

1. Consider the function $f(x) = x^3 - 5x + 8$ over the interval $[0, 4]$.
 - (a) Approximate the area between the x-axis and $f(x)$ with $n = 4$ rectangles using the right, left, and midpoint of subintervals.
 - (b) Find the area between the x-axis and $f(x)$ using integration.
 - (c) Which approximation from (a) is closest to the true value (b)?
2. Find $f(x)$ for each of the following:
 - (a) $f'(x) = 12x^3 - 15x^2 + 10$ and $f(-1) = 8$
 - (b) $f'(x) = 6e^x - 4 - 10x$ and $f(0) = -6$
 - (c) $f''(x) = 60x^4 - 60x^2$ and $f(-1) = 14$ and $f'(1) = 6$
3. If possible, integrate the following functions
 - (a) $\int_{-1}^4 (x - 2)e^{x^2 - 4x} dx$
 - (b) $\int_1^4 \frac{1}{2x-6} dx$
 - (c) $\int \frac{\sin(1+\ln(2x)) - \sqrt{1+\ln(2x)}}{x} dx$
 - (d) $\int_{-\infty}^0 xe^{2+3x} dx$
 - (e) $\int_0^\pi 2x^2 \cos(x) dx$
 - (f) $\int_{-\infty}^0 \cos(x) dx$
 - (g) $\int_0^6 |10 - 2x| dx$