

Algorithm: Given an instance of this problem with n variables and m clauses, we set each variable randomly as 0 or 1, so the probability of each variable being 0 or 1 will be 0.5.

Proof: Assuming a clause has t variables, for each clause, the P of unsatisfied will be $(1/2)^t$, so the P of satisfied will be $(1-(1/2)^t)$. assuming we have total m clauses, the optimal solution C^* must be smaller than m , so $C^* \leq m$. on average, the satisfied clause will be $(1-(1/2)^t) \cdot m$, which is definitely greater than $0.5m$. so $C' \geq 0.5m$

The approximation ratio is $C^*/C' \leq m/0.5m = 2$, so this is 2-approximation method