'You' and 'I' in modal logic

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Abstract

The article discusses the interpretation of indexical expressions within the framework of quantified modal logic. The dominant theory on this topic is, since its appearance in 1977, Kaplan's two dimensional analysis. Kaplan's theory, however, has been challenged on various grounds. I will argue that by revising the way of modelling the objects we refer to in conversation, we can account for counterexamples to Kaplan's theory, while maintaining Kaplan's basic insights concerning the meaning of 'you' and 'I'.

1 Introduction

1.1 Basic properties of indexicals

Our primary intuition concerning indexical expressions like 'you' and 'I' is that their interpretation is relative to the context of use. Distinct occurrences of indexicals may have distinct referents in distinct contexts. 'I' refers to the speaker in the context of utterance, 'today' refers to the day in the context of utterance, so (1) can mean (1-a), if used by David Kaplan on 26 March 1977; or (1-b), if used by Maria Aloni on 27 April 2016.

- (1) I am tired today.
 - a. David Kaplan is tired on 26 March 1977.
 - b. Maria Aloni is tired on 27 April 2016.

A second property of indexicals is that they typically occur in contingent a priori statements. Kripke (1972) argued that necessity and a priori are distinct notions. Kaplan (1977) showed that by using indexicals we can give compelling examples of truths where these notions do not coincide. A statement like (2) is contingent, I could have been somewhere else, but at the same time it is a priori, no empirical investigation is needed to attest its truth.

(2) I am here today.

A third alleged property of indexicals, which will be subject to scrutiny in this article, is that they appear to be insensitive to intensional operators. One classical example illustrating this property is (3) from Kaplan (1977, p. 199):

(3) It is possible that in Pakistan, in five years, only those who are actually here now are envied.

Kaplan observed that the indexicals 'actually', 'here' and 'now' are naturally interpreted with respect to the actual utterance situation despite the presence of the shifting modal, spatial and temporal operators.¹

An effective way to illustrate the property Kaplan had in mind is by contrasting indexicals with definite descriptions. An example like (4) is typically ambiguous between the readings paraphrased in (4-a) and (4-b).

- (4) The president of the US could have been a Republican.
 - a. Barack Obama could have been a Republican $De \ re: \exists x[x=the \ president \land \Diamond Rx]$
 - b. A Republican (Romney) could have won the last elections $De\ dicto: \diamondsuit \exists x [x = the\ president \land Rx]$

Modal logic provides us with a perspicuous way to represent this ambiguity. Reading (4-a) is captured by a de re representation with the definite description 'the president' occurring outside of the scope of the modal operator, while reading (4-b) is captured by a de dicto representation with 'the president' occurring within the scope of the possibility operator. Two comments are at place at this point. First, throughout the paper I will refer to the de re/de dicto distinction as a syntactic distinction rather than a metaphysical one. Secondly, definite descriptions will be left unanalysed here, because nothing I am going to say hinges on which particular analysis of definite descriptions is assumed.

Now contrast (4) with (5) where an indexical rather than a definite is used. It is normally observed that (5) is not ambiguous in the same way as (4) is. The most plausible candidate for a *de dicto* reading for (5) is (5-b), but such a reading does not seem to be available for these cases.

(5) I could have been a Republican.

(used by Barack Obama)

- And what would terrify the right, of course, is the likelihood that genuine socialized medicine would actually win that competition.
- (ii) All over England folk began to hear of the wonderful saint who lived alone in the desert island, [...] He built a house by the landing-place on the island for his visitors to stay in, and **here**, too, his monks would come on festivals to have a talk with him.
- (iii) Brutally, the banks knowingly gamed the system to grow their balance sheets ever faster and with even less capital underpinning them in the full knowledge that everything rested on the bogus claim that their lending was now much less risky.

I will not discuss anaphoric uses of indexicals in this article though and, therefore, to avoid possible ambiguity, in what follows I will exclusively focus on 'you' and 'I', which arguably don't have such anaphoric uses.

¹Potential counterexamples to this specific claim, however, have been recently presented in the linguistic literature, e.g. Hunter (2012), who provides a number of examples of anaphoric uses of the expressions 'actually', 'here' and 'now', where these words are interpreted with respect to the context created by the preceding discourse, rather than the actual utterance situation. As an illustration consider the following:

- a. Barack Obama could have been a Republican
- b. #A Republican could have been speaking

There is one strategy to account for these facts which Kaplan mentions, but quickly dismisses. We could assume that indexicals are descriptions of a special kind, namely the kind that always has primary scope in the sense of Russell (1905).

This strategy is illustrated in (6). 'I' is translated as *the speaker*, but with the assumption of an additional mechanism which prevents the *de dicto* representation (6-b) to be generated:

(6) I could have been a Republican. (used by Obama) 'Obama could have been a Republican'

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a. De re: \exists x[x = the \ speaker \land \Diamond Rx]
b. \#De \ dicto: \Diamond \exists x[x = the \ speaker \land Rx]
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Such a strategy has been recently implemented within DRT where indexicals have been analysed as presupposition triggers (like definites) with a preference for global resolution rather than local resolution (e.g. Zeevat, 1999; Hunter and Asher, 2005).

There is however a problem for this strategy discussed by Maier (2009) echoing Kripke. Consider the two sentences in (7):

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(7) a. The speaker is speaking. [necessary] b. I am speaking. [contigent] c. \exists x[x = the \ speaker \land Sx]
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While (7-a) is necessary truth, (7-b), although a priori, is merely contingent. An analysis which characterises the distinction between 'I' and 'the speaker' exclusively in terms of scope has no way to distinguish between the two sentences: since there is no scoping operator, they are both represented as (7-c).

Kaplan's own strategy to deal with these facts is his two-dimensional analysis to which we now turn.

1.2 Kaplan's two-dimensional analysis

In a two-dimensional semantics expressions are interpreted with respect to two parameters: a context c and a world of evaluation w. Assuming a language of quantified modal logic \mathcal{L} and a standard Kripke model $M = \langle W, R, D, I \rangle$ for \mathcal{L} , a context based on M is a tuple consisting of the actual speaker of the utterance, the actual addressee, the actual world and possibly more.

Definition 1 (Contexts in $2D_K$) Given a model $M = \langle W, R, D, I \rangle$, a context c based on M is a tuple $\langle s_c, a_c, \dots, w_c \rangle$, where

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(i) s_c, a_c \in D \text{ and } w_c \in W;
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(ii)
$$s_c = [the \ speaker]_{w_c}$$
 and $a_c = [the \ addressee]_{w_c}$.

While ordinary expressions are interpreted with respect to the world parameter, indexicals are interpreted with respect to the context parameter: 'I' refers to s_c , the speaker in the context, 'you' to a_c , the addressee, as in the following definition:

Definition 2 (Indexicals in $2D_K$)

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[I]_{M,c,w,g} = s_c (the speaker in c)
[you]_{M,c,w,g} = a_c (the addressee in c)
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As it is well known this analysis gives us a ready account of the basic properties of indexicals (their context dependence and their appearance in contingent a priori statements), but it also provides an explanation of the fact that indexicals do not give rise to genuine *de re-de dicto* ambiguities. This is illustrated in (8).

(8) I could have been a Republican. (used by Obama) 'Obama himself could have been a Republican'

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a. De re: \exists x[x = I \land \Diamond Rx]
b. De dicto: \Diamond \exists x[x = I \land Rx]
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Since indexical I is interpreted with respect to the context parameter, its interpretation remains stable even though we shift from one world to the other, so both logical representations (8-a) and (8-b) express the same meaning. This prediction of Kaplan's analysis relies on at least three assumptions:

- 1. Modals cannot shift the context parameter
- 2. Indexicals are directly referential and, therefore, rigid designators
- 3. Variables are rigid designators ('the paradigm of direct reference')

Assumptions 1 and 2 are essential otherwise the *de dicto* representation in (8-b) would possibly generate other readings. Assumption 3 is essential otherwise the *de re* representation in (8-a) would possibly generate other readings.

I won't further discuss assumption 1. If we confine ourself to English, our data are compatible with the assumption that modals cannot manipulate the context parameter (see however Schlenker, 2003; Anand, 2006; Maier, 2009, for challenges to assumption 1 based on cross-linguistic data). I will challenge, however, assumptions 2 and 3: I will argue against a treatment of indexicals and variables as rigid designators. Kaplan talks about direct reference, I will talk about rigidity, which is a technical modal logic notion. I will argue that Kaplan's main intuition about the genuinely referential nature of indexicals is not incompatible with a non-rigid account of these expressions, if a number of conditions are satisfied.

Once we drop assumptions 2 and 3, the resulting modal logic will be one which apparently overgenerates with respect to examples like (8): many more readings of the sentence will be predicted than observed. In the last part of the

article I propose a pragmatic rather than a logical/semantic account of the interaction between indexicals and modals, which, in terms of general constraints on pragmatic resolutions, will avoid such a overgeneration. The main motivation for a pragmatic account comes from a number of examples of so-called descriptive uses of indexical expressions.

1.3 Descriptive uses of indexicals

Consider first the following scenario. In the middle of the presidential campaign, Obama asks his secretary via WhatsApp permission to access confidential documents describing the democratic strategy. His secretary complies with his request, but later, during a security awareness meeting, Obama approaches him:²

(9) Why did you give me access to the files? You should be more careful! I could have been a Republican.

Obama's intended meaning in this case is not (10-a), but rather (10-b).

- (10) I could have been a Republican. (used by Obama)
 - a. Obama himself could have been a Republican
 - b. A Republican could have sent you the WhatsApp message

Reading (10-b) however is not predicted by Kaplan's analysis. As we just saw both representations in (11) generate reading (10-a):

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(11) a. De re: \exists x[x = I \land \Diamond Rx]
b. De dicto: \Diamond \exists x[x = I \land Rx]
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It is clear that only a pragmatic account can be flexible enough to accommodate these extraordinary cases while maintaining Kaplan's basic intuitions with respect to the ordinary cases considered above.

Example (9) has the same structure as the well-known cases of deferred reference discussed by Nunberg (1993).

(12) Condemned prisoner: I am traditionally allowed to order whatever I like for my last meal. [Nunberg 1993, p. 20]

What the speaker intends to say is 'a condemned prisoner is not allowed to order whatever he likes for his last meal', but somehow he can use an indexical to convey such descriptive meaning. Again Kaplan's logical/semantic account of the interaction between indexicals and modals is not flexible enough to account for these cases.

 $^{^2{\}rm This}$ example has the same structure of (i) from Hans Kamp as reported in Maier (2009, p. 285):

⁽i) Why did you open the door without checking? You should be more careful! I could have been a burglar.

Similarly, Kaplan has problems with another class of examples involving indexicals in 3rd person attitude reports. Consider the following scenario:

- (13) Context: Miss Jones, the new director of Lorenzo's school, would assent to 'Lorenzo's mother is Spanish'. She further has no idea who Lorenzo's mother is. Lorenzo's mother name is Maria. Maria reports to her husband:

 [Aloni 2001, 2005]
- (14) Miss Jones believes that I am Spanish. [true]

Maria's intended meaning in this case is not (15-a), but rather (15-b).

- (15) Miss Jones believes that I am Spanish.
 - a. Miss Jones would assent to 'This individual (pointing at Maria) is Spanish'
 - b. Miss Jones would assent to 'Lorenzo's mother is Spanish'

Reading (15-b), however, is again not predicted by Kaplan's logical/semantic analysis. Both representations in (16) generate reading (15-a):

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(16) a. De re: \exists x[x = I \land \Box Sx]
b. De dicto: \Box \exists x[x = I \land Sx]
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In what follows we will defend an account which is flexible enough to accommodate for these cases. On the semantic side, the interpretation of referential expressions (variables, indexicals) will be relativised to contextually selected methods of identification. If a perceptually-based method of identification is contextually operative, both representations in (16) will express meaning (15-a). If a descriptive method of identification is contextually operative, both representations in (16) can express meaning (15-b). By assuming that perceptually-based methods are the default choice, while descriptive methods can be operative only if certain conditions apply, we derive the descriptive uses of indexicals discussed in this section, but also their extraordinary nature.

The rest of the article is structured as follows: The next section presents two more arguments against Kaplan which motivate a non-rigid analysis of indexicals, and considers, but dismisses, a first attempt to model indexicals as non-rigid designators in a classical two-dimensional modal logic. Section 3 motivates Aloni's (2001) non-classical version of quantified modal logic, as better equipped to model reference in situations of partial information. Section 4 proposes a novel analysis of indexicals within a two-dimensional version of Aloni's (2001) quantified modal logic, where the interpretation of referential expressions (variables, indexicals) is relativised to contextually selected methods of identification. Section 5 concludes by spelling out the principles governing the contextual selection of a method of identification and provides a pragmatic explanation of the cases of the interaction between indexicals and modals discussed above.

2 Against rigidity

2.1 Motivating examples

In this section we discuss two more examples that have been presented against Kaplan, which involve uses of indexicals in situation of partial information. Both examples justify an analysis of indexicals as non-rigid designators. The first is Richard's (1983) classical phone booth example:

Consider A – a man stipulated to be intelligent, rational, a competent speaker of English, etc.– who both sees a woman, across the street, in a phone booth, and is speaking to a woman through a phone. He does not realize that the woman to whom he is speaking – B, to give her a name – is the woman he sees. He perceives her to be in some danger – a run-away steamroller, say, is bearing down upon her phone booth. A waves at the woman; he says nothing into the phone (Richard, 1983, p.439)

In this situation A would assent to 'she is in danger', but not to 'you are in danger', so (17-a) would be true, if used by A, while (17-b) would be false:

Kaplan, who assumes that both 'you' and 'she' refer in a rigid way, has no means to account for these intuitions.

A similar case involving 'I' can be constructed adapting a scenario discussed by Santorio (2012). Imagine Rudolf Lingens and Gustav Lauben are amnesiacs: each of them knows that he is one of the two, but doesn't know which. Both could then truly assert each of the following sentences:

Again a Kaplanian analysis of indexicals cannot account for these cases (unless one assumes that proper names are non-rigid designators).

Rudolf Lingens, Gustav Lauben and Mister A from Richard's example are all predicted to have inconsistent beliefs by Kaplan's analysis. But our three characters are not insane, they just miss some crucial information about the individuals they are referring to via their indexical expressions. Dropping epistemic rigidity for indexicals (and/or proper names) would give us a ready account of these cases. In the following section we investigate what it takes to define a two-dimensional analysis of indexicals which models them as non-rigid designators.

2.2 Two-dimensional semantics w/o rigidity: first attempt

Assuming again standard Kripke models $M = \langle W, R, D, I \rangle$, a context could be defined as providing individuating functions (or individual concepts), rather

than objects, as in the following definition where $\mathbf{s_c}$ and $\mathbf{a_c}$ are elements of D^W , rather than D.

Definition 3 (Contexts in $2D_R$) Given a model $M = \langle W, R, D, I \rangle$, a context c based on M is a tuple $\langle \mathbf{s_c}, \mathbf{a_c}, \dots w_c \rangle$ where

- (i) $\mathbf{s_c}, \mathbf{a_c} \in D^W$;
- (ii) $\mathbf{s_c}(w_c) = [the \ speaker]_{w_c}$ and $\mathbf{a_c}(w_c) = [the \ addressee]_{w_c}$.

On this analysis, $\mathbf{s_c}$ and $\mathbf{a_c}$ are functions from possible worlds to individuals (clause (i)), which must satisfy the extra condition that the value that $\mathbf{s_c}$ assigns to w_c is the speaker in w_c and the value that $\mathbf{a_c}$ assigns to w_c is the addresses in w_c (clause (ii)). So $\mathbf{s_c}(w_c) = [\![the\ speaker]\!]_{w_c}$ and $\mathbf{a_c}(w_c) = [\![the\ addressee]\!]_{w_c}$, but, crucially, $\mathbf{s_c}$ needs not be equivalent to $\lambda w.[\![the\ speaker]\!]_w$ and $\mathbf{a_c}$ needs not be equivalent to $\lambda w.[\![the\ addressee]\!]_w$. Indexicals can be interpreted as follows:

Definition 4 (Indexicals in $2D_R$)

$$\begin{split} \llbracket I \rrbracket_{M,c,w,g} &=& \mathbf{s_c}(w) \\ \llbracket you \rrbracket_{M,c,w,g} &=& \mathbf{a_c}(w) \end{split}$$

When interpreting an indexicals with respect to a world w and and context c, the context c provides the individuating functions $\mathbf{s_c}$ and $\mathbf{a_c}$, and the world w provides the argument of the function. Indexical I when interpreted with respect to the world of evaluation w and the context c denotes an individual $\mathbf{s_c}(w) \in D$, which is the value that the function $\mathbf{s_c}$ (provided by the context) assigns to w (the world of evaluation). Note that $\mathbf{s_c}(w)$ need not be speaking in w, if $w \neq w_c$.

Applications Since 'you' and 'she' can be assigned different individuating functions even though they refer to one and the same individual in the actual world, Richard's phone booth example is no longer problematic:

Since $\mathbf{s_c}$ need not be a constant function, Santorio's amnesiacs case is also easily accounted for:

Finally, since $\mathbf{s_c}$ can be equivalent to $\lambda w.\llbracket the\ P \rrbracket_w$, but need not be equivalent to $\lambda w.\llbracket the\ speaker \rrbracket_w$ we can account for descriptive uses of indexicals without incurring into Kripke/Maier problems. The speaker-function $\mathbf{s_c}$, assigned to I, can be equivalent to the function which maps each world to the WhatsApp sender in that world ($\mathbf{s_c} = \lambda w.\llbracket the\ sender\ of\ the\ WhatsApp \rrbracket_w$), which would derive the intended meaning of (21) via a $de\ dicto$ representation, but $\mathbf{s_c}$ need

not be equivalent to the function which assigns to all worlds the speaker in that world $(\mathbf{s_c} \neq \lambda w.[\![the\ speaker]\!]_w)$, which explains (22).

- (21) (Why did you give me the password?) I could have been a Republican.
 - a. $\Diamond \exists x [x = I \land Rx]$
 - b. A Republican could have sent you the WhatsApp message
- (22) a. I am speaking. [contingent]
 b. The speaker is speaking. [necessary]

Dropping rigidity, however, has consequences. Consider the principles of substitutivity of identicals and existential generalisation, which are normally validated if t and t' stand for genuinely referential expressions:

SI
$$t = t' \to (\phi[t] \to \phi[t'])$$
 (substitutivity of identicals)
EG $\phi[t] \to \exists x \phi[x]$ (existential generalisation)

In a Kaplanian system $(2D_K)$, **SI** and **EG** are validated, if t and t' are variables or indexicals, but would be invalidated if t or t' would stand for a definite description (let ιyPy denote in w the unique P in w, if there is one; \emptyset (or undefined), otherwise).

(23)
$$\models_{2D_K} y = x \to (\phi[y] \to \phi[x])$$
 (SI, variables) $\models_{2D_K} \phi[y] \to \exists x \phi[x]$ (EG, variables)

$$(24) \qquad \models_{2D_K} you/I = x \to (\phi[you/I] \to \phi[x]) \qquad \qquad \textbf{(SI, indexicals)} \\ \models_{2D_K} \phi[you/I] \to \exists x \phi[x] \qquad \qquad \textbf{(EG, indexicals)}$$

(25)
$$\not\models_{2D_K} \iota y P y = x \to (\phi[\iota y P y] \to \phi[x])$$
 (SI, definites)
$$\not\models_{2D_K} \phi[\iota y P y] \to \exists x \phi[x]$$
 (EG, definites)

The intuition formalised by $2D_K$ is that indexicals like variables are genuinely referential expressions, while definite descriptions aren't. In the system presented in the present section $(2D_R)$, in contrast, **SI** and **EG** are validated for variables, but not for indexicals or definite descriptions.

(26)
$$\models_{2D_R} y = x \to (\phi[y] \to \phi[x])$$
 (SI, variables) $\models_{2D_R} \phi[y] \to \exists x \phi[x]$ (EG, variables)

(27)
$$\not\models_{2D_R} you/I = x \to (\phi[you/I] \to \phi[x])$$
 (SI, indexicals) $\not\models_{2D_R} \phi[you/I] \to \exists x \phi[x]$ (EG, indexicals)

(28)
$$\not\models_{2D_R} \iota y P y = x \to (\phi[\iota y P y] \to \phi[x]) \\
\not\models_{2D_R} \phi[\iota y P y] \to \exists x \phi[x]$$
(SI, definites)
(EG, definites)

The following tables summarise the relevant facts:

$2D_K$	SI	\mathbf{EG}
variables	yes	\mathbf{yes}
indexicals	yes	\mathbf{yes}
definites	no	no

$2D_R$	SI	$\mathbf{E}\mathbf{G}$
variables	\mathbf{yes}	\mathbf{yes}
indexicals	no	no
definites	no	no

While in a Kaplanian semantics, indexicals are predicted to behave like variables, in $2D_R$, they are modelled as definite descriptions. The $2D_R$ classification, however, blurs the intuitive difference between indexicals and definites illustrated by the first Obama example discussed in the introductory section. While (29) is naturally ambiguous, (30) requires a very specific context to give rise to a descriptive reading:

- (29) The president of the US could have been a Republican.
 - a. Barack Obama could have been a Republican
 - b. A Republican could have won the last elections
- (30) I could have been a Republican.

(used by Obama)

- a. Obama could have been a Republican
- b. #A Republican could have been speaking

In ordinary circumstances, (30) simply means (30-a). In $2D_R$, however, nothing prevents $\mathbf{s_c}$ to be equivalent to $\lambda w.[\![the\ speaker]\!]_w$, so $de\ dicto\ (31-b)$ could mean (30-b):

(31) a. De $re: \exists x[x = I \land \Diamond \phi[x]]$ b. De $dicto: \Diamond \exists x[x = I \land \phi[x]]$

To avoid this counterintuitive result, we could try to ban descriptive concepts like 'the speaker' from our contexts, while allowing only perceptually-based concepts ('the woman over there'). Such an approach could still account for Richard's and Santorio's examples, where (non-rigid) perceptually-based concepts are operative, while it will not overgenerate readings for ordinary cases like (30). The problem with this strategy, however, is that if indexicals can only be assigned perceptually-based concepts, we lose our explanation of the Nunberg-like descriptive uses of indexicals and the intended reading of (32) can no longer be generated:

(32) (Why did you send me the password?) I could have been a Republican. 'A Republican could have sent you the WhatsApp message'

Eventually I will defend a pragmatic account of the difference between (30) and (32). But first I will propose a new way of modelling the objects we refer to in conversation. Motivation for this new logic of reference comes from cases of quantification in situations of partial information. A two-dimensional version of the resulting semantics will allow us to distinguish between indexicals and definite descriptions, while allowing an account of both Richard-like and Nunberg-like cases.

3 Reference in situations of partial information

Imagine the following situation. In front of you lie two face-down cards. One is the Ace of Hearts, the other is the Ace of Spades, but you don't know which is which. You have to choose one card: if you choose the Ace of Hearts you win \$10, if you choose the Ace of Spades you lose \$10. Now consider the following sentence:

(33) You know which card is the winning card.

Is this sentence true or false in the given situation? On the one hand, the sentence is true: you know that the Ace of Hearts is the winning card. If someone interested in the rules of the game asked you "Which card is the winning card?", you would be able to answer in an appropriate way. On the other hand, suppose someone interested in winning the game would ask you "Which card is the winning card?" In this case you would not be able to answer in the desired way: as far as you know, the winning card may be the card on the left, but it may just as well be the card on the right. Therefore you don't know which card is the winning card (similar "yes and no" cases were discussed in Boër and Lycan, 1985).

Aloni (2001) proposed the following explanation of this example. Intuitively, there are two ways in which the cards may be identified in this situation: by their position (the card on the left, the card on the right) or by their suit (the Ace of Hearts, the Ace of Spades). Whether (33) is judged true or false seems to depend on which of these perspectives is adopted. If identification by suit is adopted, as in the first context discussed above, the sentence is judged true. But if identification by position is adopted, as in the second context, the sentence is judged false.

Aloni (2001, 2005b) proposed to formalise identification methods by means of conceptual covers. A conceptual cover is a set of individual concepts (functions from possible worlds to individuals) that satisfies the following condition: in a conceptual cover, in each world, each individual constitutes the value (or instantiation) of one and only one concept.

Definition 5 (Conceptual cover) Given a set of possible worlds W and a universe of individuals D, a conceptual cover CC based on (W, D) is a set of functions $W \to D$ such that:

$$\forall w \in W : \forall d \in D : \exists! c \in CC : c(w) = d.$$

Conceptual covers are sets of concepts which exhaustively and exclusively cover the domain of individuals. In a conceptual cover each individual d is identified by at least one concept in each world (existence), but in no world is an individual counted more than once (uniqueness). In a conceptual cover, each individual is identified in one specific way. Different covers constitute different ways of conceiving one and the same domain.

For the sake of illustration consider again the card scenario described above. In that scenario there are at least three salient ways of identifying the cards which can be represented by the following conceptual covers: (34-a) represents identification by ostension, (34-b) represents identification by name, and (34-c) represents identification by description.

(34) a. {on-the-left, on-the-right} [ostension]
b. {ace-of-spades, ace-of-hearts} [naming]
c. {the-winning-card, the-losing-card} [description]

The set of concepts in (35) is not an example of a conceptual cover because it does not satisfy the conditions formulated in our definition.

(35) $\#\{\text{on-the-left, ace-of-spades}\}$

Intuitively, (35) does not represent a proper perspective over the relevant domain of individuals: as far as we know, the card on the left might be the Ace of Spades. If so: (i) one card (the Ace of Spades) would be counted twice; and (ii) another card (the Ace of Hearts) would not be identified at all.

In order to account for the "yes and no" cases discussed above, Aloni (2001, 2005b) proposed a non-classical variant of quantified modal logic where the evaluation of formulas is relativised to a contextual parameter, which assigns conceptual covers to variables as their domain of quantification. Building on (Hintikka, 1962), formula (37) can be used as the logical representation of (36). The variable z_n in (37) is indexed by a CC-index $n \in N$ ranging over conceptual covers. The evaluation of (37) varies relative to the contextually selected value of n as illustrated in (38).

- (36) You know which card is the winning card.
- $(37) \qquad \exists z_n \Box z_n = c$
- (38) a. False, if $n \mapsto \{\text{on-the-left, on-the-right}\}$
 - b. True, if $n \mapsto \{\text{ace-of-spades, ace-of-hearts}\}$
 - c. Trivial, if $n \mapsto \{\text{the-winning-card}, \text{the-losing-card}\}$

A further crucial feature of Aloni's quantified modal logic, is that differently indexed variables x_n and y_m can range over different conceptual covers. This feature allows perspicuous representations of traditionally problematic cases including example (39) and Quine's double vision cases (example (40)).

- (39) a. You don't know which card is which.
 - b. $\forall x_n \forall y_m \Diamond x_n = y_m$
- (40) a. Ralph believes Ortcutt to be a spy and Ralph believes Ortcutt not to be a spy.
 - b. $\exists x_n(x_n = o \land \Box Sx_n) \land \exists x_m(x_m = o \land \Box \neg Sx_m)$

When we talk about concepts, we implicitly assume two different levels of 'objects': the individuals (in D) and the ways of referring to these individuals (in D^W). An essential feature of the intuitive relation between the two levels of the individuals and of their representations is that to one element of the first set correspond many elements of the second: one individual can be identified in many different ways. What characterises a set of representations of a certain domain is this cardinality mismatch, which expresses the possibility of considering an individual under different perspectives which may coincide in one world

and not in another. Individuals, on the other hand, do not split or merge once we move from one world to the other. Now, since the elements of a conceptual cover also cannot merge or split (by uniqueness), they behave like individuals in this sense, rather than representations. On the other hand, a conceptual cover is not barely a set of individuals, but encodes information on how these individuals are specified. We thus can think of covers as sets of individuals each identified in one specific way. In the next section I will propose to let Kaplanian contexts map indexicals to elements of a conceptual cover rather than to plain individuals. By allowing different conceptual covers to be operative on different occasions, we will be able to account for the counterexamples to Kaplan's theory, without failing to account for the intuition that indexicals denote genuine individuals, rather than ways of specifying these individuals.

4 Two dimensional semantics under cover

In this section we present a two-dimensional version of Aloni's (2001; 2005b) quantified modal logic with conceptual covers, where expressions are interpreted with respect to a perspective (assigning CC-indices to conceptual covers) and two world parameters, with the first world playing the role of a Kaplanian context. By extending the language with CC-indexed indexical terms you_n and I_n , whose interpretation will depend on both the context-world and the adopted conceptual cover, the resulting logic will capture the basic properties of indexicals but also their descriptive uses (including Nunberg's cases) and their interpretation in situations of partial information (Richard's and Santorio's examples).

4.1 Language

We assume a set \mathcal{C} of individual constants, a set \mathcal{P} of predicates, and an enumerable set \mathcal{V}_N of CC-indexed individual variables. Then we define the terms t and formulas ϕ of our language \mathcal{L}_{CC} by the following BFN:

$$t := c \mid x_n \mid you_n \mid I_n$$

$$\phi := Pt_1, \dots, t_m \mid t_1 = t_2 \mid \neg \phi \mid \phi \land \phi \mid \exists x_n \phi \mid \Box \phi$$

where $c \in \mathcal{C}$, $x_n \in \mathcal{V}_N$, and $P \in \mathcal{P}$.

The usual abbreviations for \vee ('disjunction'), \rightarrow ('implication'), \leftrightarrow ('biimplication'), \forall ('universal quantifier') and \Diamond ('possibility') apply.

4.2 Semantics

A model for \mathcal{L}_{CC} is a quintuple $\langle W, R, D, I, C \rangle$ in which W is a non-empty set of possible worlds; R is a relation on W; D is a non-empty set of individuals; I is an interpretation function which assigns for each $w \in W$ an element $I_w(c)$ of

D to each individual constant c in C, and a subset $I_w(P)$ of D^m to each m-ary predicate P in P; and C is a set of conceptual covers over (W, D).

Given a model $M = \langle W, R, D, I, C \rangle$, a perspective \wp is a function that maps every CC-index $n \in N$ to some conceptual cover in C.

Definition 6 (Perspectives) Given a set of CC-indices N and a model $M = \langle W, R, D, I, C \rangle$, a perspective \wp is a function such that $\forall n \in N : \wp(n) \in C$.

Given a certain perspective \wp , an assignment function g_{\wp} maps every variable x_n to some individual concept in $\wp(n)$.

Definition 7 (Assignment functions) Given a set of variables \mathcal{V}_N , a model $M = \langle W, R, D, I, C \rangle$, and a perspective \wp , an assignment function g_{\wp} is a function that maps every variable x_n in \mathcal{V}_N to some individual concept in $\wp(n)$.

Thus, a variable x_n is assigned a value in two steps. First, \wp determines the conceptual cover $\wp(n)$ that x_n ranges over, and then g_{\wp} maps x_n to some individual concept in $\wp(n)$.

Well-formed expressions in \mathcal{L}_{CC} are interpreted in models with respect to a perspective-dependent assignment function g_{\wp} and two worlds $v, w \in W$, with the first world v playing the role of a Kaplanian context. Terms are interpreted as follows:

Definition 8 (Individual Constants and Variables)

Individual constants are interpreted as in classical quantified modal logic. Variables x_n , instead, range over concepts in $\wp(n)$ rather than plain individuals in D. Note however that the denotation $[x_n]_{M,v,w,g_\wp}$ of a variable x_n with respect to a world of evaluation w is not the concept $g_\wp(x_n) \in \wp(n)$, but rather the value $g_\wp(x_n)(w)$ of the concept $g_\wp(x_n)$ in w, i.e. an individual in p. Thus, variables do not refer to concepts, but to individuals. However, they do refer in a non-rigid way: different individuals can be their value in different worlds. The same holds for indexical terms you_n and I_n , which are assigned elements α of a pragmatically selected conceptual cover $\wp(n)$, but refer to individuals $\alpha(w)$ when interpreted with respect to a world of evaluation w. Which $\alpha \in \wp(n)$ an indexical term is assigned to crucially depends on the context-world v: I_n is assigned the unique $\alpha \in \wp(n)$ that maps v to the speaker in v; you_n is assigned the unique $\alpha \in \wp(n)$ that maps v to the addressee in v; that there are such unique α is guaranteed by the existence and uniqueness condition on conceptual covers.

Definition 9 (Indexicals)

$$\llbracket I_n \rrbracket_{M,v,w,g_\wp} = \alpha(w), \text{ where } \alpha \in \wp(n) \& \alpha(v) = \llbracket \text{the speaker} \rrbracket_{M,v,v,g_\wp} \\ \llbracket \text{you}_n \rrbracket_{M,v,w,g_\wp} = \alpha(w), \text{ where } \alpha \in \wp(n) \& \alpha(v) = \llbracket \text{the addressee} \rrbracket_{M,v,v,g_\wp}$$

The denotation of an indexical, given a perspective \wp , will depend on both the context-parameter v and the world of evaluation w: the context-world v, with perspective \wp , determines t the concept α , since α is the unique element of the cover $\wp(n)$ which maps the context-world v to the actual speaker/addressee in v; the world of evaluation w provides the argument of α . Note that the denotation of I_n/you_n , $\alpha(w)$, needs not be speaking/hearing in w, if $w \neq v$.

Formulas are interpreted in models M with respect to a perspective-dependent assignment function g_{ω} and two worlds $v, w \in W$. The context-world parameter v only plays a role in the interpretation of formulas containing indexicals terms. Modals shift the world of evaluation w parameter while leaving the contextworld v unchanged (clause 5). Quantifiers range over elements of contextually determined conceptual covers, rather than over individuals simpliciter (clause 6). All other clauses are standard.

Definition 10 (Formulas)

$$M, v, w \models_{g_{\wp}} Pt_1, \dots t_n \quad iff \quad \langle \llbracket t_1 \rrbracket_{M, v, w, g_{\wp}}, \dots, \llbracket t_n \rrbracket_{M, v, w, g_{\wp}} \rangle \in I_w(P) \quad (1)$$

$$M, v, w \models_{g_{\wp}} t_1 = t_2 \quad \text{iff} \quad [\![t_1]\!]_{M, v, w, g_{\wp}} = [\![t_2]\!]_{M, v, w, g_{\wp}}$$
 (2)

$$M, v, w \models_{g_{\wp}} \neg \phi \quad iff \quad not \ M, v, w \models_{g_{\wp}} \phi$$
 (3)

$$M, v, w \models_{q_n} \phi \land \psi$$
 iff $M, v, w \models_{q_n} \phi$ and $M, v, w \models_{q_n} \psi$ (4)

$$M, v, w \models_{q_n} \Box \phi \quad iff \quad \forall w' : wRw' : M, v, w' \models_{q_n} \phi$$
 (5)

$$M, v, w \models_{g_{\wp}} \neg \phi \quad iff \quad not \ M, v, w \models_{g_{\wp}} \phi \qquad (3)$$

$$M, v, w \models_{g_{\wp}} \phi \wedge \psi \quad iff \quad M, v, w \models_{g_{\wp}} \phi \quad and \ M, v, w \models_{g_{\wp}} \psi \qquad (4)$$

$$M, v, w \models_{g_{\wp}} \Box \phi \quad iff \quad \forall w' : wRw' : M, v, w' \models_{g_{\wp}} \phi \qquad (5)$$

$$M, v, w \models_{g_{\wp}} \exists x_n \phi \quad iff \quad \exists c \in \wp(n) : M, v, w \models_{g_{\wp}[x_n/c]} \phi \qquad (6)$$

Logical validity is defined as 'real-world validity' (Humberstone, 2004).

Definition 11 (Logical validity)

$$\begin{split} M &\models \phi \qquad \textit{iff} \qquad \forall v \in W, \forall g_\wp : M, v, v \models_{g_\wp} \phi \\ &\models_{2D_{CC}} \phi \qquad \textit{iff} \qquad \forall M : M \models \phi \end{split}$$

4.3 Applications

4.3.1 Basic properties, non-rigidity and descriptive uses

The basic properties of indexicals and their appearance in contingent a priori statements are accounted for as in Kaplan.

- (41)I am the speaker. (contingent a priori)
- (42)The speaker is the speaker. (necessary a priori)

Example (42) is necessary and a priori, because the following are both validated:

(43)
$$\models_{2D_{CC}} the speaker = the speaker$$
 (a priori)

$$(44) \qquad \models_{2D_{CC}} \Box the \ speaker = the \ speaker \qquad (necessary)$$

Example (41), in contrast, is contingent a priori, because, given our notion of validity, (45) is logically valid, while (46) isn't.

(45)
$$\models_{2D_{GG}} I_n = the \ speaker$$
 (a priori)

(46)
$$\not\models_{2D_{CC}} \Box I_n = the \ speaker$$
 (but not necessary)

(45) is logically valid, because for all models M, worlds v, and assignments g_{\wp} : $\llbracket I_n \rrbracket_{M,v,v,g_{\wp}} = \llbracket the \; speaker \rrbracket_{M,v,v,g_{\wp}}$ by definition. (46) instead is not valid because $\llbracket I_n \rrbracket_{M,v,w,g_{\wp}}$ need not be speaking in w, and so need not be equivalent to $\llbracket the \; speaker \rrbracket_{M,v,w,g_{\wp}}$.

The present semantics also allows us a ready account of indexicals in situations of partial information, as in Santorio's and Richard's examples.

The following principle is not valid in $2D_{CC}$, and this allows us to account for Santorio's amnesiacs cases:

$$(47) \qquad \not\models_{2D_{GG}} I_n = a \to \Box I_n = a$$

Indexicals are typically assigned elements of perceptually-based conceptual covers, which, however, don't need be sets of constant functions.

Also the following principle is invalidated in the present semantics, since n and m can be mapped to two different conceptual covers:

$$(48) \qquad \not\models_{2D_{CC}} you_n = x_m \to \Box you_n = x_m$$

This allows us to account for Richard's phone booth example, with x_m standing for she, assuming the availability of two different perceptually-based covers (visual vs auditory).

Finally, we show how descriptive uses of indexicals are captured in $2D_{CC}$. Consider again the WhatsApp example:

(49) (Why did you send me the password?) I could have been a Republican. 'A Republican could have sent you the WhatsApp message'

a. De
$$re: \exists x_n [x_n = I_m \land \Diamond Rx_n]$$
 (only n relevant here)
b. De $dicto: \Diamond \exists x_n [x_n = I_m \land Rx_n]$ (only m relevant here)

Since both variables and indexicals can refer in a non-rigid way, the descriptive intended meaning of (49) can be captured in $2D_{CC}$ via either (i) the de re or (ii) the de dicto representation. Let α be the concept $\lambda w[the\ sender\ of\ the\ WhatsApp\ message]_w$. In case (i), the intended meaning follows if we assume that x_n ranges over a cover containing α , so $\alpha \in \wp(n)$; in case (ii), the intended meaning follows if we assume that the indexical I_m is assigned the concept α , so $\alpha \in \wp(m)$. Similar explanations can be given for all examples discussed in Section 1.3. Notice that the value of a CC-index n matters only when an n-indexed term $(x_n/I_n/you_n)$ occurs free in the scope of a modal operator (see Aloni, 2016, for a proof). So in (49-a) only the value of n matters, and in (49-b) only the value of m.

4.3.2 Logic of reference

Substitutivity of identicals and existential generalisation fail in general in $2D_{CC}$:

$$(50) \qquad \not\models_{2D_{CC}} x_n = y_m \to (\phi[x_n] \to \psi[y_m])$$

$$(51) \qquad \not\models_{2D_{CC}} \phi[y_m] \to \exists x_n \phi[x_n]$$

But restricted forms of these principles are validated for variables and indexicals, while would fail for definite descriptions (assuming $\llbracket \iota x_n \phi \rrbracket_{M,v,w,g_{\wp}} = c(w)$, if there is a unique $c \in \wp(n)$ such that $\llbracket \phi \rrbracket_{M,v,w,g_{\wp}}[x_n/c] = 1$; empty (of undefined), otherwise)

(52)
$$\models_{2D_{CC}} x_n = y_n \to (\phi[x_n] \to \psi[y_n])$$
 (SI_n, variables/indexicals) $\models_{2D_{CC}} I_n = y_n \to (\phi[I_n] \to \psi[y_n])$

(53)
$$\models_{2D_{CC}} \phi[y_n] \to \exists x_n \phi[x_n]$$
 (EG_n, variables/indexicals) $\models_{2D_{CC}} \phi[I_n] \to \exists x_n \phi[x_n]$

(54)
$$\not\models_{2D_{CC}} \iota x_n P x_n = y_n \to (\phi[\iota x_n P x_n] \to \phi[y_n]) \\
\not\models_{2D_{CC}} \phi[\iota y_n P y_n] \to \exists x_n \phi[x_n]$$
(SI_n, descriptions)
(EG_n, descriptions)

The validities in (52) and (53) rely on the uniqueness and existence conditions on conceptual covers respectively. As in Kaplan, but in contrast to $2D_R$, in the newly proposed semantics indexicals behave as variables and not as definite descriptions.

$2D_K$	SI	\mathbf{EG}
variables	yes	\mathbf{yes}
indexicals	yes	\mathbf{yes}
definites	no	no

$2D_R$	SI	\mathbf{EG}
variables	\mathbf{yes}	\mathbf{yes}
indexicals	no	no
definites	no	no

$2D_{CC}$	\mathbf{SI}_n	\mathbf{EG}_n
variables	yes	yes
indexicals	yes	\mathbf{yes}
definites	no	no

The intuitive contrast between indexicals and descriptions, however, is still not fully accounted for. Consider again our Obama examples. While (55) is naturally ambiguous, (56) requires a very specific context to give rise to a descriptive reading:

- (55) The president of the US could have been a Republican.
 - a. Barack Obama could have been a Republican
 - b. A Republican (Romney) could have won the last elections
- (56) I could have been a Republican. (used by Obama)
 - a. Obama could have been a Republican (in ordinary circumstances)
 - b. A Republican could have sent you the WhatsApp message (in WhatsApp scenario)

In the following section we will propose a pragmatic explanation of these phenomena. The contextual selection of a conceptual cover will be regulated by general pragmatic principles which will prevent descriptive covers to be at work in ordinary cases, while being possibly operative in extraordinary circumstances (as in the WhatsApp scenario).

5 Pragmatic Theory

On the present account, referential expressions (variables, indexicals) are perspectivesensitive expressions, their logical representation involves CC-indices n whose value needs to be pragmatically supplied. It is well-known however that pragmatic accounts often run the risk of overgeneration. For example, consider again our Obama sentence used in a neutral context:

(57) I could have been a Republican.

(used by Obama)

- a. Obama could have been a Republican
- b. A Republican could have been speaking

Nothing prevents x_n or I_m in (58) to be assigned to $\lambda w.[the speaker]_w$, so both $de \ re$ and $de \ dicto$ (58-a-b) could mean (57-b), against intuitions:

(58) a. De re: $\exists x_n [x_n = I_m \land \Diamond Rx_n]$ b. De dicto: $\Diamond \exists x_n [x_n = I_m \land Rx_n]$

What this example shows is that the resolution process of cover indices needs to be suitably constrained. The present section discusses some factors that we take to play a role in this process.

5.1 Constraints on pragmatic resolution

We assume that there are certain default choices for the resolution of cover indices, from which however we can sometimes deviate. Deviation from the default choices though is costly and only justified if needed in order to comply with Gricean principles of conversation. More precisely, we assume the following:

Definition 12 (Constraints on pragmatic resolution)

- 1. CC-indices by default are mapped to a perceptually-based cover (if application criteria apply) or naming (if application criteria apply)
- 2. Resolution to a non-default salient cover is possible but licensed (i) only if it is needed in order to avoid trivial, contradictory or irrelevant meanings, and (ii) only if the obtained content could not have been expressed by a more perspicuous/effective form.

A proper description of the application criteria for a perceptually-based identification and naming is beyond the scope of this article, but roughly they seem to relate to the application criteria of demonstratives and proper names: perceptually-based identification requires the relevant individuals to be in the perceptual surroundings of the interlocutors, as proper uses of demonstratives do, while identification by naming requires the availability of *shared* names for these individuals. When talking to a stranger you don't refer to your son as 'John', but you refer to president of the US as 'Obama' because only the latter can be assumed to be a shared name. Similarly, only when shared names are available, naming can be adopted as identification method.

5.2 Illustrations

Default resolutions: indexicals vs definite descriptions In a neutral context deviation from default resolutions are unjustified (clause 1 in Definition 12). Like Kaplan, we predict a contrast between examples like (59), containing an indexical, and (60), containing a definite description. Only the latter are predicted to be ambiguous by our pragmatic theory.

No ambiguity arises for (59) because both *de re* and *de dicto* representations depend on the operative conceptual cover, which, in ordinary cases, is predicted to be perceptually-based by our pragmatic theory.

(59) I could have been Republican. (used by Obama) 'Obama himself could have been a Republican'

```
a. De re: \exists x_n [x_n = I_m \land \Diamond Rx_n]
b. De dicto: \Diamond \exists x_n [x_n = I_m \land Rx_n]
\Rightarrow \text{Optimal resolution: } n, m \text{ assigned } perceptually-based cover}
```

Example (60), instead, is predicted to be ambiguous: the *de re* representation (60-a) is perspective-dependent and, in ordinary cases, receives a non-descriptive interpretation (assuming that Obama is not in the perceptual surroundings of the interlocutors, naming is predicted as operative here); the *de dicto* representation (60-b), in contrast, expresses a descriptive meaning irrespective of the operative cover.

(60) The president of the US could have been a Republican.

```
a. De re: \exists x_n[x_n = \iota y_m P y_m \land \Diamond R x_n]

'Obama could have been a Republican'

\Rightarrow Optimal resolution: x_n ranges over naming cover
```

b. De dicto: $\Diamond \exists x_n [x_n = \iota y_m P y_m \land R x_n]$ 'A Republican could have won the last elections' \Rightarrow (values of n, m irrelevant here)

Deviations and blocking effects: the WhatsApp example Deviations from default resolutions are licensed if necessary to avoid violation of Gricean principles of conversation (clause 2(i) in Definition 12). This gives us an explanation of the WhatsApp example. A descriptive reading is predicted here because a default resolution would have led to a violation of the Maxim of Relevance.

(61) (Why did you send me the password?) I could have been a Republican. 'A Republican could have sent you the WhatsApp message'

```
a. De \ re: \exists x_n[x_n = I_m \land \Diamond Rx_n]
b. De \ dicto: \Diamond \exists x_n[x_n = I_m \land Rx_n]
\Rightarrow \text{Optimal resolution: } \lambda w[\![ the \ sender \ of \ the \ WhatsApp]\!]_w \in n, m
```

Numberg observed that such deferred reference readings are not available for definite descriptions. There is a contrast between (61) and (62), only the former allows a deferred reference interpretation.

- (62) (Why did you send me the password?) The speaker could have been a Republican.
 - # 'A Republican could have sent you the WhatsApp message'
 - a. De re: $\exists x_n[x_n = the \ speaker \land \Diamond Rx_n]$
 - b. De dicto: $\lozenge \exists x_n [x_n = the \ speaker \land Rx_n]$

The present pragmatic theory can account for this contrast in terms of blocking effects (clause 2(ii) in Definition 12). Note that de re representation (62-a) would express the problematic content if we resolve n to a cover containing the concept $\lambda w[\![the\ sender\ of\ the\ WhatsApp]\!]_w$. However such a relevance-justified deviation, which was licensed for (61), is blocked for (62) by the availability of a more efficient form for the target content (see Aloni, 2005a, for a formalisation of this reasoning in the framework of bi-directional optimality). Recall that resolutions to non-default salient covers are possible only if the obtained content could not have been expressed by a more perspicuous/effective form. In the present semantics, all forms in (63-b) can be interpreted as expressing content (63-a).

- (63) a. Target *content*: 'The sender of the WhatsApp could have been a Republican'
 - b. Alternative possible forms:
 - (i) The sender of the WhatsApp could have been a Republican.
 - (ii) I could have been a Republican.
 - (iii) The speaker could have been a Republican.

Interpretation (63-a) however is blocked for form (iii) by the more efficient forms (i)-(ii). So no deferred reference meaning is predicted for sentences like (64):

- (64) (Why did you send me the password?) The speaker could have been a Republican.
 - # 'A Republican could have sent you the WhatsApp message'
 - \Rightarrow non-default resolution NOT licensed

On the other hand, nothing is strictly more effective than form (ii) given the circumstances of the utterance. The 1st personal pronoun 'I' is the preferred referential device for a speaker who wants to refer to herself (see Aloni, 2005a, for more discussion on the pragmatic principles ruling the choice of a referential device). So a deferred reference meaning is predicted for sentences like (65):

- (65) (Why did you send me the password?) I could have been a Republican.
 - 'A Republican could have sent you the WhatsApp message'
 - ⇒ non-default resolution licensed

6 Conclusion

By letting indexicals and variables refer to elements of contextually supplied conceptual covers and by formulating general constraints on these pragmatic selection procedures, we have proposed an account of indexicals which captures a number of cases that have been presented against a Kaplanian analysis, while maintaining Kaplan's basic insights concerning the genuinely referential nature of 'you' and 'I'.

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