

1. Evaluate the following limits.

(a) $\lim_{(x,y) \rightarrow (0,0)} \frac{2x^2+7y^2}{4y^2+x^2}$

(b) $\lim_{(x,y,z) \rightarrow (2,1,0)} \frac{(4y-z^3)e^{3x-6}}{4z-yx^2}$

2. Find all first and second order partial derivatives for the following functions.

(a) $f(x, y) = x^4y^{-2} - 4xy + e^{7y} + \ln(2x)$

(b) $f(u, v, w) = u^4 \sin(w^2) - \frac{2v}{u^4} + \ln(v^2w)$

3. Given the following information use the Chain Rule to determine $\frac{\partial z}{\partial u}$ and $\frac{\partial z}{\partial v}$.

$$z = x \sin(y^2 - x), x = 3u - v^2, y = u^6$$

4. Find and classify all the critical points of the function $f(x, y) = xye^{-8(x^2+y^2)}$.

5. Find the absolute minimum and maximum of $f(x, y) = 18x^2 + 4y^2 - y^3x - 2$ on the triangle with the vertices $(-1, -1)$, $(5, -1)$, and $(5, 17)$.

6. Find the maximum and minimum values of $f(x, y, z) = xyz$ subject to the constraint $x^2 + 2y^2 + 4z^2 = 24$