# Assignment 3: Q-Learning

In this assignment you will implement deep Q-networks (DQN) [1], a Q-learning algorithm that leverages deep neural networks, to play Atari games. The template code is available at:

Installation instructions are provided in README.md. All of the files that need to be changed in this assignment are located in the a3/ directory. No files outside of this directory should be modified. Locations where code needs to be modified are labeled TODO.

## 1 Q-Learning

Q-learning is a family of reinforcement learning algorithms that solves an MDP by learning a Q-function  $Q(\mathbf{s}, \mathbf{a})$ , instead of directly learning a policy  $\pi(\mathbf{a}|\mathbf{s})$ . The Q-function  $Q^{\pi}$  provides an estimate of the expected return of performing an action  $\mathbf{a}$  in state  $\mathbf{s}$ , and following a policy  $\pi$  for all future timesteps,

$$Q^{\pi}(\mathbf{s}, \mathbf{a}) = \mathbb{E}_{\tau \sim p(\tau \mid \pi, \mathbf{s}_0 = \mathbf{s}, \mathbf{a}_0 = \mathbf{a})} \left[ \sum_{t} \gamma^t r_t \right]. \tag{1}$$

The optimal Q-function for a given MDP can be learned using an iterative fixed-point method, where at each iteration k, a new Q-function  $Q^{k+1}$  is constructed via the Bellman update by bootstrapping from the current Q-function  $Q^k$ :

$$Q^{k+1}(\mathbf{s}, \mathbf{a}) = \mathbb{E}_{\mathbf{s}' \sim p(\mathbf{s}'|\mathbf{s}, \mathbf{a})} \left[ r(\mathbf{s}, \mathbf{a}, \mathbf{s}') + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}') \right], \tag{2}$$

where  $r(\mathbf{s}, \mathbf{a}, \mathbf{s}')$  is the reward function,  $\gamma \in [0, 1]$  is a discount factor, and  $p(\mathbf{s}'|\mathbf{s}, \mathbf{a})$  represents the dynamics of the environment.

A policy can be recovered from a given Q-function by selecting the action with the maximum predicted Q-value at a given state:

$$\pi^{k}(\mathbf{a}|\mathbf{s}) = \begin{cases} 1 & \text{if } \mathbf{a} = \arg\max_{\mathbf{a}'} Q^{k}(\mathbf{s}, \mathbf{a}') \\ 0 & \text{otherwise} \end{cases}$$
 (3)

This arg-max procedure returns a deterministic policy that selects actions greedily according to the Q-function. If Q-function is the optimal Q-function  $Q^*$ , then the resulting arg-max policy will be an optimal policy  $\pi^*$ . However, if the Q-function is not optimal, then a deterministic greedy policy will often lead to insufficient exploration during the learning process.  $\epsilon$ -greedy exploration is a simple strategy that mitigate this exploration issue by constructing a stochastic policy

$$\pi^{k}(\mathbf{a}|\mathbf{s}) = \begin{cases} 1 - \epsilon & \text{if } \mathbf{a} = \arg\max_{\mathbf{a}'} Q^{k}(\mathbf{s}, \mathbf{a}') \\ \epsilon & \text{otherwise} \end{cases}, \tag{4}$$

which greedily select the best action according to the current Q-function with probability  $1-\epsilon$ , and selects a random action with probability  $\epsilon$ . This methods helps to ensure that the agent can explore new actions and potentially discover more optimal strategies during the training process. Pseudo-code for Q-learning is available in Algorithm 1.

### **ALGORITHM 1:** Q-Learning

```
    Q<sup>0</sup> ← initialize Q-function
    D ← {∅} initialize dataset
    for iteration k = 0, ..., n − 1 do
    Sample trajectory τ according to Q<sup>k</sup>(s, a)
    Add transitions to dataset D = D ∪ {(s<sub>i</sub>, a<sub>i</sub>, s'<sub>i</sub>)}
    Calculate target values for each sample i: y<sub>i</sub> = r<sub>i</sub> + γ max<sub>a'</sub> Q<sup>k</sup>(s'<sub>i</sub>, a')
    Update Q-function: Q<sup>k+1</sup> = arg min<sub>Q</sub> E<sub>(s<sub>i</sub>,a<sub>i</sub>,r<sub>i</sub>,s'<sub>i</sub>)~D</sub> [(y<sub>i</sub> - Q(s<sub>i</sub>,a<sub>i</sub>))<sup>2</sup>]
    end for
    return Q<sup>n</sup>
```

In this assignment, you will be implementing the deep Q-networks (DQN) algorithm to play Atari games [1]. To run DQN on the Pong task, use the following command:

```
python run.py --mode train \
--env_config data/envs/atari_pong.yaml \
--agent_config a3/atari_pong_dqn_agent.yaml \
--log_file output/log.txt \
--out_model_file output/model.pt \
--max_samples 3000000 \
--visualize
```

--visualize should be disabled for faster training. If you have a GPU that supports Cuda, then --device cuda:0 can be used to enable Cuda during training, which can be much faster. Once a model has been trained, you can load a checkpoint and test the model with the following command:

```
python run.py --mode test \
--env_config data/envs/atari_pong.yaml \
--agent_config a3/atari_pong_dqn_agent.yaml \
--model_file output/model.pt \
--test_episodes 20 \
--visualize
```

### 1.1 Epsilon-Greedy Exploration

In a3/dqn\_agent.py , implement the \_get\_exp\_prob() method, which calculates the probability  $\epsilon$  of selecting a random action in  $\epsilon$ -greedy exploration. Since the Q-function is randomly initialized at the start of training, the exploration probability typically starts with a high value (e.g.  $\epsilon = 1$ ), and then decreases to a low value (e.g.  $\epsilon = 0.1$ ) over the course of training as the Q-function improves. The exploration probability starts with a value of  $\epsilon_{\text{beg}}$ , and then linearly annealed to  $\epsilon_{\text{end}}$  over the course of  $n_{\text{max}}$  samples,

$$\epsilon(n) = (1 - l)\epsilon_{\text{beg}} + l\epsilon_{\text{end}}, \qquad l = \text{clip}\left(\frac{n}{n_{\text{max}}}, 0, 1\right),$$
(5)

where n denotes the total number of samples collected for training so far. The initial exploration probability  $\epsilon_{\text{beg}}$  is given by  $\text{self.\_exp\_prob\_beg}$ , and the final probability  $\epsilon_{\text{end}}$  is given by  $\text{self.\_exp\_prob\_end}$ . The total number of samples  $n_{\text{max}}$  for annealing the exploration probability is specified by  $\text{self.\_exp\_anneal\_samples}$ , and the number of samples n collected so far is recorded in  $\text{self.\_sample\_count}$ . The output should be a scalar value corresponding to the probability of selecting a random action.

## 1.2 Action Sampling

In a3/dqn\_agent.py , implement the \_sample\_action(qs) method, which samples actions according to the Q-values of each action. The input consists of a tensor of qs , which contains the predicted Q-values of each action. Implement  $\epsilon$ -greedy exploration (Equation 4), where the probability of sampling a random action  $\epsilon$  is specified by self.\_get\_exp\_prob(). With probability  $1 - \epsilon$ , greedily select the action with the highest Q-value. With probability  $\epsilon$ , select a random action uniformly from the set of possible actions. The output a should be a tensor containing the index of the selected action.

## 1.3 Target Values

In a3/dqn\_agent.py, implement the \_compute\_tar\_vals(r, norm\_next\_obs, done) method, which calculates target values for updating the Q-function. The inputs consist of a tensor of rewards r, normalized observations at the next timestep norm\_next\_obs, and done flags done indicating if a timestep is the last timestep of an episode. The target value  $y_i$  is then calculated according to

$$y_i = r_i + \gamma (1 - \operatorname{done}_i) \max_{\mathbf{a}_i'} Q^{\operatorname{tar}}(\mathbf{s}_i', \mathbf{a}_i').$$
 (6)

If a sample corresponds to the last timestep of an episode (i.e.  $done_i = 1$ ), then the Q-value of the next timestep should be set to 0.

One of the innovations of DQN is the use of a target model  $Q^{\text{tar}}$  to calculate the target values [1], instead of directly calculating target values using the current Q-function. The target model is a delayed version of the Q-function, which is a copy of the parameters of the main Q-function from a number of iterations ago.  $Q^{\text{tar}}$  is kept fixed for a number of iteration,

before being updated with a copy of the parameters from the latest Q-function. By keeping  $Q^{\text{tar}}$  fixed for a number of iterations, the target model provides more stable target values for updating the main Q-function. The target model is given by self.\_tar\_model, and the main model is given by self. model. The Q-function can be queried by using the method eval\_q(norm\_obs). The output tar\_vals should be a tensor containing the target values for each sample.

#### 1.4 Loss Calculation

In a3/dqn\_agent.py, implement the \_compute\_q\_loss(norm\_obs, a, tar\_vals) method, which compute the loss for updating the Q-function. The input consists of a tensor of normalized observations norm.obs, a tensor containing the indices of discrete actions selected at each timestep a, and target values for each timestep tar\_vals. The output loss should be a scalar tensor containing the loss for updating the Q-function. The loss should be calculated as the mean squared-error between the target values and the outputs of the Q-function

$$l(Q) = \mathbb{E}_{\mathbf{s}_i, \mathbf{a}_i, y_i \sim \mathcal{D}} \left[ \left( y_i - Q(\mathbf{s}_i, \mathbf{a}_i) \right)^2 \right]. \tag{7}$$

Note, the loss should only be applied to the main model self. model, and should not be applied to the target model self.\_tar\_model.

#### Target Model Update 1.5

In a3/dqn\_agent.py, implement the \_sync\_tar\_model() method, which updates the target model by copying the parameters from the main model. The main model is given by self.\_model, and the target model is given by self.\_tar\_model. This method is used to periodically synchronize the parameters of the target model and the main model. self.\_model.parameters() can be used to retrieve a list of tensors containing the parameters of a model.

#### 1.6 **Tasks**

Train DQN policies to play two Atari games, Pong and Breakout. The two games can be specified using the environment config files data/envs/atari\_pong.yaml and data/envs/atari\_breakout.yaml. The corresponding agent config files are

a3/atari\_pong\_dqn\_agent.yaml and a3/atari\_breakout\_dqn\_agent.yaml. Train each model for at least 3 million timesteps. The default hyperparameters in the agent config files should already be fairly effective. However, depending on your implementation details, some additional tuning might be required. Tune the hyperparameters in the agent config files so that the policies reach a test return of at least 19 for Pong and 40 for Breakout. Plot a learning curve of the test return of each model using the plotting script

tools/plot\_log/plot\_log.py.

## 2 Bonus

1 bonus point will be award to the submission that achieves the best performance on the Breakout tasks using DQN. To improve the performance of DQN, you can do more extensive tuning of the hyperparameters, as well as make any changes to the algorithm in dqn\_agent.py. Submit any modifications made to the DQN algorithm in a separate file bonus\_dqn\_agent.py, hyperparameters bonus\_dqn\_agent.yaml, a checkpoint of the trained model bonus\_dqn\_breakout\_model.pt, a training log bonus\_dqn\_breakout\_log.txt, a learning curve bonus\_dqn\_breakout\_curve.png, and a text file bonus.txt detailing the modifications you made.

## **Submission**

Your submission should contain the following files:

- dqn\_agent.py : code changes.
- atari\_dqn\_agent.yaml: tuned hyperparameters.
- atari\_pong\_dqn\_model.pt: trained model for the Pong task.
- atari\_breakout\_dqn\_model.pt: trained model for the Breakout task.
- atari\_pong\_dqn\_log.txt: training log for the Pong task.
- atari\_breakout\_dqn\_log.txt: training log for the Breakout task.
- atari\_pong\_dqn\_curve.png: image of the learning curve for the Pong task.
- atari\_breakout\_dqn\_curve.png: image of the learning curve for the Breakout task.
- bonus\_dqn\_agent.py: modified version of the DQN agent for the bonus component.
- bonus\_dqn\_agent.yaml: hyperparameters for the bonus component.
- bonus\_dqn\_breakout\_model.pt: trained Breakout model for the bonus component.
- bonus\_dqn\_breakout\_log.txt: training log for the bonus component.
- bonus\_dqn\_breakout\_curve.png: image of the learning curve for the bonus component.
- bonus.txt: a text file detailing any modifications you made in bonus\_dqn\_agent.py for improving the performance of the algorithm.

All files should be stored in a directory named a3, and then zip the directory for submission. Do not add any additional subdirectories.

# References

[1] V. Mnih, K. Kavukcuoglu, D. Silver, A. A. Rusu, J. Veness, M. G. Bellemare, A. Graves, M. Riedmiller, A. K. Fidjeland, G. Ostrovski, S. Petersen, C. Beattie, A. Sadik, I. Antonoglou, H. King, D. Kumaran, D. Wierstra, S. Legg, and D. Hassabis. Human-level control through deep reinforcement learning. *Nature*, 518(7540):529–533, Feb. 2015.