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4D Modeling of CME Expansion and EUV Dimming Observed with STEREO/EUVI

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Abstract. This is the first attempt to model the kinematics of a CME launch and the resulting EUV dimming quantitatively with a self-consistent model. Our 4D-model assumes selfsimilar expansion of a spherical CME geometry that consists of a CME front with density compression and a cavity with density rarefaction, satisfying mass conservation of the total CME and swept-up corona. The model contains 14 free parameters and is fitted to the 2008 March 25 CME event observed with STEREO/A and B. Our model is able to reproduce the observed CME expansion and related EUV dimming during the initial phase from 18:30 UT to 19:00 UT. The CME kinematics can be characterized by a constant acceleration (i.e., a constant magnetic driving force). While the observations of EUVI/A are consistent with a spherical bubble geometry, we detect significant asymmetries and density inhomogeneities with EUVI/B. This new forward-modeling method demonstrates how the observed EUV dimming can be used to model physical parameters of the CME source region, the CME geometry, and CME kinematics.

Keywords. Flares and mass ejections

1 Introduction

It has become a generally agreed concept that the EUV dimming observed during the onset of a *coronal mass ejection* (CME) manifests the coronal mass loss of the CME, and thus we basically expect a one-to-one correlation between the detections of CMEs and EUV dimmings, unless there exist special circumstances. For instance, the CME could originate behind the limb, in which case the EUV dimming is obscured, or the CME could start in the upper corona, where there is little EUV emission because of the gravitational stratification. The latter case would imply very low masses com-

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pared with a CME that originates at the base of the corona, i.e., $\approx 10\%$ at two thermal scale heights. However, there exists a case with an average CME mass that did not leave any footprints behind in EUV (Robbrecht et al. 2009). A statistical study on the simultaneous detection of EUV dimmings and CMEs has recently been performed by Bewsher et al. (2008). This study based on SOHO/CDS and LASCO data confirms a 55% association rate of dimming events with CMEs, and vice versa a 84% association rate of CMEs with dimming events. Some of the non-associated events may be subject to occultation, CME detection sensitivity, or incomplete temperature coverage in EUV and soft X-rays. Perhaps the CME-dimming association rate will reach 100% once the STEREO spacecraft arrive at a separation of 180° and cover all equatorial latitudes of the Sun.

A number of studies have been carried out by using the detection of coronal dimming to identify CME source regions, focusing on transient coronal holes caused by filament eruptions (Rust 1983; Watanabe et al. 1992), EUV dimming at CME onsets (Harrison 1997; Aschwanden et al. 1999), soft X-ray dimming after CMEs (Sterling & Hudson 1997), soft X-ray dimming after a prominence eruption (Gopalswamy & Hanaoka 1998), simultaneous dimming in soft X-rays and EUV during CME launches (Zarro et al. 1999; Harrison & Lyons 2000; Harrison et al. 2003), determinations of CME masses from EUV dimming from spectroscopic data (Harrison & Lyons 2000; Harrison et al. 2003) or from EUV imaging data (Zhukov and Auchere 2004; Aschwanden et al. 2009b). All these studies support the conclusion that dimmings in the corona (either detected in EUV, soft X-rays, or both) are unmistakable signatures of CME launches, and thus can be used vice versa to identify the mutual phenomena.

In this study here we attempt for the first time to model the kinematics of a CME and the resulting EUV dimming quantitatively, which provides us unique physical parameters of the CME source region and on the CME kinematics in the initial acceleration phase.

2 Model Assumptions

The dynamics of a CME can often be characterized by a rapid expansion of a magnetically unstable coronal volume that expands from the lower corona upward into the heliosphere. Different shapes have been used to approximately describe the 3D geometry of a CME, such as a spherical bubble, an ice-cone, a crescent, or a helical flux rope, which expand in a self-similar fashion and approximately maintain the aspect ratio in vertical and horizontal directions during the initial phase of the expansion. Here we develop a four-dimensional (4D=3D+T) model that describes the 3D evolution of the CME geometry in time (T) in terms of 4D electron density distributions $n_e(x,y,z,t)$ that allow us also to predict and forward-fit a corresponding EUV intensity image data cube $I_{EUV}(x,y,t)$ in an observed wavelength.

For the sake of simplicity we start in our model here with the simplest case, assuming: (1) spherical 3D geometry for the CME front and cavity; (2) self-similar expansion in time; (3) density compression in the CME front and adiabatic volume expansion in the CME cavity; (4) mass conservation for the sum of the CME front, cavity, and external coronal volume; (5) hydrostatic (gravitational stratification) or superhydrostatic density scale heights; (6) line-tying condition for the magnetic field at the CME base; and (7) a magnetic driving force that is constant during the time interval of the initial expansion phase. This scenario is consistent with the traditional characterization of a typical CME morphology in three parts, including a CME front (leading edge), a cavity, and a filament (although we do not model the filament part). The expanding CME bubble sweeps up the coronal plasma that appears as a bright rim at the observed "CME front" or leading edge. The interior of the CME bubble exhibits a rapid decrease in electron density due to the adiabatic expansion, which renders the inside of the CME bubble darker in EUV and appears as the observed "CME cavity". The assumption of adiabatic expansion implies no mass and energy exchange across the outer CME boundary, and thus is consistent with the assumption of a low plasma β -parameter in the corona with perfect magnetic confinement, while the CME bubble will become leaking in the outer corona and heliosphere, where the plasma β -parameter exceeds unity (not included in our model here).

3 Analytical Model

A spherical 3D geometry can be characterized by one single free parameter, the radius R of the sphere. The self-similar expansion maintains the spherical shape, so the boundary of the CME bubble can still be parameterized by a single time-dependent radius R(t). The time-dependence of the CME expansion is controlled by magnetic forces, e.g., by a Lorentz force or hoop force. For sake of simplicity we assume a constant force during the initial phase of the CME expansion,

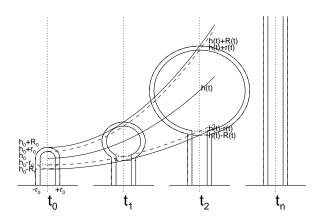


Fig. 1. The definition of the self-similar geometry of the CME model is depicted for four different times, consisting of a cyclidrical base and a spherical shell. The height of the centroid of the spherical CME volume is h(t), the outer radius of the CME sphere is R(t), and the inner radius of the CME front is r(t). These parameters increase quadratically with time. The circular footpoint area of the CME with radius r_0 stays invariant during the self-similar expansion in order to satisfy the line-tying condition of the coronal magnetic field at the footpoints.

which corresponds to a constant acceleration a_R and requires three free parameters (R_0, v_R, a_R) to characterize the radial CME expansion,

$$R(t) = R_0 + v_R(t - t_0) + \frac{1}{2}a_R(t - t_0)^2$$
 for $t > t_0$, (1)

where $R_0 = R(t = t_0)$ is the initial radius at starting time t_0 , v_R is the initial velocity and a_R is the acceleration of the radial expansion.

For the motion of the CME centroid at height h(t) we assume a similar quadratic parameterization,

$$h(t) = h_0 + v_h(t - t_0) + \frac{1}{2}a_h(t - t_0)^2$$
 for $t > t_0$, (2)

where $h_0 = h(t = t_0)$ is the initial height at starting time t_0 , v_h is the initial velocity and a_h is the acceleration of the vertical motion. This parameterization is consistent with a fit to a theoretical MHD simulation of a breakout CME (Lynch et al. 2004) as well as with kinematic fits to observed CMEs (Byrne et al. 2009).

Further we constrain the CME geometry with a cylindrical footpoint area of radius r_0 , which connects from the solar surface to the lowest part of the spherical CME bubble. In order to ensure magnetic line-tying at the footpoints, the CME bubble should always be located above the cyclidrical footpoint base, which requires that the initial height satisfies $h_0 > r_0$ and the acceleration constants are $a_h > a_r$. We visualize the model geometry in Fig. 1.

The time-invariant CME footprint area allows us a simple mass estimate of the CME from the cylindrical volume integrated over a vertical scale height, since the spherical CME bubble will eventually move to large heights with no additional mass gain (at time $t_n \gg t_0$, see right-hand panel in Fig.1).

Assuming adiabatic expansion inside the CME cavity, the electron density in the confined plasma decreases reciprocally to the expanding volume, i.e.,

$$n_e(t) = n_0 \left(\frac{r(t)}{r_0}\right)^{-3} ,$$
 (3)

so it drops with the third power as a function of time from the initial value n_0 (of the average density inside the CME).

For the mass distribution inside the CME we distinguish between a compression region at the outer envelope, containing the CME front, and a rarefaction region in the inside, which is also called CME cavity. We define an average width w_0 of the CME front that is assumed to be approximately constant during the self-similar expansion of the CME. While the radius R(t) demarcates the outer radius of the CME front or the radius of the cavity with r(t),

$$r(t) = R(t) - w_0 , \qquad (4)$$

which has an initial value of $r_0 = r(t = t_0) = R_0 - w_0$. The total volume V_0 of the CME is composed of a spherical volume with radius R(t) and the cylindrical volume beneath the CME with a vertical height of $(h_0 - r_0)$,

$$V(t) = \frac{4}{3}\pi R(t)^3 + \pi R_0^2 [h(t) - R(t)], \qquad (5)$$

which has an initial volume value of V_0 ,

$$V_0 = V(t = t_0) = \frac{4}{3}\pi R_0^3 + \pi R_0^2 [h_0 - R_0].$$
 (6)

The volume of the CME front $V_F(t)$ is essentially the difference between the outer and inner sphere (neglecting the cylindrical base at the footpoint)

$$V_F(t) \approx \frac{4}{3}\pi R(t)^3 - \frac{4}{3}\pi r(t)^3$$
, (7)

while the volume V_C of the cavity is,

$$V_C(t) \approx \frac{4}{3}\pi r(t)^3. \tag{8}$$

We have now to define the time-dependent densities in the CME, for both the CME front, which sweeps up plasma during its expansion, as well as for the CME cavity, which rarifies due to the adiabatic expansion. The total mass $m_E(t)$ of the plasma that is swept up from the external corona in a CME corresponds to the total CME volume V(t) minus the initial volume of the CME cavity,

$$m_E(t) = m_p < n_E > [V(t) - V_C(t = t_0)] = m_p < n_E > \frac{4}{3}\pi [R(t)^3 - r_0^3]$$
(9)

where m_p is the mass of the hydrogen atom and $< n_E >$ is the electron density in the external corona averaged over the

CME volume. The same mass has to be contained inside the volume V_F of the CME front,

$$m_E(t) = m_p < n_F > V_F(t)$$

= $m_p < n_F > \frac{4}{3}\pi[R(t)^3 - r(t)^3]$, (10)

Thus, mass conservation yields a ratio of the average electron density $< n_F >$ in the CME front and the average external density $< n_E >$ of

$$q_{n,front}(t) = \frac{\langle n_F \rangle}{\langle n_E \rangle} = \frac{R(t)^3 - r_0^3}{R(t)^3 - r(t)^3} \,. \tag{11}$$

This density ratio amounts to unity at the initial time, i.e., $q_n(t=t_0)=1$ and monotonically increases with time. The maximum value of the density jump in MHD shocks derived from the *Rankine-Hugoniot relations* (e.g., Priest 1982) is theoretically $q_{n,max}=4$. Fast CMEs are expected to be supersonic and will have a higher compression factor at the CME front than slower CMEs. Thus we keep the maximum compression factor $q_{n,max}$ as a free parameter, keeping in mind that physically meaningful solutions should be in the range of $1 \lesssim q_{n,max} \lesssim 4$. Since we prescribe both the width w_0 of the CME front as well as a maximum density compression ratio $q_{n,max}$ we obtain a definition of the critical value $\rho(t)$ for the cavity radius r(t) when the prescribed maximum density compression $q_{n,max}$ is reached (using Eq. 11),

$$q_{n,max} = \frac{R(t)^3 - r_0^3}{R(t)^3 - \rho(t)^3},$$
(12)

which yields the critical radius $\rho(t)$,

$$\rho(t) = \left[R(t)^3 - \frac{(R(t)^3 - r_0^3)}{q_{n,max}} \right]^{1/3} . \tag{13}$$

Therefore, only plasma outside this critical radius $\rho(t)$ can be compressed in the CME front, while the plasma inside this critical radius dilutes by adiabatic expansion and forms the cavity, yielding an average density ratio $q_{n,cav}$ inside the cavity (according to Eq. 3),

$$q_{n,cav}(t) = \frac{n_{e,cav}(t)}{n_0} = \begin{cases} \left[r_0/\rho(t) \right]^3 & \text{for } \rho(t) \ge r(t) \\ \left[r_0/r(t) \right]^3 & \text{for } \rho(t) < r(t) \end{cases} . (14)$$

Our numerical model of a spherical CME expansion has a total of 14 free parameters: 3 positional parameters (the heliographic coordinates (l,b) and height h_0 of the initial CME centroid position), 5 kinematic parameters (starting time t_0 , velocities v_h, v_R , accelerations a_h, a_R), 2 geometric parameters (initial radius r_0 and width w_0 of the CME front), and 4 physical parameters (coronal base density n_0 , maximum density compression factor $q_{n,max}$ in the CME front, the mean coronal temperature T_0 at the observed wavelength filter), and a vertical density scale height factor (or superhydrostaticity factor) q_λ that expresses the ratio of the effective density scale height to the hydrostatic scale height

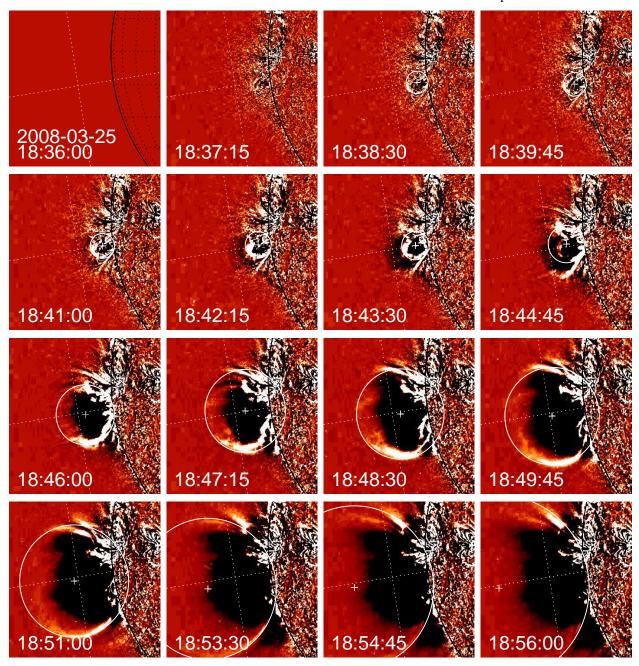


Fig. 2. Partial EUVI base-difference images from STEREO/A 171 Å during the time interval of 2008 Mar 25, 18:36-18:56 UT (with the initial image at 18:36 UT subtracted). The envelope of the lateral CME front is fitted with a circle. The dashed lines mark the locations where cross-sectional brightness profiles are extracted for fitting, shown in Fig. 5.

at temperature T_0). The temperature T_0 defines the hydrostatic scale height λ_T of the corona in the observed temperature range, which enters the definition of the effective density scale height λ (e.g., Eq. [3.1.16] in Aschwanden 2004),

$$\lambda = \lambda_T q_{\lambda} = 47 \left(\frac{T_0}{1 \text{ MK}}\right) q_{\lambda} \quad [\text{Mm}] .$$
 (15)

Thus, assuming an exponentially stratified atmosphere (Eq. 15), a density compression factor $q_n(t) \leq q_{n,max}$ in

the CME front (Eq. 12), and adiabatic expansion inside the CME cavity (Eq. 14), we have the following time-dependent 3D density model:

$$n_e(h,t) = n_0 \exp(-h/\lambda) \times \begin{cases} 1 & \text{for } d > R(t) \\ q_{n,front}(t) & \text{for } r(t) < d < R(t) \\ q_{n,cav}(t) & \text{for } d < r(t) \end{cases}$$
(16)

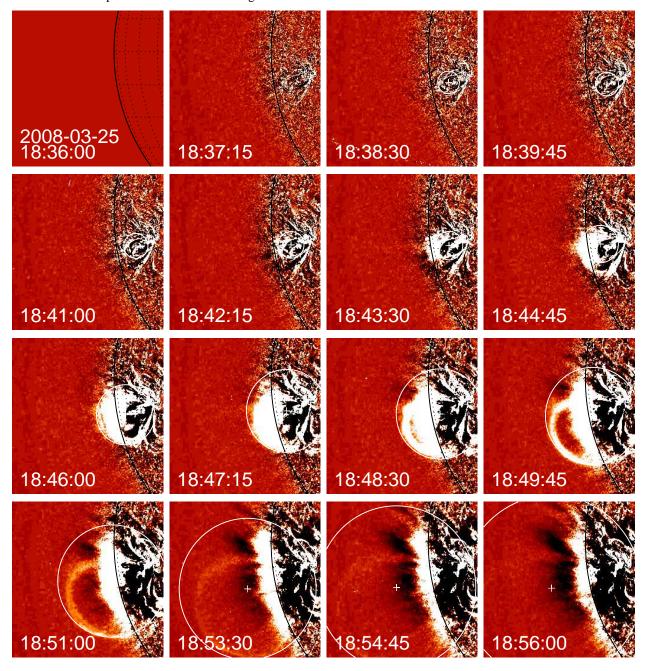


Fig. 3. EUVI base-difference images from STEREO/B 171 Å in similar representation as for STEREO/A in Fig. 2. Note that the CME origin is in the front of the solar disk in EUVI/B, while it is behind the east limb for EUVI/A.

where d is the distance of an arbitrary location with 3D coordinates (x, y, z) to the instantaneous center position $[x_0(t), y_0(t), z_0(t)]$ of the CME,

$$d = \sqrt{[x - x_0(t)]^2 + [y - y_0(t)]^2 + [z - z_0(t)]^2}, \qquad (17)$$

which is located at height h(t) vertically above the heliographic position (l,b).

4 Forward-Fitting of Model to Observations

4.1 STEREO/EUVI Observations

One CME event observed with STEREO that appears as a spherically expanding shell, and thus is most suitable for fitting with our analytical model, is the 2008-Mar-25, 18:30 UT, event. This CME occurred near the East limb for spacecraft STEREO/Ahead, and was observed on the frontside of the solar disk with spacecraft STEREO/Behind. Some

preliminary analysis of this event regarding CME expansion and EUV dimming can be found in Aschwanden et al. (2009a), the CME mass was determined in white light with STEREO/COR-2 (Colaninno and Vourlidas 2009) and with STEREO/EUVI (Aschwanden et al. 2009b), and the 3D geometry was modeled with forward-fitting of various geometric models to the white-light observations (Thernisien et al. 2009; Temmer et al. 2009; Maloney et al. 2009; Mierla et al. 2009a,b). While most previous studies model the white-light emission of this CME, typically a few solar radii away from the Sun, our model applies directly to the CME source region in the lower corona, as observed in EUV. We follow the method outlined in Aschwanden et al. (2009a). Our model also quantifies the geometry and kinematics of the CME, as well as the EUV dimming associated with the launch of the CME.

4.2 Fitting of Positional Parameters

Figures 2 and 3 show sequences of 16 (partial) EUV images, simultaneously observed with STEREO/A and B with a cadence of 75 s during the time interval of 18:36-18:56 UT on 2008-Mar-25. In order to determine the positional parameters of the CME as a function of time we trace the outer envelope of the CME bubble (by visual clicking of 3 points) in each image and each spacecraft and fit a circle through the 3 points in each image. The selected points for fitting the position of the CME bubble were generally chosen in the brightest features of the lateral CME flanks, but could not always been traced unambiguously in cases with multiple flank features. In those cases we traced the features that were closest to a continuously expanding solution. The radii and ypositions of the circular fits are fully constrained from the STEREO/A images, so that only the x-positions of the centroid of the spherical shell need to be fitted in the epipolar STEREO/B images. We note that the fits of the CME bubble roughly agree with the envelopes of the difference flux in the STEREO/B images initially (up to 18:48 UT), while there is a discrepancy later on. Apparently the CME has a more complex geometry than our spherical bubble model, which needs to be investigated further.

This procedure yields the CME centroid positions $[x_A(t_i),y_A(t_i)]$ and $[x_B(t_i),y_B(t_i)]$ for the time sequence $t_i,i=1,...,16$. The images in Fig. 2 and 3 are displayed as a baseline difference (by subtracting a pre-CME image at 18:36 UT) to enhance the contrast of the CME edge. The circular fits to the CME outer boundaries are overlayed in Fig. 2 and 3. Both images have been coaligned and rotated into epipolar coordinates (Inhester et al. 2006), so that the y-coordinates of a corresponding feature are identical in the spacecraft A and B images, while the x-coordinates differ according to the spacecraft separation angle α_{sep} , which amounts to $\alpha_{sep}=47.17^\circ$ at the time of the CME event. The epipolar coordinates measured from both spacecraft are

then related to the heliographic longitude l, latitude b, and distance r_c from Sun center as follows,

$$x_A = r_c \cos(b) \sin(l_A)$$

$$y_A = y_B = r_c \sin(b)$$

$$x_B = r_c \cos(b) \sin(l_A + \alpha_{sep})$$
(18)

which can directly be solved to obtain the spherical (epipolar) coordinates (l_A, b, r_c) ,

$$l_A = \arctan\left(\sin\left(\alpha_{sep}\right)/(x_A/x_B - \cos\left(\alpha_{sep}\right)\right)$$

$$r_c = \sqrt{y_A^2 + [x_A/\sin\left(l_A\right)]^2}$$

$$b = \arcsin\left(y_A/r_c\right)$$
(19)

Therefore, using stereoscopic triangulation, we can directly determine the spherical coordinates $(l_i, b_i, r_{c,i}), i = 1, ..., 16$ for all 16 time frames, as well as obtain the CME curvature radii $R(t_i)$ from the circular fits to the CMEs. We plot the so obtained observables $l_A(t)$, b(t), R(t), and h(t) = $r_c(t) - R_{\odot}$ in Fig. 3 and determine our model parameters l and b from the averages. We obtain a longitude of $l_A = -102.4^{\circ} \pm 0.9^{\circ}$ (for spacecraft STEREO/A), $l_B =$ $l_A + \alpha_{sep} = -54.9^{\circ} \pm 0.9^{\circ}$ (for spacecraft STEREO/B), and a latitude $b=-8.8^{\circ}\pm0.6^{\circ}$. Thus, the CME source region is clearly occulted for STEREO/A. These epipolar coordinates can be rotated into an ecliptic coordinate system by the tilt angle $\beta_{AB} = 2.66^{\circ}$ of the spacecraft A/B plane. Viewed from Earth, the longitude is approximately $l_E \approx -102.4 + \alpha_{sep}/2 \approx -78.8^{\circ}$. Thus, the CME source region is 12° behind the East limb when seen from Earth. This explains why the EUV dimming is seen uncontaminted from post-flare loops, which are seen by STEREO/B but hidden for STEREO/A.

4.3 Fitting of Kinematic Parameters

We plot also the observables h(t) and R(t) in Fig. 4 and determine the model parameters h_0 , R_0 , a_h , a_R by fitting the quadratic functions R(t) (Eq. 1) and h(t) (Eq. 2), for which we obtain the starting time $t_0=18.64$ hrs (18:38 UT), the initial CME radius $R_0=45$ Mm, the initial height $h_0=45$ Mm, and the accelerations $a_R=0.54$ km s⁻² for the CME radius expansion, and $a_h=0.52$ km s⁻² for the height motion. The initial velocity is found to be negligible ($v_R\approx 0$ and $v_h\approx 0$). We estimate the accuracy of the acceleration values to be of order $\approx 10\%$, based on the uncertainty of defining the leading edge of the CME. Thus, we determined 9 out of the 14 free parameters of our model sofar.

Note that the acceleration measured here refers to the very origin of the CME in low coronal heights of $\lesssim 0.6$ solar radii observed in EUVI data. The acceleration is expected to be initially high and to rapidly decline further out, when the driving magnetic forces decrease at large altitudes. This explains why our values for the acceleration in low coronal heights are significantly higher than measured further out in the heliosphere, typically in the order of tens of m s⁻¹ in height ranges of 5-22 solar radii,

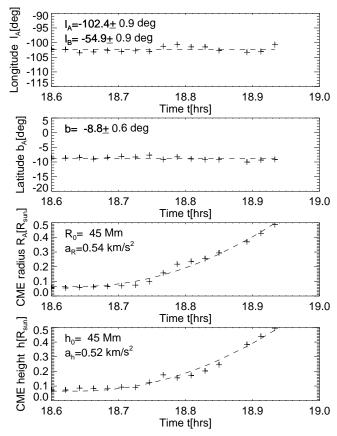


Fig. 4. Measurements of the heliographic longitude $l_A(t)$ (top panel) and latitude b(t) (second panel) of the CME centroid, the radius R(t) of the CME sphere (third panel), and CME centroid height h(t) (bottom). The average values are $l_A=-102.4^\circ\pm0.9^\circ$ and $b=-8.8^\circ\pm0.9^\circ$ for the heliographic position. The CME radius R(t) and height h(t) are fitted with quadratic functions (dashed curves), yielding the constants $t_0=18.64$ hrs (18:38 UT), $R_0=45$ Mm, $h_0=45$ Mm, and accelerations $a_R=0.54$ km s⁻² and $a_h=0.52$ km s⁻² (see Eqs. 1-2).

as measured with SOHO/LASCO. SOHO/LASCO reported even a slightly negative acceleration at altitutes of 5-22 solar radii. The driving magnetic forces that accelerate a CME are clearly confined to much lower altitudes.

4.4 Fitting of Geometric Parameters

We model the 3D geometry of the CME bubble with the time-dependent radius R(t) and the width w_0 of the CME compression region. In Fig. 5 we show cross-sectional EUV brightness profiles across the CME in horizontal direction (parallel to the solar surface) and in vertical direction for the EUVI/A 171 Å observations (indicated with dotted lines in Fig. 2). These baseline-subtracted profiles clearly show a progressive dimming with a propagating bright rim at the CME boundary, which corresponds to the density compression region at the lateral expansion fronts of the CME. The bright rims are clearly visible in the images during

18:46–18:56 UT shown in Fig. 2. The average width of the observed bright rims is $w_0 \approx 10$ Mm, a value we adopt in our model.

4.5 Fitting of Physical Parameters

Finally we are left with the four physical parameters T_0, q_λ, n_0 , and $q_{n,max}$. Since we show here only data obtained with the 171 Å filter, the mean temperature is constrained by the peak temperature of the instrumental EUVI response function, which is at $T_0=0.96$ MK. This constrains the thermal scale height to $\lambda_T=47,000\times0.96=45,000$ km.

The remaining free parameters q_{λ} , n_0 , and $q_{n,max}$ need to be determined from best-fit solutions by forward-fitting of simulated EUV brightness images (or profiles, as shown in Fig. 5) to observed EUV brightness images (or profiles). The EUV emission measure in each pixel position (x,y) can be computed by line-of-sight integration along the z-axis in our 3D density cube $n_e(x,y,z)$ per pixel area dA for each time t_i .

$$EM(x,y) = \int n_e^2(x,y,z)dzdA, \qquad (20)$$

from which the intensity $I_{171}(x,y)$ in the model image in units of DN s⁻¹ can be directly obtained by multiplying with the instrumental response function $R_{171}(T)$ of the 171 Å filter

$$I_{171}(x,y) = \int EM(x,y)R_{171}(T)dT \approx EM(x,y)R_{171}(T_0)\Delta T_{171} ,$$
 (21)

where $R_{171}=3632\times 10^{-44}~{\rm DN~s^{-1}~cm^3~MK^{-1}}$ and the FWHM of the 171 filter is $\Delta T_{171}=1.25-0.51=0.74$ MK.

In Fig. 6 we show best-fit solutions of horizontal and vertical brightness profiles. The absolute flux level is proportional to the coronal base density squared, which we obtain by minimizing the mean flux difference between simulated and observed flux profiles. We obtain a best-fit value of $n_0=6.5\times10^8~{\rm cm}^{-3}$. The super-hydrostaticity factor is most sensitive to the vertical flux profile (Fig. 5, right-hand side panels), for which we find a best-fit value of $q_\lambda=1.45$. Thus, the average density scale height in the CME region is slightly super-hydrostatic, as expected for dynamic processes. These values are typical for quiet-Sun corona and active region conditions (see Figs. 6 and 10 in Aschwanden and Acton 2001).

The last free parameter, the maximum density compression factor $q_{n,max}$, affects mostly the brightness of the CME rims. Fitting the brightness excess at the CME rims at those times where bright rims are visible are consistent with a value of $q_{n,max} \approx 2$.

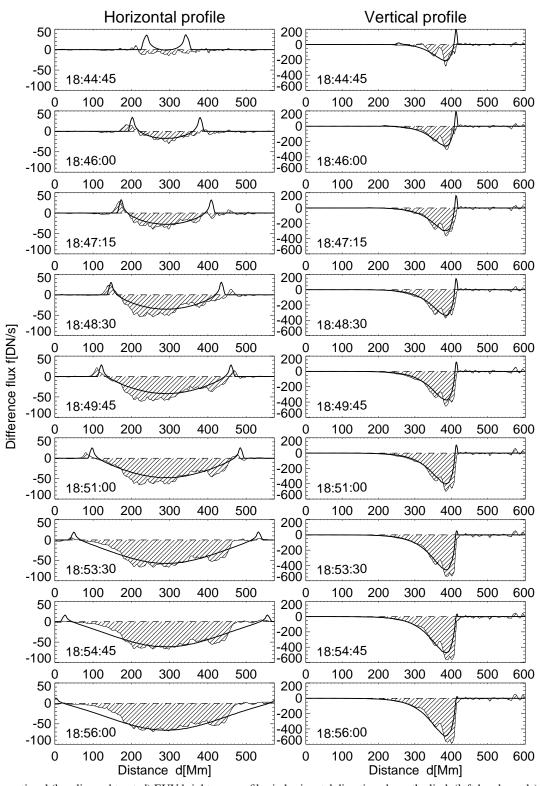


Fig. 5. Cross-sectional (baseline-subtracted) EUV brightness profiles in horizontal direction above the limb (left-hand panels) and in vertical direction through the centroid of the dimming region (right-hand panels), as marked with dashed lines in Fig. 2, for the 9 images during 18:44:56–18:56:00 UT, for EUVI/A, 171 Å. The observed dimming is represented with hatched areas, while the best-fit model profiles are plotted with thick linestyle.

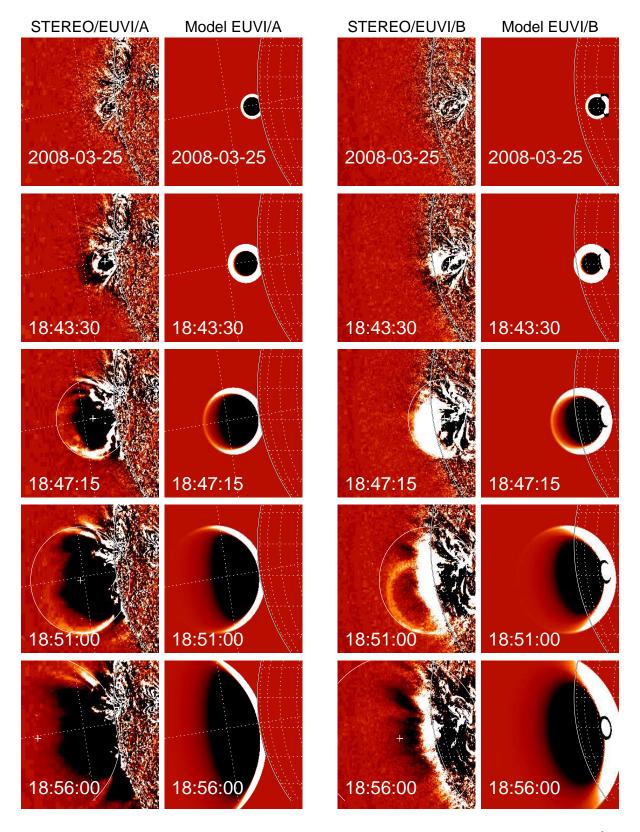


Fig. 6. Comparison of observed and simulated EUVI base-difference images at 5 times for the observations of STEREO/A 171 Å (left two columns) and STEREO/B 171 Å(right two columns). The pre-CME image at 18:36 UT was subtracted in these base-difference images.

Table 1. Model parameters

Parameter	Best-fit value
Spacecraft separation angle	$\alpha_{sep} = 47.17^{\circ}$
Spacecraft plane angle to ecliptic	$\beta_{AB} = 2.66^{\circ}$
Heliographic longitude A	$l_A = -102.4^{\circ} \pm 0.9^{\circ}$
Heliographic longitude B	$l_B = -54.9^{\circ} \pm 0.9^{\circ}$
Heliographic longitude Earth	$l_E = -78.8^{\circ} \pm 0.9^{\circ}$
Heliographic latitude A,B	$= -8.8^{\circ} \pm 0.6^{\circ}$
Start time of acceleration	t ₀ =2008-Mar-25 18:38 UT
Start time of modeling	t ₁ =2008-Mar-25 18:36 UT
End time of modeling	t ₁ =2008-Mar-25 18:56 UT
Initial height of CME center	$R_0 = 45 \text{ Mm}$
Initial radius of CME	$h_0 = 45 \text{ Mm}$
Width of CME front	$w_0 \approx 10 \ \mathrm{Mm}$
Acceleration of vertical motion	$a_h = 0.52 \text{ m s}^{-2}$
Acceleration of radial expansion	$a_R = 0.54 \mathrm{m s^{-2}}$
Inital vertical velocity	$v_h \approx 0 \text{ m s}^{-1}$
Inital expansion velocity	$v_R \approx 0 \text{ m s}^{-1}$
Maximum density compression	$q_{n,max} \approx 2.0$
Corona/CME base density	$n_0 = 6.5 \times 10^8 \text{ cm}^{-3}$
Super-hydrostaticity factor	$q_{\lambda} = 1.45$
Mean Temperature (171 filter)	$T_0 = 0.96 \text{ MK}$
Temperature width (171 filter)	$\Delta T = \pm 0.37 \text{ MK}$

4.6 Comparison of Numerical Simulations with Observations

After we constrained all 14 free parameters (listed in Table 1) of our analytical 4D model by fitting some observables, such as measured coordinates (Fig. 4) and cross-sectional horizontal and vertical brightness profiles (Fig. 5), we are now in the position to inter-compare the numerically simulated images with the observed images, as shown in Fig. 6 for 5 selected times, for both the STEREO/A and B spacecraft. The comparison exhibits a good match for the extent of the dimming region the the bright lateral rims, both extending over about 1.5 thermal scale heights above the solar surface. The base-difference images of EUVI/A reveal a fairly symmetric CME (as the model is by design), surrounded by spherical bright rims at the northern and southern CME boundaries (as the model is able to reproduce it).

The model, however, is less in agreement with the observed EUVI/B images. The extent of the EUV dimming region matches relatively exactly, although the observed dimming region is somewhat cluttered with bright postflare loops that appear in the aftermath of the CME, which are mostly hidden in the EUVI/A observations. The biggest discrepancy between the model and the EUVI/B observations is the location of the brightest rim of the CME boundary. The combination of projection effects and gravitational stratification predict a brighter rim on the west side, where we look through a longer and denser column depth tangentially to the CME bubble, which is not apparent in the observations of

EUVI/B. Instead, there is more bright emission just above the eastern limb that cannot be reproduced by the model. Apparently there exists stronger density compression on the eastern side of the CME bubble than the model predicts. Another inconsistency is the bright loop seen in EUVI/B at 18:51 UT, which does not match the surface of the modeled CME sphere as constrained by EUVI/A. Apparently, there are substantial deviations from a spherically symmetric CME bubble model that are visible in EUVI/B but not in EUVI/A. Perhaps a flux rope model could better fit the observations than a spherical shell model. These discrepancies between the observations and our simple first-cut model provide specific constraints for a more complex model (with more free parameters) that includes inhomogeneities in the density distribution of the CME.

4.7 Estimate of the CME Mass

Our model allows us, in principle, to estimate the CME mass by integrating the density $n_e(x,y,z,t)$ over the entire CME sphere, which is of course growing with time, but expected to converge to a maximum value once the CME expands far out into the heliosphere. A simple lower limit can analytically be obtained by integrating the density in the cylindrical volume above the footpoint area,

$$M_{CME} = m_p \int n_e(x,y,z) dV_{CME} \approx m_p \pi R_0^2 n_0 \lambda_T q_\lambda$$
 .(22)

From our best-fit values $R_0=45$ Mm, $q_\lambda=1.45$, $n0=6.5\times 10^8$ cm⁻³ and the thermal scale height of $\lambda_T=47$ Mm, we obtain a lower limit of $M_{CME}\geq 0.47\times 10^{15}$ g. However, this CME appears to expand in a cone-like fashion in the lowest density scale height, so the total volume and mass is likely to be about a factor of ≈ 2 higher. Moreover, the mass detected in 171 Å amounts only to about a third of the total CME mass (Aschwanden et al. 2009b), so a more realistic estimate of the total CME mass is about a factor 6 higher than our lower limit, i.e., $M_{CME}\approx 3\times 10^{15}$ g, which brings it into the ballpark of previous CME mass determinations of this particular event, i.e., $m_{CME}=2.9\times 10^{15}$ g from STEREO/COR-2 white-light observations (Colaninno and Vourlidas 2009), or $m_{CME}=(4.3\pm 1.4)\times 10^{15}$ g from STEREO/EUVI observations (Aschwanden et al. 2009b).

5 Conclusions

We developed an analytical 4D model that simulates the CME expansion and EUV dimming in form of a time sequence of EUV images that can directly be fitted to stereoscopic observations of STEREO/EUVI. The dynamic evolution of the CME is characterized by a self-similar adiabatic expansion of a spherical CME shell, containing a bright front with density compression and a cavity with density rarefaction, satisfying mass conservation of the CME and ambient

corona. We forward-fitted this model to STEREO/EUVI observations of the CME event of 2008-Mar-25 and obtained the following results:

- 1. The model is able to track the true 3D motion and expansion of the CME by stereoscopic triangulation and yields an acceleration of $a \approx 0.54 \text{ m s}^{-2}$ for both the vertical centroid motion and radial expansion during the first half hour after CME launch.
- 2. Fitting the EUV dimming region of the model to the data mostly constrains the coronal base density in the CME region ($n_0 = 6.5 \times 10^8 \text{ cm}^{-3}$) and the density scale height, which was found to be super-hydrostatic by a factor of $q_{\lambda} = 1.45$.
- 3. The average CME expansion speed during the first 10 minutes is approximately $< v > \approx 400 \ \mathrm{km \ s^{-1}}$, similar to the propagation speeds measured for EIT waves in the initial phase (i.e., $v \approx 460 \ \mathrm{km \ s^{-1}}$, Veronig et al. 2008; $v \approx 475 \ \mathrm{km \ s^{-1}}$, Long et al. 2008; $v \approx 250 \ \mathrm{km \ s^{-1}}$, Patsourakos et al. 2009), and thus the CME expansion speed seems to be closely related to the associated propagation kinematics of EIT waves.
- 4. The derived base density, scale height, and footpoint area constrain the CME mass, but accurate estimates require a more complete temperature coverage with other EUV filters (e.g., see Aschwanden et al. 2009b).
- The width and density compression factor of the CME front are also constrained by our model, but accurate values require a perfectly homogeneous CME shell.
- 6. While the spherical shell geometry reproduces the EUVI/A observations well, significant deviations are noted in the EUVI/B observations, indicating substantial inhomogeneities in the CME shell, possibly requiring a hybrid model of bubble and flux rope geometries.

The most important conclusion of this modeling study is that EUV dimming can be understood in a quantitative manner and that it provides a direct measurement of the coronal mass loss of a CME. This exercise has shown that the spherical shell geometry can reproduce a number of observed features of an evolving CME, which constrains the physical and kinematic parameters of the initial phase of the CME launch, but reveals also significant deviations that require a modification of the idealized homogeneous spherical shell model. The method of analytical 4D models with forward-fitting to stereoscopic EUV images appears to be a promising tool to investigate quantitatively the kinematics of CMEs. Combining with simultaneous magnetic or MHD modeling may further constrain the physical parameters and ultimately provide the capability to discriminate between different theoretical CME models. Full 4D modeling of the initial CME expansion may also provide a self-consistent treatment of EIT waves and CME expansion (e.g., Chen et al. 2005), for which we find similar kinematic parameters.

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