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Compiler Design

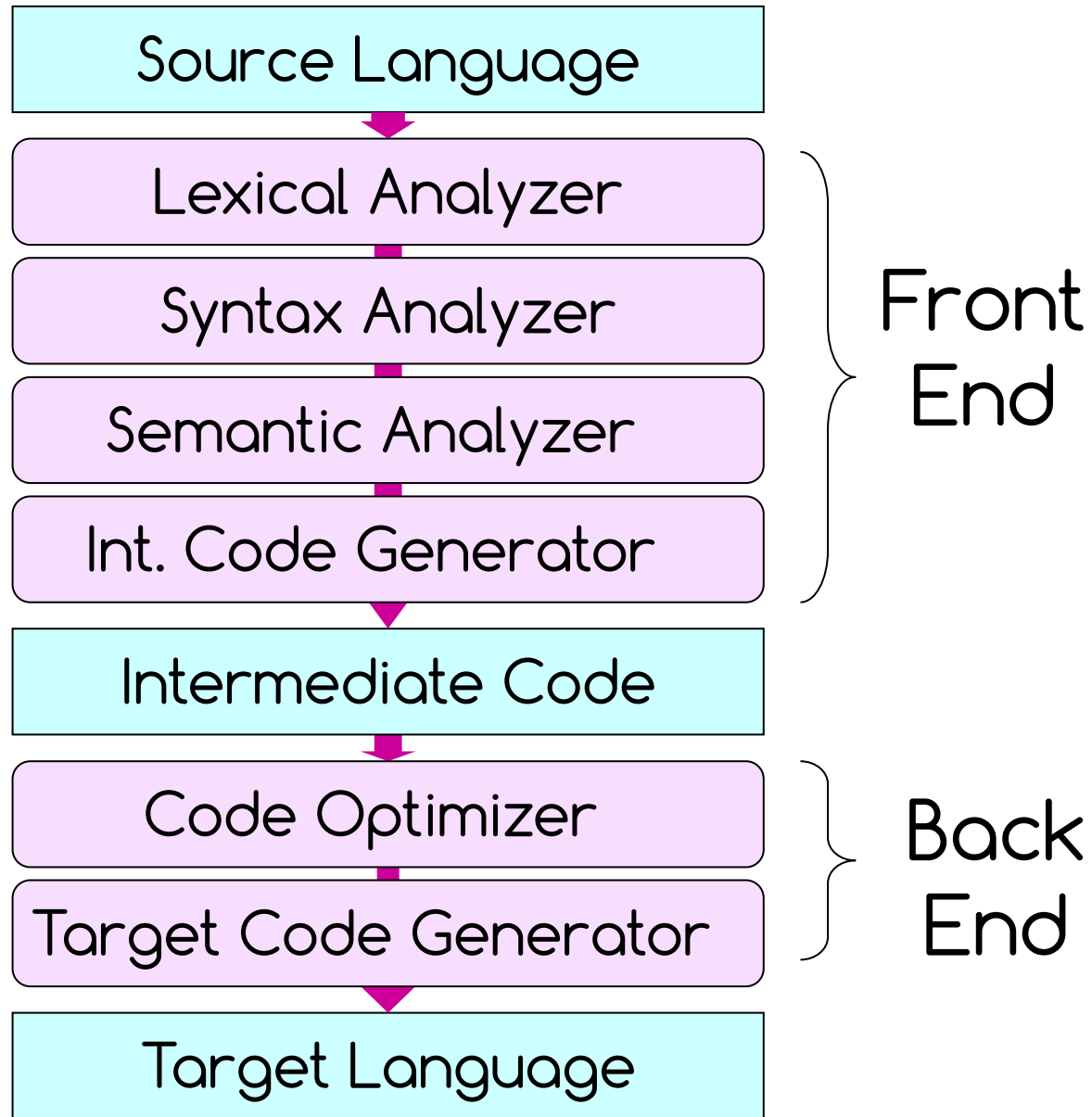
Lecture 10: Intermediate Code Generation

Sahar Selim

Agenda

- ▶ Intermediate Code Generation
- ▶ Intermediate Representations
 - 1) Postfix notation
 - 2) Three address code
 - 3) Syntax tree
 - ▶ Directed Acyclic Graph

Structure of a Compiler



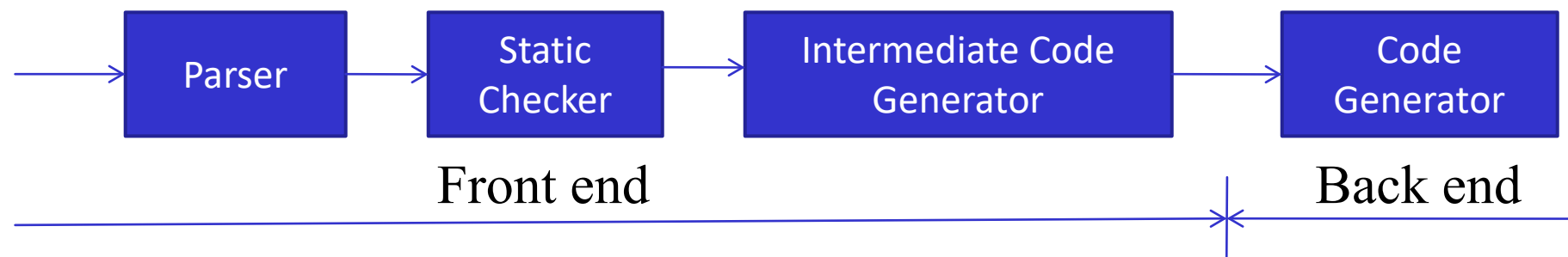
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Intermediate Code Generation

- ▶ Intermediate codes are **machine independent** codes, but they are **close to machine instructions**.
- ▶ The given program in a source language is converted to an equivalent program in an intermediate language by the intermediate code generator.
- ▶ It ties the front and back ends together

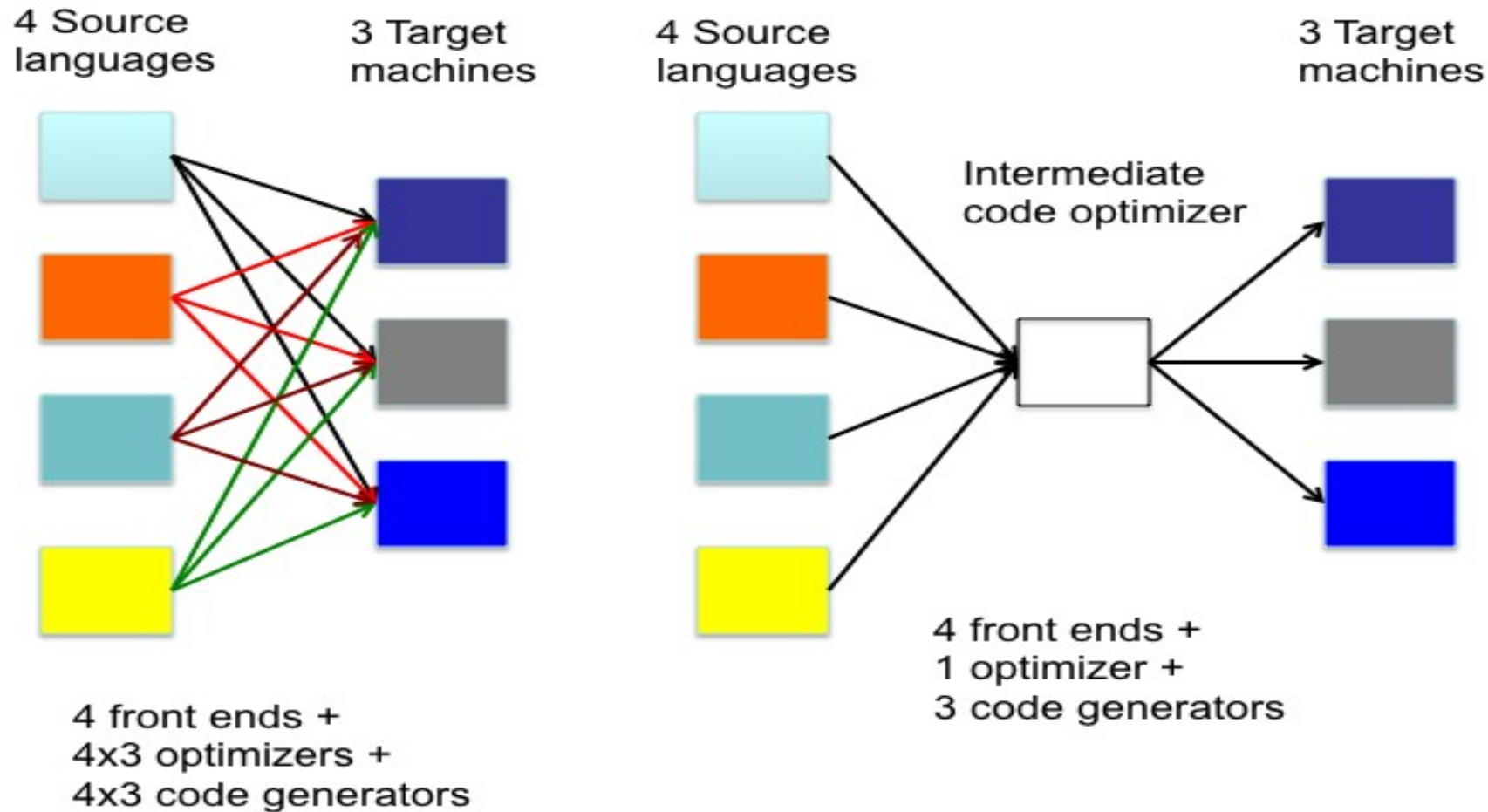
Intermediate Representation (IR)

A kind of **abstract machine language** that can express the target machine operations without committing to too much machine details.



► Why IR ?

Why Intermediate Code?



Why Intermediate Code?

- ▶ While generating machine code directly from source code is possible, it entails two problems
 - ▶ With m languages and n target machines, we need to write m front ends, $m \times n$ optimizers, and $m \times n$ code generators
 - ▶ The code optimizer which is one of the largest and very-difficult-to-write components of a compiler, cannot be reused
- ▶ By converting source code to an intermediate code, a machine-independent code optimizer may be written
- ▶ This means just m front ends, n code generators and 1 optimizer

Advantages of Using an Intermediate Language

1. Retargeting

- ▶ Build a compiler for a new machine by attaching a new code generator to an existing front-end.

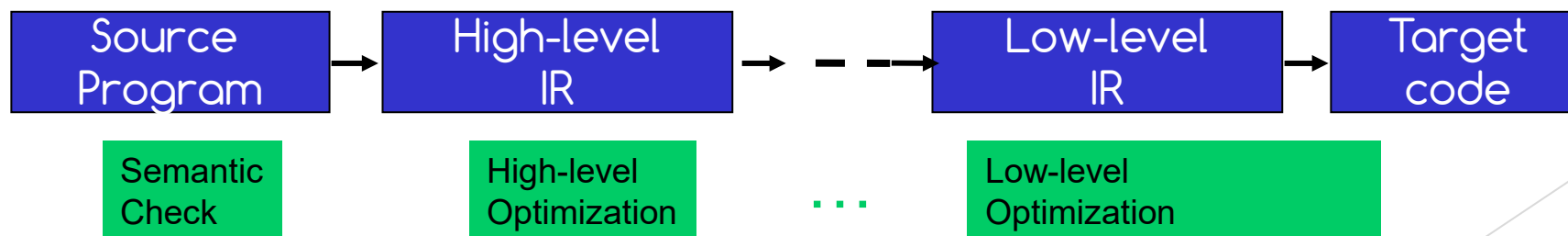
2. Optimization

- ▶ Reuse intermediate code optimizers in compilers for different languages and different machines.

- ▶ **Note:** the terms “intermediate code”, “intermediate language”, and “intermediate representation” are all used interchangeably.

Types of Intermediate Languages

- ▶ High Level Representations (e.g., syntax trees):
 - ▶ closer to the source language
 - ▶ easy to generate from an input program
 - ▶ code optimizations may not be straightforward.
- ▶ Low Level Representations (e.g., 3-address code, RTL):
 - ▶ closer to the target machine;
 - ▶ easier for optimizations, final code generation;



Intermediate Languages Types



- ▶ Graphical IRs:
 - ▶ Abstract Syntax trees
 - ▶ DAGs
 - ▶ Control Flow Graphs
- ▶ Linear IRs:
 - ▶ Stack based (postfix)
 - ▶ Three address code (quadruples)

Graphical IRs

- ▶ Abstract Syntax Trees (AST) – retain essential structure of the parse tree, eliminating unneeded nodes.
- ▶ Directed Acyclic Graphs (DAG) – compacted AST to avoid duplication – smaller footprint as well
- ▶ Control flow graphs (CFG) – explicitly model control flow

1 Postfix Notation

Postfix Notation

- In postfix notation, the operator follows the operand.
- For example, in the expression $(a-b)^* (c +d)$ the postfix representation is:
- $ab - cd +^*$

Example 2

String: $a+b*c+d*e^f$



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Example 2

String: $a+b*c+d*e^f$

postfix: $abc^*+def^{*}+$



Example 3

- Find the postfix notation of the following expressions:

Infix Notation	Postfix Notation
$a = b * - c + b * - c$	<code>a b c uminus * b c uminus * + assign</code>
$(a + b) * c$	<code>ab + c*</code>
$(a - b) * (c + d) + (a - b)$	<code>ab - cd + * ab - +</code>
$a + b * c / (d - e)$	<code>a b c * d e - / +</code>

2 Three-Address Code

Three Address Code.

- ▶ Three address code is a sequence of statement of the form $x = y \text{ op } z$.
- ▶ Since a statement involves no more than three references, it is called a “three address statement”, and a sequence of such statements is referred to as three address code.

Example

The three-address code for the expression

$$2 * a + (b - 3)$$

$$T1 = 2 * a$$

$$T2 = b - 3$$

$$T3 = T1 + T2$$

Three Address Code

- Sometimes a statement might contain less than three references; but it is still called a three-address statement.
- The following are the three address statements used to represent various programming language constructs:
- Used for representing arithmetic expressions:

$$X = Y \text{ op } Z$$
$$X = \text{op } Y$$
$$X = Y$$

Three Address Code

- Used for representing Boolean expressions:

If $A > B$ goto Z
goto Z

Data structures for three address codes

► Quadruples

- Has four fields: op, arg1, arg2 and result

► Triples

- Temporaries are not used and instead references to instructions are made

► Indirect triples

- In addition to triples we use a list of pointers to triples

Representations
for
Three Address Code

Quadruples

Triples

Indirect Triples

Quadruple Representation

► Using quadruple representation, the three-address statement $x = y \text{ op } z$ is represented by placing

- op in the operator field
- y in the operand1 field
- z in the operand2 field
- x in the result field

	Operator	Operand 1	Operand 2	Result
(1)	op	y	z	X
(2)	op	y		x
(3)				
(4)				
(5)				

Quadruple Representation

- ▶ The statement $x = op\ y$, where op is a unary operator, is represented by placing
 - ▶ op in the operator field
 - ▶ y in the operand1 field
 - ▶ x in the result field
 - ▶ the operand2 field is not used

Example 1

Define the quadruple representation of the three-address code for the statement

$$x = (a + b) * -c / d$$



Example1

$$x = ((a + b) * -c) / d$$

	Operator	Operand 1	Operand 2	Result
(1)	+	a	b	t1
(2)	-	c		t2
(3)	*	t1	t2	t3
(4)	/	t3	d	t4
(5)	=	t4		x

Example 2

- ▶ Consider expression $a = b * -c + b * -c$.
- ▶ Define the three-address code with quadruples

Example 2

- ▶ Consider expression $a = b * -c + b * -c$.
- ▶ Define the three-address code with quadruples

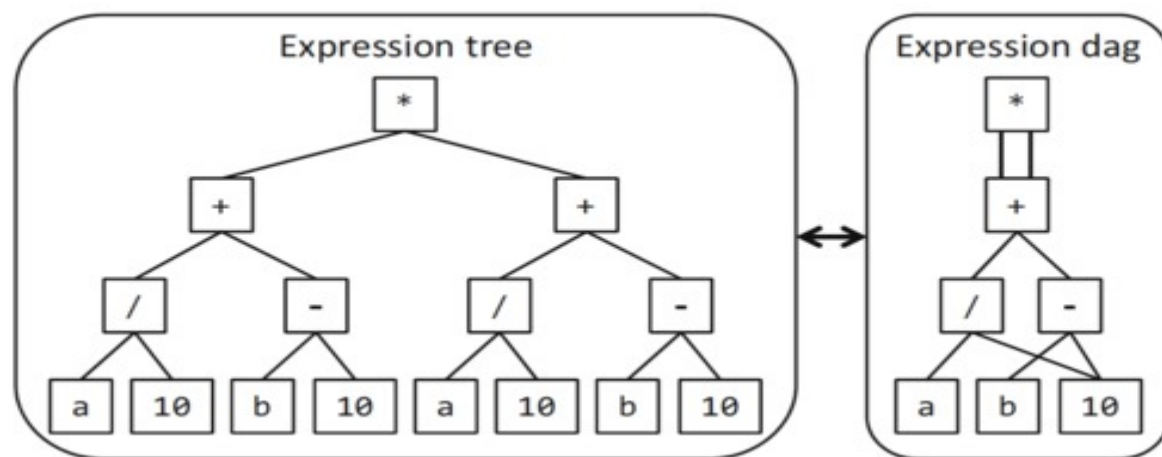
t1 = uminus c
t2 = b * t1
t3 = uminus c
t4 = b * t3
t5 = t2 + t4
a = t5

#	Op	Arg1	Arg2	Result
(0)	uminus	c		t1
(1)	*	t1	b	t2
(2)	uminus	c		t3
(3)	*	t3	b	t4
(4)	+	t2	t4	t5
(5)	=	t5		a

Quadruple representation

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3 Syntax Trees

Directed Acyclic Graphs (DAG)

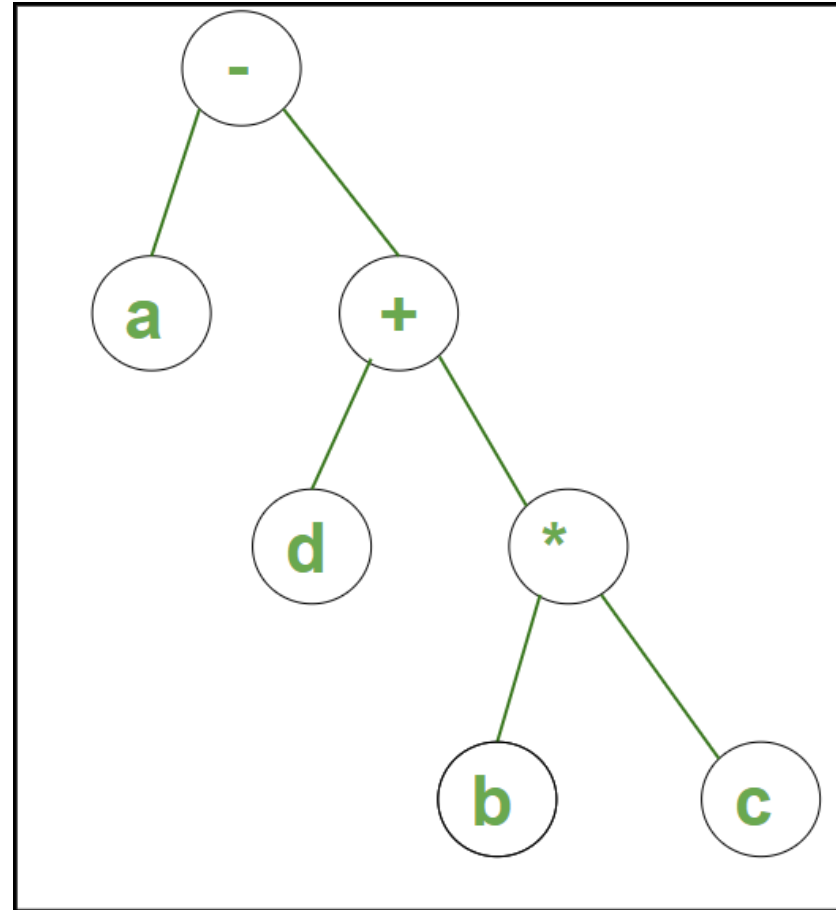
Syntax Tree



- ▶ A syntax tree is also known as **parse tree**.
- ▶ It represents the different categories of syntax used in the sentence.
- ▶ It enables one to understand the different **syntactical structure** of a sentence.

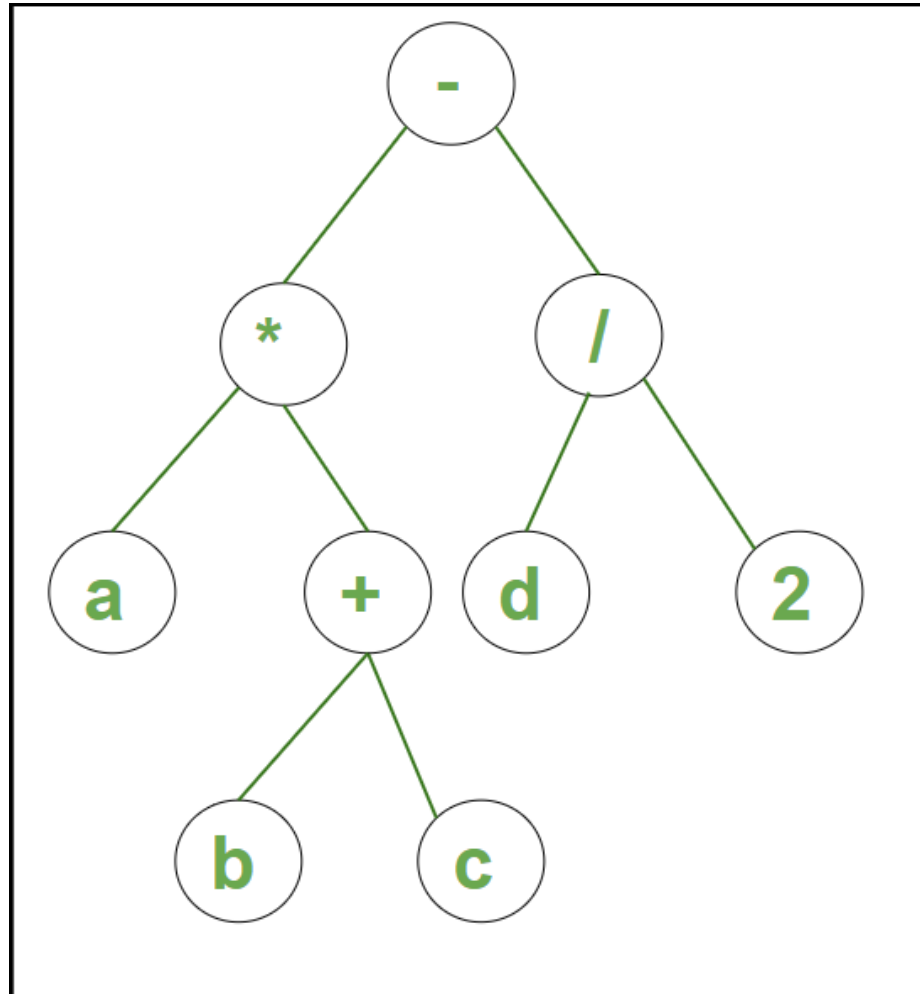
Syntax Tree: Example 1

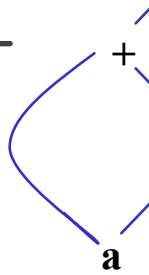
► $a - b * c + d$

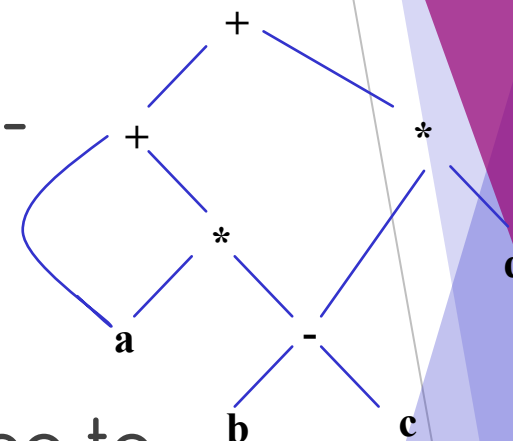


Syntax Tree: Example 2

► $a * (b + c) - d / 2$



- ▶ It is sometimes beneficial to create a DAG instead of tree for Expressions.
 - ▶ This way can easily show the common sub-expressions and then use that knowledge during code generation
 - ▶ DAG has leaves corresponding to atomic operands and interior codes corresponding to operators.
 - ▶ a **node N** in a **DAG** has more than one parent if N represents a common subexpression.
- 



SDD for creating DAG's

$a + a * (b - c) + (b - c) * d$



Production

- 1) $E \rightarrow E1 + T$
- 2) $E \rightarrow E1 - T$
- 3) $E \rightarrow T$
- 4) $T \rightarrow (E)$
- 5) $T \rightarrow id$
- 6) $T \rightarrow num$

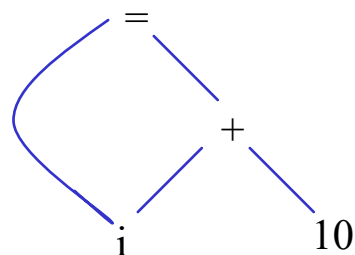
Semantic Rules

- $E.node = \text{new Node}('+', E1.node, T.node)$
 $E.node = \text{new Node}('-', E1.node, T.node)$
 $E.node = T.node$
 $T.node = E.node$
 $T.node = \text{new Leaf}(id, id.entry)$
 $T.node = \text{new Leaf}(num, num.val)$

Example:

- 1) $p1 = \text{Leaf}(id, \text{entry-}a)$
- 2) $p2 = \text{Leaf}(id, \text{entry-}a) = p1$
- 3) $p3 = \text{Leaf}(id, \text{entry-}b)$
- 4) $p4 = \text{Leaf}(id, \text{entry-}c)$
- 5) $p5 = \text{Node}('-', p3, p4)$
- 6) $p6 = \text{Node}('*', p1, p5)$
- 7) $p7 = \text{Node}('+', p1, p6)$
- 8) $p8 = \text{Leaf}(id, \text{entry-}b) = p3$
- 9) $p9 = \text{Leaf}(id, \text{entry-}c) = p4$
- 10) $p10 = \text{Node}('-', p3, p4) = p5$
- 11) $p11 = \text{Leaf}(id, \text{entry-}d)$
- 12) $p12 = \text{Node}('*', p5, p11)$
- 13) $p13 = \text{Node}('+', p7, p12)$

Value-number method for Constructing DAG's



id			→ To entry for i
num	10		
+	1	2	
3	1	3	

► Algorithm

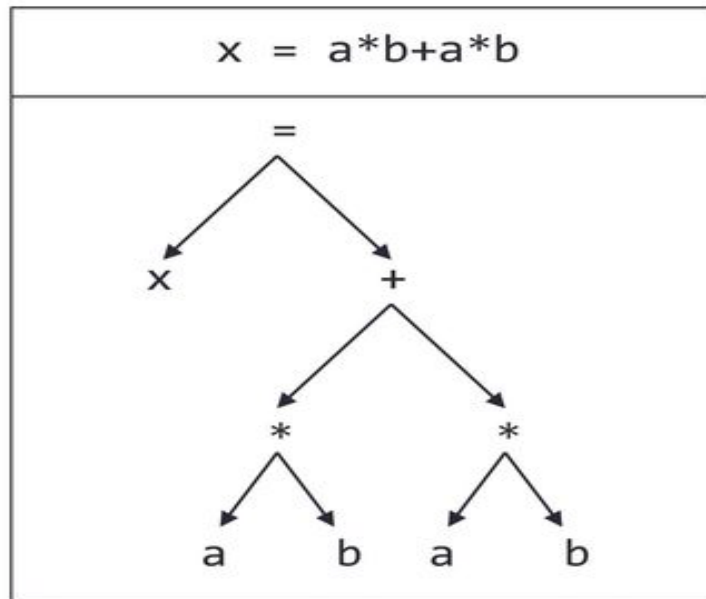
- Search the array for a node M with label op, left child l and right child r
- If there is such a node, return the value number M
- If not create in the array a new node N with label op, left child l, and right child r and return its value

Abstract Syntax Tree vs DAG:

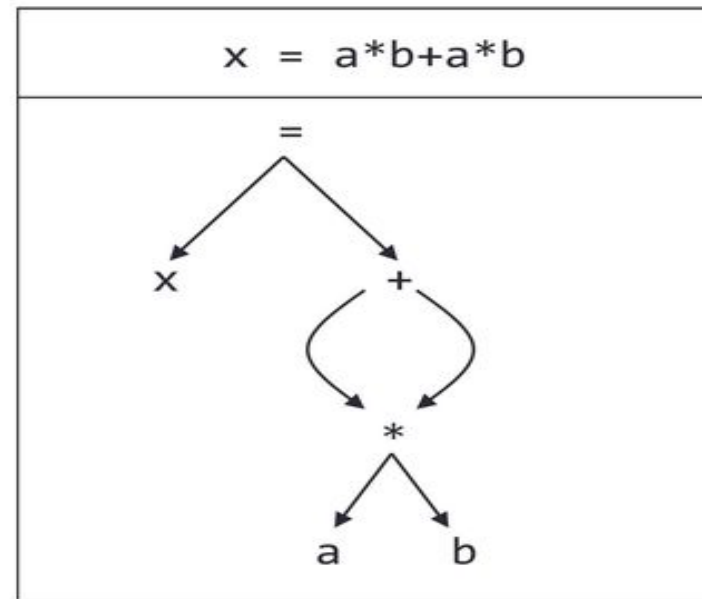
Example 1

$$x = a * b + a * b$$

Abstract Syntax Tree

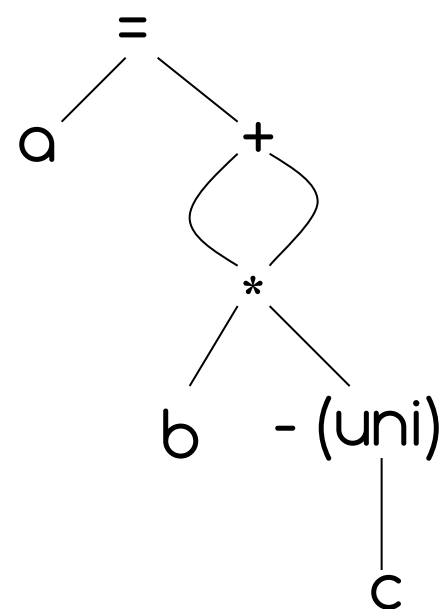
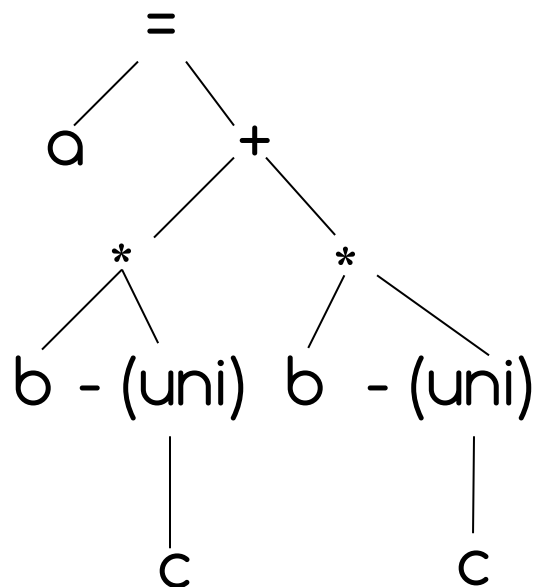


Directed Acyclic Graph



ASTs and DAGs: Example 2

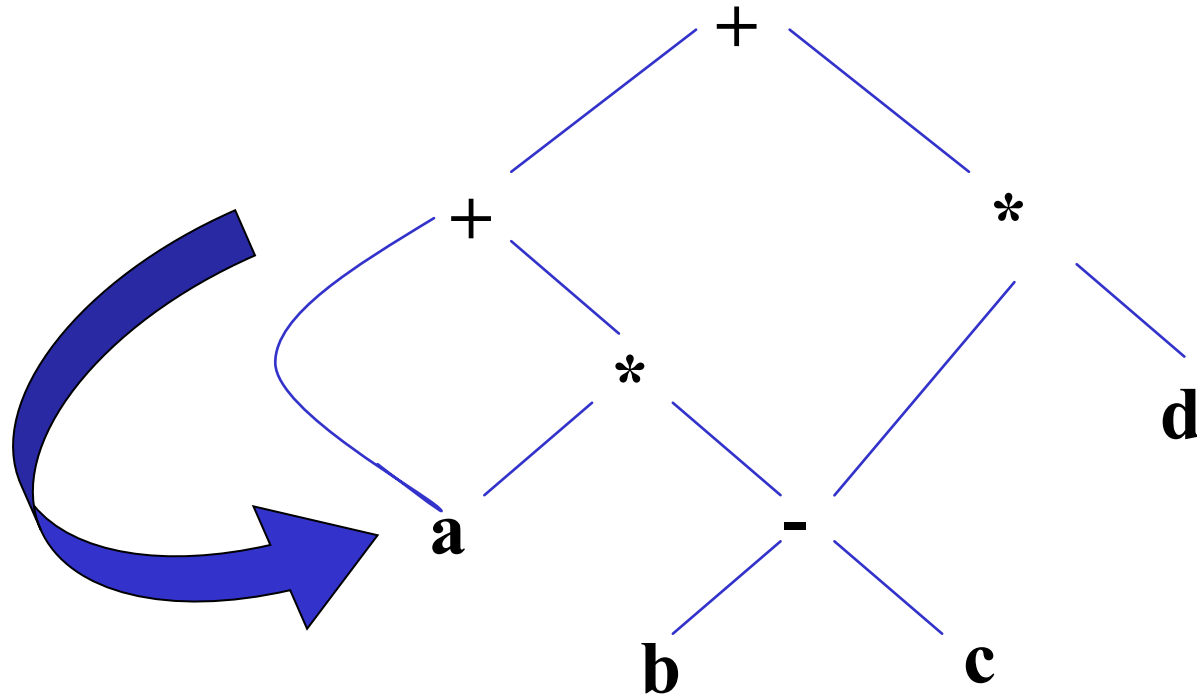
$$a = b * -c + b * -c$$



Directed Acyclic Graphs: Example



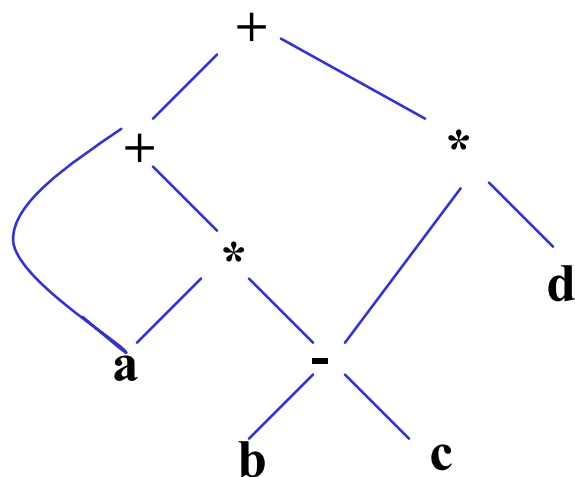
$$a + a * (b - c) + (b - c) * d$$



DAGs & Three address code

- ▶ In a three address code there is at most one operator at the right side of an instruction
- ▶ Example: $a + a * (b - c) + (b - c) * d$

DAG



Three address code

```

t1 = b - c
t2 = a * t1
t3 = a + t2
t4 = t1 * d
t5 = t3 + t4

```


Summary

- ▶ Intermediate representations span the gap between the source and target languages:
 - ▶ closer to target language;
 - ▶ (more or less) machine independent;
 - ▶ allows many optimizations to be done in a machine-independent way.

Summary: Syntax Tree vs DAG

- ▶ A syntax tree is also known as parse tree.
 - ▶ It represents different categories of syntax used in the sentence.
 - ▶ It enables one to understand the different syntactical structure of a sentence.
- ▶ DAG is the Directed Acyclic Graph used in representing the basic block structure.
 - ▶ It is used in modeling probabilities, connectivity, and causality.
 - ▶ It uses unique node for each value.

Summary



- ▶ Intermediate code must be easy to produce and easy to translate to machine code
 - ▶ A sort of universal assembly language
 - ▶ Should not contain any machine-specific parameters (registers, addresses, etc.)
- ▶ The type of intermediate code deployed is based on the application
- ▶ Quadruples, triples, indirect triples, abstract syntax trees are the classical forms used for machine-independent optimizations and machine code generation



Review Questions

Problem 1: $a+b*c-d/(b*c)$

Translate this expression into the following representations:

- ▶ Abstract Syntax Tree
- ▶ Three-address code
- ▶ Postfix notation
- ▶ DAG



Problem 1: $a+b*c-d/(b*c)$

Translate this expression into the following representations:

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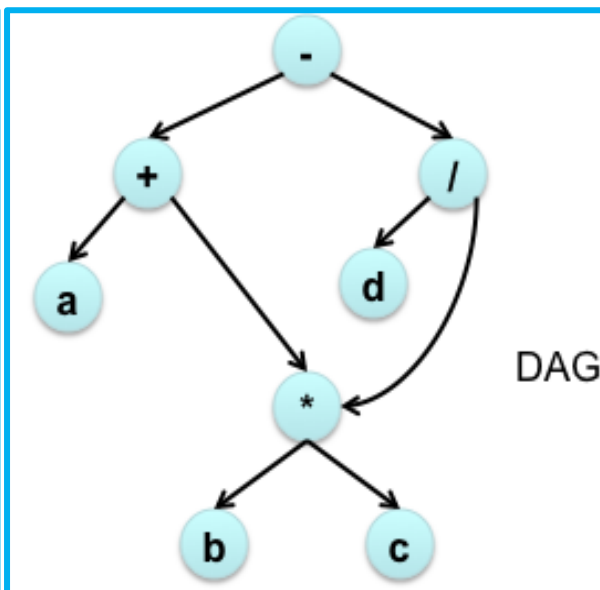
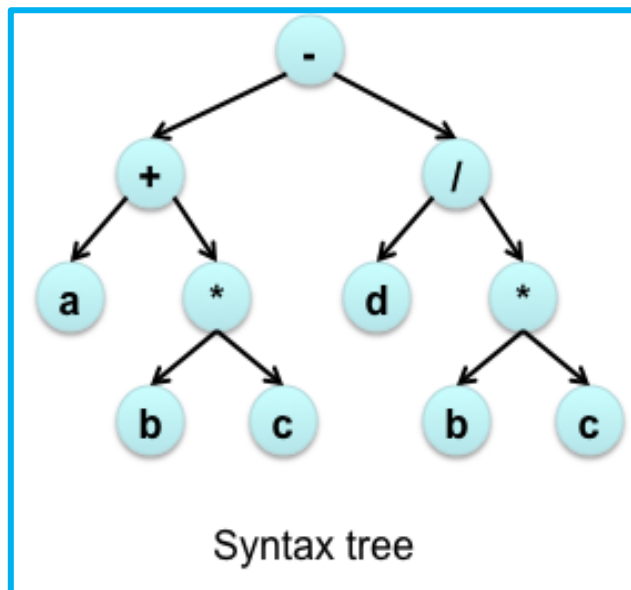
Postfix notation: $abc*+dbc*/-$

Three Address code

Quadruples

op	arg ₁	arg ₂	result
*	b	c	t1
+	a	t1	t2
*	b	c	t3
/	d	t3	t4
-	t2	t4	t5

$t1 = b * c$
 $t2 = a + t1$
 $t3 = b * c$
 $t4 = d / t3$
 $t5 = t2 - t4$



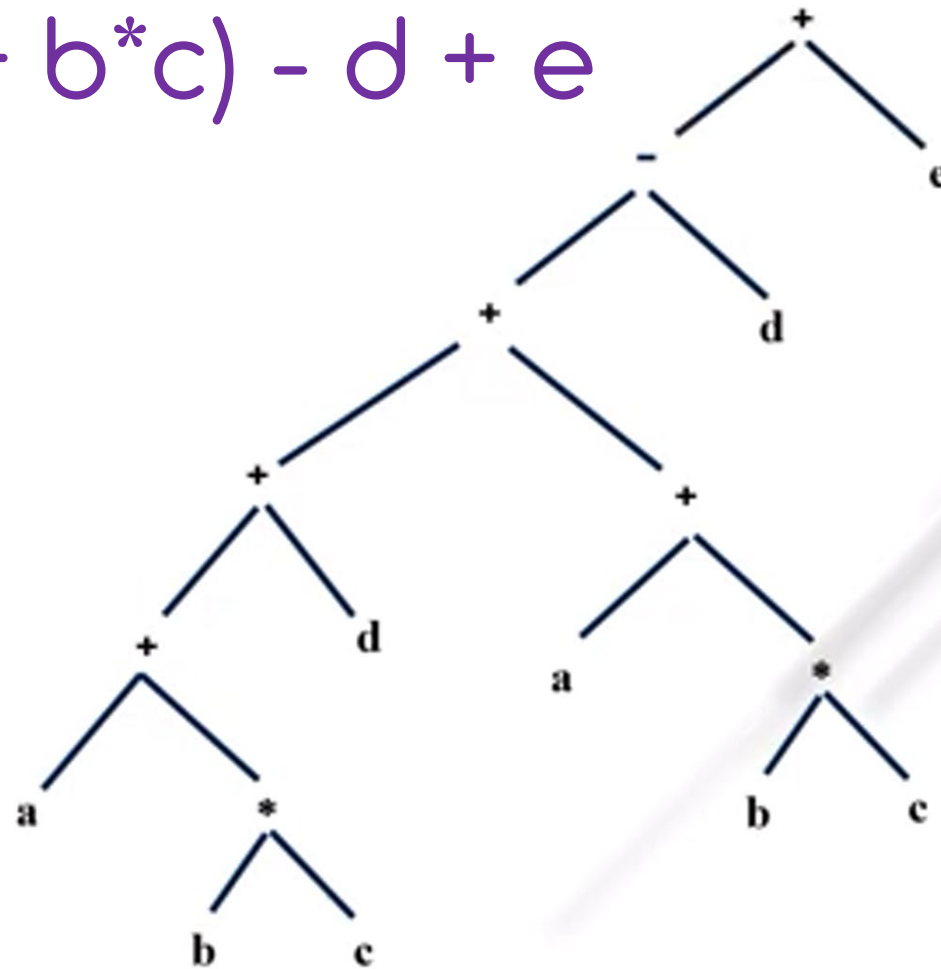
Problem 2:

$$(a + b * c) + d + (a + b * c) - d + e$$

- ▶ Translate this expression into the following representations:
 - ▶ Abstract Syntax Tree
 - ▶ Three-address code
 - ▶ Postfix notation
 - ▶ DAG

Problem 2: Syntax Tree

$(a + b * c) + d + (a + b * c) - d + e$



Problem 2: Postfix Notation

$$(a + b * c) + d + (a + b * c) - d + e$$

$(a + b * c) + d + (a + b * c) - d + e$	where,
$(a + T1) + d + (a + b * c) - d + e$	$T1 = bc*$
$T2 + d + (a + b * c) - d + e$	$T2 = aT1 +$
$T3 + (a + b * c) - d + e$	$T3 = T2d +$
$T3 + (a + T4) - d + e$	$T4 = bc*$
$T3 + T5 - d + e$	$T5 = aT4 +$
$T6 - d + e$	$T6 = T3T5 +$
$T7 + e$	$T7 = T6d -$
$T8$	$T8 = T7e +$

$T8$
$T7 e +$
$T6 d - e +$
$T3 T5 + d - e +$
$T3 aT4 ++ d - e +$
$T3 abc * ++ d - e +$
$T2 d + abc * ++ d - e +$
$aT1 + d + abc * ++ d - e +$
$abc * + d + abc * ++ d - e +$

backward Substitution the value
of temporary variables

Postfix notation

Problem 2: Three-Address Code

$$(a + b * c) + d + (a + b * c) - d + e$$

$$t_1 = b * c$$

$$t_2 = a + t_1$$

$$t_3 = t_2 + d$$

$$t_4 = b * c$$

$$t_5 = a + t_4$$

$$t_6 = t_3 + t_5$$

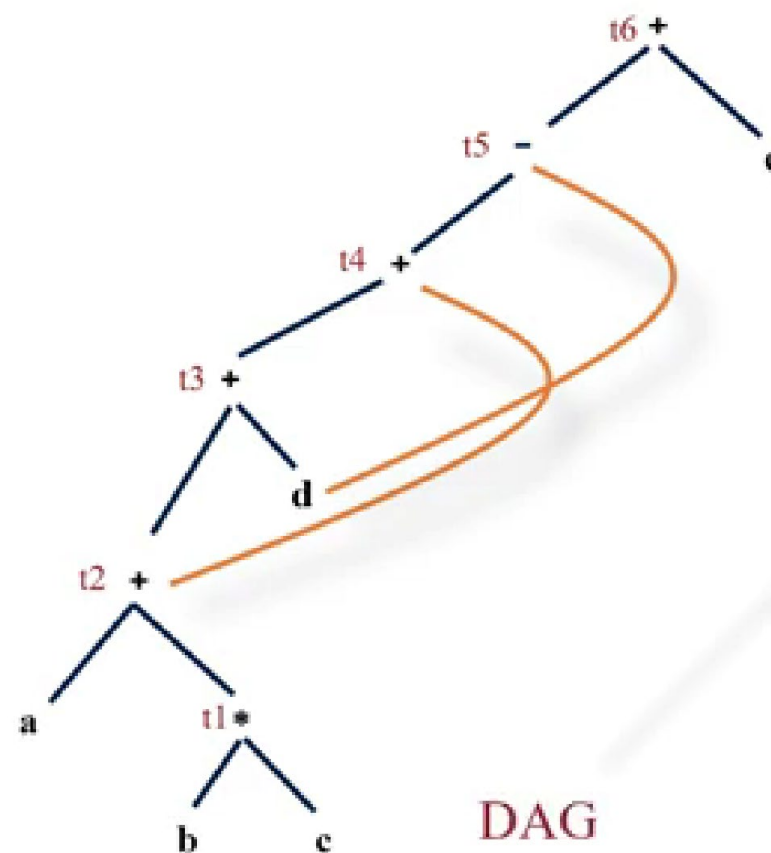
$$t_7 = t_6 - d$$

$$t_8 = t_7 + e$$

Three - address Code

Problem 2: DAG

$$(a + b * c) + d + (a + b * c) - d + e$$



Problem 3:

$$a + a * (b - c) + (b - c) * d$$

Translate this expression into:

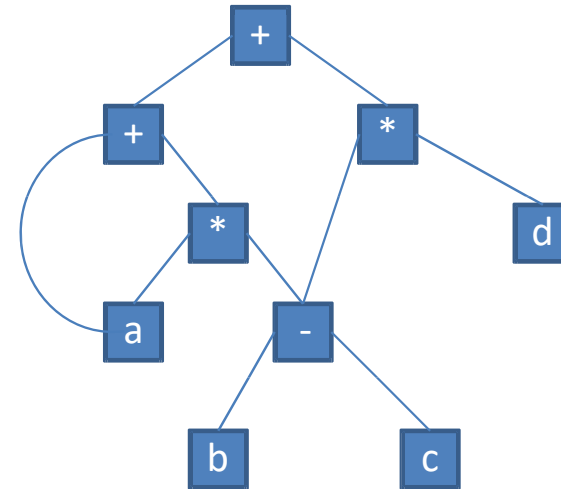
- ▶ DAG
- ▶ Three Address Code - Quadraples

Problem 3: DAG & 3-address code



► $a + a * (b - c) + (b - c) * d$

$t1 = b - c$
 $t2 = a * t1$
 $t3 = a + t2$
 $t4 = t1 * d$
 $t5 = t3 + t4$



Problem 3: Quadruples

► $a + a * (b - c) + (b - c) * d$

$t1 = b - c$
 $t2 = a * t1$
 $t3 = a + t2$
 $t4 = t1 * d$
 $t5 = t3 + t4$

	Operator	Operand 1	Operand 2	Result
(1)	-	b	c	t1
(2)	*	a	t1	t2
(3)	+	a	t2	t3
(4)	*	t1	d	t4
(5)	+	t3	t4	t5

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Compiler

Compilation Example

The Phases of a Compiler

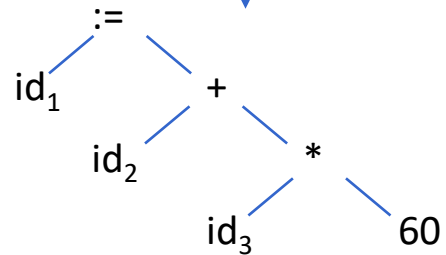
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Position := initial + rate * 60

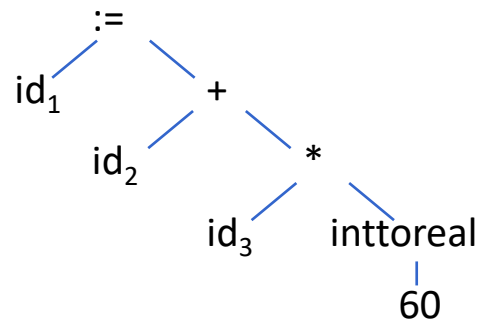
lexical analyzer

$id_1 := id_2 + id_3 * 60$

syntax analyzer



semantic analyzer



intermediate code generator

```
temp1 := inttoreal (60)
temp2 := id3 * temp1
temp3 := id2 + temp2
id1 := temp3
```

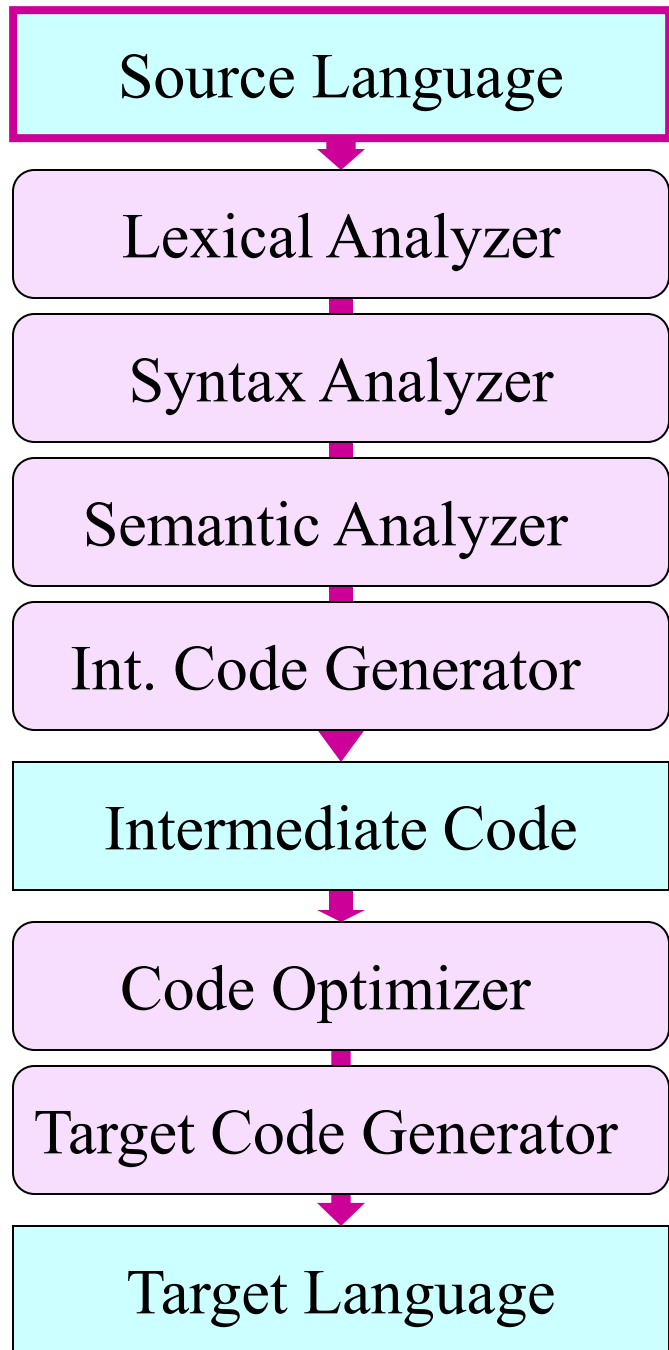
code optimizer

```
temp1 := id3 * 60.0
id1 := id2 + temp1
```

code generator

```
MOVF id3, R2
MULF #60.0, R2
MOVF id2, R1
ADDF R2, R1
MOVF R1, id1
```

Compilation Example

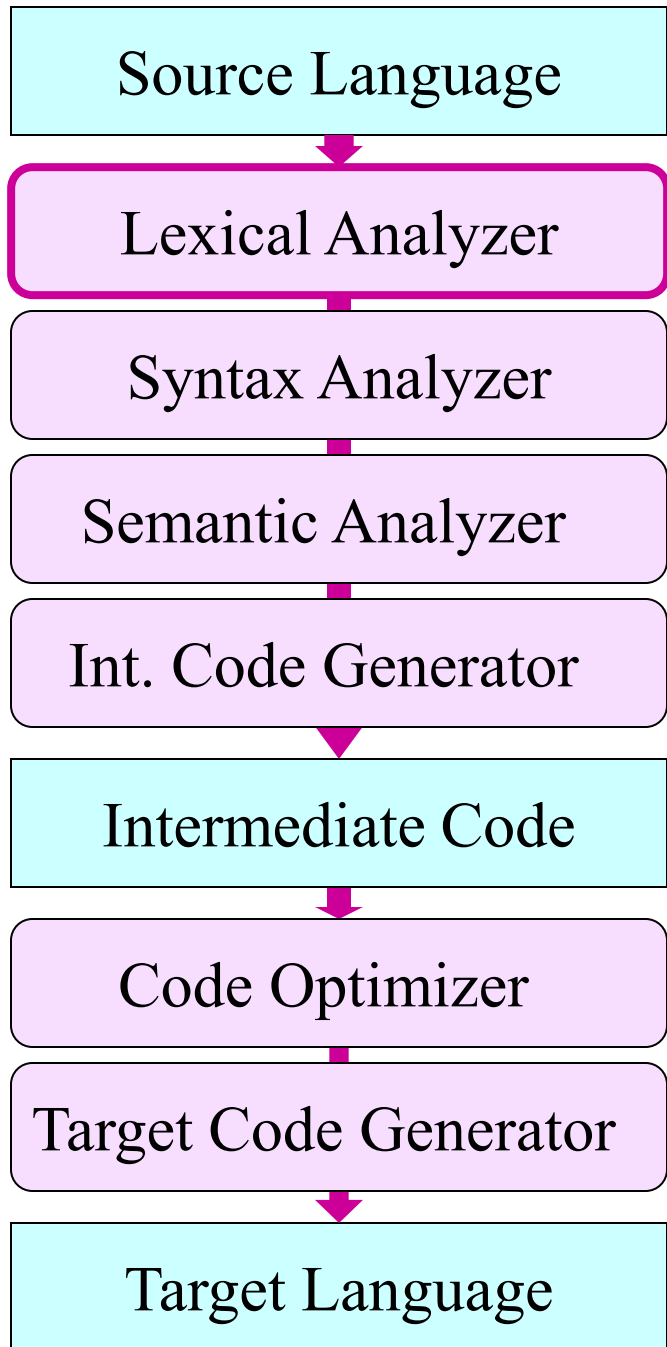


Source Code:

`Position = Initial + Rate * 60`

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Compilation Example



Source Code:

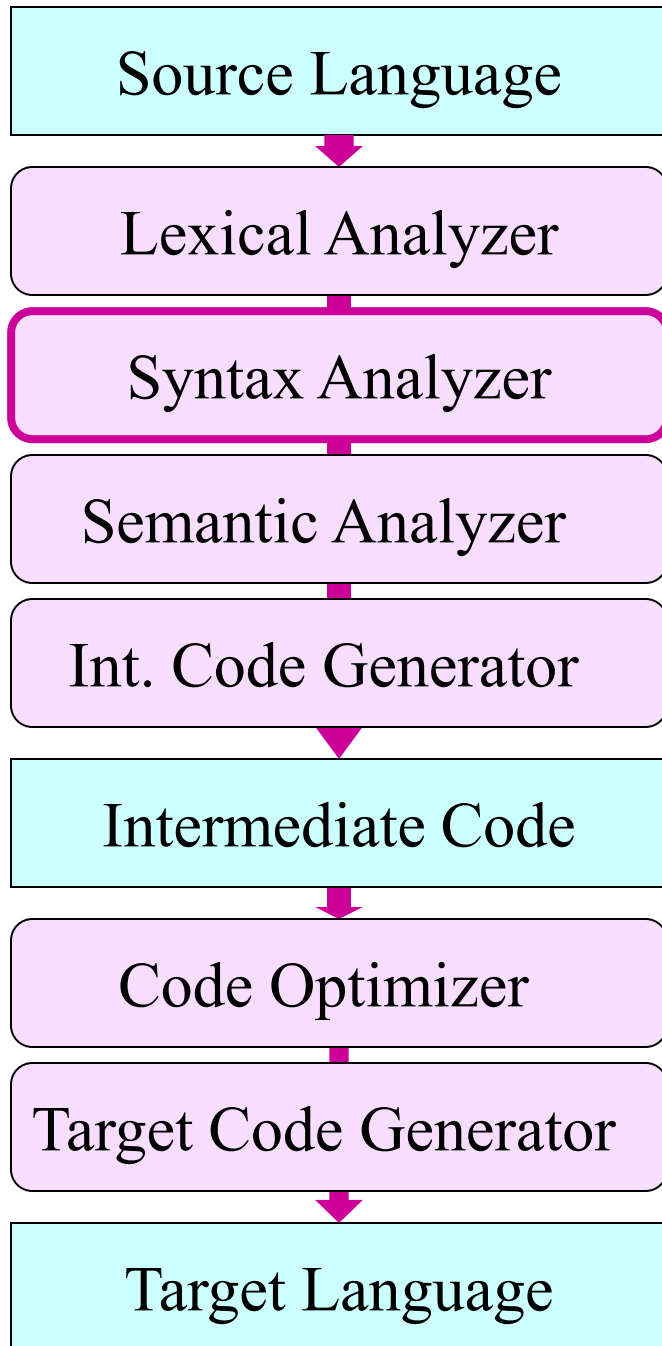
`Position = Initial + Rate * 60`

Lexical Analysis:

`ID(1) ASSIGN ID(2) ADD ID(3) MULT INT(60)`

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Compilation Example



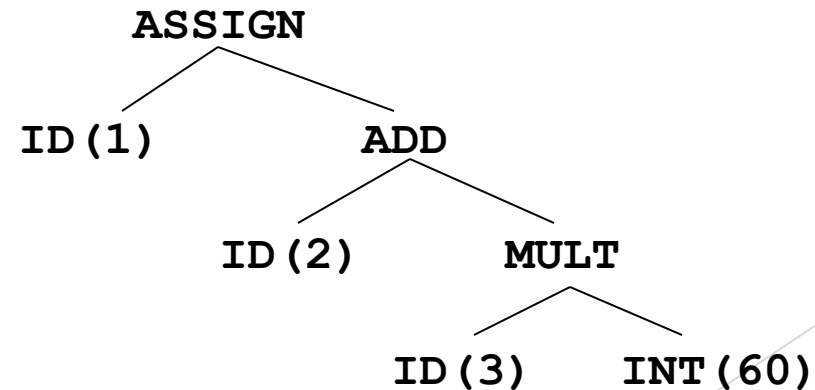
Source Code:

`Position = Initial + Rate * 60`

Lexical Analysis:

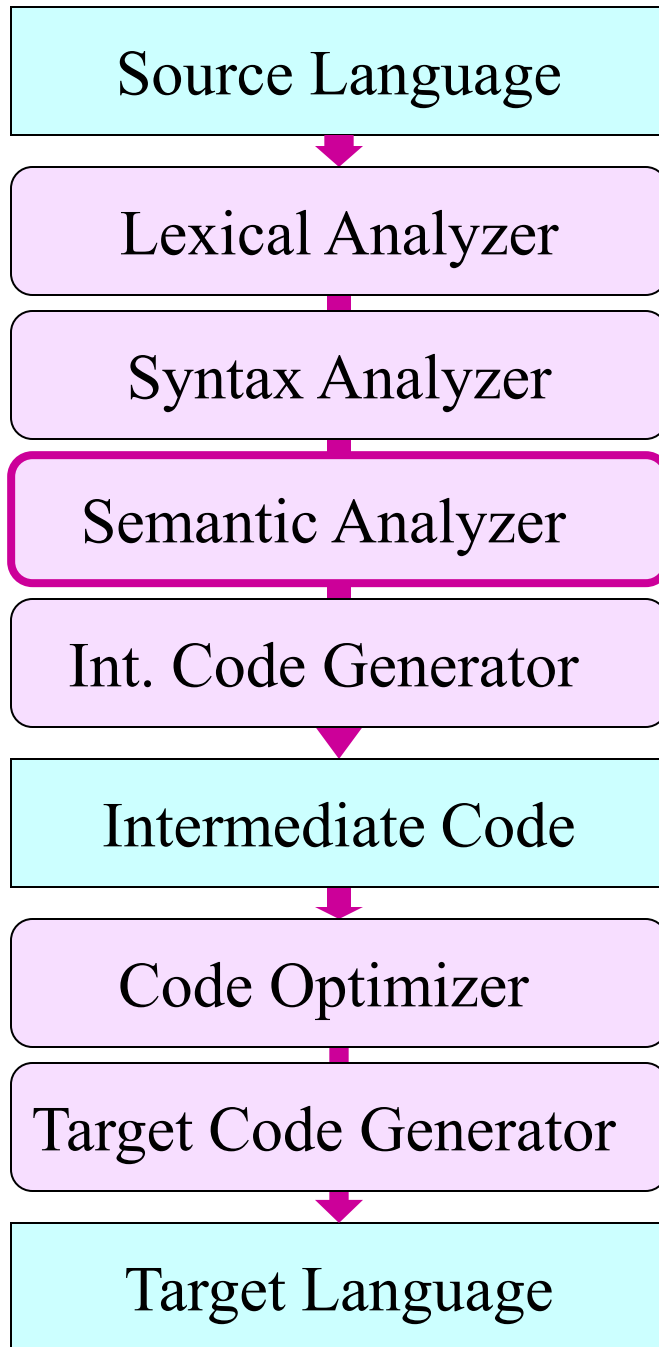
`ID (1) ASSIGN ID (2) ADD ID (3) MULT INT (60)`

Syntax Analysis:

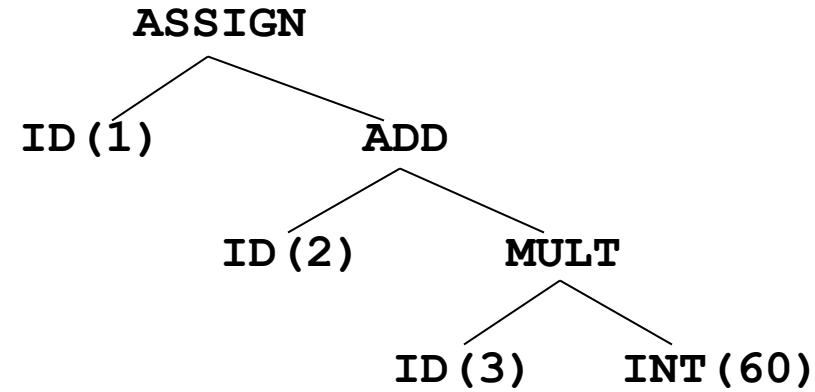


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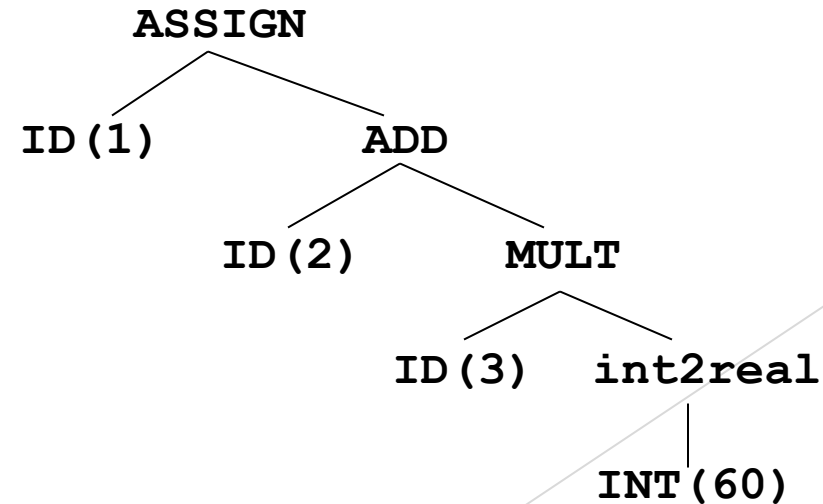
Compilation Example



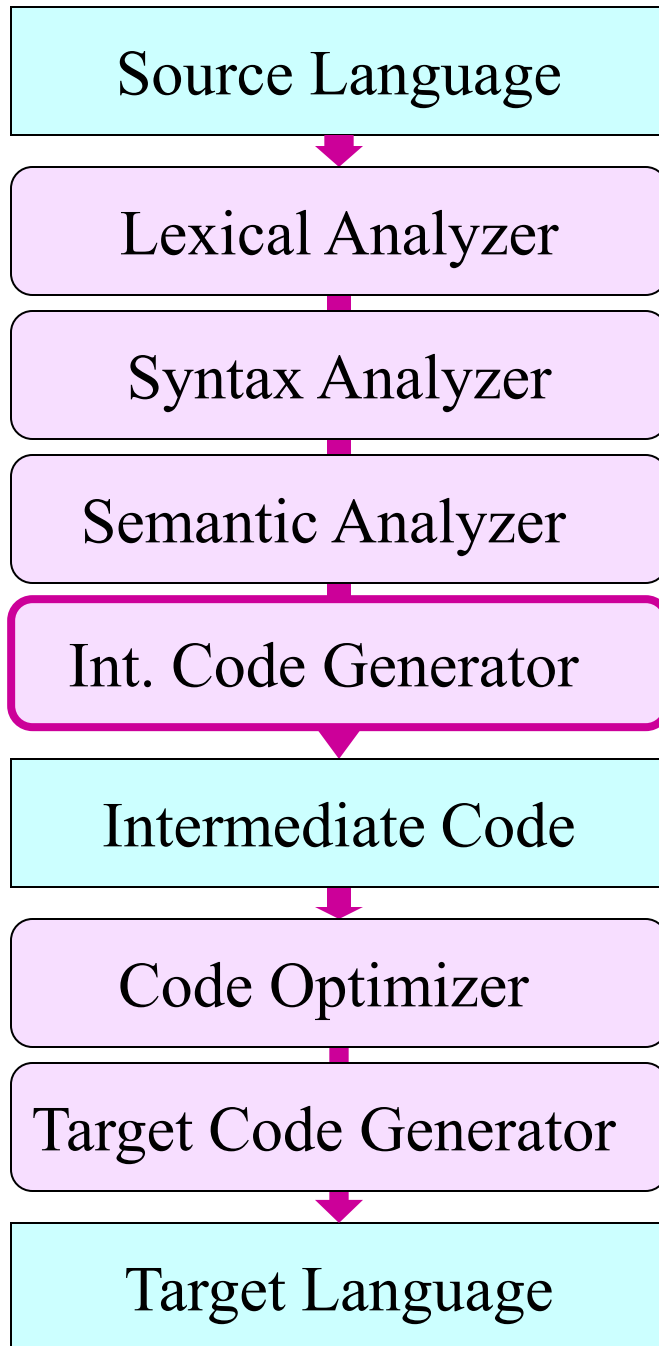
Syntax Analysis:



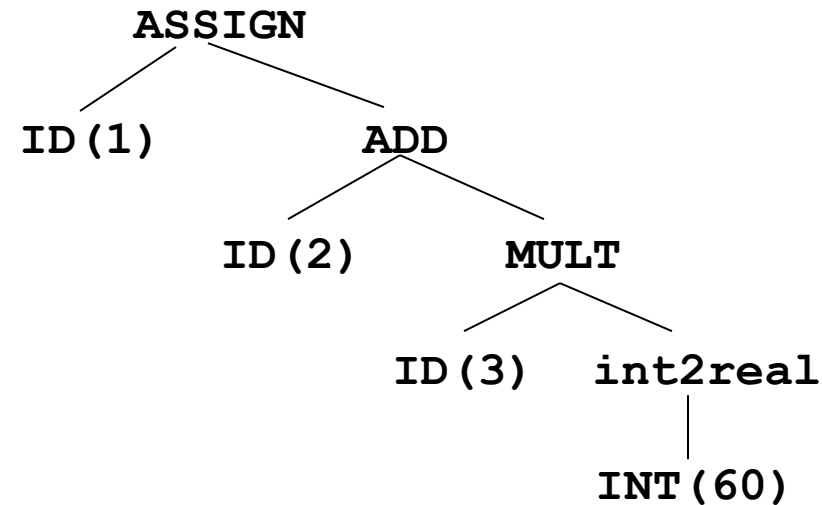
Semantic Analysis:



Compilation Example



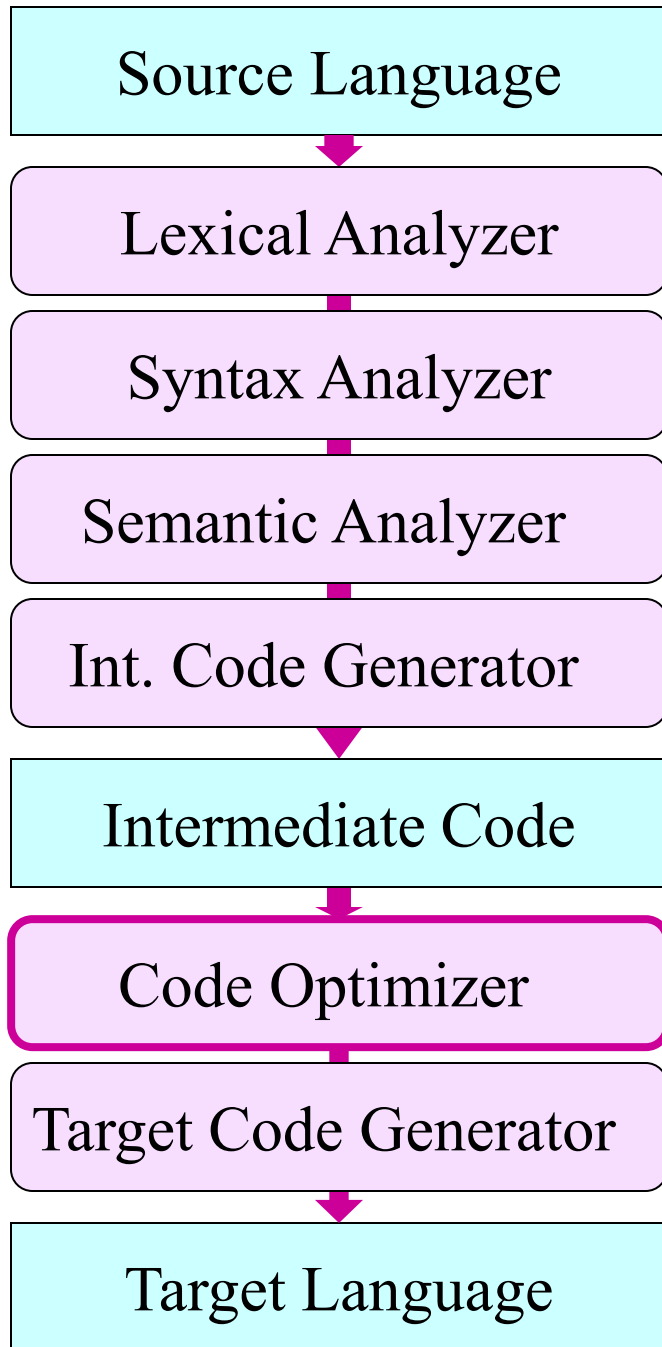
Sematic Analysis:



Intermediate Code:

```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

Compilation Example



Intermediate Code:

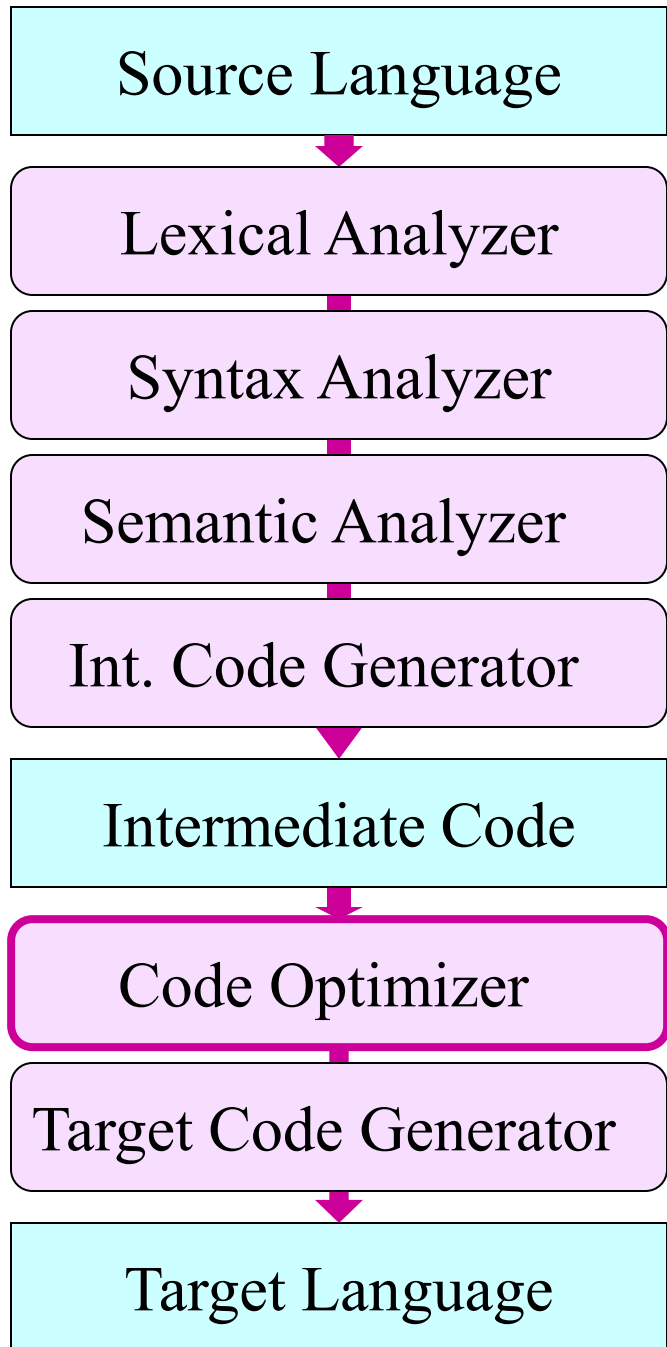
```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

Optimized Code (step 0):

```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

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Compilation Example



Intermediate Code:

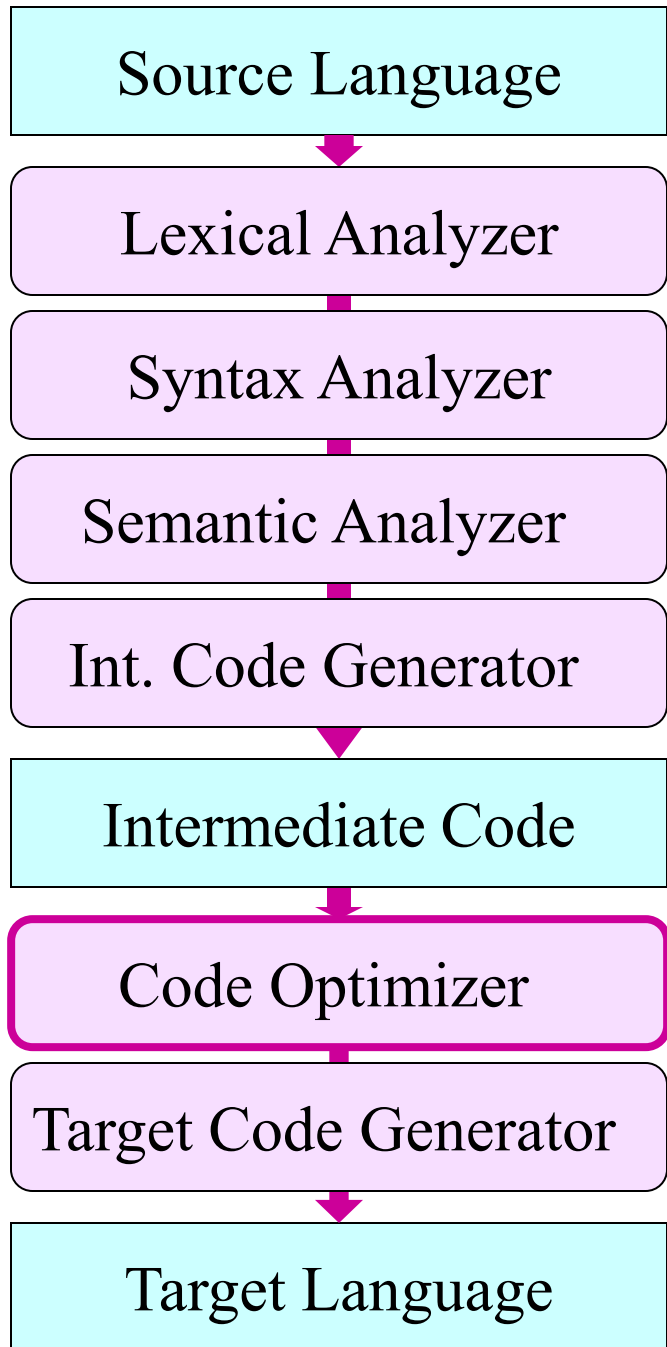
```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

Optimized Code (step 1):

```
temp1 = 60.0
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

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Compilation Example



Intermediate Code:

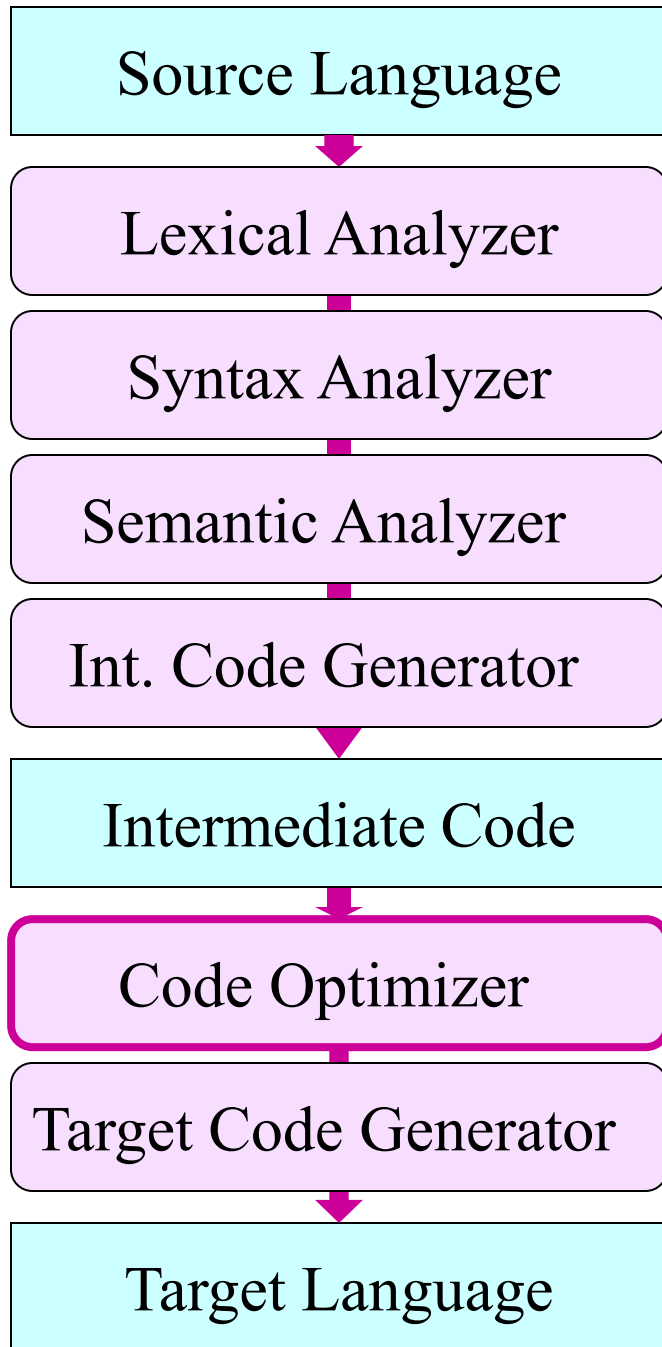
```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

Optimized Code (step 2):

```
temp2 = id3 * 60.0
temp3 = id2 + temp2
id1 = temp3
```

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Compilation Example



Intermediate Code:

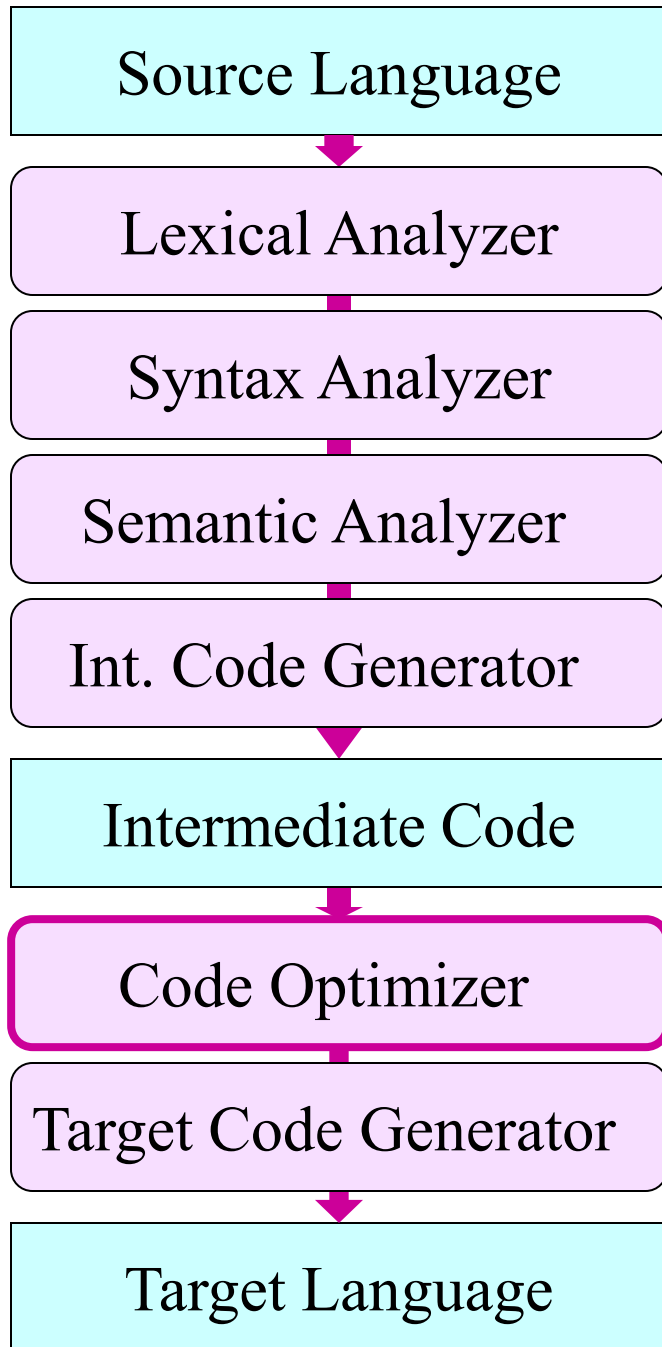
```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

Optimized Code (step 3):

```
temp2 = id3 * 60.0
id1 = id2 + temp2
```

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Compilation Example



Intermediate Code:

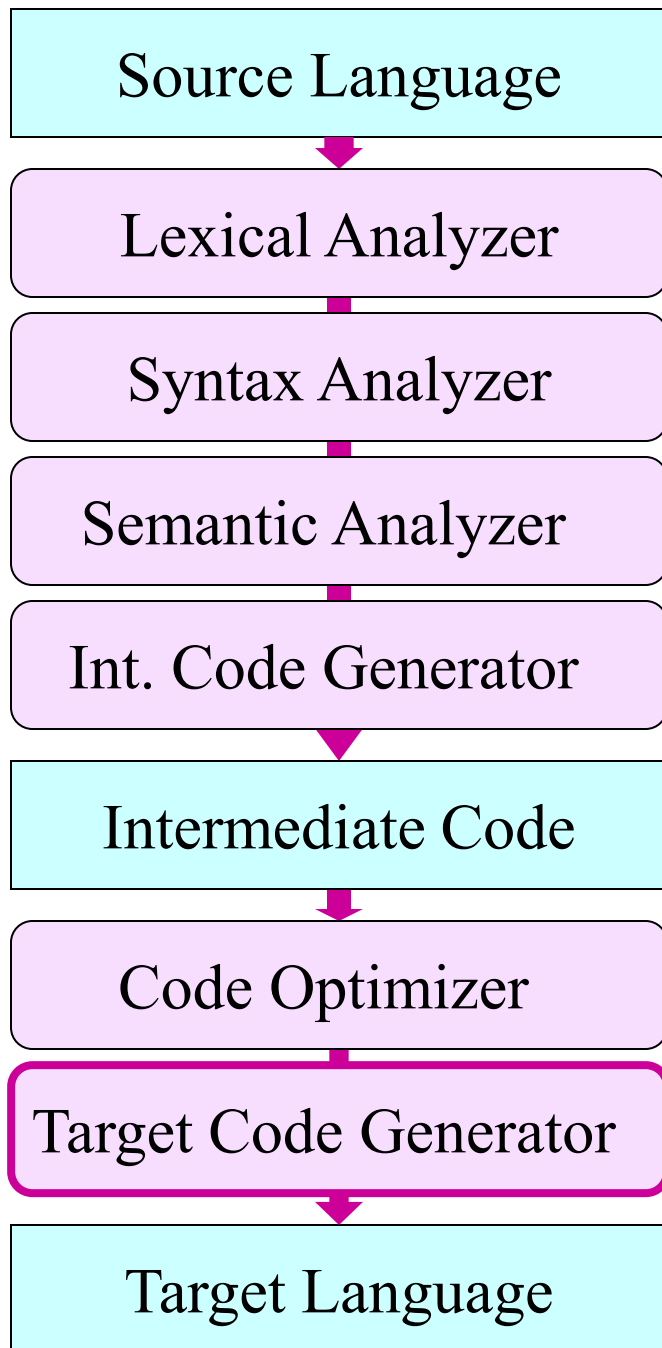
```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

Optimized Code:

```
temp1 = id3 * 60.0
id1 = id2 + temp1
```

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Compilation Example



Intermediate Code:

```
temp1 = int2real(60)
temp2 = id3 * temp1
temp3 = id2 + temp2
id1 = temp3
```

Optimized Code:

```
temp1 = id3 * 60.0
id1 = id2 + temp1
```

Target Code:

```
MOVE id3, R2
MULF #60.0, R2
MOVE id2, R1
ADDF R2, R1
MOVE R1, id1
```

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- ▶ End of Front-end
- ▶ End of Compilers Course



Useful links

Intermediate Code Generation

- ▶ <https://www.youtube.com/watch?v=OFuJK7dBdo4>
- ▶ <https://www.youtube.com/watch?v=lqAG6xmvOUI>
- ▶ <https://www.youtube.com/watch?v=XeKnqo6UKw0&list=PLI22nRq-CejDnrs4rVANI6DXoFzqqUmhe&index=16>