

# Free choice and exhaustification: an account of subtriggering effects

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# Overview

## ① Examples:

- (1)    a. #Any woman fell.  
       b.    Any woman may fall.  
       c.    Any woman who tried to jump fell.        (SUBTRIGGERING)

## ② Goal: explain distribution and meaning of *any* in (1).

## ③ Key components of the analysis:

- ▶ *Any* is an indefinite (*contra* Dayal)
- ▶ Indefinites induce sets of propositional alternatives (Aloni, K&S)
- ▶ *Any* triggers hidden structure (Menéndez-Benito):

(2)     $[\forall] \dots \mathbf{Exh} (\dots \text{any} \dots)$

- ▶ Facts in (1) explained by interactions between  $[\forall]$ , **Exh** and the modal operator (in (1b)) and the post-nominal modifier (in (1c)).

# Structure of the talk

## ① Background:

- ▶ ‘Hamblin’ semantics for indeterminate pronouns (K&S 2002);
- ▶ Menéndez-Benito (2005) on *any* in modal statements.

## ② Proposal: subtriggering and modal effects via exhaustification.

- ▶ Exhaustification (Zeevat 1994);
- ▶ Type-shift rules :  $\text{SHIFT}_e$  &  $\text{SHIFT}_{\langle s, t \rangle}$ ;
- ▶ A first application: free relatives and wh-interrogatives (Jacobson 1995);
- ▶ Main application: subtriggering and modal effects of FC *any*.

# ‘Hamblin’ semantics for indeterminate pronouns

## MOTIVATION

- Explain variety of indefinite pronouns. E.g. *any*, *a*, *some*, ...

## How

- Indefinites ‘introduce’ sets of propositional alternatives.
- These are bound by propositional operators:  $[\exists]$ ,  $[\forall]$ ,  $[\text{Neg}]$ .
- Different indefinites associate with different operators.

## EXAMPLES

- (3)
- a.  $[\exists]$  (someone fell)
  - b.  $[\forall]$  (anyone fell)
  - c.  $[\text{Neg}]$  (nessuno cadde)

- d. 

$d_1$ fell	$d_2$ fell	$d_3$ fell	...
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## A closer look

- In a Hamblin semantics, all expressions denote sets.
- Mostly singleton sets of traditional denotations. E.g.

$$(4) \quad \llbracket \text{fell} \rrbracket_{w,g} = \{\lambda x \lambda w'. \text{FELL}(x)(w')\}$$

- Indefinites map to multi-membered sets of alternatives. E.g.

$$(5) \quad \llbracket \text{someone/anyone/who} \rrbracket_{w,g} = \{x \mid \text{HUMAN}(x)(w)\}$$

- Via pointwise functional application, these alternatives expand into propositional sets:

$$(6) \quad \llbracket \text{fell} \rrbracket_{w,g}(\llbracket \text{someone/anyone/who} \rrbracket_{w,g}) = \{\text{that } d_1 \text{ fell, that } d_2 \text{ fell, that } d_3 \text{ fell, ...}\}$$

- Until they reach one of the propositional operators. E.g.

$$(7) \quad \llbracket \forall \rrbracket(\llbracket \text{fell} \rrbracket_{w,g}(\llbracket \text{anyone} \rrbracket_{w,g})) = \{\text{that everyone fell}\}$$

# Any: naif account

- $[\forall]$  quantifies over propositional alternatives.

(8)	a.	$[\forall]$ (anyone fell)	<table><tr><td><math>d_1</math> fell</td><td><math>d_2</math> fell</td><td><math>d_3</math> fell</td><td>...</td></tr></table>				$d_1$ fell	$d_2$ fell	$d_3$ fell	...
	$d_1$ fell	$d_2$ fell	$d_3$ fell	...						
	b.	$[\forall]$ (anyone may fall)	<table><tr><td><math>\diamond d_1</math> fall</td><td><math>\diamond d_2</math> fall</td><td><math>\diamond d_3</math> fall</td><td>...</td></tr></table>				$\diamond d_1$ fall	$\diamond d_2$ fall	$\diamond d_3$ fall	...
$\diamond d_1$ fall	$\diamond d_2$ fall	$\diamond d_3$ fall	...							
c.	$[\forall]$ (anyone who tried to jump fell)	<table><tr><td><math>d_1</math> fell</td><td><math>d_2</math> fell</td></tr></table>				$d_1$ fell	$d_2$ fell			
$d_1$ fell	$d_2$ fell									

- MERITS: captures universal meaning of (c);
- PROBLEMS: doesn't explain (a) & dubious truth-conditions for (b):

E.g. suppose only two options: (i) nobody falls; (ii) everybody falls.  
Then (b) would be true against intuitions [Menéndez-Benito 2005].

## Any: Menéndez-Benito account

- **Excl** transforms Hamblin alternatives into sets of mutually exclusive propositions.

(9) a.  $[\forall](\mathbf{Excl}(\text{anyone fell}))$

only $d_1$ fell	only $d_2$ fell	...
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b.  $[\forall](\diamond(\mathbf{Excl}(\text{anyone fall})))$

$\diamond$ only $d_1$ fall	$\diamond$ only $d_2$ fall	...
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c.  $[\forall](\mathbf{Excl}(\text{anyone who tried to jump fell}))$

only $d_1$ fell	only $d_2$ fell
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- MERITS: captures (a) (out because inconsistent) and (b) (consistent and unrestricted liberty of choice);
- PROBLEMS: doesn't extend to (c) (out because inconsistent).

# Synopsis

- DESIDERATA:
  - ▶ M-B's predictions for the unsubtriggered and modal cases (a) and (b) [via **Excl**];
  - ▶ Naif account's predictions for the subtriggered case (c) [no **Excl**].
- Question: why **Excl** does not seem to play a role when a post-nominal modifier is present?
- My answer will assume, rather than **Excl**, a much more general and independently motivated notion **Exh** of exhaustification.



# Exhaustification

- At work in the semantics of a large variety of constructions, a.o. free relatives, wh-interrogatives, correlatives, degree relatives (Grosu & Landman)
  - Not surprising if at work in FC constructions, which in many languages employ wh-morphology (Giannakidou & Cheng)
  - Exhaustive values: minimal/maximal elements wrt some order (e.g. Zeevat 1994)
- (10)     a.    What J can spend is less than what J can live on.  
             b.    The max amount of money that J can spend is less than the min amount of money that J can live on.
- (11)     a.    John helped who fell.  
             b.    John helped the (max collection of) people that fell.

# The **Exh** operator

- **Exh** takes a domain  $D$  and a property  $P$  and returns the property of exhaustively satisfying  $P$  wrt  $D$ :

$$(12) \quad \begin{array}{ll} \text{a.} & \mathbf{Exh}[D, P] \qquad \qquad \qquad \text{type: } \langle e, \langle s, t \rangle \rangle \\ \text{b.} & \{\lambda x \lambda w [x \text{ exhaustively satisfies } P \text{ wrt } D \text{ in } w]\} \end{array}$$

- E.g. using Zeevat 1994:

$$(13) \quad x \text{ exhaustively satisfies } P \text{ wrt } D \text{ iff } x \text{ is in } D, P(x) \text{ is true, and for all } y \text{ in } D \text{ if } P(y) \text{ is true then } P(x) \text{ entails } P(y).$$

- $x$  and  $y$  range over domains of plural individuals (e.g. Link 1983).

# Two type-shift rules for properties

①  $\text{SHIFT}_e: \langle e, \langle s, t \rangle \rangle \rightarrow e$  (from properties to **entities**)

(14) Partee iota rule:

a.  $P \rightarrow \iota x[P(x)(w)]$

b.  $\{P\} \rightarrow \{d\}$  if  $d$  is the unique  $P$  in  $w$ ,  
undefined otherwise

②  $\text{SHIFT}_{\langle s, t \rangle}: \langle e, \langle s, t \rangle \rangle \rightarrow \langle s, t \rangle$  (from properties to **propositions**)

(15) Hamblin question formation rule:

a.  $P \rightarrow \hat{p} [\exists x[P(x) = p]]$

b.  $\{P\} \rightarrow \{d_1 \text{ is } P, d_2 \text{ is } P, d_3 \text{ is } P, \dots\}$

# Type shifting exhaustive values

When applied to **exh**[D,P]

(i)  $\text{SHIFT}_e$  (always defined) yields maximal plural entities:

- (16)    a.  $\text{SHIFT}_e(\mathbf{exh}[D, P])$   
           b. {the sum of entities from  $D$  satisfying  $P$  in  $w$ }

(ii)  $\text{SHIFT}_{\langle s, t \rangle}$  yields sets of mutually exclusive propositions:

- (17)    a.  $\text{SHIFT}_{\langle s, t \rangle}(\mathbf{exh}[D, P])$   
           b. {only  $d_1$  is  $P$ , only  $d_2$  is  $P$ , only  $d_1$  &  $d_2$  are  $P$ , ... }

# First application: Free relatives and wh-interrogatives

- Free relatives and wh-interrogatives are born with the same meaning:

- (18)
- a. who fell type:  $\langle e, \langle s, t \rangle \rangle$
  - b. **exh**[who, fell]
  - c.  $\{\lambda x \lambda w [x \text{ is the sum of people falling in } w]\}$

- But typeshift differently (cf. Cooper, Jacobson):

- (19)
- a. John helped [<sub>DP</sub> who fell] type:  $e$
  - b.  $\text{SHIFT}_e(\text{exh}[\text{who, fell}])$
  - c.  $\{\text{the sum of people falling in } w\}$

- (20)
- a. John knows [<sub>Q</sub> who fell] type:  $\langle s, t \rangle$
  - b.  $\text{SHIFT}_{\langle s, t \rangle}(\text{exh}[\text{who, fell}])$
  - c.  $\{\text{only } d_1 \text{ fell, only } d_2 \text{ fell, only } d_1 \ \& \ d_2 \text{ fell, ... } \}$

# A closer look at interrogatives

- Questions and propositions have the same type in a Hamblin semantics, namely  $\langle s, t \rangle$ . Questions typically denote multi-membered sets.
- Difference between question/proposition embedding verbs explained in terms of propositional quantifiers:

(21) a. John knows who fell/that Mary fell.  
 b.  $\text{Bel}_j[\text{true}](A)$

(22) a. John believes that Mary fell/#who fell.  
 b.  $\text{Bel}_j[\exists](A)$

(23) a. John wonders who fell/# that Mary fell.  
 b.  $[\forall] \neg \text{Bel}_j(A)$

## A closer look at free relatives

- We assume a further operation  $\downarrow$  which transforms singletons of plural sets into sets of atomic alternatives:

$$\begin{array}{ll}
 (24) \quad \text{a.} & \llbracket \alpha \rrbracket_{w,g} = \{\{a, b\}\} \quad \text{a singleton set of plural entities} \\
 & \text{b.} \quad \llbracket \downarrow \alpha \rrbracket_{w,g} = \{a, b\} \quad \text{a set of atomic alternatives}
 \end{array}$$

- $\downarrow$  needed to account for universal/distributive meanings of free relatives (and degree relatives) (cf. Grosu and Landman):

$$\begin{array}{ll}
 (25) & \text{We will veto three-quarters of whatever proposals you make.} \\
 & \text{a. Of the proposals: three-quarters won't make it. (definite)} \\
 & \text{b. For each proposal: three-quarters of it will be vetoed.} \\
 & \hspace{20em} \text{(universal)}
 \end{array}$$

$$(26) \quad \text{I took with me every book there was on the table.}$$

# Subtriggering and modal effects: core idea

- FC items like wh-words trigger the application of **Exh**.

- UNSUBTRIGGERED CASES:

- (27)      a.     $[_{IP}$  Any woman fell]  
              b.     $[_{IP}$  Any woman may fall]

- ▶ Exhaustification must apply at the IP level;
- ▶  $\text{SHIFT}_{\langle s,t \rangle}$  generates sets of mutually exclusive propositional alternatives.

- SUBTRIGGERED CASES:

- (28)       $[_{DP}$  Any woman who tried to jump] fell.

- ▶ Exhaustification can apply at the DP level;
- ▶  $\text{SHIFT}_e$  and  $\downarrow$  apply and generate sets of individuals.

- Post-nominal modifier crucial for (28) because it supplies the 2nd argument essential for the application of **Exh** inside the DP.



# Any: final proposal

$$(29) \quad a. \quad [\forall](\text{SHIFT}_{(s,t)}(\mathbf{Exh}[\text{anyone, fell}]])$$

only $d_1$ fell	only $d_2$ fell	...
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$$b. \quad [\forall](\Diamond(\text{SHIFT}_{(s,t)}(\mathbf{Exh}[\text{anyone, fall}])))$$

$\Diamond$ only $d_1$ fall	$\Diamond$ only $d_2$ fall	...
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$$c. \quad [\forall](\downarrow\text{SHIFT}_e(\mathbf{Exh}[\text{anyone, who tried to jump}]) \text{ fell})$$

$d_1$ fell	$d_2$ fell
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- MERITS: captures (a) (out because inconsistent), (b) (consistent and unrestricted freedom of choice) and (c) (consistent and universal meaning).
- PROBLEMS: ...

# Problems, problems, problems

- THEORETICAL: Where do  $[\forall]$  and **Exh** come from?
- EMPIRICAL: Not every type of postnominal modifier yields (good) subtriggers. Infinitival relatives don't.

- (30)
- a. A friend to talk to is a blessing.
  - b. #Any friend to talk to is a blessing.
  - c. Any friend who you can talk to is such a blessing.

- ...

THE END