



Certainly! The equation for the cross-entropy loss in the case of multi-class classification is as follows:

Given:

- $N$  : the number of data points
- $C$  : the number of classes
- $y_{ij}$  : the indicator function (1 if data point  $i$  is of class  $j$ , 0 otherwise)
- $p_{ij}$  : the predicted probability that data point  $i$  belongs to class  $j$

The cross-entropy loss is calculated as:

$$L(y, p) = -\frac{1}{N} \sum_{i=1}^N \sum_{j=1}^C y_{ij} \log(p_{ij})$$

Here's an expansion of the terms:

- $\sum_{i=1}^N$  : This represents the sum over all data points.
- $\sum_{j=1}^C$  : This represents the sum over all classes.
- $y_{ij}$  : This is 1 if the true label of data point  $i$  is class  $j$ , and 0 otherwise. It serves as an indicator function.
- $p_{ij}$  : This is the predicted probability that data point  $i$  belongs to class  $j$ .
- $\log(p_{ij})$  : This is the natural logarithm of the predicted probability. It penalizes the model when it's confident but wrong, i.e., when it predicts a high probability for the incorrect class.
- $-$  : The negative sign is applied to make it a loss function that we want to minimize.

The overall loss is the average over all data points, which is why we divide by  $N$  at the beginning.

This loss function essentially quantifies how well the predicted probabilities align with the



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