Método de Zhou 2013

PCOM Posterior-focused catch-only method S. Zhou, Modificado por Elson Leal para sardina austral Aysen 2019, CBA 2020

This method requires time series of catch data only. However, some life history parameters, M, Linf, k, T_{max} , $T_{maturation}$, will improve the performance. Also, a rough guess of maximum depletion level D = B_{max} B will be helpful. This example is for single catch series

Modelo

```
library(knitr) # para generar reporte Rmarkdown
library(stringr)
library(reshape)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following object is masked from 'package:reshape':
##
##
       rename
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
library(ggplot2)
library(ggthemes) # para ggplot
library(patchwork) # para unir gráficos de gaplot
library(strucchange) # libreria utilizada para análisis de quiebres
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: sandwich
## Attaching package: 'strucchange'
## The following object is masked from 'package:stringr':
##
```

```
##
     boundary
getwd()
## [1] "/Users/mariajosezunigabasualto/MJZ/CTP2021/SARDINA AUSTRAL AYSEN/INFORME FINAL"
# model
BDM=function(K,dep,b,C,r){ ### biomass dynamics model
B=err.B=rep(NA,length(C))
B[1]=b*K;b1=B[1]
for(i in 2:length(B)){
 B[i] = \max(\min(B[i-1] + r * B[i-1] * (1-B[i-1]/K) - C[i-1], K), 0)
\# err.B[i] = ifelse(!is.na(U[i-1]&U[i]) & B[i]>0, (B[i-1]/B[i]-U[i-1]/U[i]^2,NA)
}
if(all(B>C) & all(B<=K)){</pre>
 abs(B[length(B)]-dep*K)
# if(any(U>0)){((B[length(B)]-dep*K)/K)^2 +sum(err.B,na.rm=T)} else ((B[length(B)]-dep*K)/K)^2
} else {10^5}
}
sim1=function(k25=k25,k75=k75,r25=r25,r75=r75,yr=yr,C=C,nsim=nsim,msy=NULL){
Bend.keep=K.keep=r.keep=dep.keep=d.keep=vector()
nyr=length(yr)
B=F2Fmsy=B2Bmsy=matrix(NA,nyr,nsim)
K=r=vector()
plot(0,0,type="n",xlim=c(min(yr),max(yr)),ylim=c(-1,round(k75,0)*1.15),
xlab="", ylab="", yaxt="n", xaxt="n")
for(j in 1:nsim){
  K[1] = runif(1, k25, k75)
  r[1]=runif(1,r25,r75)
  B[1,i]=K[1]
  for(i in 2:(nyr)){
    r[i]=runif(1,r25,r75)
    K[i]=runif(1,k25,k75)
    B[i,j]=B[i-1,j]+r[i]*B[i-1,j]*(1-B[i-1,j]/K[i])-C[i-1]
    F2Fmsy[i,j]=(C[i]/B[i,j])/(r[i]/2)
   B2Bmsy[i,j]=B[i,j]/(K[i]/2)
  cols \leftarrow rgb(runif(1,0,j)/nsim,(nsim-runif(1,0,j))/nsim,(1)/(nsim+100),
  alpha=0.6)
  lines(yr,B[,j],col=cols)
  K.keep[j]=mean(K)
  r.keep[j]=mean(r)
  F2Fmsy[,j]=(C/B[,j])/(mean(r)/2)
  B2Bmsy[,j]=B[,j]/(mean(K)/2)
}
Bend.keep=B[nyr,]
d.keep=B[nyr,]/mean(K)
lines(yr,apply(B,1,median),lty=1,lwd=3)
lines(yr,C,lwd=2,col="#363636",lty=2)
```

points(yr,C,pch=21,col=4,bg=4,cex=1.3)

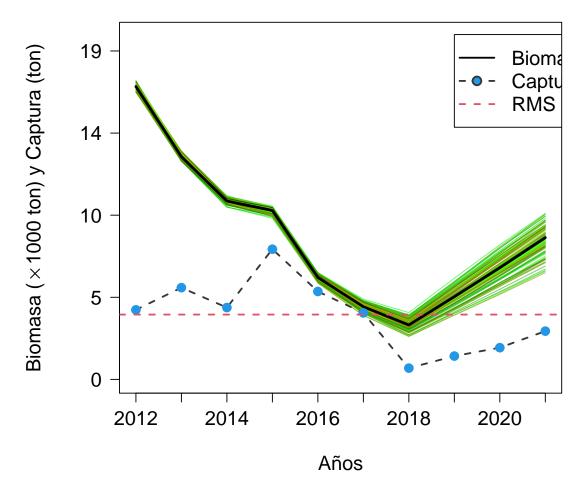
```
y1<-seq(0,round(k75,0)*1.1,le=5);x1<-seq(1,length(yr),by=1)
axis(1,at=yr[x1],labels=yr[x1],las=1)
axis(2,at=y1,labels=format(round(y1/1000,0),3),las=2)
legend(yr[nyr-2],max(y1)*1.05,c("Biomasa","Captura","RMS"),lty=c(1,2,2),
col=c(1,"#363636",2),pch=c(NA,21,NA),lwd=c(2,2,2),pt.bg=c(NA,4,NA),cex=1.3)
BC<-expression(paste('Biomasa ('%*%'1000 ton) y Captura (ton)',sep=""))
mtext(BC,side=2,line=4.0,cex=1.3)
mtext("Años",side=1,line=3.5,cex=1.3)
if(is.null(msy)){} else {abline(h=msy,lty=2,col=2,lwd=2)}
msy=K.keep*r.keep/4
return(list(K.keep,r.keep,msy,Bend.keep,d.keep,B,r,F2Fmsy,B2Bmsy))}
}</pre>
```

Ingresa datos de captura

```
# input catch data and r range for sautral XI stock
C=c(4033,5318,4163,7547,5097,3853,653,1352,1839,2797)
yr = seq(2012, 2021)
r.lci=0.85;r.uci=1.2
# search through K grids, with specific range for K1 follow
N1=100
K1=\exp(\operatorname{seq}(\log(\max(C)),\log(\max(C)*50),l=N1))
# genera los valores de la deplecion
dep=round(seq(0.1,0.8,0.05),2);nd=length(dep)
r1=obj1=matrix(0,N1,nd) #matriz que almacena los output de las funciones
b=1#Si \ (C[1]/max(C)<0.5, \ (0.5+0.9)/2 \ (0.3+0.6)/2); b=0.5
# ciclo
for(j in 1:nd){
 for(i in 1:N1){
    out=optimize(BDM,K=K1[i],b=b,C=C,dep=dep[j],
    interval=c(r.lci-.05,r.uci+.05))
   r1[i,j]=out$min
    obj1[i,j]=out$obj
  }
}
\#vLinf=58.95; vk=0.28; Tmax=10; Tmat=NA; T=17
#M=vector()
\#M[1] = exp(1.44-0.982*log(Tmax))
#M[2]=1.65/Tmat
\#M[3] = exp(1.2-0.17*log(vLinf)+log(vk))
#M[4]=1.82*vk
\#M[5] = \exp(-0.0152 - 0.279 * \log(vLinf) + 0.6543 * \log(vk) + 0.463 * \log(T))
#w=0.87 #para teleost y w=0.41 para chondrithys
\#r.mean=2*mean(M,na.rm=T)*w
\#r.sd=sd(M,na.rm=T)
\#r.backup=r
\#r[r > r.mean + 2*r.sd \mid r < r.mean - 2*r.sd] = NA
```

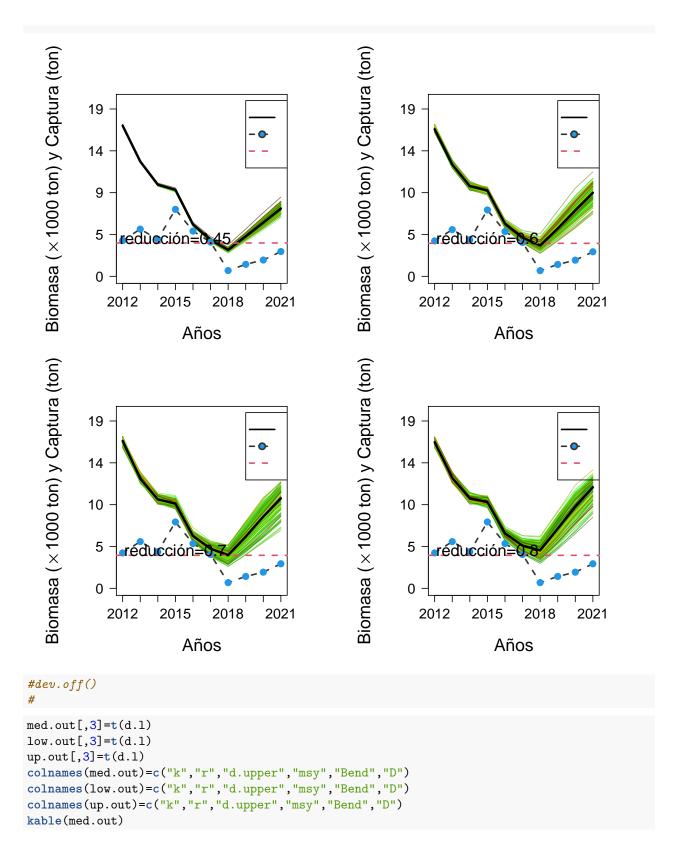
```
######################################
r1.backup=r1 ;# r1=r1.backup
r1[obj1 > K1*0.01]=NA
r1[r1 > r.uci | r1 < r.lci]=NA
######################################
kr=as.data.frame(cbind(K1,r1))
colnames(kr)=c('k',dep)
all=cbind(K1,stack(kr[,2:nd+1]))#antes nd+1
colnames(all)=c("k","r","ind")
all$d=as.numeric(as.character(all$ind))
all=all[,c(1,2,4)]
all=all[!is.na(all[,2]),]
all$msy=all[,1]*all[,2]/4
# estimate reference points
\#cutoff = ifelse(tail(C, 1)/max(C) \le 0.5, 0.5, 0.8)
all2=all[!is.na(all$r) & all$d <= 0.5,]#cutoff, assume upper depettion=0.4
quan1=apply(all2,2,quantile)
k25=quan1[,1][2];k75=quan1[,1][4]
r25=quan1[,2][2];r75=quan1[,2][4]
msy.media=quan1[,4][3]
all3=all2[all2$k>k25 & all2$k<k75 & all2$r>r25 & all2$r<r75,]
para=list(k25=k25,k75=k75,r25=r25,r75=r75)
```

Figura biomasa



```
#dev.off()
#EXTRAE DATOS DE INTERES PARA LA INCERTIDUMBRE
F2Fmsy=as.data.frame(out1[8]);B2Bmsy=as.data.frame(out1[9])
quant=function(x)quantile(x,c(0.2,0.8))
dat.out=data.frame(year=yr,B2Bmsy.med=apply(B2Bmsy,1,median),
quan1.B=apply(B2Bmsy,1,quant)[1,],quan3.B=apply(B2Bmsy,1,quant)[2,],
F2Fmsy.med=apply(F2Fmsy,1,median),quan1.F=apply(F2Fmsy,1,quant)[1,],
quan3.F=apply(F2Fmsy,1,quant)[2,])
BF2msy.end=data.frame(t(rbind(B2Bmsy[length(yr),],F2Fmsy[length(yr),])))
colnames(BF2msy.end)=c("B2Bmsy", "F2Fmsy")
out1.backup=out1 #out1=out1.backup
sp=out1[1:5]
sp=as.data.frame(sp)
                  # summary(sp)
colnames(sp)=c("k","r","msy","Bend","Depletion")
BendD=apply(sp,2,quantile)
#FINAL RESULT
```

```
tabla<-cbind(quan1[,c(1,2,4)],BendD[,4:5])
#library(rJava)
                                                      ## PROBLEMAS CON ESTO
#library(xlsx)
write.csv2(tabla, "tabla1.csv", row.names=FALSE)
print(tabla)
##
                                      Bend Depletion
              k
                              msy
## 0%
       16634.15 0.8534279 3692.060 6184.365 0.3647913
## 25% 16634.15 0.8614773 3726.883 7694.024 0.4538402
## 50% 16969.38 0.8861789 3757.632 8216.055 0.4846327
## 75% 17304.61 0.9106092 3786.803 8782.574 0.5180494
## 100% 17304.61 0.9178450 3816.893 9620.252 0.5674608
Bioma<-apply(out1.backup[[6]],1,quantile)</pre>
#note: Bmsy = k/2, Blim = k/4
B.sim=data.frame(out1[6])
BF=t(apply(B.sim,1,quantile))
BF=cbind(BF,C/BF)
BRP=c(quan1[3,1]/2,quan1[3,2]/2)
fs=data.frame(cbind(BF[,c(8,3)],yr)) # F y Biomasa media
#GRAFICA BIOMASA V/S CPUE
#plot(yr,BF[,3],type="b",ylab="Biomasa and CPUE")
#par(new=T)
#plot(yr, U, type="b", col=2, axes=F, xlab="", ylab="")
# sensitivity to assumed upper depletion (if needed) #
med.out=low.out=up.out=matrix(NA,nrow=4,ncol=6)
d.1=c(0.45,0.6,0.7,0.8) # assumed upper depletion levels
#name2<-paste(getwd(), "/Figuras/Fig2_Zhou2013_depletion.png", sep="")</pre>
\#pnq(file=name2, width=1400, height=1400)
layout(matrix(1:4,ncol=2,byrow=T),widths=c(1,1),heights=c(1,1))
for(i in 1:4){
 all2=all[!is.na(all$r) & all$d <= d.l[i],]
 quan1=apply(all2,2,quantile)
 k25=quan1[,1][2];k75=quan1[,1][4]
 r25=quan1[,2][2];r75=quan1[,2][4]
 msy.median=quan1[,4][3]
 nsim=100
 par(mar=c(5.5,6.9,4,4),cex.axis=1.3)
 out1=sim1(k25=k25,k75=k75,r25=r25,r75=r75,C=C,yr=yr,nsim=nsim,msy=msy.media)
 tex=paste("reducción=",d.l[i],sep="")
 text(2015, round(para$k25, 0)*0.26, tex, cex=1.5, xpd=T)
 sp=out1[1:5]
 sp=as.data.frame(sp)
                      # summary(sp)
 colnames(sp)= c('k','r','msy','Bend','D')
 BendD=apply(sp,2,quantile)
 med.out[i,]=(c(quan1[3,],BendD[3,4:5]))
 low.out[i,]=(c(quan1[2,],BendD[1,4:5]))
 up.out[i,]=(c(quan1[4,],BendD[5,4:5]))
}
```



k	r	d.upper	msy	Bend	D
16969.38	0.8808126	0.45	3734.416	7639.931	0.4481478
16634.15	0.9178450	0.60	3847.086	9508.414	0.5675254
16634.15	0.9344620	0.70	3940.578	10237.327	0.6151672
16634.15	0.9541809	0.80	4048.871	11491.280	0.6897368

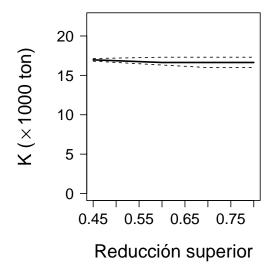
kable(low.out)

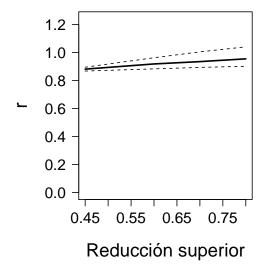
k	r	d.upper	msy	Bend	D
16801.77	0.8671203	0.45	3713.238	6613.459	0.3879364
16311.91	0.8826329	0.60	3783.249	7108.467	0.4242806
15989.66	0.8930673	0.70	3850.267	6619.545	0.3977725
15989.66	0.9011510	0.80	3912.928	8084.892	0.4852764

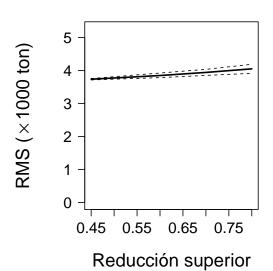
kable(up.out)

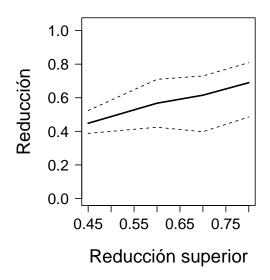
	ζ	r	d.upper	msy	Bend	D
17137.00)	0.8945050	0.45	3755.595	8931.192	0.5238914
17304.61	l	0.9622123	0.60	3922.126	11887.888	0.7095483
17304.61	L	1.0039538	0.70	4033.211	12139.221	0.7294532
17304.61	l	1.0398357	0.80	4187.036	13474.547	0.8087776

```
# parameters as a function of assumed upper depletion level
#name3<-paste(qetwd(), "/Figuras/Fig3_Zhou2013_sensitivity.png", sep="")</pre>
#pnq(file=name3, width=900, height=1000)
layout(matrix(1:4,ncol=2,byrow=T),widths=c(1,1),heights=c(1,1))
par(mar=c(5.6,6.7,4,4),cex.axis=1.4)
plot(med.out[,3],med.out[,1]/1000,ylim=c(0,max(med.out[,1]/1000*1.3)),type='l',lwd=2,xlab='',ylab='',la
lines(low.out[,3],low.out[,1]/1000,lty=2); lines(up.out[,3],up.out[,1]/1000,lty=2)
mtext(expression(paste('K ('%*%'1000 ton)')),side=2,line=3.8,cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
plot(med.out[,3],med.out[,2],ylim=c(0,max(med.out[,2]*1.3)),type='1',lwd=2,xlab='',ylab='',las=1)
mtext('r',side=2,line=3.8,cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
lines(low.out[,3],low.out[,2],lty=2); lines(up.out[,3],up.out[,2],lty=2)
plot(med.out[,3],med.out[,4]/1000,ylim=c(0,max(med.out[,4]/1000*1.3)),type='1',lwd=2,xlab='',ylab='',la
lines(low.out[,3],low.out[,4]/1000,lty=2);lines(up.out[,3],up.out[,4]/1000,lty=2)
mtext(expression(paste('RMS ('%*%'1000 ton)')),side=2,line=3.8,cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
plot(med.out[,3],med.out[,6],ylim=c(0,max(med.out[,6]*1.5)),type='l',lwd=2,xlab='',ylab='',las=1)
lines(low.out[,3],low.out[,6],lty=2);lines(up.out[,3],up.out[,6],lty=2)
mtext("Reducción", side=2, line=3.8, cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
```







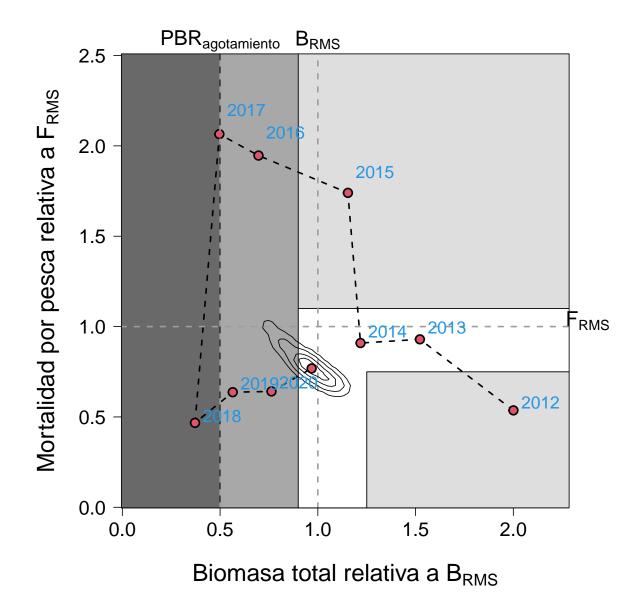


```
est<-z$z/max(z$z);z$z<-est
#Bmrs=43590;Fmrs=0.3515;Fest=C/Bioma[3,]
#Y1<-Fest/Fmrs;X1<-Bioma[2,]/Bmrs
#
soli<-cbind(yr,Bioma[3,],Fest,X1,Y1)
colnames(soli)<-c("year","BD","Fest","Brel","Frel")
kable(soli)</pre>
```

year	BD	Fest	Brel	Frel
2012	16973.734	0.2376024	2.0005129	0.5362403
2013	12914.123	0.4117972	1.5220499	0.9293772
2014	10337.422	0.4027116	1.2183616	0.9088721
2015	9789.457	0.7709315	1.1537788	1.7399003
2016	5909.892	0.8624523	0.6965359	1.9464519
2017	4211.110	0.9149606	0.4963186	2.0649569
2018	3153.544	0.2070686	0.3716746	0.4673291
2019	4791.072	0.2821915	0.5646725	0.6368727
2020	6473.296	0.2840902	0.7629383	0.6411577
2021	8216.055	0.3404310	0.9683387	0.7683122

```
## PROBLEMAS CON ESTO
#library(rJava)
#library(xlsx)
write.csv2(soli, "tabla2.csv", row.names=FALSE)
#DEFINE LAS AREAS DE LOS POLIGONOS
cols<-c("#696969","#A8A8A8","#DEDEDE")
ini < c(-0.09); xmax < -max(X1)*1.35; ymax < -max(Y1)*1.22; xmin < -(0.08)
pol1 < -matrix(c(0.9,ini,0.9,1.1,xmax,1.1,xmax,0.75,1.25,0.75,1.25,ini),
ncol=2,byrow=T)
pol2<-matrix(c(1.25,ini,1.25,0.75,xmax,0.75,xmax,ini),ncol=2,byrow=T)
pol3<-matrix(c(xmax,1.1,xmax,ymax,0.9,ymax,0.9,1.1),ncol=2,byrow=T)
pol4 < -matrix(c(0.5,ini,0.9,ini,0.9,ymax,0.5,ymax),ncol=2,byrow=T)
pol5<-matrix(c(-0.07,ini,0.5,ini,0.5,ymax,-0.07,ymax),ncol=2,byrow=T)</pre>
#name4<-paste(qetwd(), "/Figuras/Fig4_Zhou2013_fase.png", sep="")</pre>
\#pnq(file=name4, width=1200, height=1000)
par(mar=c(6.1,6.5,4.8,4.8),cex.axis=1.5,cex.lab=1.5)
plot(X1,Y1,col=0,xlab="",ylab="",yaxt="n",xlim=c(xmin,max(X1)*1.1),
ylim=c(0.09, max(Y1)*1.17))
axis(2,las=1)
polygon(pol5,col=cols[1],border=1);polygon(pol4,col=cols[2],border=1)
polygon(pol3,col=cols[3],border=1);polygon(pol2,col=cols[3],border=1)
polygon(pol1,col="white",border="black")
#points(mc.dat[,1],mc.dat[,2],pch=21,bg="#B5B5B5",cex=0.9,col=1)
lines(X1,Y1,lty=2,col=1,lwd=2)
lines(X1,Y1,type="p",bg=2,pch=21,cex=1.5,lwd=2)
abline(v=1,lty=2,col=8,lwd=2); abline(h=1,lty=2,col=8,lwd=2)
abline(v=0.5, lty=2, col=8, lwd=2)
contour(z,drawlabels=FALSE,levels=c(0.1,0.25,0.5,0.75),add=TRUE)
text(0.5,max(Y1)*1.29,expression(PBR[paste("agotamiento")]),cex=1.6,
pos=1,xpd=T)
text(1,max(Y1)*1.29,expression(B[paste("RMS")]),cex=1.6,pos=1,xpd=T)
```

```
text(max(X1)*1.19,1.11,expression(F[paste("RMS")]),cex=1.6,pos=1,xpd=T)
mtext(expression(paste("Biomasa total relativa a ",B[paste("RMS")],sep="")),
side=1,line=4.2,cex=1.8)
mtext(expression(paste("Mortalidad por pesca relativa a ",F[paste("RMS")],
sep="")),side=2,line=3.8,cex=1.8)
\#a2 < -which(yr\%in\%seq(2015,1994,by=-2)==TRUE)
a2 < -c(1,2,3,4,5,6,7,8,9)
text(X1[a2],Y1[a2]*1.06,yr[a2],cex=1.3,pos=4,col=4)
#text(1.10,0.83, "Plena Explotación", cex=1.6, pos=4, col=1, lwd=2)
#text(1.56,0.31,"Sub Explotación",cex=1.6,pos=4,col=1,lwd=2)
#text(1.33,1.51, "Sobrepesca", cex=1.6, pos=4, col=1, lwd=2)
#text(0.58,0.67, "Sobre", cex=1.6, pos=4, col=1, lwd=2)
#text(0.52,0.51, "Explotación", cex=1.6, pos=4, col=1, lwd=2)
#text(0.68,1.18, "Sobre-explotación y Sobrepesca", cex=1.6, pos=4, lwd=2, srt=90)
\#text(0.23, 1.18, "Colapso y/o Aqotamiento", cex=1.6, pos=4, lwd=2, srt=90)
box()
```

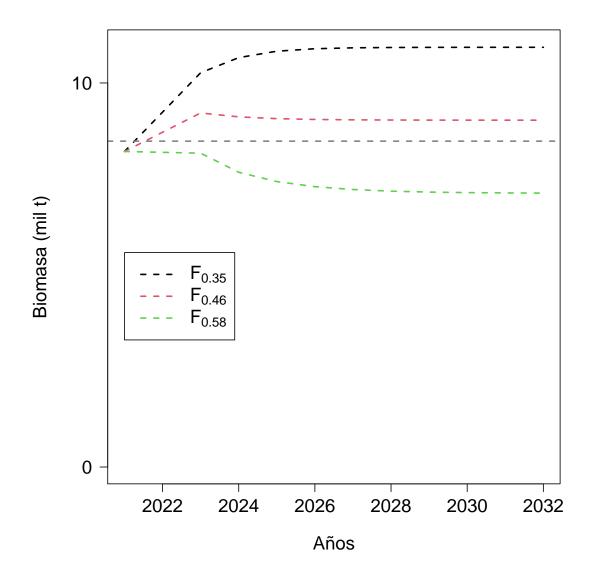


#dev.off()

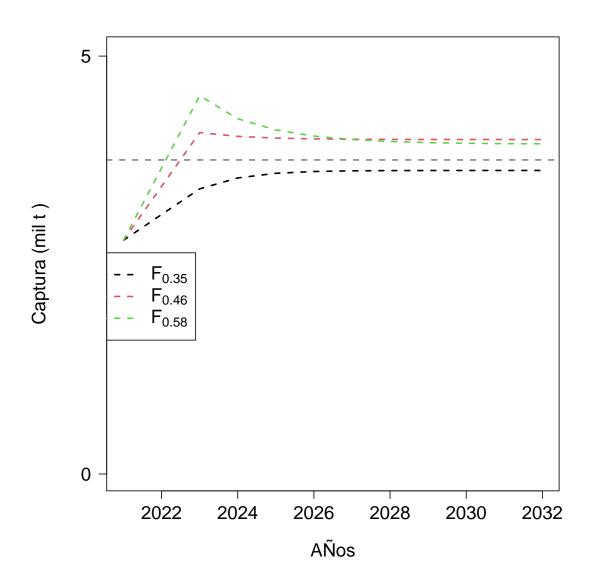
Cálculo de CBA

```
BT=CT=array(NA,c(length(prob),ss[1],length(yrs_pro)))
BT[,,1]<-Bioma[3,yy];CT[,,1]<-C[yy]
Fi=Fmrs*prob
for(y in 1:length(Fi)){
    for(n in 1:ss[1]){
        ki=sp$k[n];ri=sp$r[n]
        for(m in 1:(yyp-1)){
        if(m==1){CT[y,,1]=C[yy]} else {CT[y,n,m]=BT[y,n,m]*Fi[y]}
        BT[y,n,m+1]=BT[y,n,m]+ri*BT[y,n,m]*(1-BT[y,n,m]/ki)-CT[y,n,m]
        if(m==(yyp-1)){CT[y,n,m+1]=BT[y,n,m+1]*Fi[y]}
    }
}</pre>
```

GRAFICA LA CBA 2020 PARA sardina austral FF<-formatC(Fi,format="f",digits=2)</pre> BB<-expression(paste("Biomasa (mil t)",sep="")) $Binf \leftarrow tabla[2,1]/2; Bsup \leftarrow tabla[4,1]/2$ rng1<-range(BT[,,],na.rm=T)</pre> ax2<-seq(0,rng1[2]*1.15,by=10000);cols<-"#858585";y1<-length(yrs_pro) #name5<-paste(qetwd(), "/Figuras/Fiq5_Zhou2013_Proyeccion_B.pnq",sep="")</pre> #pnq(file=name5, width=900, height=800) #x11(width=8,height=7)par(mar=c(6.1,6.2,4.8,4.8),cex.axis=1.4,cex.lab=1.4) plot(yrs_pro[-2],seq(0,rng1[2]*1.15,le=(y1-1)),col=0,type="1",xlab="",ylab="",yaxt="n",ylim=c(0,rng1[2] for(x in 1:length(Fi)){ lines(yrs_pro[-2],apply(BT[x,,],2,quantile)[3,-2],col=x,lty=2,lwd=2) } abline(h=Bmrs,lty=2,lwd=2,col=cols) axis(2,at=ax2,labels=ax2/1000,las=1,cex=1.4) mtext(BB, side=2, line=3.5, cex=1.4) mtext("Años",side=1,line=3.4,cex=1.4) legend(2021,rng1[2]*0.5,c(expression(F[paste("0.35")]),expression(F[paste("0.46")]), expression(F[paste("0.58")])), lty=c(2,2,2,2,2), lwd=c(2,2,2,2,2), cex=1.4,col=c(1,2,3))



```
par(mar=c(6.1,6.2,4.8,4.8),cex.axis=1.4,cex.lab=1.4)
plot(yrs_pro[-2],seq(0,rng2[2]*1.15,le=11),col=0,type="l",xlab="",ylab="",yaxt="n",ylim=c(0,rng2[2]*0.9
for(x in 1:length(Fi)){
    lines(yrs_pro[-2],apply(CT[x,,],2,quantile)[3,-2],col=x,lty=2,lwd=2)
}
abline(h=MRS,lty=2,lwd=2,col=cols)
axis(2,at=ax3,labels=sprintf("%0.0f",ax3/1000),las=1,cex=1.4)
mtext(CC,side=2,line=3.5,cex=1.4)
mtext("AÑos",side=1,line=3.4,cex=1.4)
legend(2020,rng2[2]*0.5,c(expression(F[paste("0.35")]),expression(F[paste("0.46")]),
expression(F[paste("0.58")])),lty=c(2,2,2,2,2),lwd=c(2,2,2,2,2),cex=1.4,
col=c(1,2,3))
```



```
#dev.off()
# TABLA DE RESULTADOS
ct<-matrix(NA,length(Fi),5)
for(i in 1:length(Fi)){
ct[i,]<-as.numeric(quantile(CT[i,,2],probs=c(.1,.2,.3,.4,.5))) # CT[i,,2] (el 2 representa 1 año de p
}
colnames(ct)<-c("10%","20%","30%","40%","50%")</pre>
rownames(ct)<-formatC(Fi,format="f",digits=2)</pre>
cat("\n")
print(ct)
        10%
              20%
                    30%
                          40%
## 0.33 3114.226 3123.352 3129.292 3135.562 3140.357
## 0.44 4152.301 4164.469 4172.389 4180.749 4187.143
## 0.55 5190.376 5205.586 5215.486 5225.936 5233.929
# RANGO CBA PARA PBR Al MRS (2) y EL 2021(2)
rango<-quantile(CT[2,,2],prob=c(0.025,0.25,0.50,0.75,0.975))
kable(rango)
                                 х
                        2.5\%
                             4142.343
                        25\%
                             4168.543
                        50\%
                             4187.143
                        75\%
                             4206.894
                        97.5\%
                             4225.940
```

#FIN