



# julia – A pragmatic approach to scientific computing

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**Mini symposium: Modern software tools for modern statistics**

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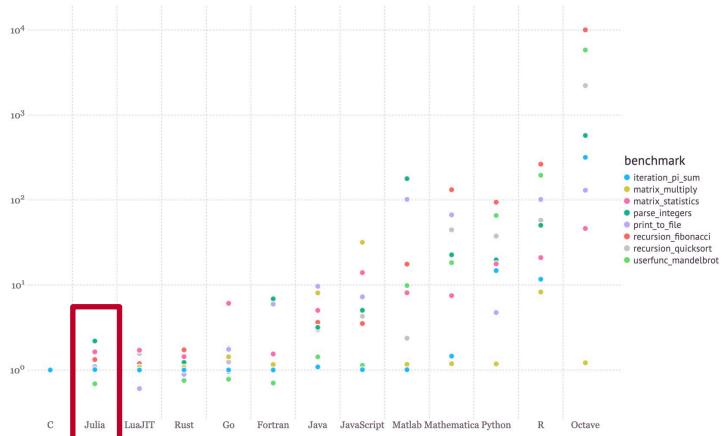
## Hello, Quarto

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# ...so why Julia?



- Fast yet easy to learn with a syntax similar to R and Python
- Everything is pure Julia
- Easy interfaces to other languages



- Young language with a smaller user community
- Less training material
- Less mature package ecosystem

Two screenshots of the Stack Overflow website. The top screenshot shows the results for the tag [python], with a total of 2,007,511 questions. The bottom screenshot shows the results for the tag [julia], with a total of 10,849 questions. Both pages include a search bar, navigation links for Home, PUBLIC, Questions, Tags, Users, and Companies, and a 'Ask Question' button.

# Julia doesn't constrain your thinking

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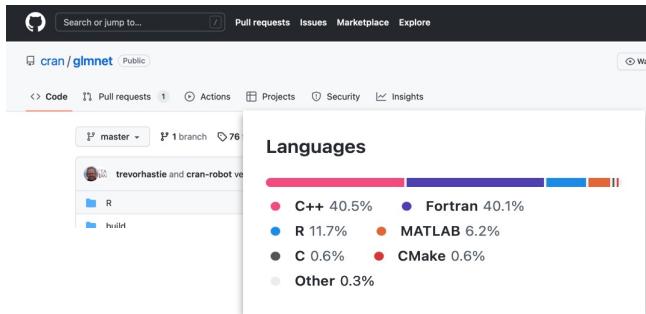
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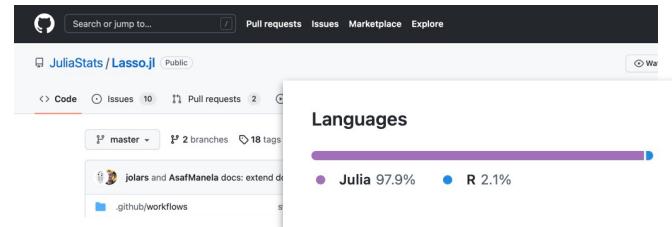
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## Julia: come for the syntax, stay for the speed

Researchers often find themselves coding algorithms in one programming language, only to have to rewrite them in a faster one. An up-and-coming language could be the answer.



- Complex algorithms can be implemented in the language itself



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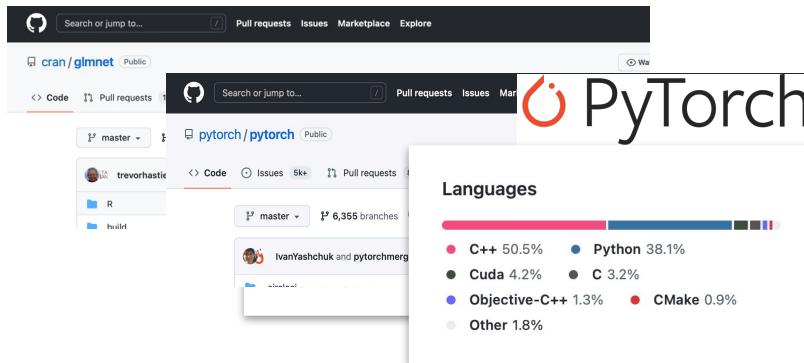
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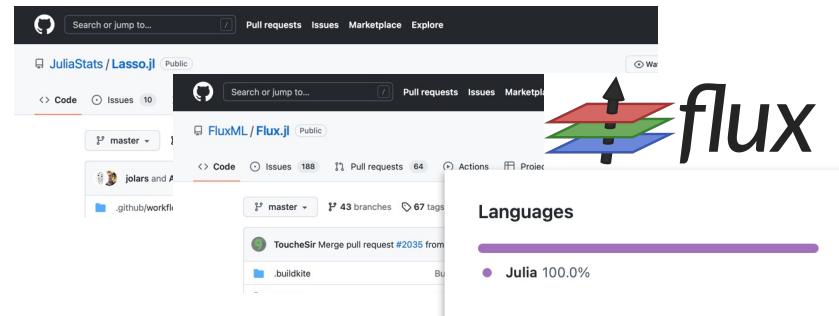
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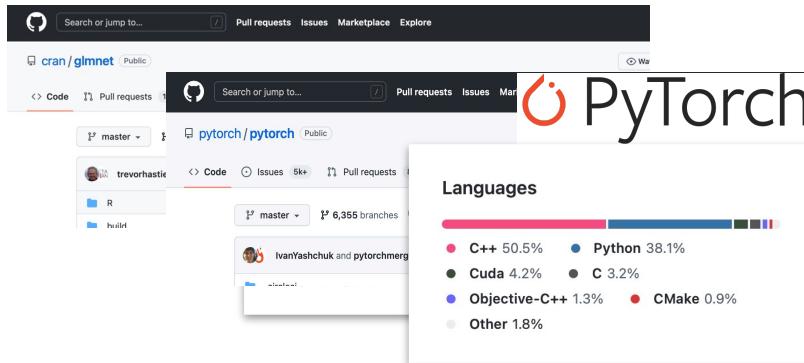
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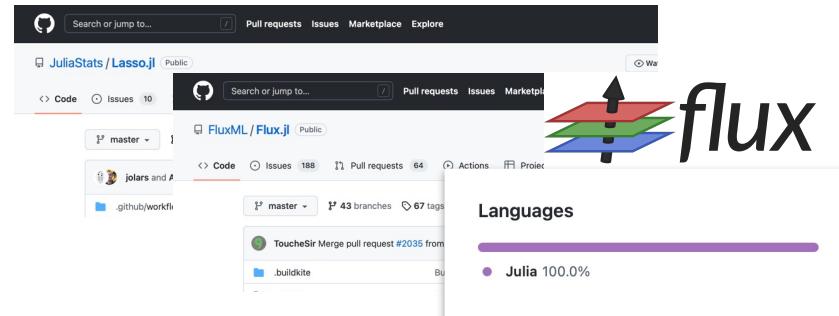
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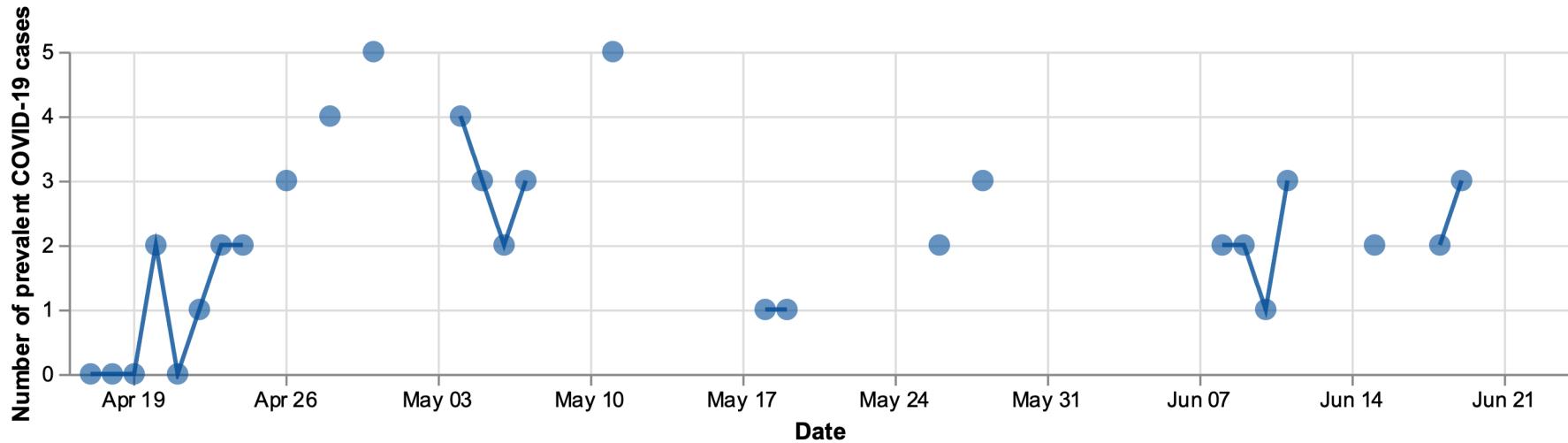
- Complex algorithms can be implemented in the language itself
- Modification of existing libraries is easy, enabling faster prototyping and methods development
- No “legacy characteristics”



# Modelling challenge I: Predict COVID-19 ICU demand

## Missing data in the “Intensivregister”

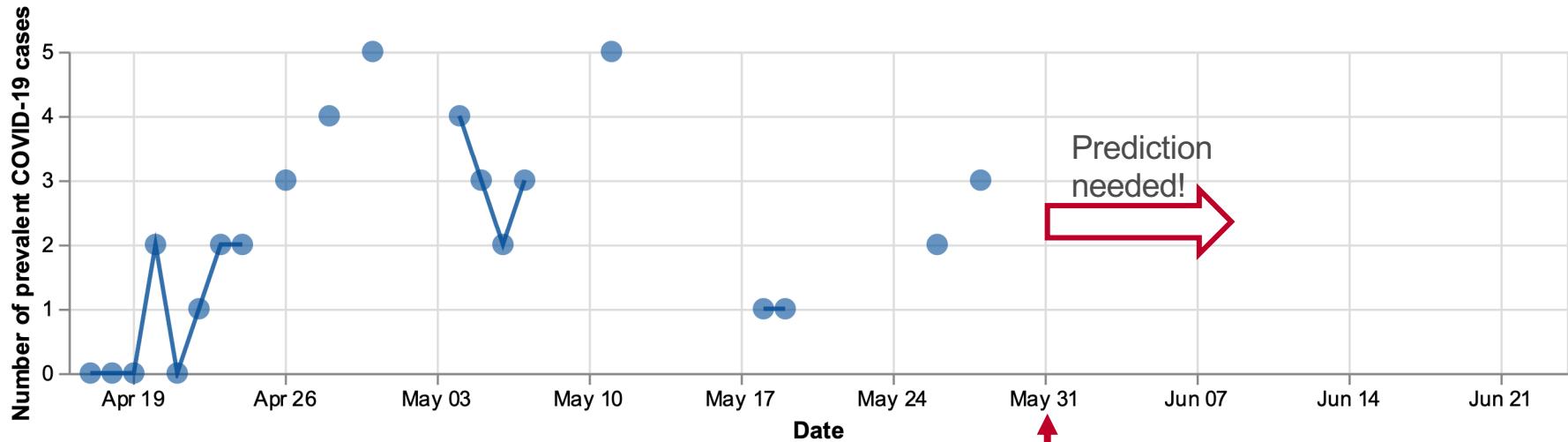
- 63% of all hospitals have missing daily reports
- 7% of hospitals with more than 25% missing daily reports



# Modelling challenge I: Predict COVID-19 ICU demand

## Missing data in the “Intensivregister”

- 63% of all hospitals have missing daily reports
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# A model to predict increments of daily cases

For each hospital:

- Linear model of the increments

$$\widehat{dy}_{t+1} = (y_{t+1} - y_t) = \beta_1 + \beta_2 \cdot y_t + \beta_3 \cdot z_t, \quad t = 2, \dots, T.$$

current ICU cases

newly infected COVID-19 cases in the county

- Accounting for missing daily reports

$$\widehat{dy}_{t+1} = \beta_1 + \beta_2 \cdot \tilde{y}_t + \beta_3 \cdot z_t, \text{ where } \tilde{y}_t = \begin{cases} y_t, & \text{if } y_t \text{ was observed,} \\ \tilde{y}_{t-1} + \widehat{dy}_t, & \text{else.} \end{cases}$$

- A non-linear optimisation problem

$$\begin{aligned}\widehat{dy}_{t+1} &= \beta_1 + \beta_2 \cdot \tilde{y}_t + \beta_3 \cdot z_t \\ &= \beta_1 + \beta_2 \cdot (\tilde{y}_{t-1} + \widehat{dy}_t) + \beta_3 \cdot z_t \\ &= \beta_1 + \beta_2 \cdot (\tilde{y}_{t-1} + (\beta_1 + \beta_2 \cdot \tilde{y}_{t-1} + \beta_3 \cdot z_{t-1})) + \beta_3 \cdot z_t\end{aligned}$$

# Defining a loss function and optimising with Zygote

```
function loss(y, z, reported, β)
    sqerror = 0.0 # squared error
    firstseen = false # set to true after skipping potential missings
    lastcur = 0.0 # prevalent cases from previous time point
    contribno = 0.0 # number of non-missing observations
    for t=1:length(y)
        # skip missings at the start until first reported value
        if !firstseen
            if reported[t] == true # first non-missing observation encountered:
                firstseen = true
                last_y = y[t]
            else
                continue
            end
        else # make a prediction for current increment:
            pred_dy = β[1] + β[2] * last_y + β[3] * z[t-1]
            if reported[t] == true # if current time point is observed:
                dy = y[t] - last_y
                sqerror += (dy - pred_dy)^2
                contribno += 1.0
                last_y = y[t]
            else # if value at current time point is missing:
                last_y += pred_dy
            end
        end
    end
    return sqerror/contribno # return MSE over all observed time points
end
```

→ If you can program it,  
you can estimate the  
model parameters

\*as long as the function is differentiable

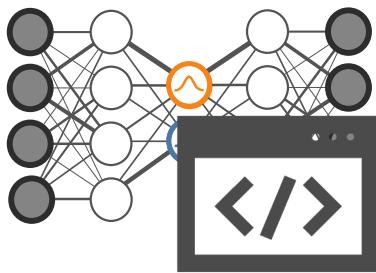
# Differentiable programming for flexible model building

Machine Learning

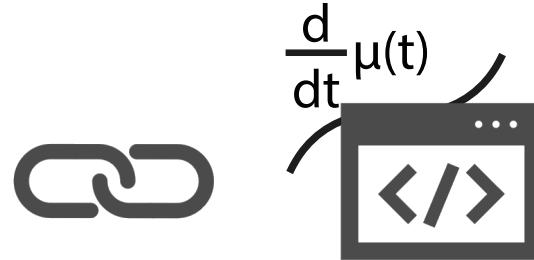
Scientific Computing

 TensorFlow  
 PyTorch

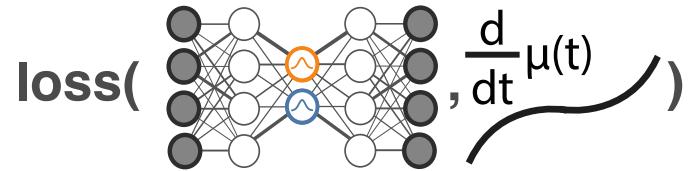
write as a  
computer program



$$\frac{d}{d \text{loss}} \text{loss}$$



$$\frac{d}{d \frac{d}{dt} \mu(t)} \text{loss}$$



optimise via automatic  
differentiation



# Engineering trade-offs in automatic differentiation tools



- Graph-building system in static sub-language: efficient but less flexible
- Tape-based method: unrolls all control flow
- Overhead partly compensated by highly efficient kernels for machine learning applications
- Source-to-source transformation
- Supports full dynamism
  - E.g., straightforward differentiation through ODE solvers
  - Supports user-defined structs and recursion
- Keeps control flow intact



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            else # if value at current time point is missing:
                last_y += pred_dy
            end
        end
    end
    return sqerror/contribno # return MSE over all observed time points
end
```

→ If you can program it,  
you can estimate the  
model parameters



```
using Zygote

β = [0.0; 0.0; 0.0]
for steps in 1:nsteps
    ∇loss = gradient(arg -> loss(y, z, r, arg), β)[1]
    β = .-= η .* ∇loss
end
```

\*as long as the function is differentiable

# Results: Comparing prediction performance

Prediction model	Sum of squared error over all hospitals
Zero model	86.0
Mean model	89.24
Modified mean model	84.34
LOCF + regression	181.07
Increment model	74.75

$$\widehat{dy}_T^{\text{zero}} := 0$$

$$\widehat{dy}_T^{\text{modmean}} := \begin{cases} 0, & \text{if } (y_{T-1} - y_{T-2}) = 0, \\ \widehat{dy}_T^{\text{mean}}, & \text{else.} \end{cases}$$

$$\widehat{dy}_T^{\text{mean}} := \frac{1}{T-2} \sum_{t=2}^{T-1} (y_t - y_{t-1})$$

$$\widehat{dy}_T^{\text{linreg}} := \beta_1 + \beta_2 \cdot \tilde{y}_t + \beta_3 \cdot z_t \text{ where } \tilde{y}_t = \begin{cases} y_t, & \text{if } y_t \text{ was observed,} \\ \tilde{y}_{t-1}, & \text{else.} \end{cases}$$

# Modelling challenge II: Learn disease trajectories of patients with spinal muscular atrophy



## Baseline characterisation

- age
- SMA subtype
- ...



Latent health status

$$\frac{d}{dt} \mu(t) = ?$$

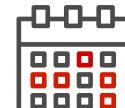
Explicit model



Subgroup-specific local models



Heterogeneity

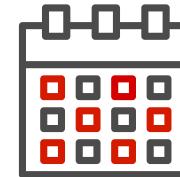


Irregular time points



RULM  
HFMSE

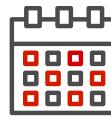
Different motor function tests



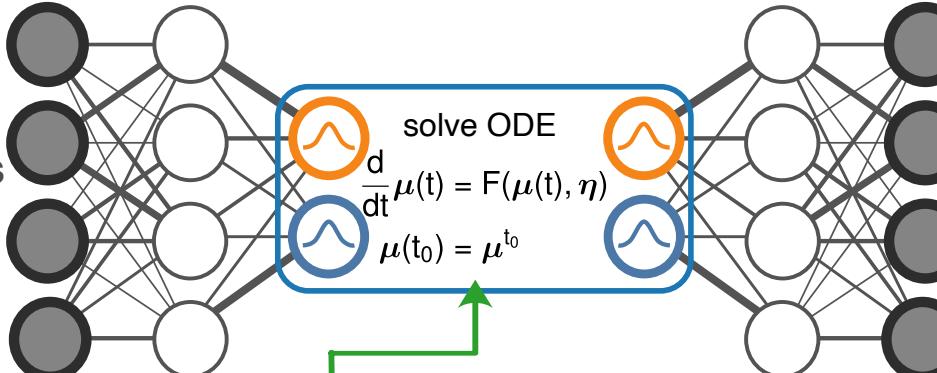
## Different motor function tests over time

- RULM
- HFMSE
- ...

# Describe individual SMA trajectories as ODEs in the latent space of a deep learning model



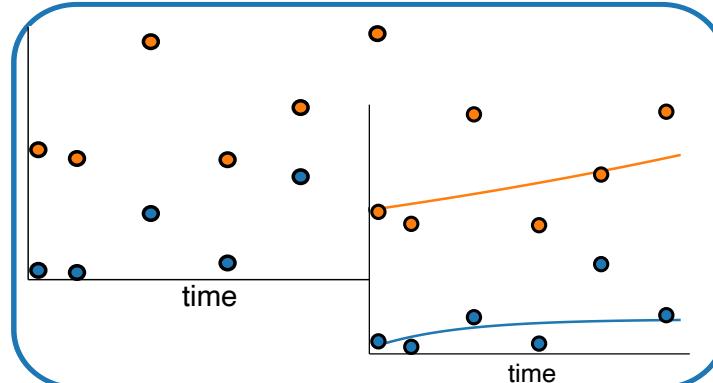
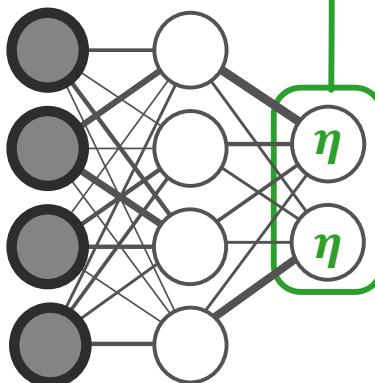
Time series  
of motor  
function  
test



Recon-  
structed  
time  
series



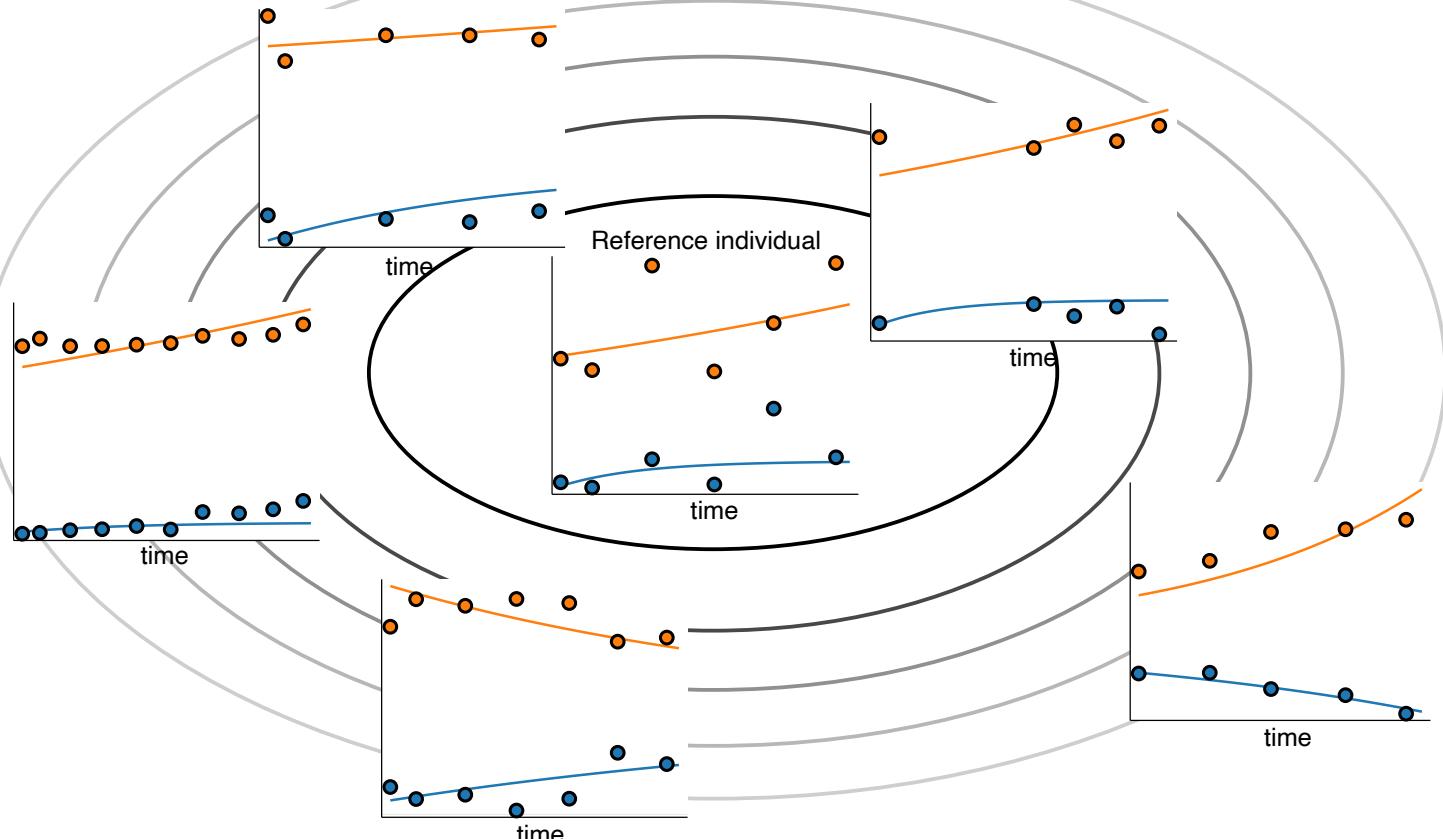
Baseline  
variables



```
m = init_ODEVAE()
ps = getparams(m)
opt = ADAM(η)
trainingdata = zip(xs, xs_baseline, tvals)

for epoch in 1:epochs
    for (X, Y, t) in trainingdata
        grads = gradient(ps) do
            loss(X, Y, t, m, args=args)
        end
    end
    update!(opt, ps, grads)
end
```

# Jointly model groups of similar individuals



# Julia – a pragmatic approach to scientific computing

## Take home messages

- Fresh approach without legacy characteristics
- Fast yet easy to use
- Removes barriers that so far limit scientific ideas, e.g., by providing straightforward access to powerful automatic differentiation libraries
- Key tool for current trends such as differentiable programming:
  - Combining deep learning and dynamic modelling for individual disease trajectories
  - Quick prototyping of a prediction model in a COVID-19 application
- Add Julia to your toolbox to expand the universe of modelling approaches available to your research!



# Thanks to...



**Special thanks to:**

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and the AG Machine  
Learning

**Colleagues at the IMBI:**

Michelle Pfaffenlehner  
Clemens Kreutz  
Marlon Grodd

And thanks to you for listening!

**If you want to know more:**

Statistical Practice

**Using Differentiable Programming for Flexible Statistical Modeling**

Maren Hackenberg, Marlon Grodd, Clemens Kreutz, Martina Fischer, Janina Esins, Linus Grabenhenrich, Christian Karagiannidis & Harald Binder ...show less

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<https://github.com/maren-ha/DifferentiableProgrammingForStatisticalModeling>



**... at the Institute of Mathematics:**

Philipp Harms, Thorsten Schmidt

**... and from the SMArtCARE registry:**

Astrid Pechmann, Janbernd Kirschner



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RESEARCH ARTICLE | Open Access

Deep dynamic modeling with just two time points: Can we still allow for individual trajectories?

Maren Hackenberg, Philipp Harms, Michelle Pfaffenlehner, Astrid Pechmann, Janbernd Kirschner, Thorsten Schmidt, Harald Binder

First published: 06 April 2022 | <https://doi.org/10.1002/bimj.202000366>



<https://doi.org/10.1002/bimj.202000366>



<https://github.com/maren-ha/DeepDynamicModelingWithJust2TimePoints>

