

1. Find the following limits. Show your work.

(a) $\lim_{x \rightarrow 1} \sqrt{x^2 - x + 1}$

(b) $\lim_{x \rightarrow 0^+} \frac{|x|}{x}$

(c) $\lim_{x \rightarrow 0} \frac{\sin(x^2)}{x}$

2. Are the following functions continuous? Justify your response.

(a) $x^4 + 2x^2 + 5$ over \mathbb{R}

(b) $\frac{1}{1+x}$ on the interval $[0, 2]$

(c) $\frac{1}{1+x}$ on the interval $(1, 2]$

(d) $\frac{|2x+3|}{2x+3}$ over \mathbb{R}

3. Find the derivative of $f(x) = 6x^2 + x - 10$ using the formal definition of the derivative.

4. Find the derivative of the functions. Show your work.

(a) $f(x) = \frac{1}{x^{2/3}}$

(b) $f(x) = e^{x^2+1} + x \log(x+3)$

(c) $f(x) = \frac{x+1}{x^2+2x+5}$

5. Find the maximum and minimum points of $f(x)$ on the interval $[-2, -1/4]$.

$$f(x) = \frac{(x-1)^3}{x}$$

(Hint: The roots of the polynomial $2x^3 - 3x^2 + 1$ are 1 and $-1/2$.)