

Theory of Electromigration

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I. Introduction

When an electric field is applied to a metal or semiconductor, a migration of atoms occurs. This phenomenon, which is known as *electromigration*,¹⁻⁵ is a subject of both fundamental and technological interest. From a fundamental point of view, electromigration is interesting because it involves