

Weatherford

$$(a) \frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2} - u(u-a)(1-u) + w$$

Discretizando: $\frac{u_{2,i} - u_{1,i}}{\Delta t} = \frac{D}{\Delta x^2} [u_{1,i+1} - 2u_{1,i} + u_{1,i-1}] - u_{1,i}(u_{1,i} - a)(1 - u_{1,i}) + w_{1,i}$

$$u_{2,i} = u_{1,i} + \left(\frac{D\Delta t}{\Delta x^2} \right) (u_{1,i+1} - 2u_{1,i} + u_{1,i-1}) - u_{1,i}\Delta t (u_{1,i} - a)(1 - u_{1,i}) + w_{1,i}\Delta t$$

$$u_{2+1,i} = u_{1,i} + \frac{D\Delta t}{\Delta x^2} (2\cos(K\Delta x) - 2)u_{1,i} - \Delta t (u_{1,i} - a)(1 - u_{1,i})u_{1,i} - w_{1,i}\Delta t$$

Para la parte que varía unos:

$$\left(1 + \frac{D\Delta t}{\Delta x^2} (2\cos(K\Delta x) - 2) \right) u_{1,i}$$

El mayor valor que puede obtener es para $\cos(K\Delta x) = 0$

Debe ser menor a 2 y $D > 0$: $1 - 2 \frac{D\Delta t}{\Delta x^2} \geq 1$

$$-1 < 2 \frac{D\Delta t}{\Delta x^2}$$

$$\Rightarrow \underline{\underline{\frac{1}{2} > \frac{D\Delta t}{\Delta x^2} = \lambda}}$$