

Algorithm: Max Squares in Right Isosceles Triangle (Reduction Technique)

Name & Purpose

Computes the maximum number of non-overlapping 2×2 squares that fit inside a right isosceles triangle with base B , where one square side is parallel to the base.

Inputs

- **b**: int, the base (and height) of the right isosceles triangle.
 - Constraint: $b \geq 1$

Outputs

- **int**: the maximum count of 2×2 squares that fit; range $[0, \infty)$

Preconditions

- b is a positive integer
- The triangle is right isosceles with the base as the shortest side

Postconditions

- Returns a non-negative integer count of squares

High-Level Idea

Use reduction (divide and conquer): peel off the bottom horizontal strip of height 2 from the triangle, count how many 2×2 squares fit there ($n = b//2 - 1$), then recursively solve the remaining smaller similar triangle with base $b-2$.

Base case: if $b < 4$, no squares fit, return 0.

Pseudocode

```
function max_squares(b):  
    if b < 4:  
        return 0  
  
    n ← b // 2 - 1                // squares in the current bottom strip  
    return n + max_squares(b - 2) // add squares from the reduced triangle
```

Complexity

- **Time**: $O(b)$ – $b/2$ recursive calls, each $O(1)$. Dominant term: $b/2$.

- **Space:** $O(b)$ – recursion depth is $b/2$; call stack stores $O(b)$ frames.

Correctness Sketch

Invariant: each strip of height 2 at level k contains exactly $(k-1)$ non-overlapping 2×2 squares (for $k \geq 2$). By induction: base case ($b < 4$) is correct; inductive step removes one valid strip and recurses, so total = $n + f(b-2)$ is correct.

Edge Cases

- **$b = 1, 2, 3$:** fewer than 4 units \rightarrow return 0 (no 2×2 square fits)
- **$b = 4, 5$:** exactly one strip fits \rightarrow return 1
- **Non-integer input:** convert to int (e.g., $5.7 \rightarrow 5$)
- **Negative b :** return 0

Example

```
13 def max_squares_in_triangle(b):
14     if b < 4:          #critical case
15         return 0
16
17     n = b // 2 - 1     #number of squares that can fit in the current base
18
19     nrSquares = n + max_squares_in_triangle(b - 2) #recursive call reducing the base by 2
20     return nrSquares
21
22 B = int(input("Enter the base of the triangle: "))
23 nr = max_squares_in_triangle(B)
24 print(nr)
25
```

DEBUG CONSOLE **TERMINAL** PORTS MEMORY

✓ **TERMINAL**

```
1
PS C:\Users\maria\Documents\uvt1\ads1> python -u "c:\Users\maria\Documents\uvt1\ads1\2025-12-06\p2-s9.py"
Enter the base of the triangle: 12
15
```