } \frac{Y}{Y_n} > 0.008856 \\ 903.3 \frac{Y}{Y_n} & \text{ak } \frac{Y}{Y_n} \le 0.008856 \end{cases}$$

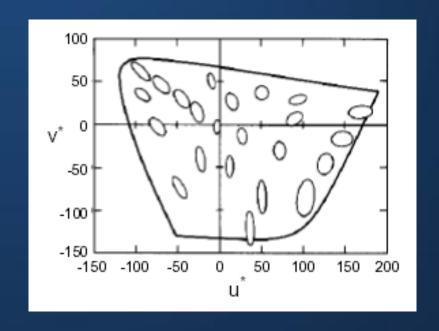
$$u^* = 13L^*(u'-u'_n)$$
  
 $v^* = 13L^*(v'-v'_n)$ 

### CIE L\*U\*V\*

Polárne súradnice Farebnosť Odtieň (u,v>0)

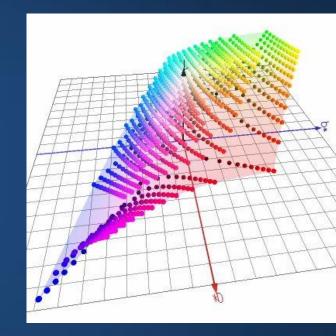
$$C = \sqrt{u^2 + v^2}$$
 $h_v = \operatorname{arc} t_u^2 = 1$ 

McAdamove elipsy



### CIE L\*A\*B\*

L\* - jas výpočet ako pri CIE L\*u\*v\* a\*, b\* - farebné súradnice n – súradnice bieleho bodu Používaný v priemysle

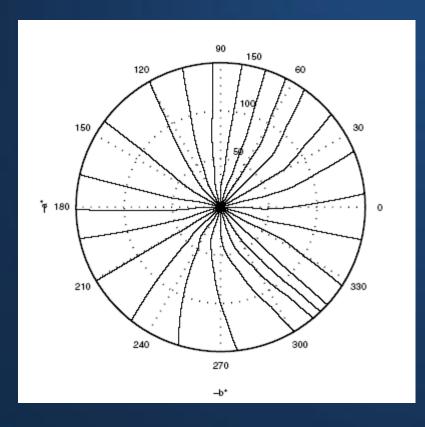


$$a^* = 500 \left( f \left( \frac{X}{X_n} \right) - f \left( \frac{Y}{Y_n} \right) \right)$$
$$b^* = 200 \left( f \left( \frac{Y}{Y_n} \right) - f \left( \frac{Z}{Z_n} \right) \right)$$

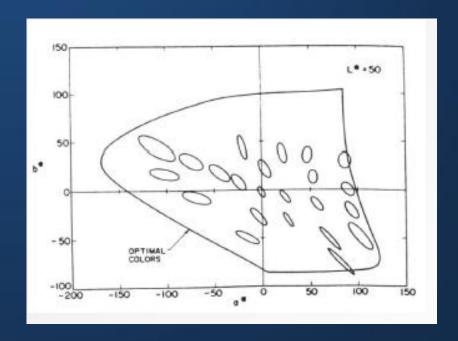
$$f(t) = \begin{cases} t^{\frac{1}{3}} & \text{ak } t > 0.008856 \\ 7.787t + \frac{16}{116} & \text{ak } t \le 0.008856 \end{cases}$$

### CIE L\*A\*B\*

# Polárne súradnice Farebnosť Odtieň (a,b>0)







# **VZDIALENOSŤ FARIEB**

### Euklidovská vzdialenosť

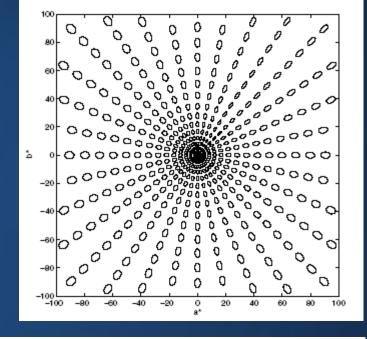
CIE L\*a\*b\*



# CIE L\*u\*v\* podobne

| $\Delta E_{Lab}^*$ | Effect                      |
|--------------------|-----------------------------|
| < 3                | Not perceptible             |
| 3 < 6              | Perceptible, but acceptable |
| > 6                | Not acceptable              |

# **VZDIALENOSŤ FARIEB**



$$\Delta E = \sqrt{\left(\frac{\Delta L^*}{k_L S_L}\right)^2 + \left(\frac{\Delta C^*}{k_C S_C}\right)^2 + \left(\frac{\Delta H^*}{k_H S_H}\right) + R_T \phi(\Delta C^* \Delta H^*)}$$
(1.43)

where  $k_{\nu}$ ,  $k_{c}$ ,  $k_{H}$  = positive, real-valued scaling parameters chosen based on the application where the formula is used

 $S_{L}$ ,  $S_{C}$ ,  $S_{H}$  = lightness-, chroma-, and hue-dependent scaling functions, respectively

 $R_T$  = an additional scaling function that depends on chroma and hue

# **NEKORELOVANÉ MODELY**

Farebné zložky (vo väčšine modelov)

- korelované (medzi sebou a najmä s jasovou zložkou)
- s malou varianciou (nízkou možnosťou diskriminácie objektov)

Nové modely, kde zložky nie sú korelované

# **NEKORELOVANÉ MODELY**

K<sub>1</sub>K<sub>2</sub>K<sub>3</sub> - Karhunen-Loeve transformácia (výpočtovo náročná, kovariančná matica, vlastné vektory, ...) Dátovo závislá – pre každý obrázok treba novú transformačnú maticu

$$\begin{bmatrix} K_1 \\ K_2 \\ K_3 \end{bmatrix} = \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \\ m_{31} & m_{32} & m_{33} \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

# INÉ FAREBNÉ MODELY

$$T = \arctan(r'/g')/\pi + 1/2$$

$$r'=(r-1/3)$$

$$S = [9/5(r'^2 + g'^2)]^{1/2}$$

$$g' = (g - 1/3)$$

$$V \quad = \quad (R+G+B)/3,$$

#### "Modrá = 0"

$$T = \begin{cases} \arctan(r'/g')/2\pi + 1/4 & g' > 0 \\ \arctan(r'/g')/2\pi + 3/4 & g' < 0 \\ 0 & g' = 0 \end{cases}$$

$$S = [9/5(r'^2 + g'^2)]^{1/2}$$

$$L = 0.299R' + 0.587G' + 0.114B',$$

#### "uhlový" model

$$\begin{bmatrix} I \\ v_1 \\ v_2 \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \\ \frac{-1}{\sqrt{6}} & \frac{-1}{\sqrt{6}} & \frac{2}{\sqrt{6}} \\ \frac{1}{\sqrt{6}} & \frac{-1}{\sqrt{6}} & 0 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

$$L(x) = 105 \log_{10}(x + 10) + 100 \log_{$$

$$H = \arctan\left\{\frac{V_2}{V_1}\right\}$$

$$S = (V_1^2 + V_2^2)^{1/2}$$

#### 111213 (Ohta) – oponent model lineárna transformácia

$$I_1 = (R + G + B)/3$$
  
 $I_2 = R - G$   
 $I_3 = B - \frac{R + G}{2}$ .

#### Log oponent model

$$\begin{split} L(x) &= 105 \log_{10}(x+1+n) \\ I &= L(G) \\ R_g &= L(R) - L(G) \\ B_y &= L(B) - \frac{L(G) + L(R)}{2}, \end{split}$$

$$L = (R+1)^{0.3}(G+1)^{0.6}(B+1)^{0.1} - 1$$

$$U = \begin{cases} \frac{M}{2} \frac{R+1}{L+1} & R < L \\ M - \frac{M}{2} \frac{L+1}{R+1} & otherwise \end{cases}$$

$$X = \begin{cases} \frac{M}{2} \frac{B+1}{L+1} & B < L \\ M - \frac{M}{2} \frac{L+1}{B+1} & otherwise, \end{cases}$$

contrast enhancement logarithmic image processing

$$\hat{U} = \begin{cases} 256 \frac{G}{R} & R > G \\ 255 & otherwise. \end{cases}$$

$$\begin{bmatrix} Y \\ E \\ S \end{bmatrix} = \begin{bmatrix} 0.253 & 0.684 & 0.065 \\ 0.5 & -0.5 & 0 \\ 0.25 & 0.25 & -0.5 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

XEROX – IR imagery

Table 1.3. Color Model

| 0.3.0        |                      |                       |
|--------------|----------------------|-----------------------|
| Color System | Transform (from RGB) | Component correlation |
| RGB          | _                    | highly correlated     |
| R'G'B'       | non linear           |                       |
| XYZ          | linear               | correlated            |
| YIQ          | linear               | uncorrelated          |
| YCC          | linear               | uncorrelated          |
| I1I2I3       | linear               | correlated            |
| HSV          | non linear           | correlated            |
| HSI          | non linear           | correlated            |
| HLS          | non linear           | correlated            |
| L*u*v*       | non linear           | correlated            |
| L*a*b*       | non linear           | correlated            |
| Munsell      | non linear           | correlated            |

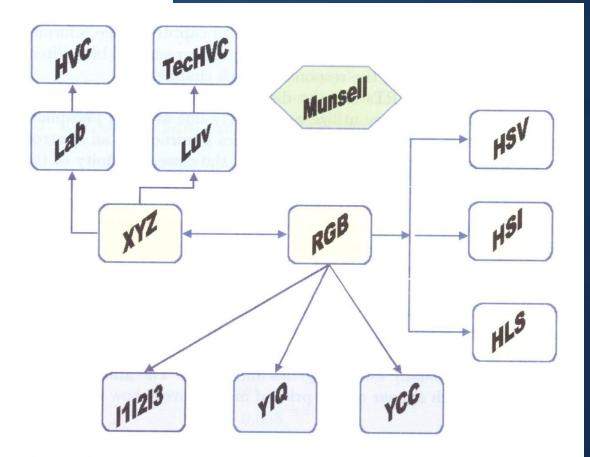
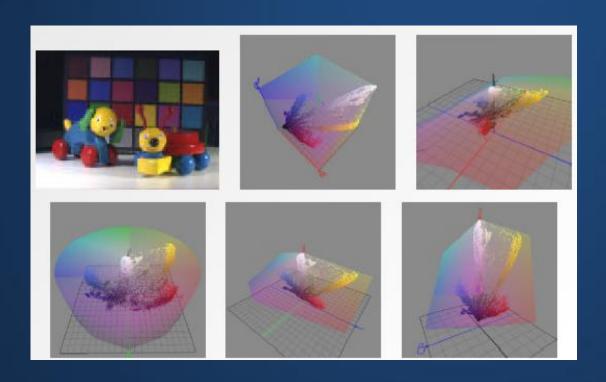
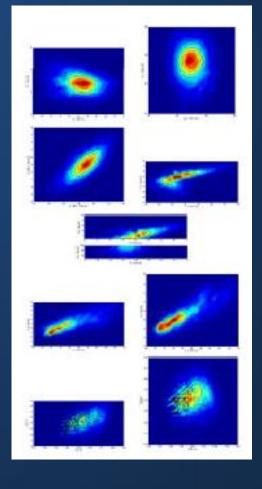


Fig. 1.16. A taxonomy of color models

### POUŽITIE MODELOV



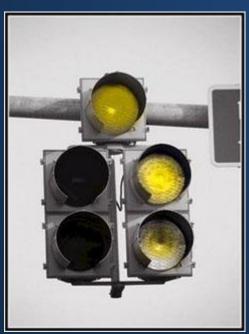
# Ľudské tváre



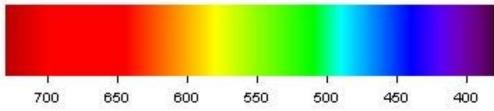
### **FARBOSLEPOTA**

- porucha farbocitu (genetická alebo získaná)
   Ku genetickým patria
- Dichromázia jeden typ čapíkov chýba
  - 1. protanope nevidí červenú Daltonizmus,
  - 2. deuteranope nevidí zelenú,
  - 3. tritanope nevidí modrú Protanopia a deuteranopia = červeno-zelená slepota 8% mužov a 0.5% žien
- Anomálna trichromázia
  - Znížená citlivosť jedného typu čapíkov => Posunuté vnímanie farieb
- Monochromázia nerozlišuje farby vôbec

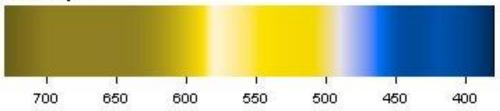




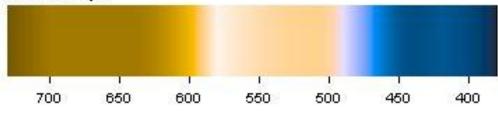




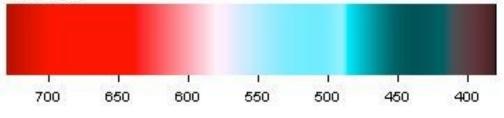
#### Protanopia



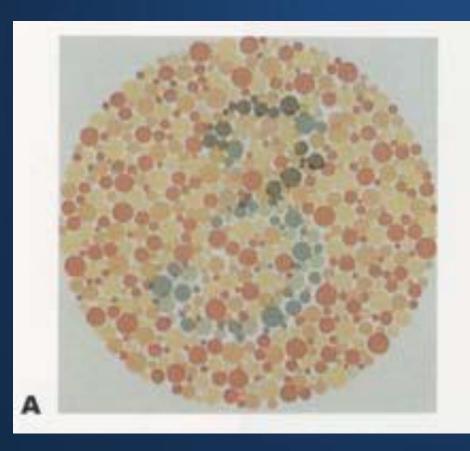
#### Deuteranopia

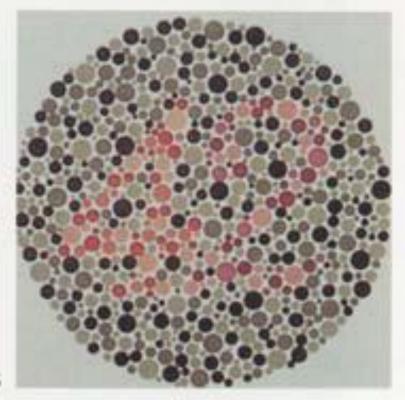


#### Tritanopia



# **TEST FARBOSLEPOTY**



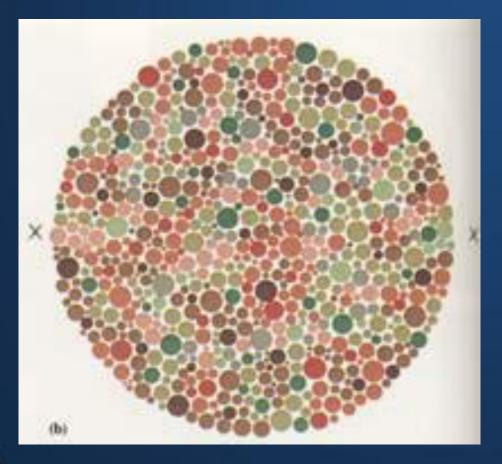


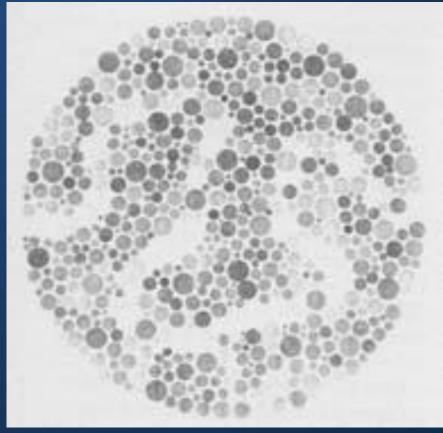
В

### **TEST FARBOSLEPOTY**

# Bludisko v intenzite farieb

viditeľné len pre farboslepých







Meryon (a colorblind painter), Le Vaisseau Fantôme