# Solução do Problema Boeing1 - Solver HiGHS

### Análise Computacional

17 de setembro de 2025

## 1 Informações do Problema

#### Informações do Problema:

• Nome: Boeing1

• Número de Variáveis: 384

• Número de Restrições: 351

• Inviabilidade Primal: 0.000e+00

• Inviabilidade Dual: 2.776e-17

• Valor Primal: -3.352e+02

• Valor Dual: -3.268e+02

• Gap: -2.526e-19

• Número de Iterações: 24

## 2 Variáveis Primais e Custos Reduzidos

Tabela 1: Variáveis primais e custos reduzidos do problema Boeing1

Coordenada x	Valor x	Coordenada z	Valor z
1	-0.000000	1	0.000000
2	12.000000	2	0.000000
3	0.000000	3	0.055156
4	0.000000	4	0.068792
5	14.000000	5	0.000000
6	0.000000	6	0.013301
7	0.000000	7	0.013311
8	-0.000000	8	0.000000
9	0.000000	9	0.029941
10	49.000000	10	0.000000
11	73.000000	11	0.000000
12	60.000000	12	0.000000

Coordenada	x Valor x	Coordenada z	Valor z
13	1.000000	13	0.00000
14	0.000000	14	0.00816
15	3.000000	15	0.00000
16	0.000000	16	0.00815
17	47.165493	17	0.00000
18	310.767862	18	0.00000
19	0.325000	19	0.00000
20	317.741645	20	0.00000
21	-0.000000	21	0.00000
22	0.000000	22	0.01629
23	0.000000	23	0.00685
24	26.000000	24	0.00000
25	0.000000	25	0.00521
26	37.000000	$\frac{26}{26}$	0.00000
27	0.000000	$\frac{27}{27}$	0.00000
28	0.000000	28	0.00000
29	215.000000	29	0.00000
30	0.000000	30	0.00000
31	27.000000	31	0.00000
32	83.000000	32	0.00000
33	0.000000	33	0.00030
34	278.000000	34	0.00230
35	104.048235	$\frac{34}{35}$	0.00000
36			0.00000
	33.040000	36	
37	68.205882	37	0.00000
38	98.000000	38	0.00000
39	0.000000	39	0.05885
40	5.000000	40	0.00000
41	0.000000	41	0.05886
42	1.000000	42	0.00000
43	-0.000000	43	0.00000
44	157.794393	44	0.00000
45	-0.000000	45	0.00000
46	35.000000	46	0.00000
47	0.000000	47	0.00080
48	0.000000	48	0.00081
49	94.205607	49	0.00000
50	-0.000000	50	0.00000
51	39.794393	51	0.00000
52	70.013273	52	0.00000
53	342.986727	53	0.00000
54	0.000000	54	0.00000
55	37.000000	55	0.00000
56	38.558824	56	0.00000
57	6.955882	57	0.00000
58	32.485294	58	0.00000
59	0.000000	59	0.00826
60	-0.000000	60	0.00000
61	0.000000	61	0.00826

Coordenada	x Valor x	Coordenada z	Valor z
62	546.014706	62	0.00000
63	3.720588	63	0.00000
64	139.000000	64	0.00000
65	66.267442	65	0.00000
66	0.000000	66	0.00449
67	75.000000	67	0.00000
68	5.415869	68	0.00000
69	33.040000	69	0.00000
70	260.848837	70	0.00000
71	839.963272	71	0.00000
72	87.906977	72	0.00000
73	168.000000	73	0.00000
74	98.000000	74	0.00000
75	1464.240914	75	0.00000
76	8.581395	76	0.00000
77	0.000000	77	0.00998
78	0.000000	78	0.00000
79	22.418605	79	0.00000
80	41.000000	80	0.00000
81	0.000000	81	0.02564
82	0.000000	82	0.02504
83	0.000000	83	0.01566
84	0.000000	84	0.01300 $0.00474$
85	153.755814	85	0.00472
86	39.244186	86	0.00000
87	0.000000	87	0.00000
88	0.000000	88	0.00000
89	2.000000	89	0.00000
90	0.000000	90	0.00000
91	151.000000	91	0.00000
92	0.000000	92	0.12838
93	-0.000000	93	0.00000
94	51.000000	94	0.00000
95	0.000000	95	0.00000
96	13.000000	96	0.00000
97	37.891085	97	0.00000
98	77.153033	98	0.00000
99	6.955882	99	0.00000
100	177.000000	100	0.00000
101	23.104320	101	0.00000
102	24.895680	102	0.00000
103	0.000000	103	0.00279
104	0.000000	104	0.00000
105	68.000000	105	0.00000
106	0.000000	106	0.12839
107	0.000000	107	0.00001
108	24.000000	108	0.00000
109	-0.000000	109	0.00000
110	291.000000	110	0.00000

Coordenada	x Valor x	Coordenada z	Valor z
111	67.000000	111	0.00000
112	-0.000000	112	0.00000
113	839.963272	113	0.00000
114	146.680914	114	0.00000
115	236.600000	115	0.00000
116	0.000000	116	0.18679
117	50.755814	117	0.00000
118	168.000000	118	0.00000
119	0.000000	119	0.00000
120	0.000000	120	0.00000
121	0.000000	121	0.00548
122	83.418605	122	0.00000
123	75.802326	123	0.00000
124	-0.000000	124	0.00000
125	0.000000	125	0.00548
126	79.197674	126	0.00000
$\frac{127}{127}$	164.859813	$\frac{127}{127}$	0.00000
128	0.000000	128	0.00098
129	0.000000	129	0.00377
130	392.000000	130	0.00000
131	0.000000	131	0.00089
132	70.013273	132	0.00000
133	-0.000000	133	0.00000
134	50.755814	134	0.00000
135	47.165493	135	0.00000
136	0.000000	136	0.00000
137	0.000000	137	0.00548
138	0.000000	138	0.00040
139	6.000000	139	0.00000
140	-0.000000	140	0.00000
141	0.000000	141	0.00548
142	0.000000	142	-0.00000
143	17.000000	143	0.00000
144	260.848837	144	0.00000
145	37.151163	145	0.00000
146	19.395349	146	0.00000
147	0.000000	147	0.00000
148	91.604651	148	0.00000
149	0.000000	149	0.00000
150	57.000000	150	0.00000
151	91.000000	151	0.00000
152	36.408451	152	0.00000
153	134.134392	153	0.00000
154	139.690491	154	0.00000
155	4.766667	155	0.00000
156	0.000000	156	0.00521
157	234.317292	157	0.00000
158	0.000000	158	0.00527
159	178.682708	159	0.00000

Coordenada	x Valor x	Coordenada z	Valor z
160	19.031690	160	0.00000
161	266.681846	161	0.00000
162	-0.000000	162	0.00000
163	412.874082	163	0.00000
164	1913.412382	164	0.00000
165	14.679577	165	0.00000
166	271.317292	166	0.00000
167	138.003130	167	0.00000
168	4.352113	168	0.00000
169	241.283575	169	0.00000
170	126.364312	170	0.00000
171	14.679577	171	0.00000
172	138.003130	172	0.00000
173	0.000000	173	0.00005
174	125.317292	174	0.00000
175	11.000000	175	0.00000
176	0.000000	176	0.01108
177	7.000000	177	0.00000
178	0.000000	178	0.00974
179	4.000000	179	0.00000
180	0.000000	180	0.00000
181	26.000000	181	0.001103
182	2.000000	182	0.00000
			0.00000
183	1.000000	183	
184	11.000000	184	0.00000
185	-0.000000	185	0.00000
186	0.000000	186	0.00524
187	24.000000	187	0.00000
188	0.000000	188	0.00673
189	0.000000	189	0.00001
190	9.705882	190	0.00000
191	6.294118	191	0.00000
192	3.000000	192	0.00000
193	24.000000	193	0.00000
194	40.000000	194	0.00000
195	5.000000	195	0.00000
196	1.000000	196	0.00000
197	13.000000	197	0.00000
198	0.000000	198	0.02764
199	0.000000	199	0.04309
200	8.000000	200	0.00000
201	0.000000	201	0.02763
202	0.000000	202	0.04309
203	1.000000	203	0.00000
204	1.000000	204	0.00000
205	1.000000	205	0.00000
206	1.000000	206	0.00000
$\frac{207}{207}$	2.000000	207	0.00000
208	7.000000	208	0.00000

Coordenada	x Valor x	Coordenada z	Valor z
209	2.000000	209	0.00000
210	2.000000	210	0.000000
211	2.000000	211	0.000000
212	1.000000	212	0.000000
213	2.000000	213	0.000000
214	5.000000	214	0.000000
215	2.000000	215	0.000000
216	21.000000	216	0.000000
217	13.000000	217	0.00000
218	6.000000	218	0.00000
219	7.000000	219	0.00000
220	17.000000	220	0.00000
221	25.000000	221	0.00000
${222}$	6.294118	${222}$	0.00000
223	0.000000	223	0.590330
224	-49.012862	$\frac{223}{224}$	0.000000
225	0.000000	$\frac{221}{225}$	0.27941
226	0.000000	$\frac{226}{226}$	-0.14551
227	0.000000	$\frac{220}{227}$	0.27664
228	-47.000000	228	0.27004
229	0.000000	$\frac{220}{229}$	0.07004
230	0.000000	230	-0.08637
230	0.000000	231	0.16300
232	-47.243540	$\frac{231}{232}$	0.10300
232	0.000000	233	0.00000
233 234	-81.000000		0.13230 $0.03730$
		234	
235	0.000000	235	9.31876
236	0.000000	236	4.80383
237	0.000000	237	2.63143
238	0.000000	238	7.58825
239	0.000000	239	2.47705
240	2.355140	240	0.00000
241	0.000000	241	0.11389
242	0.160321	242	0.00000
243	0.721444	243	0.00000
244	0.280000	244	0.00000
245	0.000000	245	0.02839
246	0.000000	246	0.09465
247	0.085938	247	0.00000
248	0.838235	248	0.00000
249	0.075827	249	0.00000
250	0.000000	250	4.90852
251	0.000000	251	2.93109
252	0.000000	252	2.10595
253	0.000000	253	1.03387
254	0.000000	254	0.52250
255	0.000000	255	0.26095
256	0.000000	256	0.08320
257	0.000000	257	0.07713

Coordenada x	Valor x	Coordenada z	Valor z
258	4.658015	258	0.00000
259	0.000000	259	0.000195
260	0.074881	260	0.000000
261	0.000000	261	0.002776
262	0.000000	262	0.061651
263	1.921948	263	0.000000
264	0.000000	264	1.269648
265	0.000000	265	0.673373
266	0.000000	266	0.368704
267	0.000000	267	0.076301
268	0.000000	268	0.149640
269	7.000000	269	-0.00759
270	0.000000	270	0.002274
271	3.085066	271	0.000000
272	0.695173	272	0.000000
273	0.000000	273	0.062747
274	3.897217	274	0.000000
275	0.000000	275	0.062469
276	1.510832	276	0.000000
277	0.000000	277	0.006356
278	0.000000	278	0.022252
279	0.000000	279	0.022336
280	2.417331	280	0.000000
281	0.000000	281	0.083204
282	0.000000	282	0.00320
283	0.000000	283	0.004213
284	0.924173	284	0.000000
285	0.000000	285	0.058283
286	0.000000	286	0.03020
287	1.691245	287	0.000000
288	0.222817	288	0.000000
289	0.222017 $0.000000$	289	0.000000
290	0.704819	290	$0.11721^{2}$ $0.000000$
290 291	0.704819 $0.159543$	290 291	0.000000
291 292	2.135638	$\frac{291}{292}$	0.000000
292 293	0.000000	293	0.102420
293 294			0.102420 $0.007011$
	0.000000 $0.700000$	294	0.00701
295		295	
296	3.300000	296	0.000000
297	0.000000	297	0.157181
298	0.000000	298	0.010044
299	0.000000	299	0.030287
300	0.161765	300	0.000000
301	0.000000	301	0.962734
302	0.000000	302	0.496810
303	0.000000	303	0.258647
304	0.000000	304	0.071536
305	0.000000	305	0.089666
306	1.196429	306	0.000000

Coordenada x	Valor x	Coordenada z	Valor z
307	0.000000	307	0.630869
308	0.000000	308	0.297180
309	0.000000	309	0.132685
310	0.234513	310	0.000000
311	0.765487	311	0.000000
312	0.222833	312	0.000000
313	0.000000	313	0.000305
314	0.000000	314	0.002520
315	0.000000	315	0.030369
316	3.200696	316	0.000000
317	0.000000	317	0.041270
318	0.664202	318	0.000000
319	0.000000	319	0.004992
320	0.000000	320	0.017817
321	0.000000	321	0.024136
322	2.453859	322	0.000000
323	-0.000000	323	0.000000
324	0.000000	324	28.386184
325	1.000000	325	0.000000
326	0.476744	326	0.000000
327	-0.000000	327	0.000000
328	0.523256	328	0.000000
329	1.000000	329	-0.428187
330	0.000000	330	1.312002
331	0.000000	331	0.622453
332	0.000000	332	0.326630
333	0.827465	333	0.000000
334	0.000000	334	0.032211
335	0.486036	335	0.000000
336	0.500477	336	0.000000
337	0.000000	337	0.059504
338	0.000000	338	0.026382
339	2.061996	339	0.000000
340	0.000000	340	5.834736
341	0.000000	341	1.900266
342	3.174784	342	0.000000
343	0.682768	343	0.000000
344	0.000000	344	0.003333
345	0.000000	345	0.061496
346	0.726937	346	0.000000
347	0.252983	347	0.000000
348	0.108333	348	0.000000
349	0.000000	349	0.201361
350	0.000000	350	0.369720
351	0.000000	351	0.058238
352	-0.000000	352	0.000000
353	0.238397	353	0.000000
354	1.271450	354	0.000000
355	0.000000	355	0.122615
	0.000000	000	U.122UI

Coordenada x	Valor x	Coordenada z	Valor z
356	2.077706	356	0.000000
357	0.000000	357	0.100193
358	0.000000	358	0.166277
359	9.513244	359	0.000000
360	8.856901	360	0.000000
361	0.000000	361	0.016149
362	20.000000	362	-0.043600
363	0.000000	363	0.100192
364	0.000000	364	0.150128
365	0.000000	365	0.043600
366	0.172535	366	0.000000
367	0.000000	367	0.472301
368	0.000000	368	0.786952
369	0.000000	369	6.729639
370	0.000000	370	2.186018
371	1.000000	371	0.000000
372	1.000000	372	0.000000
373	0.000000	373	6.527618
374	0.000000	374	2.084223
375	1.000000	375	0.000000
376	0.000000	376	0.005254
377	0.000000	377	0.054598
378	0.073187	378	0.000000
379	0.000000	379	0.347242
380	0.000000	380	0.161200
381	0.000000	381	0.065146
382	0.000000	382	0.000048
383	4.651904	383	0.000000
384	20.000000	384	-0.036499

# 3 Variáveis Duais (Multiplicadores de Lagrange)

Tabela 2: Variáveis duais do problema Boeing1

Coordenada y	Valor y
1	-0.000000
2	-0.000000
3	0.399557
4	-0.000000
5	-0.000000
6	-0.000000
7	-0.000000
8	-0.000000
9	-0.000000
10	-0.000000
11	-0.000000
~ .	

Coordenada y	Valor y
12	-0.133330
13	0.038590
14	-0.070640
15	0.086372
16	-0.000000
17	-0.037309
18	-0.000000
19	0.005483
20	-0.000000
21	0.047580
22	0.013301
23	0.051269
24	-0.000000
25	0.057318
26	-0.000000
20 27	0.052076
	-0.000000
28	
29	0.058809
30	0.045520
31	0.019858
32	0.006463
33	0.022608
34	0.013301
35	0.009256
36	0.027643
37	0.005483
38	0.022608
39	0.013301
40	0.024789
41	0.029098
42	-0.000000
43	0.029098
44	-0.000000
45	0.022608
46	0.008964
47	0.022608
48	0.008791
49	0.027643
50	-0.000000
51	0.006378
52	0.019364
53	0.005483
54	0.026338
55	0.018798
56	0.023444
57	-0.000000
58	0.133872
59	-0.000000
60	0.005483
Continua na próx	

Coordenada y	Valor y
61	-0.000000
62	-0.000000
63	-0.000000
64	-0.000000
65	-0.000000
66	0.011978
67	-0.000000
68	-0.000000
69	0.022608
70	-0.000000
71	-0.000000
72	0.009534
73	0.022608
74	0.005483
75	-0.000000
76	-0.000000
77	0.005035
78	0.003033
79	-0.000000
80	-0.000000
81	0.005483
82	0.025770
83	0.024542
84	0.010696
85	0.008970
86	0.021552
87	0.030019
88	0.008970
89	-0.000000
90	0.010696
91	0.025770
92	0.018900
93	0.044712
94	0.008970
95	0.024595
96	0.010696
97	0.020681
98	0.030019
99	0.010696
100	0.008970
101	0.010696
102	0.008970
103	0.045520
104	-0.000000
105	-0.000000
106	-0.000000
107	0.052076
108	0.013301
109	-0.000000
100	0.000000

Coordenada y	Valor y	
110	0.027643	
111	0.006722	
112	0.013301	
113	-0.000000	
114	-0.000000	
115	-0.000000	
116	-0.000000	
117	-0.169813	
118	-0.130920	
119	-0.080440	
120	-0.134810	
121	-0.299880	
122	-0.258020	
123	-0.019020	
124	-0.073058	
125	-0.035091	
126	-0.014515	
127	-0.030320	
128	-0.030320	
129	-0.020172	
130	-0.021559	
131	-0.250026	
132	-0.259296	
133	-0.058906	
134	-0.057170	
135	-0.054613	
136	-0.025712	
137	-0.025918	
138	-0.030720	
139	-0.028427	
140	-0.017419	
141	-0.278447	
142	-0.239622	
143	-0.024185	
144	-0.026220	
145	-0.222550	
146	-0.213867	
147	-0.031480	
148	-0.014012	
149	-0.022556	
150	-0.024568	
151	-0.232050	
152	-0.223377	
153	-0.018836	
154	-0.018198	
155	-0.020862	
156	-0.275730	
157	-0.222830	
158	-0.013797	
Continua na próxima página		

Coordenada y	Valor y	
159	-0.269572	
160	-0.215192	
161	-0.019909	
162	-0.071880	
163	-0.271460	
164	-0.218870	
165	-0.052451	
166	-0.033961	
167	-0.019254	
168	-0.039520	
169	-0.056918	
170	-0.030528	
171	-0.134320	
172	-0.134520	
173	-0.121039	
174	-0.026438	
175	-0.222142	
176	-0.276612	
177	-0.071642	
178	-0.070174	
179	-0.071821	
180	-0.075203	
181	-0.085681	
182	-0.082774	
183	-0.227782	
184	-0.281882	
185	-0.250190	
186	-0.259430	
187	-0.220382	
188	-0.229632	
189	-0.217278	
190	-0.216862	
191	-0.226262	
192	-0.208842	
193	-0.263202	
194	-0.226498	
195	-0.221348	
196	-0.275788	
197	-0.233232	
198	-0.233232	
	-0.274366	
199		
200	-0.278790	
201	-0.286298	
202	-0.270991	
203	-0.228621	
204	-0.241268	
205	-0.230360	
206	-0.000000	
207	-0.006328	
Continua na próxima página		

Coordenada y	Valor y	
208	-0.006788	
209	0.101117	
210	0.549857	
211	7.712595	
212	-0.000000	
213	-0.000000	
214	-0.000000	
215	-0.000000	
216	-0.000000	
217	-0.000000	
218	0.204071	
219	1.568059	
220	-0.000000	
221	-0.000000	
222	-0.000000	
223	-0.000000	
224	0.253835	
225	0.057486	
226	-0.000000	
227	-0.000000	
228	33.151195	
229	-0.000000	
230	-0.000000	
231	-0.000000	
232	-0.000000	
233	0.007267	
234	0.007207 $0.113385$	
235	0.263372	
236	-0.000000	
237	-0.000000	
238	-0.000000	
239	-0.000000	
240	-0.000000	
241	-0.000000	
242	-0.000000	
243	-0.000000	
244	-0.000000	
245	-0.000000	
246	-0.000000	
247	-0.000000	
248	-0.000000	
249	-0.000000	
250	-0.000000	
250 $251$	0.087608	
252	9.153065	
253	1.506778	
254	29.694619	
255	-0.000000	
256	-0.000000	
Continua na próxima página		

Coordenada y	Valor y	
257	-0.000000	
258	-0.000000	
259	-0.000000	
260	-0.000000	
261	-0.000000	
$\frac{-6}{262}$	-0.000000	
263	-0.000000	
264	-0.000000	
265	0.004496	
266	0.000807	
267	-0.000000	
268	-0.000000	
269	0.075004	
270	0.075004 $0.075004$	
271	0.055146	
272	0.075004	
273	0.080487	
274	-0.000000	
275	0.002894	
276	-0.000000	
277	-0.000000	
278	-0.000000	
279	-0.000000	
280	-0.000000	
281	-0.000000	
282	0.002853	
283	-0.000000	
284	0.027643	
285	0.015665	
286	-0.000000	
287	-0.000000	
288	-0.000000	
289	-0.000000	
290	-0.000000	
291	-0.000000	
292	0.003767	
293	0.008266	
294	-0.000000	
295	-0.000000	
296	0.015665	
$\frac{297}{297}$	-0.000000	
298	-0.000000	
299	-0.000000	
300	0.000726	
301	-0.000000	
302	-0.000000	
303	-0.000000	
304	0.001455	
305	-0.000000	
Continua na próxima página		

Coordenada y	Valor y
306	0.002474
307	-0.000000
308	-0.000000
309	-0.000000
310	0.000567
311	-0.000000
312	-0.000000
313	-0.000000
314	-0.000000
315	0.186799
316	-0.000000
317	-0.000000
318	-0.000000
319	-0.000000
320	-0.000000
321	-0.000000
322	-0.000000
323	-0.000000
324	-0.000000
325	-0.000000
326	-0.000000
327	-0.000000
328	0.000980
329	0.003312
330	0.012748
331	0.053624
332	0.019607
333	-0.000000
334	-0.000000
335	-0.000000
336	-0.000000
337	-0.000000
338	-0.000000
339	-0.000000
340	-0.000000
341	-0.000000
342	-0.000000
343	0.004218
344	-0.000000
345	-0.000000
346	0.050312
347	0.005642
348	-0.000000
349	0.005642
350	-0.000000
351	0.003862

## 4 Observações

- O solver HiGHS foi configurado com o método IPM (Interior Point Method).
- Este arquivo contém a solução detalhada para o problema Boeing1.
- As variáveis duais representam os multiplicadores de Lagrange das restrições.
- Os custos reduzidos (z) indicam o impacto de forçar variáveis não-básicas na base.