



QUASI-PERIODIC PULSATIONS DURING THE IMPULSIVE AND DECAY PHASES OF AN X-CLASS FLARE

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ABSTRACT

Quasi-periodic pulsations (QPPs) are often observed in X-ray emission from solar flares. To date, it is unclear what their physical origins are. Here, we present a multi-instrument investigation of the nature of QPP during the impulsive and decay phases of the X1.0 flare of 2013 October 28. We focus on the character of the fine structure pulsations evident in the soft X-ray (SXR) time derivatives and compare this variability with structure across multiple wavelengths including hard X-ray and microwave emission. We find that during the impulsive phase of the flare, high correlations between pulsations in the thermal and non-thermal emissions are seen. A characteristic timescale of ~ 20 s is observed in all channels and a second timescale of ~ 55 s is observed in the non-thermal emissions. SXR pulsations are seen to persist into the decay phase of this flare, up to 20 minutes after the non-thermal emission has ceased. We find that these decay phase thermal pulsations have very small amplitude and show an increase in characteristic timescale from ~ 40 s up to ~ 70 s. We interpret the bursty nature of the co-existing multi-wavelength QPPs during the impulsive phase in terms of episodic particle acceleration and plasma heating. The persistent thermal decay phase QPPs are most likely connected with compressive magnetohydrodynamic processes in the post-flare loops such as the fast sausage mode or the vertical kink mode.

Key words: Sun: flares – Sun: oscillations – Sun: X-rays, gamma rays

1. INTRODUCTION

During a solar flare, the X-ray flux from the Sun can increase by several orders of magnitude and be accompanied by pulsations in the flare emission. These pulsations, known as quasi-periodic pulsations (QPPs), are variations of flux as a function of time. Their nature has been examined in many previous studies of both solar (e.g., Parks & Winckler 1969; Kane et al. 1983; Asai et al. 2001; Fleishman et al. 2008; Nakariakov & Melnikov 2009; Reznikova & Shibasaki 2011; Li et al. 2015) and stellar (e.g., Balona et al. 2015; Pugh et al. 2016) observations. In a typical event, the emission from a solar flare is seen to pulsate with a characteristic timescale ranging from ≤ 1 s up to several minutes. QPPs are commonly observed during the impulsive phase of solar flares and have been reported in a wide range of wavelengths from radio and microwaves to hard X-rays (HXR) and γ -rays.

Two main interpretations outlined in a recent review by Nakariakov & Melnikov (2009) have been pursued in order to understand QPPs. These are that the observed flux variations are driven either by magnetohydrodynamic (MHD) wave behavior in the corona, or by periodic or “bursty” energy releases from the coronal magnetic field.

MHD oscillations are known to be supported in the corona (Edwin & Roberts 1982, 1983), and flare-generated MHD oscillations have been observationally identified in coronal loops (Aschwanden et al. 1999a; Nakariakov et al. 1999). Various MHD wave modes can alter physical plasma parameters and produce the quasi-periodic behavior in flaring light curves (Nakariakov & Melnikov 2009). These wave modes can modulate the emission directly, affect the dynamics of charged particles, or periodically trigger magnetic reconnection (Nakariakov & Zimovets 2011). However, it remains a challenge to interpret QPPs purely in terms of linear MHD

oscillation theory given the large modulation depths observed in light curves, along with the geometrical evolution that occurs during the impulsive phase of flares.

A second interpretation of QPPs is that the pulsations are a direct result of “bursty” regimes of energy release, in particular magnetic reconnection. Early magnetotail studies suggested that magnetic reconnection can happen in an episodic fashion (Coppi et al. 1966; Schindler 1974), with subsequent observations supporting this view (Hones et al. 1976). In coronal conditions, recent numerical models have shown that magnetic reconnection can occur in a repetitive regime (e.g., Kliem et al. 2000; Drake et al. 2006; Linton & Longcope 2006; Guidoni et al. 2016). Repeated episodes of magnetic reconnection itself could account for the modulation of emission in many different wavelengths. It could explain QPP observed in the non-thermal emission due to changing particle acceleration rates. Variations at other wavelengths such as soft X-ray (SXR) and EUV would then be explained by fluctuations in plasma heating.

The majority of previous flare QPP studies have focused on pulsations observed in emission associated with non-thermal electrons such as HXR and microwave observations. This is due to the large modulation depths observed in this type of emission, especially in the impulsive phase. Recently, however, it has been shown that fine structure pulsations are also evident in the SXR emission (Dolla et al. 2012; Simões et al. 2015; Dennis et al. 2016). The nature of these pulsations in thermal emission remains to be studied in detail, and comparisons across multiple wavelengths are required to improve our understanding of the QPP phenomenon.

In this Letter, we investigate the nature of these X-ray pulsations in a multi-instrument analysis of a *GOES* X-class flare, paying particular attention to the fine structure observed during the impulsive and decay phases.

2. OBSERVATIONS

Our investigation focuses on pulsations observed in the *GOES* X1.0 flare on 2013 October 28 (SOL2013-10-28). Examining 10 wavelength bands on 5 different instruments, our data are from high-cadence (≤ 2 s) observations of X-rays (both hard and soft) and microwave emissions from both ground-based and space-borne instruments. Pulsations in the thermal emission were observed using both channels (1–8 Å and 0.5–4 Å) of the X-ray Sensor on board the *Geostationary Operational Environment Satellite* (*GOES-15*), the Zirconium channel (< 2 nm + 6–20 nm) of the Large Yield Radiometer (LYRA; Dominique et al. 2013) on the *Project for On-Board Autonomy* (PROBA2), and the SXR channel (0.1–7 nm) of the Extreme Ultraviolet Spectrophotometer (ESP), which is part of the EUV Experiment (Woods et al. 2012) on board the *Solar Dynamic Observatory* (*SDO*). We also utilized X-ray observations provided by the *Fermi* Gamma-ray Burst Monitor (GBM; Meegan et al. 2009), focusing on emissions in the 4–100 keV range. Observations at 17 and 34 GHz from the Nobeyama Radioheliograph (NoRH; Nakajima et al. 1994) are additionally investigated.

The excellent signal-to-noise ratio of the *GOES-15* instrument allows us to study the derivative of a solar flare time series in detail, revealing a wealth of pulsations and fine structure (Simões et al. 2015). It is now certain that this type of variability is real and of solar origin based on comparisons with simultaneous observations of different events made with both *GOES* 13 and 15⁶, and with comparison with other instruments such as LYRA and ESP (Dolla et al. 2012).

Figure 1(a) gives an overview of the light curves under investigation. The impulsive nature of the flare is displayed by the non-thermal emission such as *Fermi* 25–100 keV and NoRH 17 and 34 GHz. This impulsive behavior begins at 01:55:00 UT and continues with eight distinctive peaks of growing intensity. The thermal emission seems not to show an impulsive phase signature in Figure 1(a), with the rise and decay profiles looking relatively smooth with each channel peaking at different times depending on their temperature response. However, Figure 1(b) shows the time derivative of the SXR channels. The fine-scale structure of the SXR emission is visually evident with a similar structure to the HXR light curves in Figure 1(a).

The non-thermal HXR and microwave pulsations cease at around 02:00:30 UT. After this time the correlation between *GOES*, LYRA Zr, and ESP 0.1–7 nm become less evident, but pulsations continue into the decay phase in both *GOES* channels. To investigate this further, the flare was broken into two phases—the impulsive phase: 01:55:00–02:00:30 UT and the gradual phase: 02:00:30–02:20:00 UT.

3. RESULTS

3.1. Impulsive Phase QPPs

The impulsive nature of this flare is seen from the onset of pulsations at 01:55:00 UT until 02:00:30 UT (marked within the red vertical lines in Figure 1). This “bursty” QPP regime is seen clearly in the non-thermal emissions with large modulation depths in the light curves, up to 80% in the 50–100 keV. The HXR spectra displays a soft-hard-soft evolution of these

modulated individual peaks. The modulation depth is calculated as the ratio of the amplitude of the pulsations to the overall trend of the light curve. The maximum modulation depth is given for all channels in Table 1. Each peak of a non-thermal pulsation is numbered in Figure 1 for comparison with the SXR derivatives. Notably, some pulsations in the SXR derivative appear to peak before the pulsations in the HXR, such as peaks 2, 3, 6, and 7. This seems inconsistent with the Neupert effect (Neupert 1968; Dennis & Zarro 1993), in which we would expect the SXR derivatives to peak simultaneously with the HXR if we are to believe that the same electrons that produce the HXR also heat the plasma that produces the SXR.

In order to compare the short-timescale variability, the gradual varying trend of the light curves was removed by subtracting a smoothed time series from the original time series. The smoothed time series was calculated by taking a boxcar average of the original time series using a full width window of 30 s. This timescale window was chosen to highlight small-scale fluctuations. For the thermal channels we used the original SXR light curves, rather than the derivatives. Subsampling to the longest-cadence instrument (*GOES*), cross-correlation coefficients of each waveband with respect to *GOES* 1–8 Å are presented in Table 1. We find that on these short timescales, there is minimal delay between all wavebands.

To search for characteristic timescales during the impulsive phase, wavelet analysis was employed using a Morlet wavelet. It was recently pointed out that the Fourier power spectra of many flare time series tends to approximate a power law with negative index that tails off to a constant at higher frequencies, and that this must be taken into account when searching for periodicity. Gruber et al. (2011) and Inglis et al. (2015) demonstrated the dangers of assuming a flat power spectrum when studying oscillatory signatures in flare time series. They found that what may look like an oscillation is often not statistically distinguishable from a fluctuation in a power-law-like power spectrum. Following this, we test for the significance of enhanced power assuming a background power-law spectrum, estimated for each individual time series using an autoregressive AR(1) model as described in Torrence & Compo (1998). The power-law slope that resulted from this is given in Table 1 for each time series.

Figure 2 shows the results of the wavelet analysis for the different time series spanning thermal and non-thermal emission. Figures 2(a)–(c) show wavelet analysis of ESP 0.1–7 nm, *GOES* 1–8 Å, and GBM 50–100 keV, respectively. Each shows the time series under investigation, the wavelet power spectrum, and the global time-averaged wavelet spectrum. During the impulsive phase, enhanced power is broadband with no narrow feature of a single timescale present. The dotted line in the global power spectrum is at the 99.7% significance level above the power-law background model. We find that in all channels our time-averaged global power spectrum shows a characteristic timescale at ~ 20 s. A second peak is seen at ~ 55 s but only reaches above the 99.7% significance level in the non-thermal channels. The range of characteristic timescales for each channel this is above the significance level are listed in Table 1.

3.2. Decay Phase QPP

The gradual phase of the flare has a different nature to the highly correlated “bursty” qualities of the impulsive phase.

⁶ *RHESSI* Nugget #262 *Fine Structure in Flare Soft X-ray Light Curves* (B. R. Dennis & K. Tolbert).

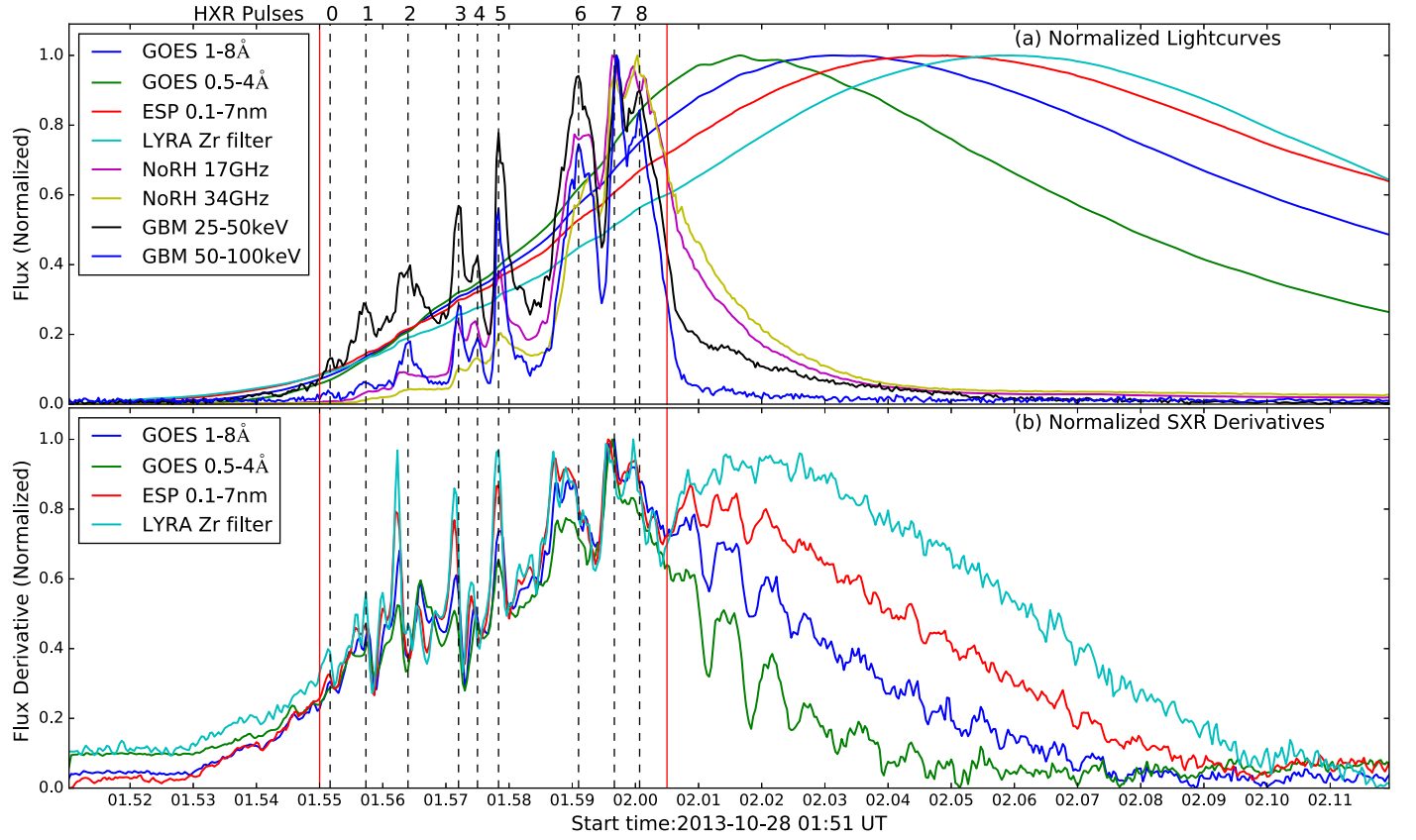


Figure 1. (a) Normalized light curves from different instruments for the flare of 2013 October 28. Detector Na 16 was used for GBM. (b) Derivatives of the soft X-ray channels. The vertical red lines show the start and end of the impulsive phase, and the dashed lines show the timing of the HXR pulses.

Table 1
Summary of Characteristics of Pulsations across Multiple Wavelengths during the Impulsive Phase

Instrument	Corr. Coef.	Modulation (%)	Power-law Index	Significant Timescale Range(s)
<i>GOES</i> 1–8 Å	1	0.9	−2.3	14–27 s
<i>GOES</i> 0.5–4 Å	0.92	1.2	−2.3	17–29 s
LYRA Zr	0.85	0.7	−2.2	13–24 s
ESP 0.1–7 nm	0.90	1.2	−2.3	12–25 s
GBM 4–15 keV	0.81	2.1	−2.2	18–32 s
GBM 15–25 keV	0.78	6.5	−2.1	14–33 s
GBM 25–50 keV	0.64	51.2	−2.3	16–26, 34–64 s
GBM 50–100 keV	0.56	80.1	−2.3	17–40, 49–68 s
NoRH 17 GHz	0.51	35.6	−2.3	15–27, 48–70 s
NoRH 34 GHz	0.48	16.2	−2.3	17–30, 54–56 s

Note. The cross-correlation coefficients are shown compared to *GOES* 1–8 Å. The “significant timescale” column gives the range of timescales for which the summed power exceeds the 99.7% significance level above the power-law background model during impulsive phase.

Modulated emission features in HXR and microwave cease at around 02:00:30 UT. However, pulsations in the *GOES* time derivative persist well into the decay phase even though the non-thermal pulsations have ceased. Some of the extended variability is seen in ESP 0.1–7 nm, but is much less pronounced and almost nothing can be detected above noise in LYRA Zr. This could be due to the precision of the instruments or due to the fact that both these channels are also sensitive to lower-temperature plasma. This raises the question of what the temperature distribution of the pulsating plasma is and requires further investigation outside the scope of this Letter.

In order to investigate the extent of the pulsations in the decay phase of this flare, we looked at both *GOES* channels

from 02:00:30 UT to 02:20:00 UT. Figures 3(a) and (b) show the time derivative and detrended time derivative light curves of the *GOES* 1–8 Å channel. The extended nature of the pulsations is clearly demonstrated. The fine structure features appear to have a less chaotic nature compared to the impulsive phase with the pulsations displaying a damped signature.

We again employ wavelet techniques to investigate the timescales of these pulsations during this phase. Wavelet power is dependent on the amplitude of the pulsations, and so due to the damping nature observed here, we first we first normalize the pulsations to have a constant amplitude. The normalization is done by dividing the time series in Figure 3(b) by an envelope (marked by the red curve), calculated as the absolute value of the light curve smoothed with a boxcar window of

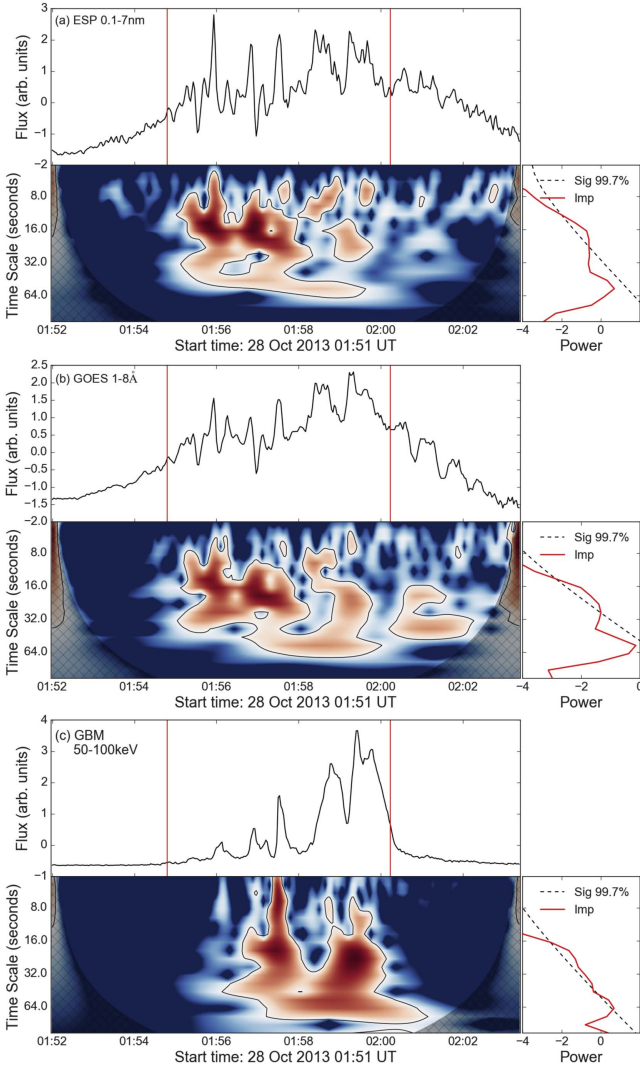


Figure 2. Wavelet analysis of different channels. (a) ESP 0.1–7 nm derivative, (b) *GOES* 1–8 Å derivative, and (c) GBM 50–100 keV.

~ 200 s. Figure 3(c) shows these normalized amplitude pulsations during the decay phase. A wavelet power spectrum of the variations is shown in Figure 3(d). Interestingly, enhanced power is seen at a timescale of ~ 40 s just after the impulsive phase at 02:00:30 UT, which then changes to ~ 70 s between 02:06:30 to 02:08:30 UT. The timescale of ~ 70 s then stays constant until approximately 02:15 UT, when the signal-to-noise level becomes comparable to the amplitude of the pulsations.

This increase in timescale of the pulsations is likely to be connected with longer loop lengths at later stages of the flare. Figures 4(a) and (b) show the contours of the SXR source of *RHESSI* 6–12 keV overlaid on AIA 94 Å images. We found that the SXR source height increases as the flare progresses, presumably a signature of continued magnetic reconnection resulting in newly formed hot loops at higher altitudes. Assuming semicircular, vertical loops seen in the plane of sky we estimate the loop length. This is done by locating the centroid of the SXR source imaged with *RHESSI* and approximating footpoints from AIA images. We then divide this observed length by $\cos(20^\circ)$ to account for projection effects from being $\sim 20^\circ$ inside the limb. We find that the loop

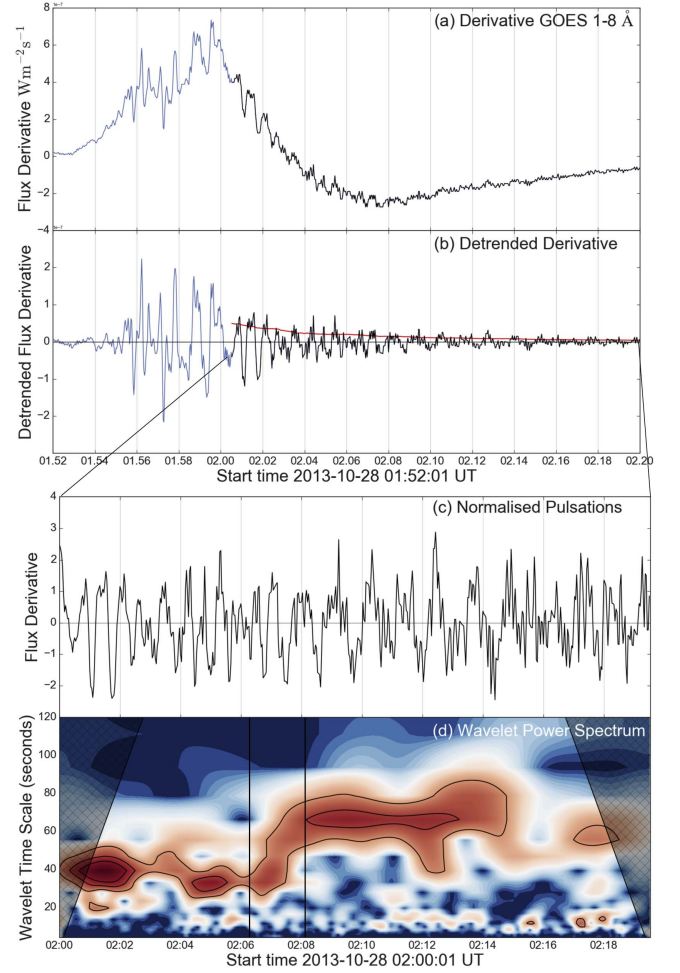


Figure 3. Decay phase QPPs observed by *GOES* 1–8 Å. The black color indicates the decay phase section of the light curve we are interested in. (a) Derivative of the *GOES* 1–8 Å light curve. (b) Detrended *GOES* derivative. (c) Normalized amplitude pulsations. (d) Wavelet power spectrum of panel (c). The vertical black lines at 02:06:30 and 02:08:30 UT highlight the region in time in which the characteristic timescale increases from ~ 40 to ~ 70 s.

length increased from approximately 38 Mm at 02:00 UT to 59 Mm at 02:20 UT. This increase is plotted as a function of time in Figure 4(c). Notably, during the increase in timescale from 02:06:30 to 02:08:30 UT, the loop length only increases by 2 Mm, which is small compared to the large increase in timescale. The loop length then continues to grow even when the timescale of the pulsations is constant at 70 s until 02:15 UT.

4. DISCUSSION AND CONCLUSION

We have detected and analyzed pulsations observed at multiple wavelengths during the X1.0 flare of 2013 October 28. Throughout the impulsive phase of the flare, highly correlated common features are observed at HXR, SXR, and microwave wavelengths with minimal time delay between peaks. Wavelet analysis of this impulsive interval shows broadband features in the wavelet power spectrum, with similar enhanced power in all channels. Characteristic peaks in the global spectrum at ~ 20 s are detected in all wavebands with enhanced power also seen at around ~ 55 s but only with significance above 99.7% in the non-thermal emissions. These characteristic timescales are consistent with previous QPP investigations of different events

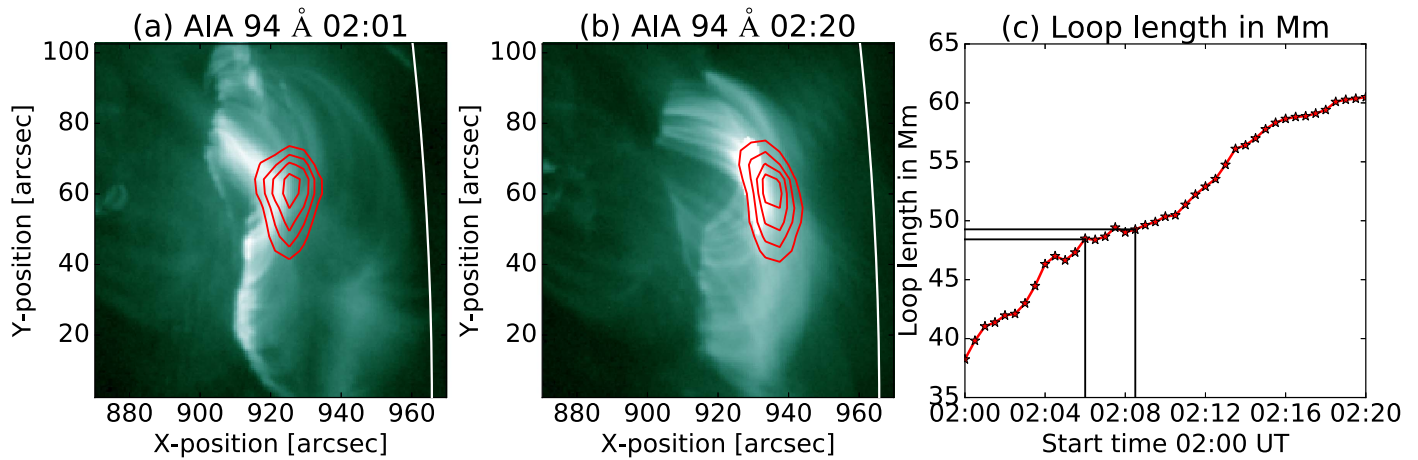


Figure 4. (a) and (b): *RHESSI* contours of the 6–12 keV energy range using the CLEAN reconstruction algorithm overlaid on AIA 94 Å images during the decay phase of the flare at 02:01 UT and 02:20 UT, respectively. The contours are at 30%, 50%, 70%, and 90% of peak value. (c) The loop length increase of the flare during the decay phase. The region noted within the black vertical lines is the time when the timescale increases from ~ 40 to ~ 70 s.

(e.g., Kupriyanova et al. 2010; Simões et al. 2015; A. R. Inglis et al. 2016, in preparation).

After the highly correlated impulsive phase, we find that emission in the non-thermal channels is no longer present. However, distinct pulsations in the high-temperature plasma observed by *GOES* persist into the decay phase. The timescale of the pulsations are seen to increase from ~ 40 s at the end of the impulsive phase at 02:00 UT to ~ 70 s at 02:15 UT. These thermal pulsations could be a manifestation of continuing weak particle acceleration (e.g., MacCombie & Rust 1979), or some other heating mechanism that persists into the decay phase of the flare. This would support the idea that continuous heating is required to describe the decay times observed in many flares that are longer than the estimated conduction and radiation cooling timescales (Cargill et al. 1995; Ryan et al. 2013).

However, what controls the timescale of the observed pulsations? The timescale of the QPPs is consistent with expected characteristic timescales of MHD modes in the corona (Pascoe et al. 2007, 2009; McEwan et al. 2008; Macnamara & Roberts 2011). However, given the complex evolution of geometrical plasma structures occurring during the impulsive phase, the identification of the specific MHD modes of oscillation producing the QPPs is unlikely. The large modulation depths of the non-thermal emission during this time suggest that the pulsations are a result of episodic reconnection. The timescale would then be determined by either dynamic or periodic variations of the magnetic reconnection process such as multi-island reconnection in coronal current sheets (Drake et al. 2006; Guidoni et al. 2016).

During the decay phase, however, the increase in timescale and small amplitude of the thermal SXR pulsations is consistent with MHD processes within the flaring site. Recent studies have attributed persistent SXR QPPs to that of compressive MHD modes such as the global fast sausage mode (Tian et al. 2016) and vertical kink mode (Dennis et al. 2016). Both of these compressive modes would result in the observed pulsations in the decay phase of this flare. The damped nature of the decay phase pulsations observed in Figure 3(b) suggest that they are a result of the global sausage mode in the leaky regime. In the leaky regime, sausage modes are subject to damping and show a decaying oscillatory behavior. The period of the sausage mode is determined by the

ratio of the wavelength (twice the loop length L) to the external Alfvén speed: $P = 2L/V_{Ae}$ (Pascoe et al. 2007). This dependence decreases in the leaky regime, and in the long-wavelength limit, the period becomes independent of the length of the oscillating loop and is determined by the transverse travel time across the loop; $P^{\text{leaky}} \approx \pi a/V_{Ai}$, where a is the loop width and V_{Ai} is the internal Alfvén speed (Nakariakov et al. 2012). This may explain why the characteristic timescale stays constant at ~ 70 s even when the loop length keeps increasing. Taking the period to be 70 s and a in the range of $\sim 2''$ – $10''$, this interpretation yields an estimation of $V_{Ai} \approx 65$ – 350 km s $^{-1}$. This is considerably low for coronal loop Alfvén speeds (e.g., Aschwanden et al. 1999b), suggesting that the loops are not sufficiently long enough to be in the long-wavelength limit and so this interpretation cannot fully explain our observations. However, given the low signal-to-noise in the late stage of the flare, it is difficult to determine the true nature of these pulsations.

We cannot conclusively determine what mechanism generates these pulsations. However, the analysis of the SXR fine structure across multiple channels and its relation with other energies provide a new diagnostic tool. When correlations between different energies are high, especially SXR and HXR (as with most peaks in the impulsive phase of this flare), we can argue that the SXR emitting plasma is heated by electron beams at that time. When pulsations in SXR are seen to occur before HXR emission, and persist late into the decay phase after the HXR emission has stopped, some other heating mechanism is taking place. Thus, detailed comparisons between thermal and non-thermal structures can potentially help us understand the distribution of the different types of heating taking place during a flare. Additionally, it has now become apparent that fine structure pulsations observed in the SXR derivative are a common (Simões et al. 2015), and maybe even an intrinsic feature of flaring emission. Hence, further investigation into the structure evident in SXR light curves and multi-wavelength comparisons will provide better insight into the origins of the QPP phenomena.

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