

# BS2280 – Econometrics I

## Homework 5: Multiple Regression Model I

### 1

When we interpret the coefficients of a multiple regression model, we always add “holding everything else constant”. Using an example, explain what it means.

### 2

Data on 935 individuals was collected to identify what factors can explain the variation in wage data. Firstly, a simple regression is run regressing wages (monthly earnings in USD) on years of education. Secondly, a multiple regression is run regressing wages on years of education and years of work experience.

- i Interpret the intercepts and coefficients of both regressions and make reference to their statistical significance.
- ii Explain why the omission of the work experience variable in the simple regression model led to an underestimation of the impact of education on wages.
- iii Using the multiple regression model, predict the wage of someone who has 12 years of education and 1 year of work experience.

### Simple regression model:

```
Call:
lm(formula = wages2$wage ~ wages2$educ)

Residuals:
    Min       1Q   Median       3Q      Max
-877.38 -268.63  -38.38   207.05  2148.26

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  146.952     77.715   1.891  0.0589 .
wages2$educ   60.214      5.695  10.573 <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 382.3 on 933 degrees of freedom
Multiple R-squared:  0.107,    Adjusted R-squared:  0.106
F-statistic: 111.8 on 1 and 933 DF,  p-value: < 2.2e-16
```

### Multiple regression model:

```
Call:
lm(formula = wages2$wage ~ wages2$educ + wages2$exper)

Residuals:
    Min       1Q   Median       3Q      Max
-924.38 -252.74  -40.88   198.16  2165.70

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -272.528     107.263  -2.541  0.0112 *
wages2$educ   76.216       6.297  12.104 < 2e-16 ***
wages2$exper  17.638       3.162   5.578 3.18e-08 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 376.3 on 932 degrees of freedom
Multiple R-squared:  0.1359,    Adjusted R-squared:  0.134
F-statistic: 73.26 on 2 and 932 DF,  p-value: < 2.2e-16
```

## 3

The output below is the result of fitting an educational attainment function, regressing  $S$  on  $ASVABC$ , a measure of cognitive ability,  $SM$ , and  $SF$ , years of schooling (highest grade completed) of the respondent's mother and father, respectively.

- Give an interpretation of the regression coefficients.
- Undertake hypothesis tests to show whether the coefficients are statistically significant. The critical  $t$ -value = 1.965 (5% significance level).

- c. Is the  $R^2$  is statistically significant? The critical F value at the 5% significance level is 2.62. Interpret your result.
- d. Calculate the 95% confidence interval for each coefficient.

```
Call:
lm(formula = EAW21$S ~ EAW21$ASVABC + EAW21$SM + EAW21$SF)

Residuals:
    Min       1Q   Median       3Q      Max
-5.9387 -1.6521  0.0186  1.5161  7.1553

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)   10.59674    0.61428    17.26 < 2e-16 ***
EAW21$ASVABC    1.24253    0.12359    10.05 < 2e-16 ***
EAW21$SM        0.09135    0.04593    1.99  0.04593 **
EAW21$SF        0.20289    0.04251    4.77  0.00011 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.254 on 496 degrees of freedom
Multiple R-squared:  0.329,    Adjusted R-squared:  0.3249
F-statistic: 81.06 on 3 and 496 DF,  p-value: < 2.2e-16
```

## 4

Explain the differences between  $R^2$  and adjusted  $R^2$  and calculate adjusted  $R^2$  using the information from question 3. The formula of adjusted  $R^2$  is

$$\bar{R}^2 = R^2 - \frac{k-1}{n-k}(1 - R^2)$$