

# Parallel implementations of matrix multiplication

This is the second mandatory assignment of INF3380. Each student should work independently and submit her/his parallel programs to the group teacher before the deadline.

## Matrix multiplication

As described in Chapter 11.2 of the textbook, *Michael J. Quinn, Parallel Programming in C with MPI and OpenMP*, the product between matrix  $A$  (of dimension  $l \times m$ ) and matrix  $B$  (of dimension  $m \times n$ ) will be a matrix  $C$  (of dimension  $l \times n$ ), whose elements are defined by

$$C_{i,j} = \sum_{k=0}^{m-1} a_{i,k} b_{k,j}, \quad \text{for } 0 \leq i \leq l-1, \quad 0 \leq j \leq n-1.$$

**Remark.** Students who have trouble understanding the above mathematical formula should familiarize themselves with simple examples of matrix multiplications, for example, given on the following webpage:

<http://www.intmath.com/matrices-determinants/4-multiplying-matrices.php>

## Task 1: MPI implementation

The student can choose either the rowwise block-striped parallel algorithm described in Chapter 11.3, or the checkerboard Cannon's algorithm described in Chapter 11.4. An MPI program should be implemented such that it can

- accept two file names at run-time,

- let process 0 read the  $A$  and  $B$  matrices from the two data files,
- let process 0 distribute the pieces of  $A$  and  $B$  to all the other processes,
- involve all the processes to carry out the chosen parallel algorithm for matrix multiplication  $C = A * B$ ,
- let process 0 gather, from all the other processes, the different pieces of  $C$ ,
- let process 0 write out the entire  $C$  matrix to a data file.

## Task 2: OpenMP-MPI implementation

The student should extend her/his MPI program from Task 1, so that OpenMP is used within each MPI process for the computation-intensive parts.

### Input of matrix

For the sake of I/O efficiency, it is assumed that the  $A$  and  $B$  matrices are stored in binary formatted data files. More specifically, the following function can be used to read in a matrix stored in a binary file:

```
void read_matrix_binaryformat (char* filename, double*** matrix,
                              int* num_rows, int* num_cols)
{
    int i;
    FILE* fp = fopen (filename,"rb");
    fread (num_rows, sizeof(int), 1, fp);
    fread (num_cols, sizeof(int), 1, fp);

    /* storage allocation of the matrix */
    *matrix = (double**)malloc((*num_rows)*sizeof(double*));
    (*matrix)[0] = (double*)malloc((*num_rows)*(*num_cols)*sizeof(double));
    for (i=1; i<(*num_rows); i++)
        (*matrix)[i] = (*matrix)[i-1]+(*num_cols);

    /* read in the entire matrix */
    fread ((*matrix)[0], sizeof(double), (*num_rows)*(*num_cols), fp);
    fclose (fp);
}
```

For example, suppose the following three variables are declared:

```
double **matrix;
int num_rows;
int num_cols;
```

Then, a matrix stored in file `mat.bin` can be read in by calling `read_matrix_binaryformat` as follows:

```
read_matrix_binaryformat ("mat.bin", &matrix, &num_rows, &num_cols);
```

## Output of matrix

Similarly, the multiplication result matrix  $C$  should be written to file in binary format by using the following function:

```
void write_matrix_binaryformat (char* filename, double** matrix,
                               int num_rows, int num_cols)
{
    FILE *fp = fopen (filename,"wb");
    fwrite (&num_rows, sizeof(int), 1, fp);
    fwrite (&num_cols, sizeof(int), 1, fp);
    fwrite (matrix[0], sizeof(double), num_rows*num_cols, fp);
    fclose (fp);
}
```

## Examples of $A$ and $B$ matrices

From the website of INF3380, the following matrices (in binary format) can be downloaded for code debugging and testing:

|                                 |                                |
|---------------------------------|--------------------------------|
| <code>small_matrix_A.bin</code> | of dimension $100 \times 50$   |
| <code>small_matrix_B.bin</code> | of dimension $50 \times 100$   |
| <code>large_matrix_A.bin</code> | of dimension $1000 \times 500$ |
| <code>large_matrix_B.bin</code> | of dimension $500 \times 1000$ |