1. Introduction

Definition 2. A *(nonarchimedean) local field* is a field complete with respect to a discrete valuation and with finite residue field.

Definition 3. A mixed characteristic local field is a finite field extension of the field \mathbb{Q}_p of p-adic numbers, for some prime p.

Definition 4. An equal characteristic local field is a finite field extension of the field $\mathbb{F}_p((X))$, for some prime p.

Lemma 5. A mixed characteristic local field is a local field.

Lemma 6. An equal characteristic local field is a local field.

Definition 7. A local field is a field

Proof. Omitted, but it uses [Ser67] and also [Ser68].

References

[Ser67] Jean-Pierre Serre. Local class field theory. In Algebraic Number Theory (Proc. Instructional Conf., Brighton, 1965), pages 128–161. Thompson, Washington, D.C., 1967.

[Ser68] Jean-Pierre Serre. Corps locaux. Hermann, Paris, 1968. Deuxième édition.