## Método de Zhou 2013

# PCOM Posterior-focused catch-only method S. Zhou, Modificado por Elson Leal y María José Zúñiga para sardina austral Aysen, CBA 2021

This method requires time series of catch data only. However, some life history parameters, M, Linf, k,  $T_{max}$ ,  $T_{max}$ ,  $T_{max}$ , a rough guess of maximum depletion level D = B end/K will be helpful. This example is for single catch series

## Modelo

```
library(knitr) # para generar reporte Rmarkdown
library(stringr)
library(reshape)
library(dplyr)
library(ggplot2)
library(ggthemes) # para ggplot
library(patchwork) # para unir gráficos de ggplot
library(strucchange) # libreria utilizada para análisis de quiebres
getwd()
```

## [1] "/Users/mariajosezunigabasualto/MJZ/CTP2022/SARDINAAUSTRAL\_AYSEN/PRIMER\_INFORME"

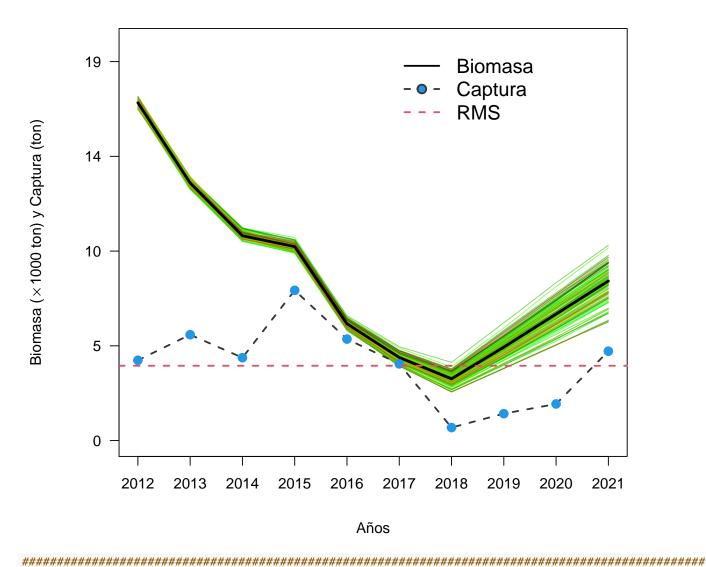
## Simulación

## Ingresa datos de captura

```
# input catch data and r range for sautral XI stock
C=c(4033,5318,4163,7547,5097,3853,653,1352,1839,4488)
yr = seq(2012, 2021)
r.lci=0.85;
r.uci=1.2
# search through K grids, with specific range for K1 follow
N1=100
K1=\exp(\operatorname{seq}(\log(\max(C)),\log(\max(C)*50),1=N1))
# genera los valores de la deplecion
dep=round(seq(0.1,0.8,0.05),2)
nd=length(dep)
r1=obj1=matrix(0,N1,nd) #matriz que almacena los output de las funciones
b=1#Si (C[1]/max(C)<0.5, (0.5+0.9)/2 (0.3+0.6)/2);b=0.5
# ciclo
for(j in 1:nd){
 for(i in 1:N1){
  out=optimize(BDM, K=K1[i], b=b, C=C, dep=dep[j],
   interval=c(r.lci-.05,r.uci+.05))
  r1[i,j]=out$min
  obj1[i,j]=out$obj
 }
}
#vLinf=58.95; vk=0.28; Tmax=10; Tmat=NA; T=17
#M=vector()
\#M[1] = exp(1.44 - 0.982 * log(Tmax))
#M[2]=1.65/Tmat
\#M[3] = exp(1.2-0.17*log(vLinf)+log(vk))
#M[4]=1.82*vk
\#M[5] = exp(-0.0152-0.279*log(vLinf)+0.6543*log(vk)+0.463*log(T))
#w=0.87 #para teleost y w=0.41 para chondrithys
\#r.mean=2*mean(M,na.rm=T)*w
\#r.sd=sd(M,na.rm=T)
\#r.backup=r
\#r[r > r.mean+2*r.sd \mid r < r.mean-2*r.sd]=NA
####################################
r1.backup=r1 ;# r1=r1.backup
r1[obj1 > K1*0.01]=NA
r1[r1 > r.uci | r1 < r.lci]=NA
####################################
```

```
kr=as.data.frame(cbind(K1,r1))
colnames(kr)=c('k',dep)
all=cbind(K1,stack(kr[,2:nd+1]))#antes nd+1
colnames(all)=c("k","r","ind")
all$d=as.numeric(as.character(all$ind))
all=all[,c(1,2,4)]
all=all[!is.na(all[,2]),]
all$msy=all[,1]*all[,2]/4
#############################
# estimate reference points
###############################
\#cutoff = ifelse(tail(C,1)/max(C) \le 0.5, 0.5, 0.8)
         =all[!is.na(all$r) & all$d <= 0.50,]#cutoff,assume upper depettion=0.50
al12
quan1
         =apply(all2,2,quantile)
k25
         =quan1[,1][2]
         =quan1[,1][4]
k75
         =quan1[,2][2]
r25
r75
         =quan1[,2][4]
msy.media=quan1[,4][3]
         =all2[all2$k>k25 & all2$k<k75 & all2$r>r25 & all2$r<r75,]
al13
para
         =list(k25=k25,k75=k75,r25=r25,r75=r75)
```

## Figura biomasa



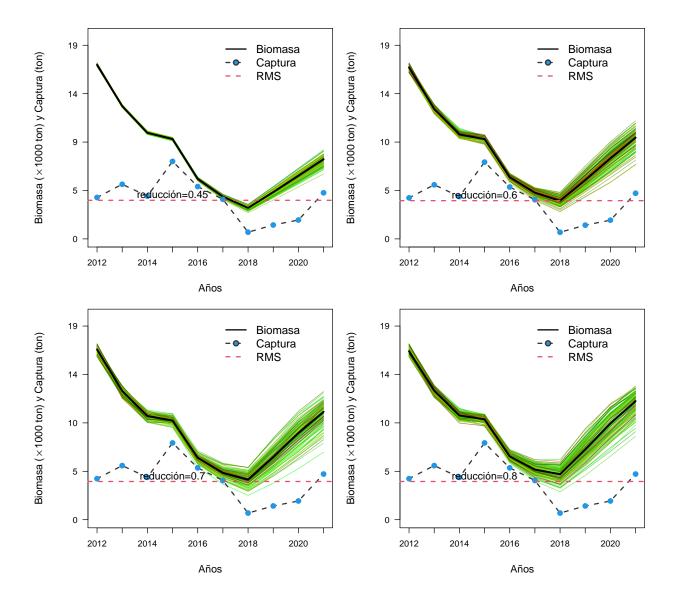
```
F2Fmsy.med=apply(F2Fmsy,1,median),
                quan1.F=apply(F2Fmsy,1,quant)[1,],
                quan3.F=apply(F2Fmsy,1,quant)[2,])
BF2msy.end = data.frame(t(rbind(B2Bmsy[length(yr),],F2Fmsy[length(yr),])))
colnames(BF2msy.end)=c("B2Bmsy","F2Fmsy")
#kable(BF2msy.end)
out1.backup=out1 #out1=out1.backup
sp=out1[1:5]
sp=as.data.frame(sp)
                  # summary(sp)
colnames(sp)=c("k","r","msy","Bend","Depletion")
BendD=apply(sp,2,quantile)
#FINAL RESULT
tabla<-cbind(quan1[,c(1,2,4)],BendD[,4:5])
write.csv2(tabla, "tabla1.csv", row.names=FALSE)
kable(tabla)
```

	k	r	msy	Bend	Depletion
0%	16634.15	0.8534279	3692.060	5955.795	0.3509165
25%	16634.15	0.8614773	3726.883	7417.435	0.4370366
50%	16969.38	0.8861789	3757.632	8014.236	0.4722002
75%	17304.61	0.9106092	3786.803	8520.308	0.5020181
100%	17304.61	0.9178450	3816.893	9811.489	0.5780947

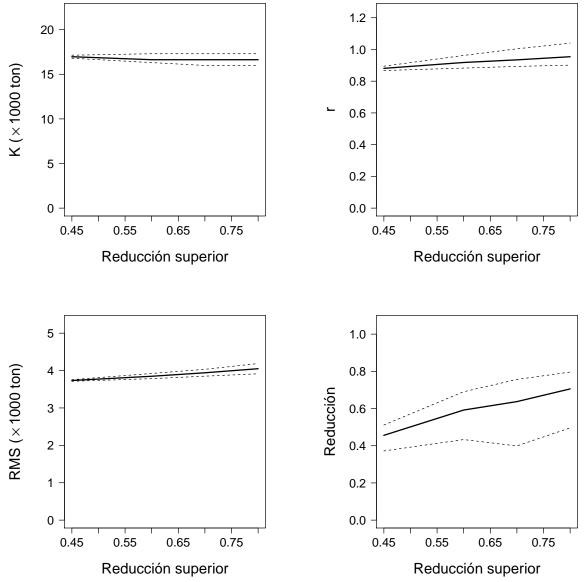
```
Bioma <-apply(out1.backup[[6]],1,quantile)
#note: Bmsy = k/2, Blim = k/4
B.sim =data.frame(out1[6])
BF =t(apply(B.sim,1,quantile))
BF =cbind(BF,C/BF)
BRP =c(quan1[3,1]/2,quan1[3,2]/2)
fs =data.frame(cbind(BF[,c(8,3)],yr)) # F y Biomasa media
#GRAFICA BIOMASA V/S CPUE
#plot(yr,BF[,3],type="b",ylab="Biomasa and CPUE")
#par(new=T)
#plot(yr,U,type="b",col=2,axes=F,xlab="",ylab="")
#plot(yr,U,type="b",col=2,axes=F,xlab="",ylab="")
#plot(yr,U,type="b",col=2,axes=F,xlab="",ylab="")</pre>
```

## Sensibilidad

```
# sensitivity to assumed upper depletion (if needed) #
med.out=low.out=up.out=matrix(NA,nrow=4,ncol=6)
d.1=c(0.45,0.6,0.7,0.8) # assumed upper depletion levels
layout(matrix(1:4,ncol=2,byrow=T),widths=c(1,1),heights=c(1,1))
for(i in 1:4){
 all2=all[!is.na(all$r) & all$d <= d.l[i],]
 quan1=apply(all2,2,quantile)
 k25=quan1[,1][2]
 k75=quan1[,1][4]
 r25=quan1[,2][2]
 r75=quan1[,2][4]
 msy.median=quan1[,4][3]
 nsim=100
 #Figura
 par(mar=c(5,5.5,1,1),cex.axis=1.3)
 out1=sim1(k25=k25,k75=k75,r25=r25,r75=r75,C=C,yr=yr,nsim=nsim,msy=msy.media)
 tex=paste("reducción=",d.l[i],sep="")
 text(2015,round(para$k25,0)*0.26,tex,cex=1.2,xpd=T)
 # Tablas
 sp = out1[1:5]
 sp = as.data.frame(sp) # summary(sp)
 colnames(sp)= c('k','r','msy','Bend','D')
 BendD = apply(sp,2,quantile)
 med.out[i,] =(c(quan1[3,],BendD[3,4:5]))
 low.out[i,] =(c(quan1[2,],BendD[1,4:5]))
 up.out[i,] =(c(quan1[4,],BendD[5,4:5]))
 med.out[,3] = t(d.1)
 low.out[,3] = t(d.1)
 up.out[,3] = t(d.1)
 colnames(med.out)=c("k","r","d.upper","msy","Bend","D")
 colnames(low.out)=c("k","r","d.upper","msy","Bend","D")
 colnames(up.out)=c("k","r","d.upper","msy","Bend","D")
 kable(med.out)
 kable(low.out)
 kable(up.out)
 }
```



```
# parameters as a function of assumed upper depletion level
#name3<-paste(getwd(), "/Figuras/Fig3_Zhou2013_sensitivity.png",sep="")</pre>
#pnq(file=name3, width=900, height=1000)
layout(matrix(1:4,ncol=2,byrow=T),widths=c(1,1),heights=c(1,1))
par(mar=c(5.6,6.7,4,4),cex.axis=1.4)
plot(med.out[,3],med.out[,1]/1000,ylim=c(0,max(med.out[,1]/1000*1.3)),type='l',lwd=2,xlab='',ylab='',la
lines(low.out[,3],low.out[,1]/1000,lty=2);lines(up.out[,3],up.out[,1]/1000,lty=2)
mtext(expression(paste('K ('%*%'1000 ton)')),side=2,line=3.8,cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
plot(med.out[,3],med.out[,2],ylim=c(0,max(med.out[,2]*1.3)),type='1',lwd=2,xlab='',ylab='',las=1)
mtext('r', side=2, line=3.8, cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
lines(low.out[,3],low.out[,2],lty=2);lines(up.out[,3],up.out[,2],lty=2)
plot(med.out[,3],med.out[,4]/1000,ylim=c(0,max(med.out[,4]/1000*1.3)),type='1',lwd=2,xlab='',ylab='',la
lines(low.out[,3],low.out[,4]/1000,lty=2); lines(up.out[,3],up.out[,4]/1000,lty=2)
mtext(expression(paste('RMS ('%*%'1000 ton)')),side=2,line=3.8,cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
plot(med.out[,3],med.out[,6],ylim=c(0,max(med.out[,6]*1.5)),type='l',lwd=2,xlab='',ylab='',las=1)
lines(low.out[,3],low.out[,6],lty=2);lines(up.out[,3],up.out[,6],lty=2)
mtext("Reducción", side=2, line=3.8, cex=1.4)
mtext("Reducción superior", side=1, line=3.6, cex=1.4)
```



```
#dev.off()
# GRAFICA DIAGRAMA DE FASE
library(MASS)
K
   <- med.out[1,1]
mc.dat <-BF2msy.end
   <-tabla[3,1]/2 #BMRS
{\tt Bmrs}
Fmrs
   <-tabla[3,2]/2 #FMRS
   <-C/Bioma[3,] #F anual
Fest
Y1
   <-Fest/Fmrs;
   <-Bioma[3,]/Bmrs
X1
```

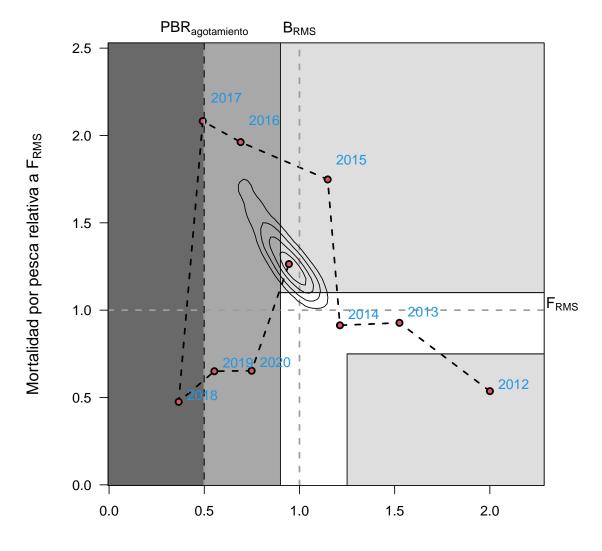
year	ВТ	Fest	B_Bo	Brel	Frel
2012	16972	0.24	1.00	2.00	0.54
2013	12940	0.41	0.76	1.53	0.93
2014	10288	0.40	0.61	1.21	0.91
2015	9743	0.77	0.57	1.15	1.75
2016	5863	0.87	0.35	0.69	1.96
2017	4176	0.92	0.25	0.49	2.08
2018	3102	0.21	0.18	0.37	0.48
2019	4692	0.29	0.28	0.55	0.65
2020	6353	0.29	0.37	0.75	0.65
2021	8014	0.56	0.47	0.94	1.26

#### kable(rbind(Bmrs,Fmrs))

Bmrs 8484.6911038 Fmrs 0.4430894

```
#library(rJava)
                                                           ## PROBLEMAS CON ESTO
#library(xlsx)
write.csv2(soli, "tabla2.csv", row.names=FALSE)
#DEFINE LAS AREAS DE LOS POLIGONOS
cols<-c("#696969","#A8A8A8","#DEDEDE")
ini < -c(-0.09);
xmax < -max(X1) * 1.35;
ymax < -max(Y1)*1.22;
xmin < -(0.08)
pol1 < -matrix(c(0.9,ini,0.9,1.1,xmax,1.1,xmax,0.75,1.25,0.75,1.25,ini),
ncol=2,byrow=T)
pol2<-matrix(c(1.25,ini,1.25,0.75,xmax,0.75,xmax,ini),ncol=2,byrow=T)
pol3<-matrix(c(xmax,1.1,xmax,ymax,0.9,ymax,0.9,1.1),ncol=2,byrow=T)</pre>
pol4<-matrix(c(0.5,ini,0.9,ini,0.9,ymax,0.5,ymax),ncol=2,byrow=T)
pol5<-matrix(c(-0.07,ini,0.5,ini,0.5,ymax,-0.07,ymax),ncol=2,byrow=T)
#name4<-paste(getwd(),"/Figuras/Fig4_Zhou2013_fase.png",sep="")</pre>
\#png(file=name4, width=1200, height=1000)
par(mar=c(6.1,6.5,4.8,4.8),cex.axis=1,cex.lab=1)
plot(X1,Y1,col=0,xlab="",ylab="",yaxt="n",xlim=c(xmin,max(X1)*1.1),
ylim=c(0.09, max(Y1)*1.17))
```

```
axis(2,las=1)
polygon(pol5,col=cols[1],border=1);polygon(pol4,col=cols[2],border=1)
polygon(pol3,col=cols[3],border=1);polygon(pol2,col=cols[3],border=1)
polygon(pol1,col="white",border="black")
#points(mc.dat[,1],mc.dat[,2],pch=21,bq="#B5B5B5",cex=0.9,col=1)
lines(X1,Y1,lty=2,col=1,lwd=2)
lines(X1,Y1,type="p",bg=2,pch=21,cex=1,lwd=2)
abline(v=1,lty=2,col=8,lwd=2); abline(h=1,lty=2,col=8,lwd=2)
abline(v=0.5, lty=2, col=8, lwd=2)
contour(z,drawlabels=FALSE,levels=c(0.1,0.25,0.5,0.75),add=TRUE)
text(0.5,max(Y1)*1.29,expression(PBR[paste("agotamiento")]),cex=1.1,
pos=1,xpd=T)
text(1,max(Y1)*1.29,expression(B[paste("RMS")]),cex=1.1,pos=1,xpd=T)
text(max(X1)*1.19,1.11,expression(F[paste("RMS")]),cex=1.1,pos=1,xpd=T)
mtext(expression(paste("Biomasa total relativa a ",B[paste("RMS")],sep="")),
side=1,line=4.2,cex=1.2)
mtext(expression(paste("Mortalidad por pesca relativa a ",F[paste("RMS")],
sep="")),side=2,line=3.8,cex=1.2)
\#a2 < -which(yr\%in\%seq(2015, 1994, by=-2) == TRUE)
a2 < -c(1,2,3,4,5,6,7,8,9)
text(X1[a2],Y1[a2]*1.06,yr[a2],cex=1,pos=4,col=4)
#text(1.10,0.83, "Plena Explotación", cex=1.6, pos=4, col=1, lwd=2)
#text(1.56,0.31, "Sub Explotación", cex=1.6, pos=4, col=1, lwd=2)
#text(1.33,1.51, "Sobrepesca", cex=1.6, pos=4, col=1, lwd=2)
#text(0.58,0.67, "Sobre", cex=1.6, pos=4, col=1, lwd=2)
#text(0.52,0.51, "Explotación", cex=1.6, pos=4, col=1, lwd=2)
#text(0.68,1.18, "Sobre-explotación y Sobrepesca", cex=1.6, pos=4, lwd=2, srt=90)
#text(0.23,1.18, "Colapso y/o Agotamiento", cex=1.6, pos=4, lwd=2, srt=90)
box()
```



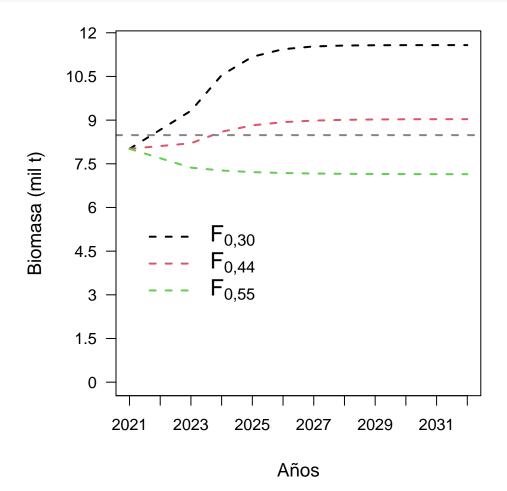
Biomasa total relativa a  $B_{\text{RMS}}$ 

#dev.off()

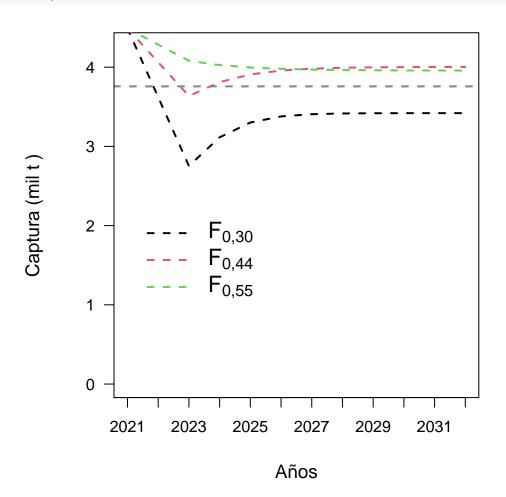
## Cálculo de CBA

```
#CALCULO DE LA CBA PARA SARDINA AUSTRAL XI
mata <-out1.backup[1:5];</pre>
   <-length(mata)
mato <-vector()</pre>
for(p in 1:mm){
 mato <-cbind(mato,mata[[p]])}</pre>
 mate <-as.data.frame(mato)</pre>
 colnames(mate)<-c("k","r","msy","Bend","Depletion")</pre>
      <-length(yr)
уу
prob
      <-c(0.6666667,1.00,1.25) # pnderadores de Frms
      <-dim(sp)
yrs_pro <-seq(yr[yy],yr[yy]+11,by=1) # años de proyección
      <-length(yrs_pro)
уур
BT=CT=array(NA,c(length(prob),ss[1],length(yrs_pro)))
BT[,,1] \leftarrow Bioma[3,yy]
CT[,,1] \leftarrow C[yy]
Fi
      <-Fmrs*prob
# y = Frms ponderados
\# n = n\'umero de simulaciones
# m = años de proyección
for(y in 1:length(Fi)){
for(n in 1:ss[1]){
 ki=sp$k[n] # parámetro K simulado
 ri=sp$r[n] # parámetro r simulado
 for(m in 1:(yyp-1)){ # PROYECCIÓN
  if(m==1){
    CT[y,,1]=C[yy]} # igual a la captura del último año
    CT[y,n,m]=BT[y,n,m]*Fi[y]} # captura proyectada
    BT[y,n,m+1] = BT[y,n,m] + ri*BT[y,n,m]*(1-BT[y,n,m]/ki) - CT[y,n,m] * biomasa total proyectada
  if(m==(yyp-1)){
    CT[y,n,m+1] = BT[y,n,m+1] *Fi[y]
 }
}
}
# GRAFICA LA CBA 2 PARA sardina austral
FF
    <-formatC(Fi,format="f",digits=2)
    <-expression(paste("Biomasa (mil t)",sep=""))</pre>
Binf <-tabla[2,1]/2
Bsup -tabla[4,1]/2
rng1 <-range(BT[,,],na.rm=T)</pre>
```

```
ax2 <-seq(0,rng1[2]*1.15,by=1500)
cols <-"#858585"
                    <-length(yrs_pro)
y1
xxxx<-matrix(ncol=3,nrow=11)</pre>
par(mar=c(5,5,1,1),cex.axis=1,cex.lab=1)
plot(yrs_pro[-2],seq(0,rng1[2]*1.15,le=(y1-1)),col=0,type="o",xlab="",ylab="",yaxt="n",ylim=c(0,rng1[2]
for(x in 1:length(Fi)){
       xxxx[,x] \leftarrow apply(BT[x,,],2,quantile)[3,-2]
   lines(yrs_pro[-2],xxxx[,x],col=x,lty=2,lwd=2)
abline(h=Bmrs,lty=2,lwd=2,col=cols)
axis(2,at=ax2,labels=ax2/1000,las=1,cex=1)
mtext(BB,side=2,line=3.5,cex=1.2)
mtext("Años",side=1,line=3.4,cex=1.2)
legend(2021,rng1[2]*0.5,c(expression(F[paste("0,30")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[paste("0,44")]),expression(F[past
expression(F[paste("0,55")])),lty=c(2,2,2,2,2),lwd=c(2,2,2,2,2),cex=1.4,
col=c(1,2,3),bty="n")
```



```
CC
                  <-expression(paste("Captura (mil t )",sep=""))</pre>
MRS <-tabla[3,3] #50%
rng2 <-range(CT[,,],na.rm=T)</pre>
ax3 <-seq(0,rng2[2]*1.15,by=1000)
xxxx<-matrix(ncol=3,nrow=11)</pre>
par(mar=c(5,5,1,1),cex.axis=1,cex.lab=1)
plot(yrs_pro[-2],seq(0,rng2[2]*1.15,le=11),col=0,type="o",xlab="",ylab="",yaxt="n",ylim=c(0,rng2[2]*0.9
for(x in 1:length(Fi)){
       xxxx[,x] \leftarrow apply(CT[x,,],2,quantile)[3,-2]
   lines(yrs_pro[-2],xxxx[,x],col=x,lty=2,lwd=2)
abline(h=MRS,lty=2,lwd=2,col=cols)
axis(2,at=ax3,labels=sprintf("%0.0f",ax3/1000),las=1,cex=1.4)
mtext(CC, side=2, line=3.5, cex=1.2)
mtext("Años",side=1,line=3.4,cex=1.2)
legend(2021, rng2[2]*0.5, c(expression(F[paste("0,30")]), expression(F[paste("0,44")]), expres
expression(F[paste("0,55")])),lty=c(2,2,2,2,2),lwd=c(2,2,2,2,2),cex=1.4,
col=c(1,2,3),bty="n")
```



```
# TABLA DE RESULTADOS CAPTURA 2021
ct<-matrix(NA,length(Fi),5)
for(i in 1:length(Fi)){
ct[i,]<-as.numeric(quantile(CT[i,,2],probs=c(.1,.2,.3,.4,.5))) # CT[i,,2] (el 2 representa 1 año de p
colnames(ct)<-c("10%","20%","30%","40%","50%")</pre>
rownames(ct)<-formatC(Fi,format="f",digits=2)</pre>
cat("\n")
print(ct)
               20%
                     30%
         10%
## 0.30 2209.873 2213.901 2222.323 2226.953 2231.200
## 0.44 3314.810 3320.851 3333.484 3340.430 3346.799
## 0.55 4143.512 4151.063 4166.855 4175.537 4183.499
# TABLA DE RESULTADOS biomasa 2021
bt <-matrix(NA,length(Fi),5)
for(i in 1:length(Fi)){
bt[i,]<-as.numeric(quantile(BT[i,,2],probs=c(.1,.2,.3,.4,.5))) # CT[i,,2] (el 2 representa 1 año de p
colnames(bt)<-c("10%","20%","30%","40%","50%")
rownames(bt)<-formatC(Fi,format="f",digits=2)</pre>
cat("\n")
print(bt)
year < -seq(2012, 2021)
bioHil<-c(NA,17712,12394,11186,6911,5161,4212,6108,7933,8592)
par(mar=c(5,5,1,1),cex.axis=1,cex.lab=1)
plot(year,c(soli[,2],bt[2,5]),type="o",pch=19,ylim=c(0,20000), xaxp=c(2012,2022,10),ylab="Biomasa total
lines(year,bioHil,type="o",col=2,pch=19)
legend(2017,16000,c("Hilborn y Mangel 1997","Zhou 2013"),
    bty="n", lwd=1, pch=19, col=c(2,1), title="Método de estimación")
# RANGO CBA PARA PBR Al MRS (2) y EL 2021(2)
rango<-quantile(CT[2,,2],prob=c(0.025,0.25,0.50,0.75,0.975))
kable(rango)
                                    x
```

	2
2.5%	3297.362
25%	3328.960
50%	3346.799
75%	3366.987
97.5%	3396.586

#

#FIN