Examples: Transformations for ANOVA models

Sleuth3 Sections 3.5 and 5.5

Example: Cloud Seeding (Sleuth3 Case Study 3.1.1)

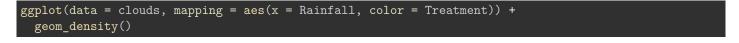
Quote from book: "On each of 52 days that were deemed suitable for cloud seeding, a random mechanism was used to decide whether to seed the target cloud on that day or to leave it unseeded as a control. ... [P]recipitation was measured as the total rain volume falling from the cloud base following the airplane seeding run."

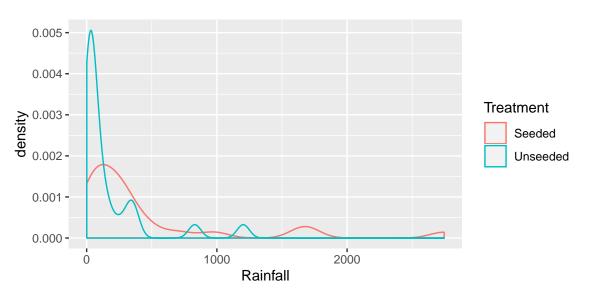
```
clouds <- read_csv("http://www.evanlray.com/data/sleuth3/case0301_cloud_seeding.csv")
head(clouds, 4)</pre>
```

```
## # A tibble: 4 x 2
## Rainfall Treatment
## <dbl> <chr>
## 1 1203. Unseeded
## 2 830. Unseeded
## 3 372. Unseeded
## 4 346. Unseeded
```

Starting Point

Here are density plots and box plots, separately for each Treatment.





Standard deviations for each group:

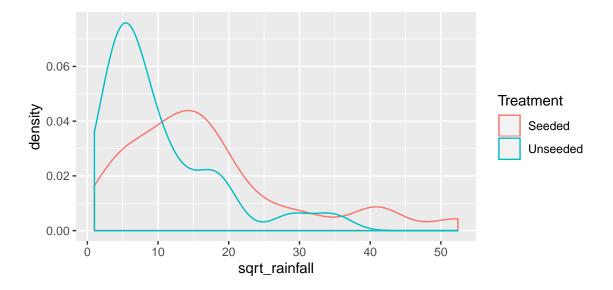
```
clouds %>%
  group_by(Treatment) %>%
  summarize(
    sd_rainfall = sd(Rainfall)
)
```

The standard deviations are very different, and the distributions are skewed right, so move down one step on the ladder.

Down 1 Step: $\sqrt{Rainfall}$

```
clouds <- clouds %>%
  mutate(
    sqrt_rainfall = sqrt(Rainfall)
)
```

```
ggplot(data = clouds, mapping = aes(x = sqrt_rainfall, color = Treatment)) +
  geom_density()
```



```
clouds %>%
  group_by(Treatment) %>%
  summarize(
   sd_rainfall = sd(sqrt_rainfall)
)
```

These distributions are closer to symmetric – probably good enough.

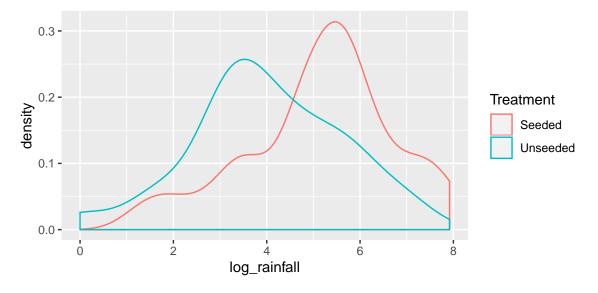
The ratio of these standard deviations is less than 2 – often used as a guide for when we're OK.

However, we can make it even better if we go down another step.

Down 2 Steps: $\log(Rainfall)$

```
clouds <- clouds %>%
  mutate(
    log_rainfall = log(Rainfall)
)
```

```
ggplot(data = clouds, mapping = aes(x = log_rainfall, color = Treatment)) +
  geom_density()
```



```
clouds %>%
  group_by(Treatment) %>%
  summarize(
   sd_rainfall = sd(log_rainfall)
)
```

Good enough! We can conduct our analysis on this scale.

Analysis on transformed scale

```
clouds %>%
  group_by(Treatment) %>%
  summarize(
    mean_log_rainfall = mean(log_rainfall)
## # A tibble: 2 x 2
##
     Treatment mean_log_rainfall
##
     <chr>
                           <dbl>
                            5.13
## 1 Seeded
## 2 Unseeded
                            3.99
rainfall_fit <- lm(log_rainfall ~ Treatment, data = clouds)</pre>
summary(rainfall_fit)
##
## Call:
## lm(formula = log_rainfall ~ Treatment, data = clouds)
## Residuals:
##
       Min
                1Q Median
                                3Q
## -3.9904 -0.7453 0.1624 1.0187 3.1018
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                       5.1342
                                 0.3179 16.152 <2e-16 ***
## (Intercept)
## TreatmentUnseeded -1.1438
                                  0.4495 - 2.544
                                                   0.0141 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.621 on 50 degrees of freedom
## Multiple R-squared: 0.1146, Adjusted R-squared: 0.09693
## F-statistic: 6.474 on 1 and 50 DF, p-value: 0.01408
confint(rainfall_fit)
##
                         2.5 %
                                  97.5 %
## (Intercept)
                      4.495729 5.772645
## TreatmentUnseeded -2.046697 -0.240865
library(gmodels)
fit.contrast(rainfall_fit, "Treatment", c(1, -1), conf.int = 0.95)
##
                        Estimate Std. Error t value
                                                       Pr(>|t|) lower CI
## Treatment c=( 1 -1 ) 1.143781 0.4495342 2.544369 0.01408266 0.240865
                        upper CI
## Treatment c=( 1 -1 ) 2.046697
## attr(,"class")
## [1] "fit_contrast"
```

We can interpret these numbers either on the new, transformed, data scale or on the original data scale.

. Interpret the group mean estimates above on the original data scale (works if we got to a place where istributions were approximately symmetric after transformation!):
xp(5.13)
[1] 169.0171
xp(3.99)
[1] 54.05489

1. Interpret the group mean estimates above on the transformed scale (always works!):

3. Interpret the estimated difference in means above on the transformed scale (always works!):	
4. Interpret the estimted difference in means above on the original data scale (works only if the transfer	ır_
mation selected was the log transformation and the resulting distribution was approximately symmetric	
exp(1.143781)	
## [1] 3.138613	
exp(0.240865)	
## [1] 1.272349	
exp(2.046697)	
## [1] 7.742286	
## [1] 7.742286	
## [1] 7.742286	
## [1] 7.742286	