

**Homework 10**  
**Due Wednesday, November 30th**

1. Let  $R$  be a ring, let  $L, M, Q$  be left  $R$ -modules, and let  $f : L \longrightarrow M$ ,  $g : L \longrightarrow Q$  be  $R$ -module homomorphisms. Show that  $M \oplus_L Q$  satisfies the universal property of fiber sums given in class.
2. Do the following exercises from Dummit and Foote:  
p. 403–404 (1st copy): 4, 5 (also deduce that projective modules are flat), 6, 7, 10(c): show that if  $N$  is an injective module, then  $\text{Hom}_R(R, N)$  is injective;  
p. 385–387 (2nd copy): 15, 16, 27(a).