

$$r_i = (1-u) \cdot p_i + u \cdot p_{i+1}$$

$$s_i = (1-u) r_i + u r_{i+1}$$

$$t_0 = (1-u) s_0 + u s_1$$

$$t_0 = (1-u) s_0 + u s_1$$

$$= (1-u) ((1-u) r_0 + u r_1) + u ((1-u) r_1 + u r_2)$$

$$= (1-u)^2 r_0 + u(1-u) r_1 + u(1-u) r_1 + u^2 r_2$$

$$= (1-u)^2 r_0 + 2u(1-u) r_1 + u^2 r_2$$

$$= (1-u)^2 ((1-u) p_0 + u p_1) + 2u(1-u) ((1-u) p_1 + u p_2) + u^2 ((1-u) p_2 + u p_3)$$

$$= (1-u)^3 p_0 + \underline{u(1-u)^2 p_1} + \underline{2u(1-u)^2 p_1} + \underline{2u^2(1-u) p_2} + \underline{u^2(1-u) p_2} + \underline{u^3 p_3}$$

$$= (1-u)^3 p_0 + 3u(1-u)^2 p_1 + 3u(1-u)^2 p_2 + u^3 p_3$$

Bézierov spline

stupňa 3

$$f(u) = B_0(u) p_0 + B_1(u) p_1 + B_2(u) p_2 + B_3(u) p_3$$

Bernstein polinomi - baza f-je

$$B_i(u) = \binom{3}{i} u^i (1-u)^{3-i}$$

$$B_0(u) = \binom{3}{0} u^0 (1-u)^3 = (1-u)^3$$

$$B_1(u) = \binom{3}{1} u^1 (1-u)^2 = 3u(1-u)^2$$

$$B_2(u) = \binom{3}{2} u^2 (1-u) = 3u^2(1-u)$$

$$B_3(u) = \binom{3}{3} u^3 (1-u)^0 = u^3$$

$$\binom{n}{m} = \frac{n!}{m!(n-m)!}$$

$$f(u) = (1-u)^3 p_0 + 3u(1-u)^2 p_1 + 3u^2(1-u) p_2 + u^3 p_3 = t_0$$