Model that works

January 12, 2022

Chemical Equation

$$CO \frac{k_{OA}}{\overleftarrow{k_{AO}}} CO^{A} \frac{k_{AB}}{\overleftarrow{k_{BA}}} CO^{B} \frac{k_{BO}}{\overleftarrow{k_{OB}}} CO$$
 (1)

Reaction Rate Equations

Region I

$$\frac{\partial \theta_{\tau}^{B}}{\partial \tau} = -k_{BO}\theta_{\tau}^{B} + k_{OB}P(M^{B} - \theta_{\tau}^{B}) \tag{2}$$

$$\frac{\partial \theta_{\tau}^{A}}{\partial \tau} = 0 \tag{3}$$

Region II

$$\frac{\partial \theta_{\tau}^{B}}{\partial \tau} = -k_{BA} P \theta_{\tau}^{B} + k_{AB} \theta_{\tau}^{A} (M - \theta_{\tau}^{X}) \tag{4}$$

$$\frac{\partial \theta_{\tau}^{A}}{\partial \tau} = k_{OA} P(M - \theta_{\tau}^{X}) - k_{AO} \theta_{\tau}^{A} - k_{AB} \theta_{\tau}^{A} (M - \theta_{\tau}^{X}) + k_{BA} P \theta_{\tau}^{B}$$

$$\tag{5}$$

Region III

$$\frac{\partial \theta_{\tau}^{B}}{\partial \tau} = k_{AB} \theta_{\tau}^{A} (M - \theta_{\tau}^{X}) \tag{6}$$

$$\frac{\partial \theta_{\tau}^{A}}{\partial \tau} = -k_{AO}\theta_{\tau}^{A} - k_{AB}\theta_{\tau}^{A}(M - \theta_{\tau}^{X}) \tag{7}$$

Region IV

$$\frac{\partial \theta_{\tau}^{B}}{\partial \tau} = -k_{BO} \theta_{\tau}^{B} \tag{8}$$

$$\frac{\partial \theta_{\tau}^{A}}{\partial \tau} = 0 \tag{9}$$

Relations

$$\begin{aligned} \theta_{\tau}^{A} + \theta_{\tau}^{B} &= \theta_{\tau}^{X} \\ 0.5X_{\tau}^{A} + 0.33X_{\tau}^{B} &= \theta_{\tau}^{X} \\ X_{\tau}^{A} + X_{\tau}^{B} &= 1. \end{aligned} \tag{10}$$

Equations used for fitting

Region I

Fitting B

$$\theta_{\tau+1}^B = [1 - k_{BO}\Delta\tau]\,\theta_{\tau}^B + k_{OB}P\Delta\tau(M - \theta_{\tau}^X) \tag{11}$$

Fitting A

$$\theta_{\tau+1}^A = 0 \tag{12}$$

Region II

Fitting B

$$\theta_{\tau+1}^B = \left[1 - k_{BA} P \Delta \tau\right] \theta_{\tau}^B + k_{AB} \Delta \tau \theta_{\tau}^A (M - \theta_{\tau}^X) \tag{13}$$

Fitting A

$$\theta_{\tau+1}^A = \left[1 - k_{AO}\Delta\tau - k_{AB}\Delta\tau(M - \theta_{\tau}^X)\right]\theta_{\tau}^A + k_{BA}P\Delta\tau\theta_{\tau}^B + k_{OA}\Delta\tau P(M - \theta_{\tau}^X) \tag{14}$$

Region III

Fitting B

$$\theta_{\tau+1}^B = \theta_{\tau}^B + k_{AB} \Delta \tau \theta_{\tau}^A (M - \theta_{\tau}^X) \tag{15}$$

Fitting A

$$\theta_{\tau+1}^{A} = \left[1 - k_{AO}\Delta\tau - k_{AB}\Delta\tau(M - \theta_{\tau}^{X})\right]\theta_{\tau}^{A} \tag{16}$$

Region IV

Fitting B

$$\theta_{\tau+1}^B = \left[1 - k_{BO} \Delta \tau\right] \theta_{\tau}^B \tag{17}$$

Fitting A

$$\theta_{\tau+1}^A = 0 \tag{18}$$

Get
$$k_{BO}$$
 from

$$ln(\frac{\theta_{\tau}^{B}}{\theta_{0}^{B}}) = -k_{BO}\tau \tag{19}$$

Get
$$k_{OB}$$
 from

$$\theta_{\tau+1}^{B} - (1 - k_{BO})\theta_{\tau}^{B} = k_{OB}\Delta\tau P(M - \theta_{\tau}^{X})$$
(20)

Get
$$k_{AB}$$
 from

$$\theta_{\tau+1}^B - \theta_{\tau}^B = k_{AB} \Delta \tau \theta_{\tau}^A (M - \theta_{\tau}^X) \tag{21}$$

Get
$$k_{AO}$$
 from

$$\theta_{\tau+1}^A - (1 - k_{AB}\Delta\tau(M - \theta_{\tau}^X))\theta_{\tau}^A = -k_{AO}\Delta\tau\theta_{\tau}^A$$
(22)

Get
$$k_{BA}$$
 from

$$\theta_{\tau+1}^B - \theta_{\tau}^B - k_{AB}\Delta \tau \theta_{\tau}^A (M - \theta_{\tau}^X) = -k_{BA}\Delta \tau P \theta_{\tau}^B$$
(23)

Get
$$k_{OA}$$
 from

$$\theta_{\tau+1}^X - \theta_{\tau}^X + k_{AO}\Delta \tau \theta_{\tau}^A = -k_{OA}\Delta \tau P(M - \theta_{\tau}^X)$$
(24)

Results

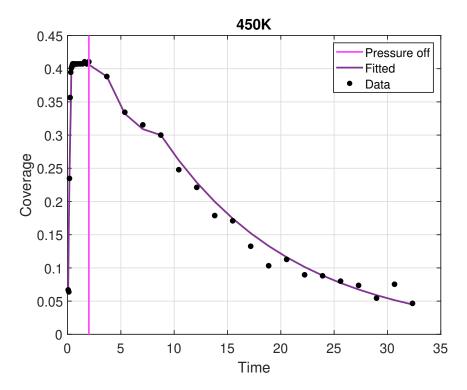


Figure 1: Overall 450K

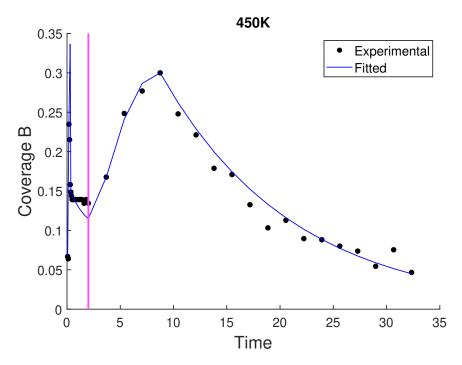


Figure 2: State B 450K

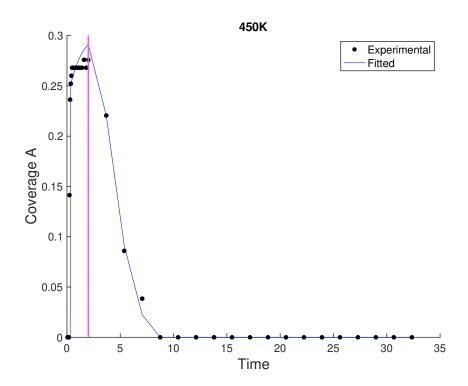


Figure 3: State A 450K

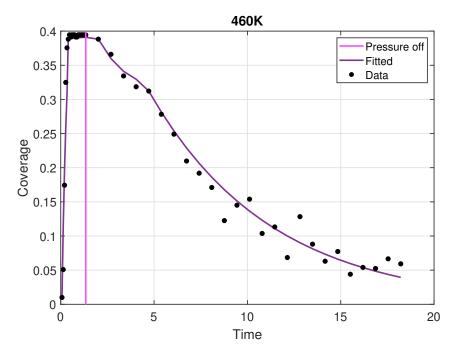


Figure 4: Overall 460K

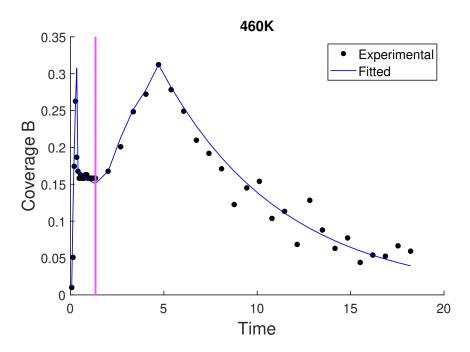


Figure 5: State B 460K

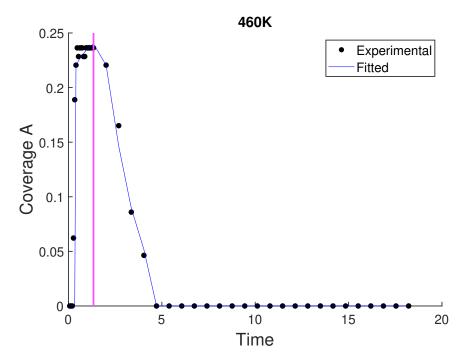


Figure 6: State A 460K

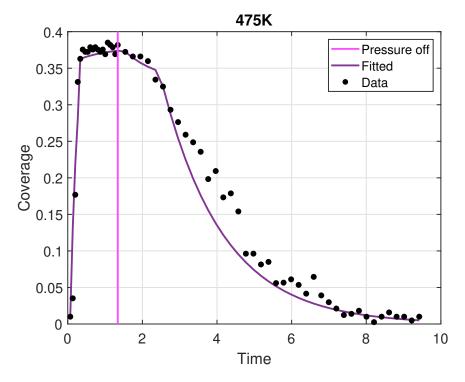


Figure 7: Overall 475K

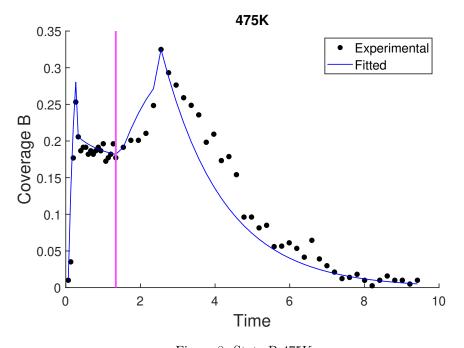


Figure 8: State B 475K

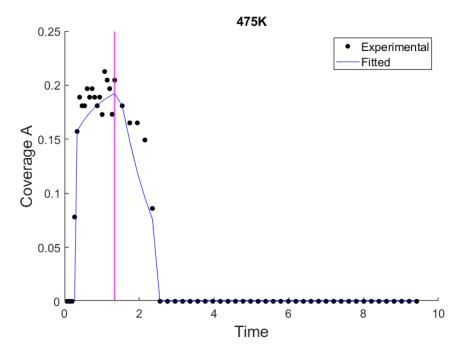


Figure 9: State A 475K

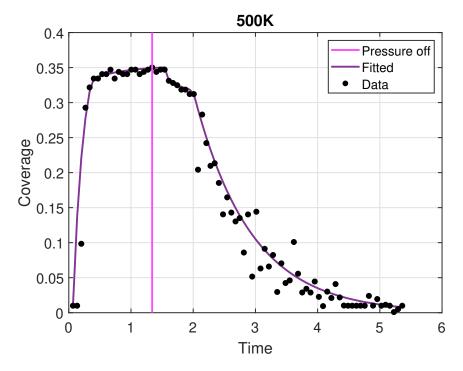


Figure 10: Overall 500K

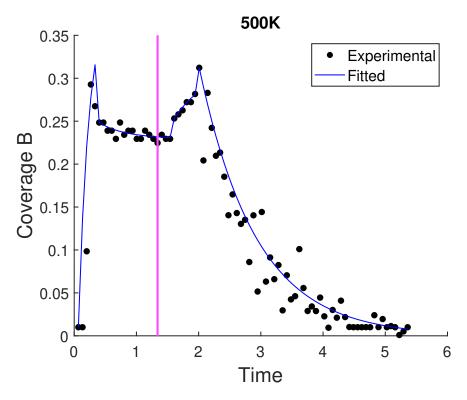


Figure 11: State B $500\mathrm{K}$

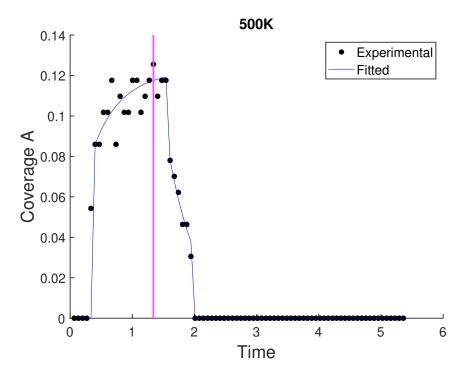


Figure 12: State A 500K