

Quiz 4 Solutions

1. Question: 5.5 points

Given the LP program:

$$\begin{array}{ll} \text{Minimize} & p = 3x - 2y + z \\ \text{Subject to} & -x - y + z \leq 1 \\ & x + 2y - z \leq 5 \\ & x, y, z \geq 0 \end{array}$$

Set up the initial simplex tableau.

- **Solution:**

$$\begin{array}{c} u \\ v \end{array} \left[\begin{array}{cccccc|c} x_1 & x_2 & x_3 & u & v & z & \\ \hline -1 & -1 & 1 & 1 & 0 & 0 & 1 \\ 1 & 2 & -1 & 0 & 1 & 0 & 5 \\ \hline 3 & -2 & 1 & 0 & 0 & 1 & 0 \end{array} \right]$$

The **grading scheme** for this question is as follows:

- 1 mark off for incorrect objective function
- 0.5 mark off for incorrect objective row (check signs)
- 0.5 mark off for no z or P column present in tableau

2. Question: 4.5 points

Consider the following tableau for a maximization problem:

$$\left[\begin{array}{ccccccccc|c} x_1 & x_2 & x_3 & x_4 & x_5 & s_1 & s_2 & s_3 & \\ \hline 0 & 1/3 & 1 & 2 & 1 & 0 & 3 & -3 & 1 \\ 0 & 1 & 0 & 1/2 & 1 & 1 & -1/3 & -1/2 & 2 \\ 1 & -1 & 0 & 0 & 1/3 & 0 & 0 & 1 & 0 \\ \hline 0 & -6 & 0 & -3 & -1 & 0 & 3 & 9 & 24 \end{array} \right]$$

- Identify the basic variables in the above tableau.
- What basic feasible solution does the tableau represent?
- Indicate which variable should be the entering variable and which variable should be the departing variable.
- Compute the next tableau using Simplex method, and what can you tell from the new tableau?

- **Solution:**

- x_1, x_3, s_1
- $(0, 0, 1, 0, 0, 2, 0, 0)$

- (c) x_2 enters, s_1 departs
 (d) The next tableau is as follows

$$\left[\begin{array}{cccccccc|c} x_1 & x_2 & x_3 & x_4 & x_5 & s_1 & s_2 & s_3 & \\ \hline 0 & 0 & 1 & 11/6 & 2/3 & -1/3 & 11/3 & -17/6 & 1 \\ 0 & 1 & 0 & 1/2 & 1 & 1 & -1/3 & -1/2 & 2 \\ 1 & 0 & 0 & 1/2 & 4/3 & 1 & -1/3 & -1/2 & 2 \\ \hline 0 & 0 & 0 & 0 & 5 & 6 & 1 & 6 & 36 \end{array} \right]$$

The **grading scheme** for this question is as follows:

- 1 mark for correct answer to each of (a) to (c)
- 2 marks for correct answer to (d): 1 mark for correct next tableau and 1 mark for correct analysis of tableau