# CHEM352: Physical Chemistry I Homework Set II - due $24^{th}$ of Sept, 5.00 pm

Instructor: Dr. Mateusz Marianski Room#: HN-1321B

email: mmarians@hunter.cuny.edu

Lecture: Tue, 2.10-3.25 pm & Fri 2.10-3.25 pm, C111

Office hours: Wed, 4-6 pm, **HN-1321B** 

## Problem 1 CH3/5pts

Using definitions o heat capacities at constant volume and pressure, cyclic rule (equations a/P3.32 and b/P3.37) and expression for  $\left(\frac{\partial U}{\partial V}\right)_T = T\left(\frac{\partial P}{\partial T}\right)_V - P$  (equation c/P3.38), prove that:

$$C_P = -\frac{\left(\frac{\partial H}{\partial P}\right)_T}{\left(\frac{\partial T}{\partial P}\right)_H} \tag{1a}$$

$$C_V = -\left(\frac{\partial U}{\partial V}\right)_T \left(\frac{\partial V}{\partial T}\right)_U \tag{1b}$$

$$\left(\frac{\partial C_V}{\partial V}\right)_T = T \left(\frac{\partial^2 P}{\partial T^2}\right)_V \tag{1c}$$

Show that the equation 1c simplifies to 0 for ideal and van der Waals gas (P3.39).

## Problem 2 (P4.14 and P4.21)

CH4/5pts

1. From the following data, compute the  $\Delta_f H^o$  of  $CaC_{2(s)}$  at 298 K.

$$CaC_{2(s)} + 2H_2O_{(l)} \rightarrow Ca(OH)_{2(s)} + C_2H_{2(g)}$$
  $\Delta H_R^o = -127.9[kJ/mol]$  (2a)

$$Ca_{(s)} + \frac{1}{2}O_{2(g)} \to CaO_{(s)}$$
  $\Delta H_R^o = -635.1[kJ/mol]$  (2b)

$$CaO_{(s)} + H_2O(l) \to Ca(OH)_{2(s)}$$
  $\Delta H_R^o = -65.2[kJ/mol]$  (2c)

The combustion enthalpies of  $C_{(s)}$  and  $C_2H_{2(q)}$  are -393.5 and -1299.8 kJ/mol respectively.

2. From the following data, compute  $\Delta H_{R,391.4K}^o$  for the  $CH_3COOH_{(g)}+2O_{2(g)}\rightarrow 2H_2O_{(g)}+2CO_{2(g)}$ :

$$CH_{3}COOH_{(l)} + 2O_{2(g)} \rightarrow 2H_{2}O_{(l)} + 2CO_{2(g)} \qquad \qquad \Delta H_{R,298.1K}^{o} = -871.5[kJ/mol] \qquad (3a)$$

$$H_{2}O_{(l)} \rightarrow H_{2}O_{(g)} \qquad \qquad \Delta H_{R,298.1K}^{o} = 40.6[kJ/mol] \quad (3b)$$

$$CH_{3}COOH_{(l)} \rightarrow CH_{3}COOH_{(g)} \qquad \qquad \Delta H_{R,391.4K}^{o} = 24.4[kJ/mol] \quad (3c)$$

The molar  $\frac{C_P}{R}$  are equal 14.9, 3.53, 4.46, 9.055 and 4.048 for  $CH_3COOH_{(l)}, O_{2(g)}, CO_{2(g)}, H_2O_{(l)}$  and  $H_2O_{(g)}$  respectively  $(C_P = \frac{C_P}{R} \cdot R)$ .

### Problem 3 (variation of P5.7)

CH5/5pts

Consider a classical reversible Carnot cycle with 1.0 mole of an ideal gas with  $C_V = \frac{5}{2}R$  as a working substance that undergoes, as we discussed in the lecture (figure 5.2 in the book), following transitions:

- 1.  $(a \rightarrow b)$  Isothermal expansion from  $V_a$ =2.5 L to  $V_b$ =10 L at  $T_{hot}$  = 640 K
- 2.  $(b \rightarrow c)$  Adiabatic expansion until system reaches  $T_{cold} = 240 \text{ K}$
- 3.  $(c \to d)$  Isothermal compression at  $T_{cold} = 240$  K.
- 4.  $(d \rightarrow a)$  Adiabatic compression until gas reaches the  $T_{hot}$  and  $V_a$ =2.5 L.

#### Please calculate:

- 1. Volume at points c and d  $(V_c \text{ and } V_d)$ .
- 2. Work for the each step of the cycle and the total work.
- 3. The efficiency  $\theta$  of the cycle and the amount of heat that needs to be extracted from the reservoir  $T_{hot}$  to provide 1.5 kJ of work in the surroundings.

## Problem 4 (P5.39)

CH5/5pts

- 1. Calculate  $\Delta S$  if 1.00 mol of liquid water is heated from  $0.00^{o}C$  to  $10.00^{o}C$  under constant pressure and  $C_{P,m}=75.3$  [J/mol·K].
- 2. The melting point of water at the pressure of interest is  $0.00^{\circ}C$  and the enthalpy of fusion is 6.010 [kJ/mol]. The boling point is  $100^{\circ}C$  and the enthalpy of vaporization is 40.65 [kJ/mol]. Calculate  $\Delta S$  for the transformation from ice to vapor:  $H_2O(s,0^{\circ}C) \rightarrow H_2O(g,100^{\circ}C)$

Problem 5 CH5/5pts

Using the thermodynamic cycles, explain the difference between the heat engine (Carnot cycle) and Otto and diesel engines. Why diesel engine requires different type of fuel than regular (Otto) engine? Finally, what is your opinion on Volkswagen emission scandal?