

Lazy Evaluation

Lazy Evaluation

- The proposed implementation suffers from a serious performance problem: If tail is called several times, the corresponding stream will be recomputed each time
- This problem can be avoided by storing the result of the first evaluation of tail and re-using the stored result instead of recomputing tail
- This optimization is sound, since in a purely functional language an expression produces the same result each time it is evaluated
- We call this scheme lazy evaluation (as opposed to by-name evaluation in the case where everything is recomputed and strict evaluation, for normal parameters and val definitions)
- Roughly, laziness means: do things as late as possible and never do them twice
- Lazy evaluation is a very powerful principle because it avoids both unnecessary or repeated computations
- Haskell is a functional programming language that uses lazy evaluation by default
- Scala does not use lazy evaluation every time because it is quite unpredictable in when computations happen and how much space they take; this is mostly caused by the mutable side effects
- Scala uses strict evaluation by default, but allows lazy evaluation of value definitions with the lazy val form: **lazy val x = expr**
- The behavior of **lazy val** and **def** diverge from the second time the variables are called; for **def x**, every time you call, the expression is reevaluated, whereas for **lazy val**, the expression is reused every time except for the first time, when it is evaluated

Exercise: Consider the following program:

```
def expr = {  
  val x = { print("x"); 1 }  
  lazy val y = { print("y"); 2 }  
  def z = { print("z"); 3 }  
  z + y + x + z + y + x  
}  
expr
```

If you run this program, what gets printed as a side effect of evaluating expr? – **xzyz**, val x is evaluated when it is declared, and never afterwards, lazy val is evaluated when first called and never afterwards and def z is evaluated each time it is called.

Lazy Vals and Streams

- Using a lazy value for tail, Stream.cons can be implemented more efficiently:

```
def cons[T](hd: T, tl: => Stream[T]) = new Stream[T] {  
  def head = hd  
  lazy val tail = tl  
  ...  
}
```

Evaluation Trace

- To convince ourselves that the implementation of streams really does avoid unnecessary computation, let's observe the execution trace of the expression:

(streamRange(1000, 10000) filter isPrime) apply 1

--> (if (1000 >= 10000) empty

else cons(1000, streamRange(1000 + 1, 10000))

.filter(isPrime).apply(1)

--> cons(1000, streamRange(1000 + 1, 10000))

.filter(isPrime).apply(1)

Let's abbreviate cons(1000, streamRange(1000 + 1, 10000)) to C1

--> C1.filter(isPrime).apply(1)

--> (if (C1.isEmpty) C1

else if (isPrime(C1.head)) cons(C1.head, C1.tail.filter(isPrime))

else C1.tail.filter(isPrime))

.apply(1)

--> if (isPrime(C1.head)) cons(C1.head, C1.tail.filter(isPrime))

else C1.tail.filter(isPrime))

.apply(1)

--> if (isPrime(1000)) cons(C1.head, C1.tail.filter(isPrime))

else C1.tail.filter(isPrime))

.apply(1)

--> if (false) cons(C1.head, C1.tail.filter(isPrime))

else C1.tail.filter(isPrime))

.apply(1)

--> C1.tail.filter(isPrime)).apply(1)

--> streamRange(1001, 10000)

.filter(isPrime).apply(1)

The evaluation sequence continues like this until:

--> streamRange(1009, 10000)

.filter(isPrime).apply(1)

--> cons(1009, streamRange(1009 + 1, 10000))

.filter(isPrime).apply(1)

Let's abbreviate cons(1009, streamRange(1009 + 1, 10000)) to C2

--> C2.filter(isPrime).apply(1)

--> cons(1009, C2.tail.filter(isPrime)).apply(1)

--> if (1 == 0) cons(1009, C2.tail.filter(isPrime)).head

else cons(1009, C2.tail.filter(isPrime)).tail.apply(0)

--> cons(1009, C2.tail.filter(isPrime)).tail.apply(0)

--> C2.tail.filter(isPrime).apply(0)

--> streamRange(1010, 10000).filter(isPrime).apply(0)

The process continues until:

--> streamRange(1013, 10000).filter(isPrime).apply(0)

--> cons(1013, streamRange(1013 + 1, 10000)).filter(isPrime).apply(0)

Let C3 be a shorthand for cons(1013, streamRange(1013 + 1, 10000))

--> C3.filter(isPrime).apply(0)

--> cons(1013, C3.tail.filter(isPrime)).apply(0)

--> 1013

Only the part of the stream necessary to compute the result has been constructed