

$$\begin{aligned} \text{d) } f(z) &= z^3 - 1 = (x+iy)^3 - 1 = (x+iy)(x+iy)(x+iy) - 1 = x^3 + 3x^2iy + 3x(iy)^2 + (iy)^3 - 1 = \\ &= x^3 + 3x^2iy - 3xy^2 - iy^3 - 1 \quad \therefore f(z) = x^3 + 3x^2iy - 3xy^2 - iy^3 - 1 = (x^3 - 3xy^2 - 1) + (3x^2y - y^3)i \end{aligned}$$

$$f(\bar{z}) = (x^3 - 3xy^2 - 1) + i(3x^2y - y^3)$$

$$\text{e) } J = \begin{pmatrix} \frac{\partial f_1}{\partial x} & \frac{\partial f_1}{\partial y} \\ \frac{\partial f_2}{\partial x} & \frac{\partial f_2}{\partial y} \end{pmatrix}$$

$$\therefore J = \begin{pmatrix} 3x^2 - 3y^2 & -6xy \\ 6xy & 3x^2 - 3y^2 \end{pmatrix} ; f_1 = \operatorname{Re}(f(z)), f_2 = \operatorname{Im}(f(z))$$

$$* \frac{\partial f_1}{\partial x} = \frac{\partial}{\partial x}(x^3 - 3xy^2 - 1) = 3x^2 - 3y^2$$

$$* \frac{\partial f_2}{\partial x} = \frac{\partial}{\partial x}(3x^2y - y^3) = 6xy$$

$$* \frac{\partial f_1}{\partial y} = \frac{\partial}{\partial y}(x^3 - 3xy^2 - 1) = -6xy$$

$$* \frac{\partial f_2}{\partial y} = \frac{\partial}{\partial y}(3x^2y - y^3) = 3x^2 - 3y^2$$