		pe by the whole foo least number of fee	ent Mathematics Lead ot. If a landscaper et she must purcha C. 56 feet	needs a rope at le ase? Use 1 inch =	2.54 cm.		
	2. Let $A = \{1, 2, 3, 4\}$. Let $M =$ the number of distinct proper subsets of A . Let $N =$ the number of distinct differences that can be found by subtracting two distinct elements of A (for example, 1 would be one such difference since $3 - 2 = 1$). Find $M + N$. A. 18 B. 19 C. 21 D. 22 E. 23						
	smaller denomina	ations) a \$50 bill if		ited number of \$2	ollar amount in 20, \$10, \$5, and \$1 e indistinguishable. E. 61		
	4. An isosceles triangle has two sides of length 40 and a base of length 48. A circle circumscribes the triangle. What is the radius of the circle?						
	A. $20\sqrt{2}$	B. 28	C. $18\sqrt{3}$	D. $12\sqrt{5}$	E. 25		
	5. Let M be the number of digits $\{0, 1\}$ required to express the largest prime factor of 2019 in base 2. Let N be the number of hex digits $\{0, 1, 2, E, F\}$ required to express 2019 in base 16. Find $M - N$.						
	A. 7	B. 6	C. 5	D. 4	E. 3		
6. Triangle ABC has vertices at (8,8), (6,4), and (10, 7). Find the sum of the lengths of three altitudes of this triangle, rounded to the nearest tenth. A. 8.7 B. 8.9 C. 9.2 D. 9.5 E. 9.7							
			is divisible by x + non-real roots of th C. 0		ntegers with E. 1		
	8. Let N be the smallest integer greater than 2 such that N^{N-1} is not the square of an integer. Find the product of all rational numbers that could be roots of $5x^4 + bx^3 + cx^2 + dx + N$, where b , c , and d can be any integers. Round your answer to the nearest hundredth. A. 0 B. 2.07 C. 3.14 D. 4.30 E. 6.22						
	Three people (X, Y, Z) are in a room with you. One is a knight (knights always tell the ruth), one is a knave (knaves always lie), and the other is a spy (spies may either lie or tell he truth). X says "I am a spy." Y says "X is telling the truth." Z says "I am not a spy." Which of the following correctly identifies all three people?						
	A. X is the spy.	B. X is the spy.	C. X is the knight.	D. X is the knight.	E. X is the knave.		
	Y is the knight. Z is the knave.	Y is the knave. Z is the knight.	Y is the knave. Z is the spy.	Y is the spy. Z is the knave.	Y is the spy. Z is the knight.		
	five-character cod However, it was k than the others, a	le five different tim nown that each er and no transmissic	es, but only one of roneous transmiss on had five errors.	the five transmission had a differen The first transmissionellisted below. With	attempted to send a sions was correct. t number of errors sion was • — — • —, hich one is correct? apossible to determine		

Test #2 AMATYC Student Mathematics League Winter/Spring 11. A checker is placed on a 5×5 checkerboard as pictured. The checker may be moved one square at a time but only to the left or down. Also, the checker may not move to any of the three black squares. In how many different ways can the checker be moved to the lower left corner of the board? A. 7 B. 8 C. 9 D. 10 E. 12							
12. The function $P(t) = \cos(8t)$ can be written as sums and differences of powers of cos only. When $P(t)$ is written this way, what is the coefficient of $(\cos t)^3$?							
A2	B1	C. 0	D. 1	E. 2			
through (7, 8) tha	at is parallel to the	ine segment with o vector <3, -4> and nd your answer to C. 10.0	the other endpoin	nt on the circle with			
A. 2319	B. 2540	with $a^2 + b^2 = 2019$ C. 2711	D. 2719	E. 2811 x = 6y = 8z = 15			
15. Which describ	bes the graph (in ${\mathbb R}$	(3) of all solutions o	of this system? $\begin{cases} -8 \\ x \end{cases}$	x - 6y - 6z = 15 $x - 8y + 6z = -65$ $- 19y - 17z = 5$			
A. A point	B. A line	C. Two lines	D. A plane	E. Two planes			
	n equilateral trians	s symmetric about gle. If the maximu C. 3/4					
17. How many of $g(x) = \ln(e^x)$, $h(x)$ $r(x) = \frac{x}{ x +1}$.	$f(x) = \arctan(x),$						
A. 2	B. 3	C. 4	D. 5	E. 6			
18. Let $\{a_n\}$ be an arithmetic sequence with initial value m and common difference d . Let $\{g_n\}$ be a geometric sequence with initial value k and common ratio 2 . The sum of the first 100 terms of $\{a_n\}$ and the sum of the first 10 terms of $\{g_n\}$ are equal. If m , d , and k are all positive integers, which of the following numbers must divide m ? A. 2 B. 5 C. 17 D. 31 E. 33							
same path back t	o where they bega	t noon. At some pon, and arrive there 6 mi/hr downhill. C. 28 D. 24	at 8:00 p.m. Their How many miles				
20. In the game of craps, a player (known as the shooter) rolls two fair six-sided dice. The shooter immediately loses if the sum of the dice is 2, 3, or 12 and immediately wins if the sum of the dice is 7 or 11 on the first roll. If the sum is anything else (4, 5, 6, 8, 9, or 10), that number becomes the <i>point</i> and the shooter rolls again. The shooter now wins by rolling that same point again and loses by rolling a 7. If any other number is rolled, the shooter rolls again and keeps rolling until the shooter wins by rolling the point or loses by rolling a Find the probability that the shooter wins. A. 17/36 B. 187/385 C. 244/495 D. 107/216 E. 647/1296							