Lab 7

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#Rcpp

We will get some experience with speeding up R code using C++ via the Rcpp package.

First, clear the workspace and load the Rcpp package.

```
#TO-DO
pacman::p_load(Rcpp)
```

Create a variable n to be 10 and a vaiable Nvec to be 100 initially. Create a random vector via rnorm Nvec times and load it into a Nvec x n dimensional matrix.

```
#TO-DO
n = 10
Nvec = 100
X = matrix(data = rnorm(Nvec*n), nrow = 100)
head(X)
```

```
##
              [,1]
                          [,2]
                                     [,3]
                                                [,4]
                                                            [,5]
                                                                       [,6]
## [1,] -0.6834808 -1.30457911 -1.0278770 -0.7091122 -0.3588667 -0.7938312
## [2,] -0.2854185   0.77254482 -1.2683973 -0.3131827 -1.5579927
## [3,] -0.2127186  0.90092019  0.2513183
                                           0.2243160 -0.5437677
## [4,]
        0.2286666 -0.06374408 -1.4474031
                                          1.5733885 0.6660421 -1.1475801
## [5,] -0.1129078 -0.02359415 -0.4901920 -1.7845102 -1.2944602 -0.5739799
##
  [6,]
        0.2658279
                   0.64257442 1.3475198
                                          1.6892505
                                                      0.2358499 -0.2848843
                                    [,9]
##
              [,7]
                         [,8]
                                               [,10]
## [1,]
        0.8783623 -0.5184424 -0.9983798 -0.25648178
## [2,] -0.7699091 -0.2612830 0.4721700 0.39094697
## [3,] -1.3085383 0.7536592
                              0.3977048 -1.11754252
## [4,]
        0.6828859 -0.9714645
                               2.4128410 -0.43675636
## [5,]
         0.8651046 2.4481522 0.9933471 -0.40332703
## [6,]
         2.0007758
                   0.9188241
                               0.3941356 -0.08542126
```

Write a function all_angles that measures the angle between each of the pairs of vectors. You should measure the vector on a scale of 0 to 180 degrees with negative angles coerced to be positive.

```
#TO-DO
angle = function(u,v){
  acos(sum(u*v)/sqrt(sum(u^2)*sum(v^2)))*(180/pi)
}
```

```
all_angles = function(X){
    A = matrix(NA, nrow=nrow(X), ncol=nrow(X))
    for(i in 1:(nrow(X)-1)){
        for(j in (i+1):nrow(X)){
            A[i,j] = angle(X[i,],X[j,])
        }
    }
}
all_angles(X)
```

##		[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]
##	[1,]	NA	92.96163	126.14924	91.33681	81.41249	108.04412	101.50051	89.30027
##	[2,]	NA	NA	66.14781	88.90066	78.21263	119.86235	130.65064	85.92698
##	[3,]	NA	NA	NA	104.77015	86.03254	96.71089	106.26462	98.34278
##	[4,]	NA	NA	NA	NA	96.51874	77.04727	102.32236	111.46164
##	[5,]	NA	NA	NA	NA	NA	87.33802	112.38187	112.04775
##	[6,]	NA	NA	NA	NA	NA	NA	82.00564	103.00972
##	[7,]	NA	NA	NA	NA	NA	NA	NA	63.86235
##	[8,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[9,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[10,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[11,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[12,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[13,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[14,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[15,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[16,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[17,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[18,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[19,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[20,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[21,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[22,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[23,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[24,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[25,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[26,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[27,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[28,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[29,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[30,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[31,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[32,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[33,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[34,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[35,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[36,]	NA	NA	NA	NA	NA	NA NA	NA	NA NA
##	[37,]	NA	NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[38,]	NA	NA	NA NA	NA	NA NA	NA NA	NA NA	NA NA
##	[39,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[40,]	NA	NA	NA NA	NA	NA NA	NA NA	NA NA	NA NA
##	[41,]	NA	NA	NA	NA	NA	NA	NA	NA

##	[42,]	NA							
##	[43,]	NA							
##	[44,]	NA							
##	[45,]	NA							
##	[46,]	NA							
##	[47,]	NA							
##	[48,]	NA							
##	[49,]	NA							
##	[50,]	NA							
##	[51,]	NA							
##	[52,]	NA							
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##	[62,]	NA							
##	[63,]	NA							
##	[64,]	NA							
##	[65,]	NA							
##	[66,]	NA							
##	[67,]	NA							
##	[68,]	NA	NA	NA NA	NA NA	NA NA	NA	NA	NA NA
##	[69,]	NA							
##	[70,]	NA	NA	NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[71,]	NA	NA	NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[72,]	NA	NA	NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[73,]	NA	NA NA						
##	[74,]	NA	NA NA						
##	[75,]			NA NA					NA NA
	[76,]	NA NA							
## ##	[77,]		NA NA		NA NA	NA NA	NA NA	NA NA	NA NA
	[78,]	NA NA							
##		NA NA							
##	[79,]	NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA	NA
##	[80,]	NA	NA NA	NA	NA	NA	NA	NA	NA NA
##	[81,]	NA							
##	[82,]	NA							
##	[83,]	NA							
##	[84,]	NA							
##	[85,]	NA							
##	[86,]	NA							
##	[87,]	NA							
##	[88,]	NA							
##	[89,]	NA							
##	[90,]	NA							
##	[91,]	NA							
##	[92,]	NA							
##	[93,]	NA							
##	[94,]	NA							
##	[95,]	NA							

##	[96,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[97,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[98,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[99,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[100,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[100,]	[,9]	[,10]	[,11]	[,12]	[,13]	[,14]	[,15]	
##	[1,]		128.16096	96.33568			90.36160		
##	[2,]		81.97685				73.44154		
##	[3,]		61.06160		104.52283				
##	[4,]						107.72862		
##	[5,]		81.40243						
##	[6,]		101.72663						
##	[7,]						100.13227		
##	[8,]		101.91719			115.58430		106.86387	
##	[9,]		101.56552	64.38433				109.64924	
##	[10,]	NA	NA	73.94297				91.38220	
##	[11,]	NA	NA	NA					
##	[12,]	NA	NA	NA	NA	94.96438		100.96035	
##	[13,]	NA	NA	NA	NA	NA	77.66984	80.12661	
##	[14,]	NA	NA	NA	NA	NA	NA	80.71216	
##	[15,]	NA	NA	NA	NA	NA	NA	NA	
##	[16,]	NA	NA	NA	NA	NA	NA	NA	
##	[17,]	NA	NA	NA	NA	NA	NA	NA	
##	[18,]	NA	NA	NA	NA	NA	NA	NA	
##	[19,]	NA	NA	NA	NA	NA	NA	NA	
##	[20,]	NA	NA	NA	NA	NA		NA	
##	[21,]	NA	NA	NA		NA		NA	
##	[22,]	NA	NA	NA		NA		NA	
##	[23,]	NA	NA	NA		NA		NA	
##	[24,]	NA	NA	NA		NA		NA	
##	[25,]	NA	NA	NA		NA		NA	
##	[26,]	NA	NA	NA		NA		NA	
##	[27,]	NA NA	NA NA	NA		NA		NA NA	
## ##	[28,]	NA NA	NA NA	NA NA		NA NA		NA NA	
##	[29,] [30,]	NA NA	NA NA	NA NA	NA NA	NA NA		NA NA	
##	[31,]	NA NA	NA NA	NA NA	NA NA	NA NA		NA NA	
##	[32,]	NA NA	NA NA	NA NA				NA NA	
##	[33,]	NA NA	NA NA	NA NA	NA NA	NA NA		NA NA	
##	[34,]	NA NA	NA NA	NA NA	NA NA	NA		NA NA	
##	[35,]	NA	NA	NA	NA			NA	
##	[36,]	NA	NA	NA	NA	NA		NA	
##	[37,]	NA	NA	NA	NA	NA		NA	
##	[38,]	NA	NA	NA	NA	NA		NA	
##	[39,]	NA	NA	NA	NA	NA		NA	
##	[40,]	NA	NA	NA	NA	NA		NA	
##	[41,]	NA	NA	NA	NA	NA	NA	NA	
##	[42,]	NA	NA	NA	NA	NA	NA	NA	
##	[43,]	NA	NA	NA	NA	NA	NA	NA	
##	[44,]	NA	NA	NA	NA	NA	NA	NA	
##	[45,]	NA	NA	NA	NA	NA		NA	
##	[46,]	NA	NA	NA	NA	NA		NA	
##	[47,]	NA	NA	NA	NA	NA		NA	
##	[48,]	NA	NA	NA	NA	NA	NA	NA	

	5.4.3							
##	[49,]	NA	NA	NA	NA	NA	NA	NA
##	[50,]	NA	NA	NA	NA	NA	NA	NA
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##	[52,]	NA	NA	NA	NA	NA	NA	NA
##	[53,]	NA	NA	NA	NA	NA	NA	NA
##	[54,]	NA	NA	NA	NA	NA	NA	NA
##	[55,]	NA	NA	NA	NA	NA	NA	NA
##	[56,]	NA	NA	NA	NA	NA	NA	NA
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##	[58,]	NA	NA	NA	NA	NA	NA	NA
##	[59,]	NA	NA	NA	NA	NA	NA	NA
##	[60,]	NA	NA	NA	NA	NA	NA	NA
##	[61,]	NA	NA	NA	NA	NA	NA	NA
##	[62,]	NA	NA	NA	NA	NA	NA	NA
##	[63,]	NA	NA	NA	NA	NA	NA	NA
##	[64,]	NA	NA	NA	NA	NA	NA	NA
##	[65,]	NA	NA	NA	NA	NA	NA	NA
##	[66,]	NA	NA	NA	NA	NA	NA	NA
##	[67,]	NA	NA	NA	NA	NA	NA	NA
##	[68,]	NA	NA	NA	NA	NA	NA	NA
##	[69,]	NA	NA	NA	NA	NA	NA	NA
##	[70,]	NA	NA	NA	NA	NA	NA	NA
##	[71,]	NA	NA	NA	NA	NA	NA	NA
##	[72,]	NA	NA	NA	NA	NA	NA	NA
##	[73,]	NA	NA	NA	NA	NA	NA	NA
##	[74,]	NA	NA	NA	NA	NA	NA	NA
##	[75,]	NA	NA	NA	NA	NA	NA	NA
##	[76,]	NA	NA	NA	NA	NA	NA	NA
##	[77,]	NA	NA	NA	NA	NA	NA	NA
##	[78,]	NA	NA	NA	NA	NA	NA	NA
##	[79,]	NA	NA	NA	NA	NA	NA	NA
##	[80,]	NA	NA	NA	NA	NA	NA	NA
##	[81,]	NA	NA	NA	NA	NA	NA	NA
##	[82,]	NA	NA	NA	NA	NA	NA	NA
##	[83,]	NA	NA	NA	NA	NA	NA	NA
##	[84,]	NA	NA	NA	NA	NA	NA	NA
##	[85,]	NA	NA	NA	NA	NA NA	NA NA	NA
##	[86,]	NA	NA	NA	NA	NA NA	NA NA	NA
##	[87,]	NA	NA	NA	NA	NA	NA NA	NA
##	[88,]	NA	NA	NA	NA	NA	NA NA	NA
##	[89,]	NA	NA	NA	NA	NA	NA NA	NA
##	[90,]	NA	NA	NA	NA	NA	NA NA	NA
##	[91,]	NA	NA	NA	NA	NA	NA NA	NA
##	[92,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[93,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	
##								NA NA
	[94,]	NA NA	NA NA	NA NA	NA NA	NA	NA	NA NA
##	[95,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[96,]	NA NA	NA NA	NA NA	NA NA	NA	NA	NA NA
##	[97,]	NA	NA	NA	NA	NA	NA	NA
##	[98,]	NA	NA	NA	NA	NA	NA	NA
##	[99,]	NA	NA	NA	NA	NA	NA	NA
##	[100,]	NA L 103	NA 5 473	NA L 103	NA L 103	NA L coll	NA L 043	NA Food
##	F . 3	[,16]	[,17]	[,18]	[,19]	[,20]	[,21]	[,22]
##	[1,]	99.23899	67.30492	82.90617	92.21570	79.39312	125.05783	108.08541

##	[2,]	119.92448	75.33580	110.89758	121.58660	88.20434	103.02694	68.95935
##	[3,]	91.65655	88.20636	105.22732	78.42957	89.40283	62.27731	83.43537
##	[4,]	87.78692	88.57858	97.81250	79.00961	125.26780	95.22395	77.55021
##	[5,]	69.08589	63.80883	113.69746	91.27715	53.86534	68.58181	116.78681
##	[6,]	59.05590	116.55986	98.05791	80.46275	93.18601	49.45812	114.07163
##	[7,]	76.12192	115.50133	83.74683	79.05632	88.66779	86.80893	100.80121
##	[8,]	89.93024	90.22122	73.48421	111.68530	104.09557	99.21487	93.50844
##	[9,]	109.40839	84.97061	89.03869	88.28098	70.00873	120.70246	92.37257
##	[10,]	94.86657	104.64493	99.14571	92.98717	63.68926	80.23622	65.72763
##	[11,]	105.00988	84.41584	73.64419	104.88164	90.14323	113.87810	46.78589
##	[12,]	105.21917	78.92081	101.96732	127.50647	56.17662	110.54102	89.11674
##	[13,]	107.22717	86.40273	93.10762	76.58921	73.85462	89.04189	62.69209
##	[14,]	77.85253	100.09185	130.28489	77.90098	64.74042	86.76540	97.87103
##	[15,]	69.59809	84.00053	92.03927	74.69273	112.75018	63.99158	75.87117
##	[16,]	NA	86.87263	95.54301	58.22029	86.58507	56.19922	116.54043
##	[17,]	NA	NA	77.10114	80.04927	90.41232	98.18504	95.55856
##	[18,]	NA	NA	NA	95.14991	117.85776	99.48059	77.18756
##	[19,]	NA	NA	NA	NA	91.01903	79.57438	99.56496
##	[20,]	NA	NA	NA	NA	NA		105.70586
##	[21,]	NA	NA	NA	NA	NA	NA	121.01759
##	[22,]	NA						
##	[23,]	NA						
##	[24,]	NA						
##	[25,]	NA						
##	[26,]	NA						
##	[27,]	NA						
##	[28,]	NA						
##	[29,]	NA						
##	[30,]	NA NA						
## ##	[31,] [32,]	NA NA						
##	[33,]	NA NA						
##	[34,]	NA NA						
##	[35,]	NA NA						
##	[36,]	NA NA						
##	[37,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA
##	[38,]	NA						
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##	[65,]	NA NA	NA NA	NA	NA	NA NA	NA	NA
##	[66,]							
		NA NA	NA NA	NA	NA	NA NA	NA	NA
##	[67,]	NA						
##	[68,]	NA						
##	[69,]	NA						
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##	[79,]	NA						
##	[80,]	NA						
##	[81,]	NA						
##	[82,]	NA						
##	[83,]	NA						
##	[84,]	NA	NA NA	NA	NA	NA NA	NA NA	NA
##	[85,]	NA						
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##	[91,]	NA						
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##	[96,]	NA						
##	[97,]	NA						
##	[98,]	NA						
##	[99,]	NA						
##	[100,]	NA						
##		[,23]	[,24]	[,25]	[,26]	[,27]	[,28]	[,29]
##	[1,]	100.25705		110.63606			129.80918	69.38425
##	[2,]	56.58168		119.70312	72.43670			93.43687
##	[3,]		127.84397			106.88566		104.98930
	[4,]							
##		96.63428		94.64061		117.68956	88.46679	38.11183
##	[5,]	62.26077		104.73476		103.02739	97.24426	79.43648
##	[6,]	78.41951	74.48668	61.99312		107.83458	87.24298	90.27612
##	[7,]		100.84691		118.68839			108.87186
##	[8,]	88.26391	86.14057	79.34768	101.61840	85.00010	60.54885	126.50741

##	[9,]	94.72397	97.35384	106.74424	111.25408	54.95985	112.16214	107.06247
##	[10,]	79.99174	134.11269	97.82441	84.97386	90.96791	81.95017	111.42663
##	[11,]	92.99933	93.94554	107.46535	79.22036	88.98026	91.30395	115.88409
##	[12,]	55.06839	78.20501	131.66026	109.82328	71.65243	119.42339	99.13826
##	[13,]	97.73261	133.83090	98.93088	71.64233	86.05978	92.53090	99.17914
##	[14,]	62.99942	95.93333	98.29689	84.22118	99.30979	86.90305	100.15477
##	[15,]	89.17770	72.77231	77.54160	44.77588	139.51445	72.36715	82.05380
##	[16,]	92.49796	69.40984	66.00504	77.97050	133.03405	70.95612	83.63739
##	[17,]	104.90472	70.84395	106.84386	83.59955	99.97648	84.98482	79.37230
##	[18,]	137.70469	87.63755	69.77714	87.62084	76.44599	96.33733	99.69062
##	[19,]	121.76878	85.81070	78.09886	79.74947	113.55498	79.70505	68.92968
##	[20,]	63.25713	106.00198	118.46903	121.36944	72.11337	108.57322	105.17561
##	[21,]	75.51375	102.49446	47.29759	66.99733	116.62064	66.14127	99.75926
##	[22,]	102.20831	94.19803	112.44849	75.75817	93.85033	91.38054	89.31110
##	[23,]	NA	92.21940	106.53458	95.90120	94.02175	85.86304	103.16369
##	[24,]	NA	NA	103.39241	94.79664	114.03819	91.79491	64.42892
##	[25,]	NA	NA	NA	65.46848	100.57930	71.68791	98.07257
##	[26,]	NA	NA	NA	NA	128.43073	74.43361	73.61824
##	[27,]	NA	NA	NA	NA	NA	126.66602	105.48205
##	[28,]	NA	NA	NA	NA	NA	NA	110.07348
##	[29,]	NA						
##	[30,]	NA						
##	[31,]	NA						
##	[32,]	NA						
##	[33,]	NA						
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##	[39,]	NA						
##	[40,]	NA NA						
##	[41,]	NA NA						
## ##	[42,] [43,]	NA NA						
##	[44,]	NA NA						
##	[45,]	NA NA						
##	[46,]	NA						
##	[47,]	NA						
##	[48,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA
##	[49,]	NA						
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##	[63,]	NA	NA	NA	NA	NA	NA	NA
##	[64,]	NA	NA	NA	NA	NA	NA	NA
##	[65,]	NA	NA	NA	NA	NA	NA	NA
##	[66,]	NA	NA	NA	NA	NA	NA	NA
##	[67,]	NA	NA	NA	NA	NA	NA	NA
##	[68,]	NA	NA	NA	NA	NA	NA	NA
##	[69,]	NA	NA	NA	NA	NA	NA	NA
##	[70,]	NA	NA	NA	NA	NA	NA	NA
##	[71,]	NA	NA	NA	NA	NA	NA	NA
##	[72,]	NA	NA	NA	NA	NA	NA	NA
##	[73,]	NA	NA	NA	NA	NA	NA	NA
##	[74,]	NA	NA	NA	NA	NA	NA	NA
##	[75,]	NA	NA	NA	NA	NA	NA	NA
##	[76,]	NA NA	NA NA	NA	NA	NA	NA NA	NA
##	[77,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
	[78,]							
##		NA	NA	NA	NA	NA	NA	NA
##	[79,]	NA	NA	NA	NA	NA	NA	NA
##	[80,]	NA	NA	NA	NA	NA	NA	NA
##	[81,]	NA	NA	NA	NA	NA	NA	NA
##	[82,]	NA	NA	NA	NA	NA	NA	NA
##	[83,]	NA	NA	NA	NA	NA	NA	NA
##	[84,]	NA	NA	NA	NA	NA	NA	NA
##	[85,]	NA	NA	NA	NA	NA	NA	NA
##	[86,]	NA	NA	NA	NA	NA	NA	NA
##	[87,]	NA	NA	NA	NA	NA	NA	NA
##	[88,]	NA	NA	NA	NA	NA	NA	NA
##	[89,]	NA	NA	NA	NA	NA	NA	NA
##	[90,]	NA	NA	NA	NA	NA	NA	NA
##	[91,]	NA	NA	NA	NA	NA	NA	NA
##	[92,]	NA	NA	NA	NA	NA	NA	NA
##	[93,]	NA	NA	NA	NA	NA	NA	NA
##	[94,]	NA	NA	NA	NA	NA	NA	NA
##	[95,]	NA	NA	NA	NA	NA	NA	NA
##	[96,]	NA	NA	NA	NA	NA	NA	NA
##	[97,]	NA	NA	NA	NA	NA	NA	NA
##	[98,]	NA	NA	NA	NA	NA	NA	NA
##	[99,]	NA	NA	NA	NA	NA	NA	NA
##	[100,]	NA	NA	NA	NA		NA	NA
##		[,30]	[,31]	[,32]	[,33]	[,34]	[,35]	[,36]
##	[1,]	111.20300	82.90801	69.44965	98.55994	73.74304	69.80843	123.31421
##	[2,]	86.97624	67.81577	88.90540	86.29554	97.01883	102.83419	76.47578
##	[3,]	73.78741	61.11909	124.16422	71.83129	130.30815	91.43575	77.23622
##	[4,]	87.21083	79.99520	63.97809	92.12547	68.06450	95.82753	88.09594
##	[5,]	91.79708	86.09856	123.01233	97.89656	106.08676	96.90609	75.73459
##	[6,]	65.81474	102.21706	94.99740	107.60992	102.28214	111.50190	94.61472
##	[7,]	86.30742	128.10554	89.71627	75.91094	71.86395	101.95678	93.23580
##	[8,]	99.44339	120.07128	73.32840	88.09264			102.60102
##	[9,]	86.52733						125.13679
##	[10,]	85.85016		127.68401				42.33446
##	[11,]	99.13714			89.34970			
##	[12,]	94.42151				85.40955		
##	[13,]	82.02516		121.56432		111.39958		70.54380
##	[14,]	74.28790		124.77047		92.61950		94.85179
##	[15,]	75.82028		101.76261		104.77570	89.64522	
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##	[16,]	95.60539		121.53359		87.02279		84.60524
##	[17,]	97.86730	79.13705		111.89053	97.60390		106.58939
##	- ,-	119.12267			112.81012	91.96623		97.64999
##	[19,]	79.77126		114.65481	74.97387	87.62390	73.88834	104.84379
##	[20,]	77.51207	85.02831	129.23501	87.87568	94.09814	101.16614	83.60028
##	[21,]	74.30810	100.41447	118.54307	94.59208	133.42876	105.81130	79.96039
##	[22,]	97.86452	76.09975	79.67809	81.69782	67.29487	75.88158	61.94196
##	[23,]	69.25554	91.32567	104.69095	88.22549	98.73822	136.85317	74.42042
##	[24,]	93.15688	90.94807	68.60026	111.47736	59.86905	93.14513	106.55817
##	[25,]	97.96219	106.89757	90.57279	84.65897	117.61132	80.68188	94.08847
##	[26,]	105.07623	63.76215	101.17732	72.06979	108.99222	70.06785	67.72288
##	[27,]	94.07889	101.84378	68.88733	99.69774	94.14984	84.17901	108.63903
##	[28,]	71.37645	102.50021	101.09585	82.15426	95.92216	114.83442	86.77880
##	[29,]	106.23398	66.83940	78.79668	79.06967	70.59688	73.59896	87.97723
##	[30,]	NA	83.66862	99.38767	108.45806	106.68534	138.06811	108.76157
##	[31,]	NA	NA	109.00112	69.98617	92.88793	73.36191	94.07305
##	[32,]	NA	NA	NA	111.03134	73.35039	89.73574	111.47478
##	[33,]	NA	NA	NA	NA	72.38222	79.59246	67.34992
##	[34,]	NA	NA	NA	NA	NA	85.91888	83.54848
##	[35,]	NA	NA	NA	NA	NA	NA	87.15278
##	[36,]	NA						
##	[37,]	NA						
##	[38,]	NA						
##	[39,]	NA						
##	[40,]	NA						
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##	[60,]	NA						
##	[61,]	NA						
##	[62,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA
##	[63,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA
##		NA NA		NA NA	NA NA	NA NA	NA NA	
##	[64,] [65,]	NA NA						
##	[66,]	NA NA						
##	[67,]	NA NA						
##	[68,]	NA NA						
##	[69,]	NA						

##	[70,]	NA	NA	NA	NA	NA	NA	NA
##	[71,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[72,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
##	[73,]							
##	[74,]	NA NA	NA	NA NA	NA NA	NA NA	NA NA	NA NA
	-	NA	NA	NA	NA	NA	NA	NA
##	[75,]	NA	NA	NA	NA	NA	NA	NA
##	[76,]	NA	NA	NA	NA	NA	NA	NA
##	[77,]	NA	NA	NA	NA	NA	NA	NA
##	[78,]	NA	NA	NA	NA	NA	NA	NA
##	[79,]	NA	NA	NA	NA	NA	NA	NA
##	[80,]	NA	NA	NA	NA	NA	NA	NA
##	[81,]	NA	NA	NA	NA	NA	NA	NA
##	[82,]	NA	NA	NA	NA	NA	NA	NA
##	[83,]	NA	NA	NA	NA	NA	NA	NA
##	[84,]	NA	NA	NA	NA	NA	NA	NA
##	[85,]	NA	NA	NA	NA	NA	NA	NA
##	[86,]	NA	NA	NA	NA	NA	NA	NA
##	[87,]	NA	NA	NA	NA	NA	NA	NA
##	[88,]	NA	NA	NA	NA	NA	NA	NA
##	[89,]	NA	NA	NA	NA	NA	NA	NA
##	[90,]	NA	NA	NA	NA	NA	NA	NA
##	[91,]	NA	NA	NA	NA	NA	NA	NA
##	[92,]	NA	NA	NA	NA	NA	NA	NA
##	[93,]	NA	NA	NA	NA	NA	NA	NA
##	[94,]	NA	NA	NA	NA	NA	NA	NA
##	[95,]	NA	NA	NA	NA	NA	NA	NA
##	[96,]	NA	NA	NA	NA	NA	NA	NA
##	[97,]	NA	NA	NA	NA	NA	NA	NA
##	[98,]	NA	NA	NA	NA	NA	NA	NA
##	[99,]	NA	NA	NA	NA	NA	NA	NA
##	[100,]	NA	NA	NA	NA	NA	NA	NA
##	- ,-	[,37]	[,38]	[,39]	[,40]	[,41]	[,42]	[,43]
##	[1,]	85.71328		144.57788	92.59273	80.57686	64.36607	95.39872
##	[2,]		117.68412		51.87437	88.97980	63.93323	21.53727
##	[3,]	91.80135	93.46660	72.03985		111.24698		74.74008
##	[4,]	111.62249	93.47519	75.46330	99.01045		104.85690	89.61710
##	[5,]	109.47742		99.76969		130.78212	93.77550	73.06229
##	[6,]	99.67380					123.46690	
##	[7,]	78.85927					92.30996	
##	[8,]		106.74871		84.98471			85.53057
##	[9,]	69.64351			93.70480			
##		102.06949					107.30294	
##	[11,]	74.24491					63.33064	
##	[12,]					95.71539		
##	[13,]	92.01483					110.90948	
##	[14,]	104.98694					79.32763	
							109.03981	
##	[15,]	95.78286						
##	-	102.66427					98.39613	
##	[17,]					81.61798		77.13509
##	[18,]		86.00473					103.33830
##	[19,]	93.23426					116.84852	
##	[20,]	99.54930				130.29408		86.82955
##							122.39491	
##	[22,]	91.99243	71.09158	66.67011	76.65562	76.23321	86.02728	64.20291

##	_ /-	111.01048				110.81523		58.28067
##	[24,]	89.27757			105.90959			95.00411
##	[25,]	85.58506			91.29512		108.87110	
##		108.36497		68.49941	52.44023		100.52228	73.53019
##	[27,]	74.02077		133.07769	99.66736		82.31744	93.52433
##	[28,]		110.53638	54.44918			84.09999	88.30658
##		126.08169	81.33538	92.55742		102.57472		92.43234
##	[30,]	76.16814	101.40023		127.84777		111.81740	100.02218
##	[31,]	108.80312	68.30056	91.95951	73.92833	110.80975	96.00644	80.66798
##	[32,]		105.89629		103.45522	40.64836	74.49085	89.00887
##	[33,]	125.46988	61.58415	79.79624	59.40967	106.82228	85.59215	85.41681
##	[34,]	102.95296	66.03854	83.91517	95.89359	71.94586	68.05109	90.85458
##	[35,]	90.78540	59.37520	94.36683	69.26436	87.48982	87.61961	97.83614
##	[36,]	126.29394	81.51568	61.10748	56.61682	115.03880	99.87810	60.23193
##	[37,]	NA	108.49722	95.64893	112.28426	48.77521	72.55357	100.93593
##	[38,]	NA	NA	72.96590	96.48288	103.58593	105.06194	116.63928
##	[39,]	NA	NA	NA	97.47264	96.34620	117.30680	99.91359
##	[40,]	NA	NA	NA	NA	100.02211	67.72744	44.10508
##	[41,]	NA	NA	NA	NA	NA	54.72310	90.90494
##	[42,]	NA	NA	NA	NA	NA	NA	63.77748
##	[43,]	NA						
##	[44,]	NA						
##	[45,]	NA						
##	[46,]	NA						
##	[47,]	NA						
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##	[77,]	NA						
##	[78,]	NA NA	NA NA	NA	NA NA	NA	NA NA	NA
##	[79,]	NA						
##	[80,]	NA						
##	[81,]	NA						
##	[82,]	NA						
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##	[97,]	NA						
##	[98,]	NA						
##	[99,]	NA						
##	[100,]	NA						
##	[100,]	[,44]	[,45]	[,46]	[,47]	[,48]	[,49]	[,50]
##	[1,]	79.94970	67.82696	76.88869	50.70326	83.40976	66.07910	97.60072
##	[2,]	64.04633		109.18906	88.88024	69.18843	98.41018	82.02021
##	[3,]	86.73173			126.05178		84.08194	89.97156
##	[4,]		109.40123	87.35857	72.43665		129.06666	
##	[5,]	76.20836		108.58227		117.52682	97.74362	79.85530
##	[6,]	91.75446	98.77601	87.36461	98.18558		104.41210	96.55655
##	[7,]	124.90499	95.02283	84.38727	99.53790	84.18162	80.28161	82.27452
##	[8,]	121.77278		110.80649	88.99234	41.49042	78.82380	77.69986
##	[9,]	100.12210	68.37332	77.99362	75.68616	79.19326		109.60138
##	[10,]	109.00253	112.35631		116.60063	114.84122	96.34602	72.92646
##	[11,]	110.65248	75.55826	81.10520	83.87683	72.00391	97.35051	94.67097
##	[12,]	85.58937	87.99353	82.33093	69.41483	76.01413	89.92040	83.80975
##	[13,]	90.95667	100.22430	83.54135	115.47110	121.52762	82.53202	98.18009
##	[14,]	93.49404	73.11192	95.33598	81.84856	90.95522	85.39649	92.28030
##	[15,]	76.49278	86.33650	104.97793	101.53053	96.31916	128.08303	107.11627
##	[16,]	108.48382	60.99460	104.06303	89.32417	109.14930	110.32833	85.44721
##	[17,]	73.17622	65.38974	120.96654	96.51091	91.63197	90.93354	112.86701
##	[18,]	115.96046	70.82055	80.20520	90.69107	85.13719	79.30800	93.78837
##	[19,]	87.50692	76.09456	92.48678	97.04718	121.52802	93.17090	119.53572
##	[20,]	99.56448	95.74703	80.29175	94.78775	111.67978	77.13454	88.29262
##	[21,]	94.85052	88.37919	118.07415	126.50677	116.84555	92.93804	80.09487
##	[22,]	90.05853	108.21818	66.67897	82.69026	77.98054	116.26137	92.73917
##	[23,]	77.84051	107.82704	103.73580	92.53958	78.49757	99.15689	70.11810
##	[24,]	73.37176		93.47753			123.78115	108.29233
##	[25,]	111.06506	71.53118	102.87806	106.41410	102.28119	75.65967	75.48268
##	[26,]	79.35396	75.29109	107.60950	94.24376	104.55200	108.21119	77.74956
##	[27,]	98.13541	99.95196	63.15813	84.14240	85.01800	39.94899	88.11054
##	[28,]	97.64342	86.39805	137.72462	123.94823	73.65721	105.74821	92.37246
##	[29,]	48.90553	93.84906	78.44980	59.16801	107.00714	109.12513	91.97322

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##	[30,]				125.36412			127.65805
##	[31,]	64.18900	81.31433	86.24673		106.20277		109.62828
##	[32,]	74.86914	99.81996	79.98863	69.91422	50.76349		94.85468
##	[33,]	99.44499	82.06571	82.35227		100.14270	88.86468	59.72999
##	[34,]	93.79369	92.86254	62.83885	46.46084	67.22579	115.81619	87.46092
##	[35,]	105.69396	55.84683	68.79312	68.82146	111.96016	79.21733	86.25541
##	[36,]	99.32856	107.31721	78.43983	90.53561	106.76480	120.83608	49.77230
##	[37,]	105.78282	77.42828	109.90294	116.38594	65.44348	68.90066	121.80195
##	[38,]	112.94536	83.49815	42.45874	67.79749	111.74863	92.14946	93.49800
##	[39,]	101.44809	103.08223	93.09683	113.72143	102.58156	129.65441	95.64396
##	[40,]	91.10689	70.57506	101.08176	78.06019	94.55140	91.72392	48.78252
##	[41,]	98.71317	77.58870	97.55919	81.07464	34.49286	88.65022	101.24114
##	[42,]	102.16883	60.57163	103.07141	64.88661	43.69462	84.52095	78.62032
##	[43,]	72.64323	99.42869	102.59779	85.90742	73.20439	104.93811	68.17819
##	[44,]	NA	114.18138	101.02094	86.55590	90.10053	102.97273	108.08638
##	[45,]	NA	NA	106.07859	74.11061	89.29221	76.05444	86.36021
##	[46,]	NA	NA	NA	58.40145	100.60683	89.52880	85.32274
##	[47,]	NA	NA	NA	NA	76.27657	97.91725	75.26476
##	[48,]	NA	NA	NA	NA	NA	96.16838	92.99192
##	[49,]	NA	NA	NA	NA	NA	NA	88.36685
##	[50,]	NA						
##	[51,]	NA						
##	[52,]	NA						
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##	[73,]	NA						
##	[74,]	NA						
##	[75,]	NA						
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##	[77,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA
##	[78,]	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA
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##
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##
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                     71.92411 113.91479 115.95039
                                                   79.65523
                                                              58.74793
                                                                        82.91058
##
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                    82.77181 106.41511 107.23393 94.04827
                                                              84.63210 108.78817
    [85.] 103.52906
                     74.38899 131.76778 115.32977 66.88083
                                                              98.03093
                                                                        80.46576
    [86,] 137.37225
                     74.31518 76.07683 58.24561 117.15286
                                                              77.21283
##
                                                                        91.97939
##
    [87.] 108.11055
                     63.32046 145.99896 113.34830 65.31082
                                                              96.53391
                                                                        87.26539
##
          99.14298 120.34889 83.09782 103.69231 108.40064
                                                              89.79583 107.97467
    [88,]
    [89,]
          73.87886
                    88.35773 43.02600 53.57778 131.19937
                                                              88.24985
                                                                        82.10773
                    82.34142 68.63111 73.29301 134.67261
##
    [90,]
           77.03421
                                                              84.42991
                                                                        91.10242
          97.91367 107.37886 109.52215 114.07020 87.13494 101.98305
##
    [91.]
                                                                        89.35309
##
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                                                                        87.71530
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##
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##
     Γ1. ] 41.37340
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     [3,] 121.66252
##
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##
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##
```

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    [41,] 93.65894
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    [43,] 115.74585
##
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##
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##
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    [47,] 50.57218
##
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##
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##
    [51,] 74.72545
##
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##
    [53,] 96.45217
    [54,] 64.75773
##
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##
    [56,] 91.60708
    [57,] 64.65118
##
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##
    [59,] 83.59224
##
    [60,] 82.62959
##
    [61,]
           82.78660
##
    [62,]
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    [63,] 83.94533
##
    [64,] 114.45950
##
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           83.72271
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    [66,]
##
    [67,] 86.06028
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    [68,] 62.56155
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    [69,] 91.34271
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    [71,] 120.66618
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    [73,] 64.47977
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    [75,] 90.42319
    [76,] 137.05383
    [77,] 113.00002
##
##
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##
    [79,] 109.30296
##
    [80,] 98.57995
    [81,] 108.07978
##
##
    [82,] 89.13637
##
    [83,] 105.64172
##
    [84,] 99.10465
##
    [85,] 111.16878
```

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## [86,] 92.61285
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  [87,] 133.73024
  [88,] 49.41310
## [89,] 60.95005
## [90,] 64.26975
## [91,] 100.95113
## [92,] 119.04128
## [93,] 72.91321
## [94,] 127.74825
## [95,] 55.51334
## [96,] 89.64537
## [97,] 115.51882
## [98,] 85.71343
## [99,] 101.85334
## [100,]
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all_angles(X)

##		[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]
##	[1,]	NA	92.96163	126.14924	91.33681	81.41249	108.04412	101.50051	89.30027
##	[2,]	NA	NA	66.14781	88.90066	78.21263	119.86235	130.65064	85.92698
##	[3,]	NA	NA	NA	104.77015	86.03254	96.71089	106.26462	98.34278
##	[4,]	NA	NA	NA	NA	96.51874	77.04727	102.32236	111.46164
##	[5,]	NA	NA	NA	NA	NA	87.33802	112.38187	112.04775
##	[6,]	NA	NA	NA	NA	NA	NA	82.00564	103.00972
##	[7,]	NA	NA	NA	NA	NA	NA	NA	63.86235
##	[8,]	NA	NA	NA	NA	NA	NA	NA	NA
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##	[10,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[11,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[12,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[13,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[14,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[15,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[16,]	NA	NA	NA	NA	NA	NA	NA	NA
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##	[18,]	NA	NA	NA	NA	NA	NA	NA	NA
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##	[35,]	NA	NA	NA	NA	NA	NA	NA	NA

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##	[78,]	NA	NA	NA	NA	NA	NA	NA	NA
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##	[82,]	NA	NA	NA	NA	NA	NA	NA	NA NA
##	[83,]	NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA	NA NA
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##	[86,]	NA NA	NA NA	NA NA	N A N A	NA NA	NA NA	NA NA	NA NA
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##	[98,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[99,]	NA	NA	NA	NA	NA	NA	NA	NA
##	[100,]	NA .	NA L 103	NA .	NA L 103	NA F. 4.03	NA .	NA	NA
##	F4 7	[,9]	[,10]	[,11]	[,12]	[,13]	[,14]	[,15]	
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##	[2,]			63.51225		74.79280		80.89861	
##	[3,]		61.06160			43.63118		63.78853	
##	-	121.31606							
##		103.20692							
##		110.09199							
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##	[9,]		101.56552					109.64924	
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##	[99,]	NA						
##	[100,]	NA						
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##	[2,]	119.92448	75.33580	110.89758	121.58660	88.20434	103.02694	68.95935
##	[3,]	91.65655	88.20636	105.22732	78.42957	89.40283	62.27731	83.43537
##	[4,]	87.78692	88.57858	97.81250	79.00961	125.26780	95.22395	77.55021
##	[5,]	69.08589	63.80883	113.69746	91.27715	53.86534	68.58181	116.78681
##	[6,]	59.05590	116.55986	98.05791	80.46275	93.18601	49.45812	114.07163
##	[7,]	76.12192	115.50133	83.74683	79.05632	88.66779	86.80893	100.80121
##	[8,]	89.93024	90.22122	73.48421	111.68530	104.09557	99.21487	93.50844
##	[9,]	109.40839	84.97061	89.03869	88.28098	70.00873	120.70246	92.37257
##	[10,]	94.86657	104.64493	99.14571	92.98717	63.68926	80.23622	65.72763
##	[11,]	105.00988	84.41584	73.64419	104.88164	90.14323	113.87810	46.78589
##	[12,]	105.21917	78.92081	101.96732	127.50647	56.17662	110.54102	89.11674
##	[13,]	107.22717	86.40273	93.10762	76.58921	73.85462	89.04189	62.69209
##	[14,]	77.85253	100.09185	130.28489	77.90098	64.74042	86.76540	97.87103
##	[15,]	69.59809	84.00053	92.03927	74.69273	112.75018	63.99158	75.87117
##	[16,]	NA	86.87263	95.54301	58.22029	86.58507	56.19922	116.54043
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##	[30,]	NA						
##	[31,]	NA NA						
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##	[2,]	56.58168	94.38858	119.70312	72.43670	93.14959	85.63976	93.43687

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##
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                                                                   65.31978 104.98930
                                                                   88.46679
##
     [4.]
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                                             72.79703 117.68956
            96.63428 53.81703
                                                                              38.11183
                       84.45967 104.73476
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##
     [5,]
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                                                                   87.24298
##
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##
     [7,] 102.62902 100.84691
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                       86.14057
                                  79.34768 101.61840
                                                        85.00010
                                                                   60.54885 126.50741
##
                       97.35384 106.74424 111.25408
                                                        54.95985 112.16214 107.06247
     [9.]
            94.72397
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            92.49796
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##	[3,]	73.78741		124.16422		130.30815		77.23622
##	[4,]	87.21083		63.97809	92.12547	68.06450		88.09594
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##	[4,]	111.62249	93.47519	75.46330	99.01045	82.70229	104.85690	89.61710
##	[5,]	109.47742	110.22272	99.76969	73.77255	130.78212	93.77550	73.06229
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                               97.69407 67.63838
                                                   96.23143
                                                              85.59857
                                                                        98.42304
##
           85.29711 101.71365 73.34972 83.54354 85.34160 103.83357
                                                                        69.01372
     [4,]
##
                     76.83118 101.00191 100.77204 111.35792
                                                              96.99153 112.09838
     [5,]
           70.58725
##
     [6,] 123.27274
                     99.53267 114.19866 101.55555 104.25807
                                                              65.85917
                                                                        60.47265
           87.50638 110.26568 109.09747 115.59971 51.96485
                                                              76.65562
##
     [7.]
                                                                        70.24752
##
                    74.41162 100.15821 94.17830 54.00989
                                                              70.64658
     [8,] 109.77944
                                                                        76.36109
           89.42712
                     81.57716 64.02680 59.38432 118.02114
                                                              93.50756
     [9,]
                                                                        94.82344
    [10,]
                     84.85067 124.16249 116.30023 76.16867
##
           70.58589
                                                              86.30297 102.86151
                                                              82.40723
                               92.95175
##
    [11,]
           95.11774
                     60.13059
                                        79.17211 92.03911
                                                                        96.59002
                     78.49689
                               94.24592
                                         98.71113 111.81993
                                                              91.82364
                                                                        98.91146
##
    [12,]
           85.27716
    [13,]
           73.48504
                     75.92620
                               90.82504
                                         76.31229 101.73952 104.59535 116.87237
##
    [14,]
           84.95114
                     64.08211
                               88.52506
                                         71.12487 115.81495
                                                              65.56988
                                                                        67.34951
##
    [15,] 111.60704
                     59.98368
                               98.66070
                                         70.53397 104.29261
                                                              81.99531
                                                                        78.98786
                     80.52167 103.47865
##
    [16,] 87.79568
                                         97.16715 94.38300
                                                              61.70966
                                                                       77.41765
##
    [17.]
          77.88469
                    58.72955 70.42230 60.69320 100.21530 128.16865 126.63054
    [18,] 108.01164 100.03082 80.78551 88.42493 79.39310 94.78043 118.48050
##
```

```
71.91750 86.32591 72.34982 62.66140 104.98195
                                                           98.23984 87.22808
##
         65.68643 86.46589 107.00618 105.59966 112.04672
                                                           92.57896 100.36921
    [20.]
                    81.10949 120.19644 97.94164 94.66529
##
    [21,] 114.72553
                                                           68.86520
                    85.00917
                             90.27583 91.52450
                                                 73.34917
                                                           98.07266
##
    [22,]
          79.50832
                                                                     90.33241
##
    [23,]
          95.89672
                    75.69322 119.95750 109.40497
                                                 93.73553
                                                           73.73336
                                                                     68.88190
##
    [24,] 93.65755 83.30898 79.38228 83.03398 96.20977
                                                           93.97726
                                                                     70.35964
    [25.] 122.80370 100.44097 94.53150 89.82040
                                                 82.82700
                                                           59.18769
                                                                     87.00049
         95.92978 72.73081 81.14055
                                       72.34534
##
    [26.]
                                                 93.18885
                                                           75.80848
                                                                     96.33244
##
    [27,] 91.16472 119.07097 76.96255
                                       94.84181
                                                 97.05153 103.10849 108.77796
    [28,] 102.38639 55.21617 115.99911
                                       86.00393 52.03314 83.33300
##
                                                                     70.58535
    [29,]
         61.42506 112.31124 51.86748 80.53591 103.70711 105.64517
                                                                     90.93299
    [30,] 108.47854
                   70.80778 112.45191
                                       76.69873 98.13838 105.72209
                                                                     65.31159
##
##
    [31.]
         71.67818 71.72199 57.90167
                                       46.98512 128.37595 98.20990
                                                                     91.41009
    [32,] 109.59479 112.90071
                             68.72263 86.63726 74.17373 103.83418
                                                                     83.28284
##
##
    [33,]
          57.42251 97.81233
                              78.93919 94.25822 77.39461
                                                           64.06068
                                                                     76.02114
##
    [34,]
          60.03981 105.04784
                              80.09169 104.87060 69.74850
                                                           87.94661
                                                                     65.32806
##
    [35,]
          74.30421 101.26580 53.84736 75.88196 104.43175
                                                           89.63730 126.24460
##
    [36,]
          70.52744 93.92210 118.06864 130.66278 70.87397
                                                           71.72517
                                                                     94.48774
    [37,] 117.99980 68.06840 93.13667 69.19726 80.22603 110.80805 102.85005
##
##
    [38.]
          69.29973 109.54664 77.89634 90.59937 103.49559
                                                           72.74538
                                                                     81.80798
##
    [39,]
          88.43548
                   78.56025 119.57893 100.56564 66.99336
                                                           81.76469
                                                                     74.36550
##
    [40,]
          72.77714
                    76.82801 81.35728
                                       91.98254
                                                 85.20369
                                                           74.61788 110.43811
##
    [41,] 115.12628
                    84.13212
                              79.97868
                                       78.25578
                                                 62.04848
                                                           94.13402 79.75646
          87.36068
                    69.66606
                              80.39655
                                       85.69659
                                                 75.13563
                                                           83.02111 87.72941
##
    [42.]
          80.36905
                    67.57462
                              96.20840 96.21877 80.44444
##
    [43,]
                                                           95.77836 101.02257
    [44,]
          82.21916
                    88.35542
                              67.45362 67.55709 105.83394 125.24571 87.89819
##
    [45,]
          92.88937
                    71.29881
                              68.43744 67.54857 103.03885
                                                           69.86232 102.50987
          75.12709 133.92872 80.32056 109.19443 101.05517
                                                           83.86157
##
    [46,]
                                                                     87.93411
         71.08774 112.52713 57.29263 93.42204 100.13368
                                                           74.99856
##
    [47,]
                                                                     77.66871
    [48,] 111.54820 76.47720 92.18162 87.13217 63.47372
##
                                                           86.67755
                                                                     61.67624
##
    [49,]
          97.40218 103.54501 70.79435 76.01100 102.38529
                                                           93.82307 112.32447
##
    [50,]
          81.61297 109.36101 102.08209 131.43448 68.53059
                                                           52.60307
                                                                     92.08806
    [51,] 105.47848 124.88151 84.62554 102.76051 81.10538
                                                           57.70967
##
                                                                     52.91578
    [52,] 124.84278 69.32485
                             89.92922 69.44213 73.93128
                                                           70.95209 72.75202
##
##
    [53,]
          96.57234
                    70.15712
                              91.00608 80.20894 77.68323
                                                           95.86707 122.12885
##
          91.59275 82.23819 66.03395 59.22393 157.89315
                                                           87.85257 106.02776
    [54.]
##
          77.83757 90.88669 111.66634 94.97547 83.47897 109.19028
##
    [56,]
          79.11871 113.12730 91.71212 116.71932 66.68135 104.24613
                                                                     84.34580
##
    [57,]
          97.30836 91.88570 52.74581 62.86427 102.83670
                                                           99.65864 128.29891
          99.24211 63.27635 113.45854 79.58249 103.11023
##
                                                           95.04020
                                                                     99.07342
    [58,]
          99.08682 102.27219 77.66165 80.50229 70.51790
                                                           84.97445
    [59,]
                                                                     45.45198
##
    [60,] 88.33911 104.93947 78.60400 89.66270 105.79780
                                                           56.15151
                                                                     81.63350
          70.08308 85.64377 97.93128 100.16223 83.04690 78.23970
##
    [61.]
                                                                     92.02801
##
    [62,] 112.43627 84.43756 103.39609 86.34029 102.04515 112.88502 112.06487
    [63,] 103.48845 104.90541 105.49392 103.86375 113.68313 82.19549
                                                                     87.83845
    [64,] 116.30160 77.97440 131.61049 106.14336 104.55587
##
                                                           77.19539
                                                                     73.71051
         83.05863 125.47735 85.68675 117.25468 90.17653
##
    [65,]
                                                           54.06704
                                                                     64.68236
          71.12198 78.04547 93.56130 86.18450 91.38048 108.93320 120.22783
##
    [66,]
##
    [67,] 94.82181
                   85.00303 103.83947 96.30088 102.02233
                                                           39.84816
                                                                     63.54408
##
    [68,] 97.19743 142.91258 72.10962 93.49043 99.43526 107.66566
                                                                     98.26117
##
                   74.87941 69.81405 54.01206 113.63490 79.00017
    [69,] 117.38580
                                                                     65.07557
##
    [70,] 112.82426 55.22377 105.83104 83.70341 70.52922 65.50057
                                                                     85.79638
##
    [71,] 68.95290 79.75848 105.29887 97.16483 72.11462 104.62040 101.36037
    [72,] 126.37342 95.82315 111.52961 110.68936 86.01848 35.88695 71.95067
```

```
76.77719 95.78284 36.14327 52.60806 111.94618 114.03673 134.13747
##
    [74.] 77.48651
                   79.95250 91.23660 89.75898 95.50486 60.43563 82.13587
                                                             61.46889
    [75,] 107.03875 116.10382 114.39973 124.81313 55.01177
                                                                       53.23534
                    69.36769 114.25745
                                       87.49824 69.07063
                                                             94.75633 86.13978
##
    [76,] 101.92425
##
    [77,] 81.02897
                    82.91881 89.15192 91.81178 75.69001
                                                             98.88906 100.18895
##
    [78,]
          69.39382 88.64356 80.12342 89.99460 118.05525
                                                             94.64366
                                                                     79.27758
          86.57843
                     66.14969 127.20088 97.48467 103.53724 105.14416 103.66762
    [79.]
                    71.11613 78.60455 73.38443 114.88662
##
    [80,]
          85.60883
                                                            73.46922 71.58084
    [81,] 121.75887
##
                     96.83623 104.57683 95.03886 80.77469
                                                             58.87318
                                                                       64.76364
##
                    48.98137 83.12018 47.23714 116.42021 102.89215 105.38992
    [82,] 96.99114
    [83,] 93.11584
                    71.92411 113.91479 115.95039 79.65523
                                                             58.74793
                                                                      82.91058
                    82.77181 106.41511 107.23393 94.04827
                                                             84.63210 108.78817
##
    [84,] 55.00851
                    74.38899 131.76778 115.32977 66.88083
                                                             98.03093
##
    [85,] 103.52906
                                                                       80.46576
##
    [86,] 137.37225
                    74.31518 76.07683 58.24561 117.15286
                                                             77.21283
                                                                       91.97939
##
    [87,] 108.11055 63.32046 145.99896 113.34830 65.31082
                                                             96.53391
                                                                       87.26539
##
    [88,]
          99.14298 120.34889 83.09782 103.69231 108.40064
                                                             89.79583 107.97467
##
    [89,]
          73.87886 88.35773 43.02600 53.57778 131.19937
                                                             88.24985
                                                                       82.10773
          77.03421 82.34142 68.63111 73.29301 134.67261
##
    [90,]
                                                             84.42991
                                                                       91.10242
          97.91367 107.37886 109.52215 114.07020 87.13494 101.98305
                                                                       89.35309
##
   [91,]
##
    [92,]
          87.32527
                    46.17287 128.51186 101.30954 81.01526
                                                           92.15197
                                                                       87.71530
##
    [93,]
                NA
                    99.38443 73.27084 97.42527 88.04286 106.65053 103.44752
##
    [94,]
                NA
                           NA 103.16748
                                        63.00456 93.31094 94.30248
##
    [95,]
                                         50.29732 111.63184 107.90860 103.89551
                NA
                           NA
                                    NA
##
    [96.]
                           NA
                                              NA 117.35210 111.31346
                                                                       95.95925
                NA
                                    NA
##
                           NA
                                     NA
                                              NA
                                                        NA 85.57998
    [97,]
                NA
                                                                      77.51524
    [98,]
                NA
                           NA
                                    NA
                                              NA
                                                        NA
                                                                   NA
                                                                      62.97335
##
    [99,]
                NA
                           NA
                                     NA
                                              NA
                                                         NA
                                                                   NA
                                                                             NA
##
   [100,]
                NA
                           NA
                                    NA
                                              NA
                                                         NA
                                                                   NA
                                                                             NA
##
             [,100]
##
     [1,] 41.37340
##
     [2,] 117.53819
##
     [3,] 121.66252
##
     [4,] 100.91451
##
         95.25365
     [5,]
##
     [6,]
          95.16299
##
     [7,]
          84.47505
##
     [8,]
          98.30146
##
     [9,] 57.64726
##
    [10,] 106.71911
##
    [11,] 93.90649
    [12,] 79.80621
##
    [13,] 97.86763
##
    [14.] 87.87539
##
    [15,] 121.29610
    [16,] 91.02834
    [17,]
##
          95.95233
##
    [18,] 75.75578
##
    [19,] 81.39240
   [20,] 75.58179
##
    [21,] 116.03235
##
    [22,] 100.79698
##
   [23,] 112.44747
##
   [24,] 86.92298
   [25,] 93.25503
##
```

```
[26,] 112.87091
##
    [27,] 55.24991
##
    [28,] 141.26434
   [29,] 75.07985
##
##
    [30,] 117.65251
##
    [31,] 84.48028
##
    [32,] 82.01545
##
    [33,] 82.88150
##
    [34,] 72.50954
##
    [35,] 54.83681
   [36,] 107.31831
   [37,] 97.56372
##
    [38,] 54.91510
##
##
   [39,] 121.50284
   [40,] 97.20218
##
##
    [41,] 93.65894
##
   [42,] 85.96354
    [43,] 115.74585
##
##
   [44,] 103.64640
##
    [45,] 71.30141
##
   [46,] 47.35525
##
    [47,] 50.57218
   [48,] 103.18454
##
##
    [49,] 62.00319
##
   [50,] 87.74946
    [51,] 74.72545
##
    [52,] 102.79722
##
    [53,] 96.45217
##
   [54,] 64.75773
    [55,] 102.95519
##
    [56,] 91.60708
##
##
    [57,] 64.65118
##
    [58,] 122.30827
##
    [59,] 83.59224
##
    [60,] 82.62959
##
    [61,] 82.78660
##
    [62,] 84.50027
##
    [63,] 83.94533
##
    [64,] 114.45950
##
    [65,] 65.06410
    [66,] 83.72271
##
    [67,] 86.06028
##
    [68,] 62.56155
##
    [69,] 91.34271
##
   [70,] 124.35323
##
   [71,] 120.66618
##
    [72,] 97.59547
##
   [73,] 64.47977
##
   [74,] 100.16772
   [75,] 90.42319
##
##
   [76,] 137.05383
##
   [77,] 113.00002
##
  [78,] 84.36740
```

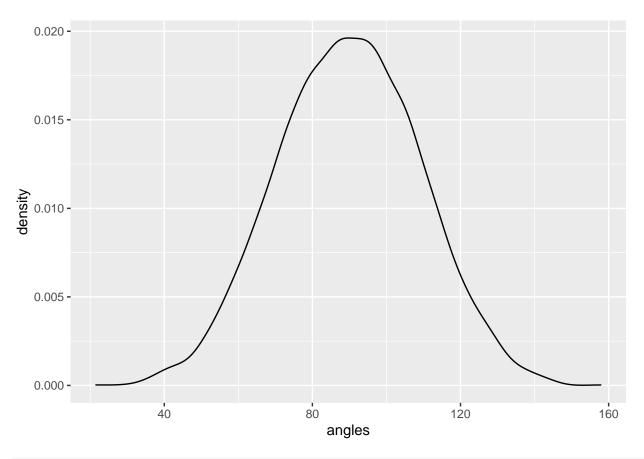
[79,] 109.30296

```
[80,] 98.57995
##
   [81,] 108.07978
##
##
   [82,] 89.13637
##
   [83,] 105.64172
##
   [84,] 99.10465
##
   [85,] 111.16878
##
   [86,] 92.61285
   [87,] 133.73024
##
##
   [88,] 49.41310
##
  [89,] 60.95005
  [90,] 64.26975
   [91,] 100.95113
##
##
   [92,] 119.04128
## [93,] 72.91321
##
   [94,] 127.74825
   [95,] 55.51334
##
## [96,] 89.64537
## [97,] 115.51882
## [98,] 85.71343
## [99,] 101.85334
## [100,]
                NA
```

Plot the density of these angles.

```
#TO-DO
#TO-DO
pacman:: p_load(ggplot2)
ggplot(data.frame(angles =c(all_angles(X))))+
  aes(x= angles)+
  geom_density()
```

Warning: Removed 5050 rows containing non-finite values (stat_density).



angle between 2 random vec on avarage they should be orthogonal

Write an Rcpp function all_angles_cpp that does the same thing. Use an IDE if you want, but write it below in-line.

```
#TO-DO in line rcpp function
cppFunction('
 NumericMatrix all_angles_cpp(NumericMatrix X) {
   int n = X.nrow();
   int p = X.ncol();
   NumericMatrix A(n, n);
   std::fill(A.begin(), A.end(), NA_REAL);
   for (int i_1 = 0; i_1 < (n - 1); i_1++){
     //Rcout << "computing for row #: " << (i_1 + 1) << "\\n";
     for (int i_2 = i_1 + 1; i_2 < n; i_2++){
       double sum_sqd_u = 0;
       double sum_sqd_v = 0;
       double sum_u_v = 0;
       for (int j = 0; j < p; j++){
          //sqd_diff += pow(X(i_1, j) - X(i_2, j), 2); //by default the cmath library in std is loaded
          sum_sqd_u += pow(X(i_1, j), 2);
          sum_sqd_v += pow(X(i_2, j), 2);
          sum_u_v += X(i_1, j) * X(i_2, j);
```

```
}
        A(i_1, i_2) = acos(sum_uv / sqrt(sum_sqd_u * sum_sqd_v)) * (180 / M_PI); //by default the cmat.
    }
    return A;
  }
')
head(all_angles_cpp(X))
##
        [,1]
                  [,2]
                            [,3]
                                       [,4]
                                                [,5]
                                                           [,6]
                                                                     [,7]
                                                                                [,8]
## [1,]
          NA 92.96163 126.14924
                                  91.33681 81.41249 108.04412 101.50051
   [2,]
##
          NA
                    NA
                        66.14781
                                  88.90066 78.21263 119.86235 130.65064
                                                                           85.92698
  [3,]
                              NA 104.77015 86.03254
                                                      96.71089 106.26462
          NA
                    NA
   [4,]
##
                                         NA 96.51874
                                                      77.04727 102.32236 111.46164
          NA
                    NA
                              NA
   [5,]
                    NA
                              NA
                                                      87.33802 112.38187 112.04775
##
          NA
                                         NA
                                                  NA
   [6,]
                    NA
                                                  NA
                                                             NA 82.00564 103.00972
##
          NA
                              NA
                                         NA
                                 [,11]
##
              [,9]
                       [,10]
                                            [,12]
                                                       [,13]
                                                                 [,14]
                                                                            [,15]
         56.13061 128.16096
                              96.33568
                                         63.07440 111.33446
                                                              90.36160 120.86324
## [1,]
         83.52186 81.97685
                              63.51225
                                        57.92624
## [2,]
                                                   74.79280
                                                              73.44154
## [3,]
         89.44478 61.06160 75.78117 104.52283
                                                  43.63118
                                                             64.37778
                                                                        63.78853
## [4,] 121.31606 113.90406 110.05262 106.71648 108.73637 107.72862
                                                                        65.86154
                                                   88.65334
  [5,] 103.20692 81.40243 106.03555
                                        62.47102
                                                              82.98753
                                                                        88.01526
   [6,] 110.09199 101.72663 113.46293 101.75819 111.99458
                                                              87.52168
                                                                        64.08977
##
            [,16]
                       [,17]
                                 [,18]
                                            [,19]
                                                       [,20]
                                                                 [,21]
                                                                            [,22]
## [1,]
         99.23899
                    67.30492
                              82.90617
                                        92.21570
                                                   79.39312 125.05783 108.08541
## [2,] 119.92448
                   75.33580 110.89758 121.58660
                                                   88.20434 103.02694
                    88.20636 105.22732
                                         78.42957
                                                   89.40283
                                                              62.27731
                                                                        83.43537
  [3,]
         91.65655
   [4,]
         87.78692
                    88.57858
                              97.81250
                                         79.00961 125.26780
                                                              95.22395
                                                                        77.55021
         69.08589
                    63.80883 113.69746
                                         91.27715
                                                   53.86534
                                                              68.58181 116.78681
   [5,]
         59.05590 116.55986
                              98.05791
                                         80.46275
                                                   93.18601
                                                              49.45812 114.07163
##
            [,23]
                       [,24]
                                  [,25]
                                            [,26]
                                                       [,27]
                                                                 [,28]
                                                                            [,29]
## [1,] 100.25705
                    67.70055 110.63606 115.41352
                                                   60.29615 129.80918
                                                                        69.38425
                   94.38858 119.70312
                                         72.43670
                                                   93.14959
                                                              85.63976
## [2,]
         56.58168
                                                                        93.43687
         81.19470 127.84397
## [3,]
                              75.57356
                                         50.51787 106.88566
                                                              65.31978 104.98930
                                                                        38.11183
## [4,]
         96.63428
                   53.81703
                              94.64061
                                        72.79703 117.68956
                                                              88.46679
  [5,]
         62.26077
                    84.45967 104.73476
                                         88.50339 103.02739
                                                              97.24426
                                                                        79.43648
         78.41951
                    74.48668
                              61.99312
                                         90.04270 107.83458
                                                              87.24298
                                                                        90.27612
##
   [6,]
            [,30]
                       [,31]
                                 [,32]
                                            [,33]
                                                       [,34]
                                                                 [,35]
                                                                            [,36]
                                                   73.74304
## [1,] 111.20300
                    82.90801
                              69.44965
                                         98.55994
                                                              69.80843 123.31421
## [2,]
         86.97624
                   67.81577
                              88.90540
                                         86.29554
                                                   97.01883 102.83419
                                                                        76.47578
                    61.11909 124.16422
                                         71.83129 130.30815
                                                              91.43575
## [3,]
         73.78741
                                                                        77.23622
## [4,]
         87.21083
                   79.99520
                              63.97809
                                         92.12547
                                                   68.06450
                                                              95.82753
                                                                        88.09594
   [5,]
         91.79708
                   86.09856 123.01233
                                         97.89656 106.08676
                                                              96.90609
                                                                        75.73459
         65.81474 102.21706
                              94.99740 107.60992 102.28214 111.50190
##
   [6,]
                                                                        94.61472
            [,37]
                       [,38]
                                  [,39]
                                            [,40]
                                                       [,41]
                                                                 [,42]
                                                                            [,43]
## [1,]
                                                   80.57686
         85.71328
                   88.87987 144.57788
                                         92.59273
                                                              64.36607
                                                                        95.39872
## [2,]
         95.24121 117.68412 104.63905
                                         51.87437
                                                   88.97980
                                                              63.93323
                                         64.91486 111.24698 104.50312
## [3,]
         91.80135
                   93.46660
                              72.03985
                                                                        74.74008
## [4,] 111.62249 93.47519
                              75.46330
                                         99.01045 82.70229 104.85690
                                                                        89.61710
## [5,] 109.47742 110.22272
                              99.76969
                                        73.77255 130.78212 93.77550
                                                                        73.06229
   [6,]
                   86.46539
                              73.12182 123.28868 101.82004 123.46690 122.27939
         99.67380
##
           [,44]
                      [,45]
                                [,46]
                                           [,47]
                                                     [,48]
                                                                [,49]
                                                                          [,50]
```

```
## [1,] 79.94970 67.82696 76.88869 50.70326 83.40976 66.07910 97.60072
## [2,] 64.04633 97.02177 109.18906 88.88024 69.18843 98.41018 82.02021
  [3,] 86.73173 87.95100 116.35391 126.05178 108.79968 84.08194
  [4,] 45.97527 109.40123 87.35857 72.43665 83.52017 129.06666 100.71600
  [5,] 76.20836 85.06165 108.58227 95.64211 117.52682 97.74362
                                                                  79.85530
  [6,] 91.75446 98.77601 87.36461 98.18558 99.58540 104.41210
                                                                  96.55655
           [,51]
                     [,52]
                              [,53]
                                       [,54]
                                                 [,55]
                                                           [,56]
                                                                     [,57]
## [1,] 96.28040 95.39164 86.99857 66.63064 120.46785
                                                        73.12799
                                                                  54.67292
## [2,] 112.37632 87.71696 77.53000 98.47164 114.62260 76.99140
                                                                  88.45843
  [3,] 110.14031 75.82208 68.55210 80.98278 72.38883 119.72577
                                                                  88.30409
  [4,] 65.21078 107.99719 136.13056 96.88779 95.32768 76.35538 113.20774
  [5,] 130.27883 115.77677 87.08733 66.63206 88.81302 80.67996 93.95176
        63.79206 90.16236 122.31089 75.38750 81.19408 100.81737 116.82594
           [,58]
                     [,59]
                             [,60]
                                        [,61]
                                                  [,62]
##
                                                            [,63]
## [1,] 126.81117 86.84353 104.69138 83.28171 85.89616 85.65498 109.82154
## [2,]
        95.01499 112.98407 87.41001 85.18562 104.48231 105.54867
        49.22614 113.98617 67.21112 79.10392 99.67253 92.79466
## [3,]
                                                                   80.88102
  [4,]
        92.78485 64.31990 78.59315 132.64871 112.30297 100.34142
        66.70054 137.73741 95.28994 74.56062 94.69651 59.21990
                                                                   61.21659
  [5,]
  [6.]
        66.81981 78.55979
                            77.74506 109.20083 83.49021 52.68843
                                                                  48.04190
##
           [,65]
                     [,66]
                               [,67]
                                         [,68]
                                                 [,69]
                                                           [,70]
                                                                     [,71]
        80.11754
                  90.51814 102.75331 76.51891 75.67960 114.10180 112.18659
## [1,]
       87.76240 77.69642 87.32514 122.06117 88.60525 62.38321
## [2,]
                                                                  83.61566
## [3,] 107.99509 72.23484 67.86783 114.61380 88.85589 52.88848
                                                                  90.59846
       85.99155 131.27303 115.17096 71.37069 72.36853 111.95753
  [4,]
  [5,]
        98.80936 92.73704 87.67547 108.26048 91.36396 91.50868
                                                                  60.81835
  [6,]
        83.69150 128.53731 74.10459 74.07603 65.60226
                                                        99.08473
                                                                  98.36323
                     [,73]
                               [,74]
           [,72]
                                       [,75]
                                                 [,76]
                                                           [,77]
                                                                     [,78]
## [1,] 110.41418 60.68545 114.08593 102.9991 125.18155 106.55911
                                                                  65.86617
                                                                  68.29867
## [2,]
        82.49636 92.83018 90.54822 107.8869 79.03979
                                                        37.21738
## [3,]
        79.36427 80.76970 65.31174 108.2137 52.34699
                                                        64.27151 101.11633
  [4,] 102.35784 91.78837 75.13896 95.8457 96.60974
                                                        84.87289
                                                                 70.58544
  [5,]
        98.24763 89.45079
                           77.78294 116.2963 81.63898 95.15731
                                                                  50.91598
        66.65454 117.40959 78.14549 72.1343 86.44351 123.81666
  [6,]
                                                                 84.77727
           [,79]
                    [08,]
                            [,81]
                                      [,82]
                                                [,83]
                                                          [,84]
                                                                    [,85]
## [1,] 112.78636 90.13496 124.25554 85.12431 94.95979 112.93388
                                                                97.54438
       90.74477 50.07845 80.75850 84.63440 75.05193 85.97629
## [3,] 73.01201 68.14990 62.02095 64.74728 97.02559 63.98014 112.51426
## [4,] 107.41239 75.90009 92.50272 120.62137 92.10283 97.45704
                                                                 98.66752
        61.03987 76.88850 115.66502 90.94790 60.05157 55.33888
## [5,]
                                                                 85.47923
        78.25788 89.33371 72.07398 101.40812 82.59217
                                                       95.62155
                                                                 84.94075
           [,86]
                     [,87]
                               [,88]
                                        [,89]
                                                [,90]
                                                          [,91]
                                                                    [,92]
## [1,]
        87.55629 117.30465 65.27000 59.49894 65.49559 91.27943 106.23791
        78.12841 77.97323 114.69685 84.17390 69.00798 104.86763 61.26024
## [2,]
        75.25660 88.63362 127.41933 90.87544 89.27728 108.73543 81.15022
        88.65919 100.66546 95.52494 73.71937 94.65139 73.62849 110.54857
## [5,] 100.98971 75.19209
                            96.53697 91.59301 82.43354 61.26896 72.15026
## [6,]
        74.89693 81.73531
                            79.75560 94.26199 98.77007 59.49791 100.51878
           [,93]
                     [,94]
                              [,95]
                                         [,96]
                                                  [,97]
                                                            [,98]
## [1,]
        74.10660 105.48932
                           45.69325
                                     75.24901 114.81986 106.25030 105.51880
## [2,]
        86.92835 58.23375 88.60820 78.45310 90.19446 99.25227 94.46381
## [3,]
        95.85172 57.43475 97.69407 67.63838 96.23143 85.59857 98.42304
## [4,]
        85.29711 101.71365 73.34972 83.54354 85.34160 103.83357 69.01372
## [5,] 70.58725 76.83118 101.00191 100.77204 111.35792 96.99153 112.09838
```

```
## [6,] 123.27274 99.53267 114.19866 101.55555 104.25807 65.85917 60.47265
## [,100]
## [1,] 41.37340
## [2,] 117.53819
## [3,] 121.66252
## [4,] 100.91451
## [5,] 95.25365
## [6,] 95.16299
```

Test the time difference between these functions for n = 1000 and Nvec = 100, 500, 1000, 5000 using the package microbenchmark. Store the results in a matrix with rows representing Nvec and two columns for base R and Rcpp.

```
pacman::p_load(microbenchmark)

n = 1000
Nvec = c(100,500, 1000, 5000)

X = matrix(data = rnorm(Nvec*n), nrow = 100)
timer =microbenchmark(all_angles(X), all_angles_cpp(X), times =10)
```

```
## Warning in acos(sum(u * v)/sqrt(sum(u^2) * sum(v^2))): NaNs produced
## Warning in acos(sum(u * v)/sqrt(sum(u^2) * sum(v^2))): NaNs produced
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## Warning in acos(sum(u * v)/sqrt(sum(u^2) * sum(v^2))): NaNs produced
## Warning in acos(sum(u * v)/sqrt(sum(u^2) * sum(v^2))): NaNs produced
## Warning in acos(sum(u * v)/sqrt(sum(u^2) * sum(v^2))): NaNs produced
timer
```

```
## Unit: microseconds
## expr min lq mean median uq
## all_angles(X) 77631.367 114780.43 173283.6292 153068.8115 247354.211
## all_angles_cpp(X) 59.983 70.42 234.1121 102.3785 133.394
```

```
## max neval

## 268912.437 10

## 1465.035 10

#cpp should be faster by 20x
```

Plot the divergence of performance (in log seconds) over n using a line geometry. Use two different colors for the R and CPP functions. Make sure there's a color legend on your plot. We wil see later how to create "long" matrices that make such plots easier.

```
#TO-DO

#pacman::p_load(ggplot2)
#ggplot()+

#geom_line()+
#aes(y= Nvec, x= log(timer))
```

Let Nvec = 10000 and vary n to be 10, 100, 1000. Plot the density of angles for all three values of n on one plot using color to signify n. Make sure you have a color legend. This is not easy.

```
#T0-D0
#ggplot() +
# geom\_line(aes(x = Nvec, y = log(timer), col = "time-R")) +
# geom\_line(aes(x = Nvec, y = log(time\_cpp), col = "time-Rcpp")) +
# xlab("Number of Columns") +
 # ylab("Time in seconds")
#Nvec = 10000
\#X < - c()
#for (i in 1:10){
\# x \leftarrow rnorm(Nvec)
\# X \leftarrow cbind(X, x)
#}
###r (i in 1:100){
\# x \leftarrow rnorm(Nvec)
\# X \leftarrow cbind(X, x)
#}
#ang2 <- all_angles(X)
\#X < - c()
#for (i in 1:1000){
# x <- rnorm(Nvec)
\#X \leftarrow cbind(X, x)
#ang3 <- all_angles(X)
#ggplot() +
\# geom\_density(aes(x = ang1, fill = "red"), alpha = .4) +
\#geom\_density(aes(x = ang2, fill = "blue"), alpha = .4) +
\#geom\_density(aes(x = ang3, fill = "green"), alpha = .4) +
\#scale\_fill\_discrete(labels = c("n=10", "n=100", "n=1000"))
```

Write an R function nth_fibonnaci that finds the nth Fibonnaci number via recursion but allows you to

specify the starting number. For instance, if the sequency started at 1, you get the familiar 1, 1, 2, 3, 5, etc. But if it started at 0.01, you would get 0.01, 0.01, 0.02, 0.03, 0.05, etc.

```
#TO-DO
cppFunction("
  double nth_fibonnaci_cpp(int n, double start){
    if (n-1 <= 1)
        return start;
    return nth_fibonnaci_cpp(n-1, start) + nth_fibonnaci_cpp(n-2, start);
}
    ")</pre>
```

Write an Rcpp function nth_fibonnaci_cpp that does the same thing. Use an IDE if ou want, but write it below in-line.

```
#TO-DO
nth_fibonacci <- function(n, start){
  if (n == 1 | n == 2) return(start)
  else return(nth_fibonacci(n-1, start) + nth_fibonacci(n-2, start))
}
nth_fibonacci(8, 1)</pre>
```

```
## [1] 21
```

```
cppFunction(
  'double nth_fibonacci_cpp(int n, double start){
   if (n == 1 || n == 2) return start;
   else return (nth_fibonacci_cpp(n-1, start) + nth_fibonacci_cpp(n-2, start));
  }'
)
nth_fibonacci_cpp(5, 1)
```

[1] 5

Time the difference in these functions for $n = 100, 200, \ldots, 1500$ while starting the sequence at the smallest possible floating point value in R. Store the results in a matrix.

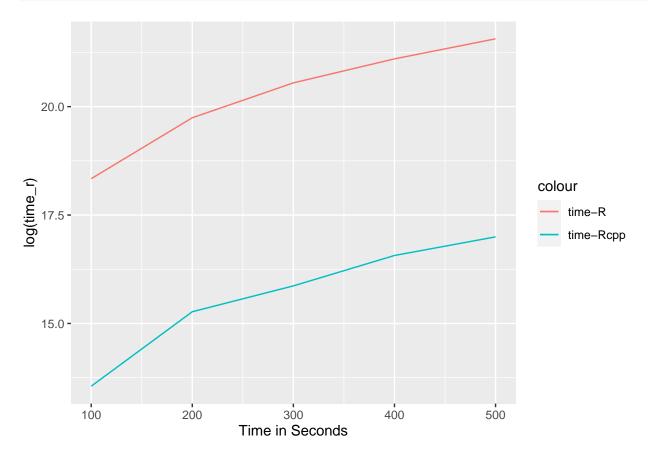
```
#TO-DO

pacman::p_load(microbenchmark)

n <- 100
Nvec <- c(100, 200, 300, 400, 500)
time_r <- c()
time_cpp <- c()
for (i in 1:length(Nvec)){
    X <- c()
    for (j in 1:n){
        x <- rnorm(Nvec[i])
        X <- cbind(X, x)
    }
    time_r <- c(time_r, mean(microbenchmark(angles_r = all_angles(X), times = 3, unit = "s")$time))
    time_cpp <- c(time_cpp, mean(microbenchmark(angles_cpp = all_angles_cpp(X), times = 3, unit = "s")$time})</pre>
```

Plot the divergence of performance (in log seconds) over n using a line geometry. Use two different colors for the R and CPP functions. Make sure there's a color legend on your plot.

```
pacman::p_load(ggplot2)
ggplot() +
  geom_line(aes(x = Nvec, y = log(time_r), col = "time-R")) +
  geom_line(aes(x = Nvec, y = log(time_cpp), col = "time-Rcpp")) +
  xlab("Time in Seconds")
```



Data Wrangling / Munging / Carpentry

Throughout this assignment you can use either the tidyverse package suite or data.table to answer but not base R. You can mix data.table with magrittr piping if you wish but don't go back and forth between tbl_df's and data.table objects.

```
#pacman::p_load(tidyverse, magrittr, data.table)
pacman::p_load(dplyr, magrittr, data.table)
```

Load the storms dataset from the dplyr package and investigate it using str and summary and head. Which two columns should be converted to type factor? Do so below.

```
#TO-DO
data(storms)
str(storms)
```

```
## tibble[,13] [10,010 x 13] (S3: tbl_df/tbl/data.frame)
                 : chr [1:10010] "Amy" "Amy" "Amy" "Amy" ...
##
   $ name
   $ year
                 : num [1:10010] 1975 1975 1975 1975 ...
                 : num [1:10010] 6 6 6 6 6 6 6 6 6 6 ...
##
   $ month
##
   $ day
                 : int [1:10010] 27 27 27 27 28 28 28 28 29 29 ...
##
                 : num [1:10010] 0 6 12 18 0 6 12 18 0 6 ...
  $ hour
                 : num [1:10010] 27.5 28.5 29.5 30.5 31.5 32.4 33.3 34 34.4 34 ...
                 : num [1:10010] -79 -79 -79 -79 -78.8 -78.7 -78 -77 -75.8 -74.8 ...
##
   $ long
##
                 : chr [1:10010] "tropical depression" "tropical depression" "tro
   $ status
                 : Ord.factor w/ 7 levels "-1"<"0"<"1"<"2"<...: 1 1 1 1 1 1 1 2 2 ...
##
   $ category
                 : int [1:10010] 25 25 25 25 25 25 25 30 35 40 ...
  $ wind
                 : int [1:10010] 1013 1013 1013 1013 1012 1012 1011 1006 1004 1002 ...
##
   $ ts_diameter: num [1:10010] NA ...
   $ hu_diameter: num [1:10010] NA ...
head(storms)
## # A tibble: 6 x 13
##
           year month
                         day hour
                                     lat long status
                                                            category wind pressure
     <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                             <ord>
                                                                      <int>
                                                                               <int>
## 1 Amy
            1975
                          27
                                 0
                                    27.5 - 79
                                               tropical de~ -1
                                                                                1013
                     6
## 2 Amy
            1975
                     6
                          27
                                 6
                                    28.5 - 79
                                               tropical de~ -1
                                                                         25
                                                                                1013
## 3 Amy
                                12
                                    29.5 -79
                                               tropical de~ -1
                                                                         25
                                                                                1013
            1975
                     6
                          27
## 4 Amy
            1975
                     6
                          27
                                18
                                    30.5 - 79
                                               tropical de~ -1
                                                                         25
                                                                                1013
## 5 Amy
            1975
                          28
                                    31.5 -78.8 tropical de~ -1
                                                                         25
                                                                                1012
                     6
                                 0
            1975
                     6
                          28
                                 6 32.4 -78.7 tropical de~ -1
                                                                         25
                                                                                1012
## 6 Amy
## # ... with 2 more variables: ts_diameter <dbl>, hu_diameter <dbl>
```

#category = how bad the storm is

Reorder the columns so name is first, status is second, category is third and the rest are the same.

```
storms%>%
select(name, status, category, everything())
```

```
## # A tibble: 10,010 x 13
##
      name status
                        category year month
                                                day hour
                                                            lat long wind pressure
##
      <chr> <chr>
                        <ord>
                                  <dbl> <dbl> <int> <dbl> <dbl> <int>
                                                                                 1013
##
  1 Amy
            tropical d~ -1
                                  1975
                                                 27
                                                        0
                                                           27.5 - 79
                                            6
##
    2 Amy
            tropical d~ -1
                                   1975
                                            6
                                                 27
                                                           28.5 - 79
                                                                          25
                                                                                 1013
##
  3 Amy
            tropical d~ -1
                                            6
                                                           29.5 -79
                                                                          25
                                                                                 1013
                                   1975
                                                 27
                                                       12
            tropical d~ -1
  4 Amy
                                   1975
                                            6
                                                 27
                                                       18
                                                           30.5 - 79
                                                                                 1013
                                                                                 1012
## 5 Amy
            tropical d~ -1
                                   1975
                                            6
                                                 28
                                                        0
                                                           31.5 -78.8
                                                                          25
##
   6 Amy
            tropical d~ -1
                                  1975
                                            6
                                                 28
                                                        6
                                                           32.4 - 78.7
                                                                          25
                                                                                 1012
                                            6
                                                 28
                                                           33.3 -78
                                                                          25
##
            tropical d~ -1
                                  1975
                                                       12
                                                                                 1011
  7 Amy
   8 Amy
            tropical d~ -1
                                  1975
                                            6
                                                 28
                                                       18
                                                           34
                                                                 -77
                                                                          30
                                                                                 1006
                                                           34.4 -75.8
                                                                                 1004
            tropical s~ 0
                                  1975
                                            6
                                                 29
                                                        0
                                                                          35
##
   9 Amy
                                                                                 1002
## 10 Amy
            tropical s~ 0
                                  1975
                                            6
                                                 29
                                                        6
                                                           34
                                                                -74.8
## # ... with 10,000 more rows, and 2 more variables: ts_diameter <dbl>,
      hu_diameter <dbl>
```

Find a subset of the data of storms only in the 1970's.

```
#TO-DO
storms%>%
  filter(year>= 1970 & year <= 1979)</pre>
```

```
## # A tibble: 546 x 13
##
      name
             year month
                           day hour
                                        lat long status
                                                               category wind pressure
##
      <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                               <ord>
                                                                         <int>
                                                                                  <int>
##
   1 Amy
             1975
                       6
                            27
                                   0 27.5 -79
                                                  tropical d~ -1
                                                                            25
                                                                                   1013
## 2 Amy
             1975
                            27
                                   6 28.5 -79
                                                                            25
                                                                                   1013
                       6
                                                  tropical d~ -1
##
   3 Amy
             1975
                       6
                            27
                                  12 29.5 -79
                                                  tropical d~ -1
                                                                            25
                                                                                   1013
## 4 Amy
                            27
                                                                            25
             1975
                       6
                                  18 30.5 -79
                                                  tropical d~ -1
                                                                                   1013
                                                                                   1012
## 5 Amy
             1975
                       6
                            28
                                   0
                                      31.5 -78.8 tropical d~ -1
                                                                            25
## 6 Amy
                            28
                                      32.4 - 78.7 \text{ tropical } d^{-1}
                                                                            25
                                                                                   1012
             1975
                       6
                                   6
##
   7 Amy
             1975
                       6
                            28
                                  12
                                      33.3 -78
                                                  tropical d~ -1
                                                                            25
                                                                                   1011
## 8 Amy
                            28
                                            -77
                                                                            30
                                                                                   1006
             1975
                       6
                                  18
                                     34
                                                  tropical d~ -1
                                      34.4 -75.8 tropical s~ 0
## 9 Amy
             1975
                            29
                                   0
                                                                            35
                                                                                   1004
             1975
                                            -74.8 tropical s~ 0
                                                                            40
                                                                                   1002
## 10 Amy
                       6
                            29
                                   6 34
## # ... with 536 more rows, and 2 more variables: ts_diameter <dbl>,
     hu_diameter <dbl>
```

Find a subset of the data of storm observations only with category 4 and above and wind speed 100MPH and above.

```
#TO-DO
storms%>%
filter(category >= 4 & wind >= 100)
```

```
## # A tibble: 416 x 13
##
     name
            year month
                                      lat long status
                                                          category wind pressure
                          day hour
      <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                                    <int>
                                                                             <int>
   1 Anita 1977
                                                                               931
##
                      9
                            2
                                  0
                                     24.6 -96.2 hurricane 5
                                                                      140
                      9
                            2
##
   2 Anita 1977
                                  6
                                     24.2 -97.1 hurricane 5
                                                                      150
                                                                               926
##
   3 Anita 1977
                      9
                            2
                                 12 23.7 -98
                                                hurricane 4
                                                                      120
                                                                               940
  4 David 1979
                      8
                           28
                                    12.2 -52.9 hurricane 4
                                                                      115
                                                                               947
## 5 David 1979
                                  6 12.5 -54.4 hurricane 4
                      8
                           28
                                                                      125
                                                                               941
   6 David 1979
                           28
##
                      8
                                 12
                                     12.8 -55.7 hurricane 4
                                                                      130
                                                                               938
##
  7 David 1979
                      8
                           28
                                 18 13.2 -56.9 hurricane 4
                                                                      125
                                                                               941
  8 David 1979
                      8
                           29
                                  0 13.7 -58
                                                hurricane 4
                                                                      120
                                                                               944
## 9 David 1979
                      8
                           29
                                  6
                                     14.2 -59.2 hurricane 4
                                                                      120
                                                                               942
## 10 David 1979
                      8
                           29
                                 12 14.8 -60.3 hurricane 4
                                                                      125
                                                                               938
## # ... with 406 more rows, and 2 more variables: ts_diameter <dbl>,
      hu_diameter <dbl>
```

Create a new feature wind_speed_per_unit_pressure.

```
#TO-DO
storms%>%
  mutate(wind_speed_per_unit_pressure = wind/pressure)
```

A tibble: 10,010 x 14

```
##
      name
              vear month
                            day hour
                                         lat long status
                                                                  category wind pressure
##
      <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                                  <ord>
                                                                            <int>
                                                                                      <int>
                                                    tropical d~ -1
##
    1 Amy
              1975
                        6
                             27
                                        27.5 - 79
                                                                               25
                                                                                       1013
                             27
                                        28.5 -79
                                                                               25
                                                                                       1013
##
    2 Amy
              1975
                        6
                                     6
                                                     tropical d~ -1
##
    3 Amy
              1975
                        6
                             27
                                    12
                                        29.5 - 79
                                                    tropical d~ -1
                                                                               25
                                                                                       1013
                                                                               25
##
    4 Amy
              1975
                        6
                             27
                                       30.5 -79
                                                     tropical d~ -1
                                                                                       1013
                                    18
##
    5 Amy
              1975
                        6
                             28
                                     0
                                        31.5 -78.8 tropical d~ -1
                                                                               25
                                                                                       1012
                                        32.4 -78.7 tropical d~ -1
##
    6 Amy
              1975
                        6
                             28
                                     6
                                                                               25
                                                                                       1012
##
    7 Amy
              1975
                        6
                             28
                                    12
                                        33.3 -78
                                                     tropical d~ -1
                                                                               25
                                                                                       1011
##
    8 Amy
              1975
                        6
                             28
                                    18
                                        34
                                              -77
                                                     tropical d~ -1
                                                                               30
                                                                                       1006
##
    9 Amy
              1975
                        6
                             29
                                     0
                                        34.4 - 75.8 \text{ tropical s} \sim 0
                                                                               35
                                                                                       1004
              1975
                             29
                                                                                       1002
## 10 Amy
                        6
                                     6
                                        34
                                              -74.8 tropical s~ 0
                                                                               40
## # ... with 10,000 more rows, and 3 more variables: ts_diameter <dbl>,
       hu_diameter <dbl>, wind_speed_per_unit_pressure <dbl>
```

Create a new feature: average_diameter which averages the two diameter metrics. If one is missing, then use the value of the one that is present. If both are missing, leave missing.

```
storms%>%
  rowwise()%>%
  arrange(desc(year))%>%
  mutate(average_diameter = mean(c(ts_diameter, hu_diameter) , na.rm =TRUE) )
## # A tibble: 10,010 x 14
## # Rowwise:
##
                                       lat long status
      name
             year month
                           day
                                hour
                                                               category
                                                                         wind pressure
##
      <chr> <dbl> <dbl> <int> <dbl> <dbl> <dbl> <dbl> <chr>
                                                               <ord>
                                                                        <int>
                                                                                  <int>
##
   1 Ana
             2015
                      5
                             9
                                   6 32.2 - 77.5 \text{ tropical s} \sim 0
                                                                           50
                                                                                    998
                       5
##
   2 Ana
             2015
                             9
                                  12 32.5 -77.8 tropical s~ 0
                                                                           50
                                                                                   1001
## 3 Ana
                                                                                   1001
             2015
                      5
                             9
                                  18 32.7 -78
                                                  tropical s~ 0
                                                                           45
## 4 Ana
             2015
                      5
                            10
                                   0
                                      33.1 -78.3 tropical s~ 0
                                                                           45
                                                                                   1001
                                                                           40
## 5 Ana
             2015
                      5
                            10
                                   6 33.5 -78.6 tropical s~ 0
                                                                                   1002
## 6 Ana
             2015
                      5
                            10
                                  10 33.8 -78.8 tropical s~ 0
                                                                           40
                                                                                   1002
                                                                           35
                                                                                   1002
## 7 Ana
             2015
                      5
                            10
                                  12 33.9 -78.8 tropical s~ 0
                       5
                                                                           30
                                                                                   1006
##
   8 Ana
             2015
                            10
                                  18
                                      34.3 -78.7 tropical d~ -1
## 9 Ana
             2015
                       5
                                                                           30
                                                                                   1009
                            11
                                   0
                                      34.7 -78.5 tropical d~ -1
## 10 Ana
             2015
                       5
                                   6 35.5 -78
                                                                                   1010
                            11
                                                  tropical d~ -1
## # ... with 10,000 more rows, and 3 more variables: ts_diameter <dbl>,
       hu_diameter <dbl>, average_diameter <dbl>
#we need a vector mean function
#the mean function does the entire matrx and not row by row
#hw
```

For each storm, summarize the maximum wind speed. "Summarize" means create a new dataframe with only the summary metrics you care about.

```
#TO-DO
storms%>%
  group_by(name)%>%
  summarise(max_wind_speed = max(wind, na.rm= TRUE))
```

```
## # A tibble: 198 x 2
##
     name max_wind_speed
##
      <chr>
                       <int>
                          30
  1 AL011993
##
##
   2 AL012000
                           25
## 3 AL021992
                           30
  4 AL021994
##
                           30
## 5 AL021999
                           30
## 6 AL022000
                           30
                           25
## 7 AL022001
## 8 AL022003
                           30
## 9 AL022006
                           45
## 10 AL031987
                           40
## # ... with 188 more rows
```

Order your dataset by maximum wind speed storm but within the rows of storm show the observations in time order from early to late.

```
#T0-D0
storms%>%
group_by(name)%>%
  mutate(max_wind_storm =max(wind, na.rm = TRUE))%>%
  select(name, max_wind_storm, everything())%>%
  arrange(max_wind_storm, year, day, hour)
## # A tibble: 10,010 x 14
## # Groups: name [198]
##
     name max_wind_storm year month
                                         day hour
                                                     lat long status
                                                                          category
##
                    <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dr>
      <chr>
                                                                          <ord>
##
   1 AL101~
                        25 1991
                                  10
                                          24
                                                12 13.4 -42.3 tropical ~ -1
   2 AL101~
                        25 1991
                                    10
                                                18 13.7 -43.6 tropical ~ -1
##
```

24 ## 3 AL101~ 25 1991 10 25 0 13.8 -44.9 tropical ~ -1 10 6 14 25 1991 25 ## 4 AL101~ -46.4 tropical ~ -1 ## 5 AL101~ 25 1991 10 25 12 14.1 -47.7 tropical ~ -1 25 2000 18 21 ## 6 AL012~ 6 7 -93 tropical ~ -1 7 AL012~ 25 2000 6 8 0 20.9 -92.8 tropical ~ -1 ## 25 2000 6 6 20.7 -93.1 tropical ~ -1 ## 8 AL012~ 8 ## 9 AL012~ 25 2000 12 20.8 -93.5 tropical ~ -1 6 8 ## 10 AL022~ 25 2001 7 11 18 10.9 -42.1 tropical ~ -1 ## # ... with 10,000 more rows, and 4 more variables: wind <int>, pressure <int>,

Find the strongest storm by wind speed per year.

ts_diameter <dbl>, hu_diameter <dbl>

```
#TO-DO
storms%>%
  group_by(year)%>%
  arrange(desc(wind))%>%
  slice(1)%>% #wil give us the first row
  select(name, year)
```

A tibble: 41 x 2

```
## # Groups:
              year [41]
##
     name
              year
##
     <chr>
              <dbl>
## 1 Caroline 1975
## 2 Belle
               1976
## 3 Anita
               1977
## 4 Cora
              1978
## 5 David
              1979
## 6 Ivan
              1980
## 7 Harvey
               1981
## 8 Debby
               1982
## 9 Alicia
               1983
## 10 Diana
               1984
## # ... with 31 more rows
```

returning -Inf

returning -Inf

returning -Inf

For each named storm, find its maximum category, wind speed, pressure and diameters. Do not allow the max to be NA (unless all the measurements for that storm were NA).

```
#TO-DO
storms%>%
  group_by(name)%>%
  mutate(max_pressure = max(pressure, na.rm =TRUE))%>%
  mutate(max_wind_speed =max(wind, na.rm = TRUE))%>%
  mutate( max_ts_diameter = max(ts_diameter, na.rm =TRUE))%>%
  mutate(max_hu_diameter = max(hu_diameter, na.rm =TRUE))%>%
  select(max_pressure, max_wind_speed, max_ts_diameter,max_hu_diameter)%>%
  #arrange(name)
  distinct

## Warning in max(ts_diameter, na.rm = TRUE): no non-missing arguments to max;
## returning -Inf

## Warning in max(ts_diameter, na.rm = TRUE): no non-missing arguments to max;
## returning -Inf
```

Warning in max(ts_diameter, na.rm = TRUE): no non-missing arguments to max;

Warning in max(ts_diameter, na.rm = TRUE): no non-missing arguments to max;

Warning in max(ts_diameter, na.rm = TRUE): no non-missing arguments to max;

```
## Warning in max(ts_diameter, na.rm = TRUE): no non-missing arguments to max;
## returning -Inf
## Warning in max(ts_diameter, na.rm = TRUE): no non-missing arguments to max;
## returning -Inf
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## Warning in max(hu_diameter, na.rm = TRUE): no non-missing arguments to max;
## returning -Inf
## Warning in max(hu_diameter, na.rm = TRUE): no non-missing arguments to max;
## returning -Inf
## Adding missing grouping variables: 'name'
## # A tibble: 198 x 5
## # Groups: name [198]
##
              max_pressure max_wind_speed max_ts_diameter max_hu_diameter
     name
```

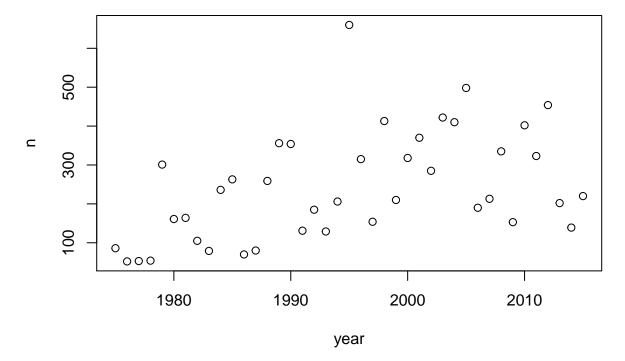
```
##
       <chr>
                        <int>
                                         <int>
                                                           <dbl>
                                                                             <dbl>
##
    1 Amy
                          1013
                                             60
                                                            -Inf
                                                                              -Inf
##
    2 Caroline
                          1014
                                           100
                                                            -Inf
                                                                              -Inf
    3 Doris
                          1005
##
                                            95
                                                            -Inf
                                                                              -Inf
##
    4 Belle
                          1012
                                           105
                                                            -Inf
                                                                              -Inf
##
    5 Gloria
                          1009
                                                            -Inf
                                                                              -Inf
                                           125
##
    6 Anita
                          1012
                                           150
                                                            -Inf
                                                                              -Inf
                                                                              -Inf
    7 Clara
                                                            -Inf
##
                          1015
                                             65
##
    8 Evelyn
                          1010
                                             70
                                                            -Inf
                                                                              -Inf
##
    9 Amelia
                                             45
                                                            -Inf
                                                                              -Inf
                          1010
## 10 Bess
                          1012
                                             45
                                                            -Inf
                                                                              -Inf
## # ... with 188 more rows
```

```
# summarise(max_wind_speed = max(wind, na.rm= TRUE))
data(storms)
```

For each year in the dataset, tally the number of storms. "Tally" is a fancy word for "count the number of". Plot the number of storms by year. Any pattern?

```
#TO-DO

storms%>%
  group_by(year)%>%
  tally()%>%
  plot
```



#the number of stomers per year seems to increase and the storms also seem to be seasonal

For each year in the dataset, tally the storms by category.

```
storms%>%
 group_by(year,category)%>%
 summarise(tally = n())
## 'summarise()' has grouped output by 'year'. You can override using the '.groups' argument.
## # A tibble: 233 x 3
## # Groups:
              year [41]
      year category tally
##
      <dbl> <ord>
                    <int>
##
   1 1975 -1
                       30
##
  2 1975 0
                       33
##
  3 1975 1
                       12
## 4 1975 2
                        9
                        2
## 5 1975 3
## 6 1976 -1
                       10
## 7 1976 0
                       20
## 8 1976 1
                       10
## 9 1976 2
                        9
## 10 1976 3
                        3
## # ... with 223 more rows
For each year in the dataset, find the maximum wind speed per status level.
storms%>%
 group_by(year, status)%>%
 summarise(max_wind_speed = max(wind))
## 'summarise()' has grouped output by 'year'. You can override using the '.groups' argument.
## # A tibble: 123 x 3
## # Groups:
              year [41]
##
      year status
                               max_wind_speed
##
     <dbl> <chr>
                                        <int>
## 1 1975 hurricane
                                          100
##
   2 1975 tropical depression
                                           30
## 3 1975 tropical storm
                                           60
## 4 1976 hurricane
                                          105
```

For each storm, summarize its average location in latitude / longitude coordinates.

5 1976 tropical depression

8 1977 tropical depression

6 1976 tropical storm

9 1977 tropical storm

... with 113 more rows

7 1977 hurricane

10 1978 hurricane

30

60

150

30

60

80

```
#T0-D0
storms%>%
  group_by(name)%>%
  summarize(average_latitude = mean(lat), avrage_longitude = mean(long))
## # A tibble: 198 x 3
##
     name
              average_latitude avrage_longitude
##
      <chr>
                          <dbl>
                                           <dbl>
##
  1 AL011993
                          24.7
                                           -78.0
## 2 AL012000
                          20.8
                                           -93.1
                          26.7
## 3 AL021992
                                           -84.5
## 4 AL021994
                          33.6
                                           -79.7
## 5 AL021999
                          20.4
                                           -96.4
## 6 AL022000
                          9.9
                                           -28.5
```

-45.3

-43.4

-63.5

-88.7

For each storm, summarize its duration in number of hours (to the nearest 6hr increment).

11.9

41.3

30.8

9.62

```
#TO-DO
storms%>%
  group_by(name)%>%

#summarise(neareast_6hr_increment = round((hour)/6)) nope
mutate(duration = (n()-1)*6)%>%
select(name, duration)%>%
distinct
```

```
## # A tibble: 198 x 2
## # Groups: name [198]
##
     name
              duration
##
                 <dbl>
      <chr>
                   174
##
  1 Amy
## 2 Caroline
                   192
## 3 Doris
                   132
## 4 Belle
                   102
## 5 Gloria
                   744
## 6 Anita
                   114
## 7 Clara
                   138
## 8 Evelyn
                    48
## 9 Amelia
                    30
## 10 Bess
                    72
## # ... with 188 more rows
```

7 AL022001

8 AL022003

9 AL022006

10 AL031987

... with 188 more rows

For storm in a category, create a variable storm_number that enumerates the storms 1, 2, ... (in date order).

```
#TO-DO
storms%>%
```

```
group_by(name)%>%
mutate(storm_number =dense_rank(paste(year,month,day)))
## # A tibble: 10,010 x 14
                name [198]
  # Groups:
##
              year month
                                                                            wind pressure
      name
                                 hour
                                         lat long status
                                                                 category
                            day
##
      <chr>
             <dbl> <dbl> <int>
                                <dbl> <dbl> <dbl> <chr>
                                                                 <ord>
                                                                           <int>
                                                                                     <int>
##
              1975
                             27
                                    0
                                        27.5 - 79
                                                                              25
                                                                                      1013
    1 Amy
                        6
                                                    tropical d~ -1
##
    2 Amy
              1975
                        6
                             27
                                        28.5 - 79
                                                    tropical d~ -1
                                                                              25
                                                                                      1013
                             27
                                                                              25
##
    3 Amy
              1975
                                       29.5 -79
                                                    tropical d~ -1
                                                                                      1013
                        6
                                    12
##
    4 Amy
              1975
                        6
                             27
                                    18
                                       30.5 - 79
                                                    tropical d~ -1
                                                                              25
                                                                                      1013
                                                                              25
                                                                                      1012
##
   5 Amy
              1975
                        6
                             28
                                    0
                                       31.5 -78.8 tropical d~ -1
##
    6 Amy
              1975
                        6
                             28
                                    6
                                        32.4 -78.7 tropical d~ -1
                                                                              25
                                                                                      1012
                                                                                      1011
##
    7 Amy
              1975
                        6
                             28
                                    12
                                        33.3 -78
                                                    tropical d~ -1
                                                                              25
##
    8 Amy
              1975
                        6
                             28
                                        34
                                             -77
                                                    tropical d~ -1
                                                                              30
                                                                                      1006
                                    18
                        6
                             29
                                        34.4 - 75.8 \text{ tropical s} \sim 0
                                                                              35
                                                                                      1004
##
  9 Amy
              1975
                                    0
              1975
                        6
                                                                                      1002
## 10 Amy
                             29
                                    6
                                       34
                                             -74.8 tropical s~ 0
                                                                              40
## # ... with 10,000 more rows, and 3 more variables: ts_diameter <dbl>,
       hu diameter <dbl>, storm number <int>
```

Convert year, month, day, hour into the variable timestamp using the lubridate package. Although the new package clock just came out, lubridate still seems to be standard. Next year I'll probably switch the class to be using clock.

```
#TO-DO
pacman::p_load(lubridate)
storms%>%
  mutate(timestamp =make_datetime(year, month, day, hour))%>%
  select(timestamp, everything())
```

```
## # A tibble: 10,010 x 14
##
      timestamp
                                  year month
                                                     hour
                                                            lat
                                                                long status category
                           name
                                                day
##
      <dttm>
                           <chr>
                                 <dbl> <dbl>
                                                    <dbl> <dbl> <chr> <ord>
                                             <int>
##
    1 1975-06-27 00:00:00 Amy
                                  1975
                                            6
                                                 27
                                                        0
                                                           27.5 - 79
                                                                       tropi~ -1
##
    2 1975-06-27 06:00:00 Amy
                                  1975
                                            6
                                                 27
                                                           28.5 - 79
                                                                       tropi~ -1
                                                        6
    3 1975-06-27 12:00:00 Amy
                                  1975
                                            6
                                                 27
                                                       12
                                                           29.5 - 79
                                                                       tropi~ -1
##
    4 1975-06-27 18:00:00 Amy
                                  1975
                                            6
                                                 27
                                                       18
                                                           30.5 -79
                                                                       tropi~ -1
                                                           31.5 -78.8 tropi~ -1
##
    5 1975-06-28 00:00:00 Amy
                                  1975
                                            6
                                                 28
                                                        0
##
   6 1975-06-28 06:00:00 Amy
                                  1975
                                            6
                                                 28
                                                           32.4 -78.7 tropi~ -1
                                                        6
   7 1975-06-28 12:00:00 Amy
                                  1975
                                            6
                                                 28
                                                       12
                                                           33.3 -78
                                                                       tropi~ -1
                                                       18
##
   8 1975-06-28 18:00:00 Amy
                                  1975
                                            6
                                                 28
                                                           34
                                                                 -77
                                                                       tropi~ -1
## 9 1975-06-29 00:00:00 Amy
                                  1975
                                            6
                                                 29
                                                        0
                                                           34.4 -75.8 tropi~ 0
## 10 1975-06-29 06:00:00 Amy
                                  1975
                                            6
                                                 29
                                                        6
                                                           34
                                                                 -74.8 tropi~ 0
## # ... with 10,000 more rows, and 4 more variables: wind <int>, pressure <int>,
       ts_diameter <dbl>, hu_diameter <dbl>
```

Using the lubridate package, create new variables day_of_week which is a factor with levels "Sunday", "Monday", ... "Saturday" and week of year which is integer 1, 2, ..., 52.

```
#TO-DO
storms %>%
```

```
## # A tibble: 10,010 x 16
##
                          day hour
             year month
                                       lat long status
                                                              category wind pressure
##
      <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                                       <int>
                                                              <ord>
                                                                                <int>
##
   1 Amy
             1975
                      6
                           27
                                   0 27.5 -79
                                                 tropical d~ -1
                                                                          25
                                                                                 1013
                                     28.5 -79
##
   2 Amy
             1975
                      6
                           27
                                   6
                                                 tropical d~ -1
                                                                          25
                                                                                 1013
## 3 Amy
             1975
                      6
                           27
                                  12 29.5 -79
                                                 tropical d~ -1
                                                                          25
                                                                                 1013
## 4 Amy
             1975
                      6
                           27
                                 18 30.5 -79
                                                 tropical d~ -1
                                                                          25
                                                                                 1013
                                                                                 1012
## 5 Amy
             1975
                      6
                           28
                                  0 31.5 -78.8 tropical d~ -1
                                                                          25
## 6 Amy
             1975
                      6
                           28
                                  6 32.4 -78.7 tropical d~ -1
                                                                          25
                                                                                 1012
                                                                          25
                                                                                 1011
## 7 Amy
             1975
                      6
                           28
                                 12
                                     33.3 -78
                                                 tropical d~ -1
## 8 Amy
             1975
                      6
                           28
                                 18 34
                                           -77
                                                 tropical d~ -1
                                                                          30
                                                                                 1006
## 9 Amy
             1975
                      6
                           29
                                  0
                                     34.4 -75.8 tropical s~ 0
                                                                          35
                                                                                 1004
             1975
                                   6 34
                                          -74.8 tropical s~ 0
                                                                                 1002
## 10 Amy
                      6
                           29
                                                                          40
## # ... with 10,000 more rows, and 5 more variables: ts_diameter <dbl>,
       hu_diameter <dbl>, timestamp <dttm>, day_of_the_week <ord>,
       week_of_year <dbl>
```

For each storm, summarize the day in which is started in the following format "Friday, June 27, 1975".

```
## # A tibble: 198 x 2
               start date
##
     name
##
      <chr>
               <chr>
  1 AL011993 Tuesday, June 1, 1993
   2 AL012000 Wednesday, June 7, 2000
   3 AL021992 Thursday, June 25, 1992
  4 AL021994 Wednesday, July 20, 1994
## 5 AL021999 Friday, July 2, 1999
## 6 AL022000 Friday, June 23, 2000
   7 AL022001 Wednesday, July 11, 2001
## 8 AL022003 Wednesday, June 11, 2003
## 9 AL022006 Monday, July 17, 2006
## 10 AL031987 Sunday, August 9, 1987
## # ... with 188 more rows
```

Create a new factor variable decile_windspeed by binning wind speed into 10 bins.

```
#T0-D0
x = (1:10)/10
\#x = seq(0, 1, by = 0.1)
storms %>%
 mutate(decile_windspeed = cut(wind, quantile(wind, x ), labels =FALSE)) #flase wlil bring the binds i
## # A tibble: 10,010 x 14
##
             year month
                          day hour
                                      lat long status
                                                            category wind pressure
##
      <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                            <ord>
                                                                     <int>
                                                                               <int>
## 1 Amy
             1975
                                  0 27.5 -79
                                                                                1013
                      6
                           27
                                                tropical d~ -1
                                                                        25
## 2 Amy
             1975
                      6
                           27
                                  6 28.5 -79
                                                tropical d~ -1
                                                                        25
                                                                                1013
## 3 Amy
             1975
                      6
                           27
                                 12 29.5 -79
                                                tropical d~ -1
                                                                        25
                                                                                1013
## 4 Amy
                           27
                                 18 30.5 -79
                                                                        25
                                                                               1013
             1975
                      6
                                                tropical d~ -1
## 5 Amy
             1975
                      6
                           28
                                 0 31.5 -78.8 tropical d~ -1
                                                                        25
                                                                               1012
## 6 Amy
             1975
                           28
                                 6 32.4 -78.7 tropical d~ -1
                                                                        25
                                                                               1012
                      6
## 7 Amy
             1975
                      6
                           28
                                 12 33.3 -78
                                                tropical d~ -1
                                                                        25
                                                                                1011
## 8 Amy
             1975
                      6
                           28
                                 18 34
                                          -77
                                                tropical d~ -1
                                                                        30
                                                                               1006
## 9 Amy
             1975
                           29
                                  0 34.4 -75.8 tropical s~ 0
                                                                        35
                                                                                1004
                                                                                1002
             1975
                                        -74.8 tropical s~ 0
                                                                        40
## 10 Amy
                      6
                           29
                                  6 34
## # ... with 10,000 more rows, and 3 more variables: ts_diameter <dbl>,
     hu_diameter <dbl>, decile_windspeed <int>
```

Create a new data frame serious_storms which are category 3 and above hurricanes.

```
#TO-DO
serious_storms = storms%<>%
filter(category >=3)
serious_storms
```

```
## # A tibble: 779 x 13
##
               year month
                             day hour
                                        lat long status
                                                            category wind pressure
##
      <chr>
               <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dr>
                                                            <ord>
                                                                     <int>
                                                                              <int>
##
   1 Caroline 1975
                                       24
                                            -97
                                                                       100
                                                                                973
                        8
                              31
                                                  hurrica~ 3
## 2 Caroline 1975
                              31
                                       24.1 -97.5 hurrica~ 3
                                                                      100
                                                                                963
                        8
## 3 Belle
               1976
                        8
                                   18 29.5 -75.3 hurrica~ 3
                                                                      100
                                                                                958
## 4 Belle
                                       30.9 -75.3 hurrica~ 3
                                                                      105
               1976
                        8
                               9
                                    0
                                                                                957
## 5 Belle
               1976
                        8
                              9
                                    6
                                       32.5 -75.2 hurrica~ 3
                                                                      105
                                                                                959
## 6 Anita
                        9
                                                                                945
               1977
                              1
                                   18 25.2 -95.5 hurrica~ 3
                                                                      110
                        9
                              2
                                    0 24.6 -96.2 hurrica~ 5
## 7 Anita
               1977
                                                                      140
                                                                                931
## 8 Anita
                                    6 24.2 -97.1 hurrica~ 5
               1977
                        9
                               2
                                                                      150
                                                                               926
## 9 Anita
               1977
                        9
                              2
                                    12 23.7 -98
                                                  hurrica~ 4
                                                                      120
                                                                                940
## 10 David
               1979
                        8
                              28
                                    0 12.2 -52.9 hurrica~ 4
                                                                      115
                                                                               947
## # ... with 769 more rows, and 2 more variables: ts_diameter <dbl>,
## # hu diameter <dbl>
```

In serious_storms, merge the variables lat and long together into lat_long with values lat / long as a string.

```
serious_storms%>%
  mutate(lat_long = paste(lat, long, sep = " / "))
```

A tibble: 779 x 14

```
##
      name
                vear month
                              day hour
                                           lat long status
                                                                category wind pressure
##
      <chr>
                <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dr>
                                                                <ord>
                                                                         <int>
                                                                                   <int>
##
    1 Caroline
               1975
                          8
                                31
                                          24
                                                -97
                                                      hurrica~ 3
                                                                           100
                                                                                     973
                                                                           100
    2 Caroline
                1975
                                31
                                          24.1 -97.5 hurrica~ 3
                                                                                     963
##
                          8
                                       6
##
    3 Belle
                 1976
                          8
                                 8
                                      18
                                          29.5 -75.3 hurrica~ 3
                                                                           100
                                                                                     958
    4 Belle
                                 9
                                          30.9 -75.3 hurrica~ 3
##
                 1976
                          8
                                       0
                                                                           105
                                                                                     957
    5 Belle
                                          32.5 -75.2 hurrica~ 3
##
                1976
                          8
                                 9
                                       6
                                                                           105
                                                                                     959
##
    6 Anita
                1977
                          9
                                 1
                                      18
                                          25.2 -95.5 hurrica~ 3
                                                                           110
                                                                                     945
##
    7 Anita
                1977
                          9
                                 2
                                       0
                                          24.6 -96.2 hurrica~ 5
                                                                           140
                                                                                     931
##
   8 Anita
                1977
                          9
                                 2
                                       6
                                          24.2 -97.1 hurrica~ 5
                                                                           150
                                                                                     926
   9 Anita
                1977
                          9
                                 2
                                      12
                                          23.7 -98
                                                      hurrica~ 4
                                                                           120
                                                                                     940
                                         12.2 -52.9 hurrica~ 4
## 10 David
                 1979
                          8
                                28
                                       0
                                                                           115
                                                                                     947
## # ... with 769 more rows, and 3 more variables: ts_diameter <dbl>,
       hu_diameter <dbl>, lat_long <chr>
```

Let's return now to the original storms data frame. For each category, find the average wind speed, pressure and diameters (do not count the NA's in your averaging).

```
#T0-D0
storms%>%
group_by(category) %>%
mutate(average_wind_speed = mean(wind), average_pressure = mean(pressure), average_ts_diameter = mean(t
## # A tibble: 779 x 17
## # Groups:
               category [3]
##
      name
                year month
                                          lat long status
                                                              category
                                                                        wind pressure
                              day hour
##
      <chr>
               <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <chr>
                                                              <ord>
                                                                        <int>
                                                                                 <int>
   1 Caroline 1975
                               31
                                      0
                                         24
                                               -97
                                                                          100
                                                                                   973
##
                          8
                                                     hurrica~ 3
##
    2 Caroline
                1975
                          8
                               31
                                      6
                                         24.1 -97.5 hurrica~ 3
                                                                          100
                                                                                   963
##
   3 Belle
                1976
                          8
                                8
                                     18
                                         29.5 -75.3 hurrica~ 3
                                                                          100
                                                                                   958
##
   4 Belle
                1976
                          8
                                9
                                      0
                                         30.9 -75.3 hurrica~ 3
                                                                          105
                                                                                   957
  5 Belle
                                         32.5 -75.2 hurrica~ 3
                                                                          105
                                                                                   959
##
                1976
                          8
                                9
                                      6
##
    6 Anita
                1977
                          9
                                1
                                     18
                                         25.2 -95.5 hurrica~ 3
                                                                          110
                                                                                   945
##
   7 Anita
                1977
                          9
                                2
                                      0
                                         24.6 -96.2 hurrica~ 5
                                                                          140
                                                                                   931
##
   8 Anita
                1977
                          9
                                2
                                      6
                                         24.2 -97.1 hurrica~ 5
                                                                          150
                                                                                   926
                1977
                                2
                                         23.7 -98
                                                                          120
                                                                                   940
##
   9 Anita
                          9
                                     12
                                                     hurrica~ 4
## 10 David
                1979
                          8
                               28
                                         12.2 -52.9 hurrica~ 4
                                                                                   947
                                      0
                                                                          115
## # ... with 769 more rows, and 6 more variables: ts_diameter <dbl>,
       hu_diameter <dbl>, average_wind_speed <dbl>, average_pressure <dbl>,
## #
       average_ts_diameter <dbl>, avg_hu_diam <dbl>
```

For each named storm, find its maximum category, wind speed, pressure and diameters (do not allow the max to be NA) and the number of readings (i.e. observations).

```
#TO-DO
storms%>%
group_by(name) %>%
filter(!is.na(ts_diameter), !is.na(hu_diameter))%>%
summarise(max_category = max(category),max_wind_speed = max(wind), max_pressure = max(pressure),max_t
```

A tibble: 32 x 6

```
##
      name
               max_category max_wind_speed max_pressure max_ts_diameter
##
      <chr>
                <ord>
                                       <int>
                                                     <int>
                                                                      <dbl>
##
    1 Alex
               3
                                         105
                                                       962
                                                                      437.
                                         100
    2 Beta
                3
                                                       962
                                                                      115.
##
##
    3 Bill
                4
                                         115
                                                       962
                                                                      460.
                                                                      207.
##
   4 Charley
               4
                                         125
                                                       966
   5 Danielle 4
##
                                         115
                                                       953
                                                                      357.
##
  6 Danny
                                         110
                                                       966
                                                                       92.1
##
   7 Dean
                5
                                         150
                                                       961
                                                                      351.
## 8 Edouard
               3
                                         105
                                                       956
                                                                      322.
## 9 Emily
                5
                                         140
                                                       971
                                                                      270.
## 10 Felix
                                                                      201.
                5
                                         150
                                                       962
## # ... with 22 more rows, and 1 more variable: max_hu_diameter <dbl>
```

Calculate the distance from each storm observation to Miami in a new variable distance_to_miami. This is very challenging. You will need a function that computes distances from two sets of latitude / longitude coordinates.

```
MIAMI_LAT_LONG_COORDS = c(25.7617, -80.1918)
distance <- function(lat1, long1, lat2, long2){</pre>
  lat1 = lat1 * 180/pi
  lat2 = lat2 * 180/pi
  long1 = long1 * 180/pi
  long2 = long2 * 180/pi
  # Haversine formula
  a = \sin(1at2 - 1at1 / 2)^2 + (\cos(1at2) * \cos(1at1)) * \sin(1ong2 - 1ong1 / 2)^2
  b = 2 * atan2(sqrt(a), sqrt(1 - a))
  distance = 6373.0 * b # Multiplying by radius of earth in KM
  return(distance)
}
storms %>%
  mutate(distance_to_miami = distance(lat, long, MIAMI_LAT_LONG_COORDS[1], MIAMI_LAT_LONG_COORDS[2]))
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## # A tibble: 779 x 14
##
      name
                year month
                              day hour
                                          lat long status
                                                                        wind pressure
                                                              category
##
      <chr>
               <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dr>
                                                              <ord>
                                                                       <int>
                                                                                 <int>
##
   1 Caroline 1975
                         8
                               31
                                      0
                                         24
                                              -97
                                                    hurrica~ 3
                                                                         100
                                                                                   973
##
  2 Caroline
               1975
                         8
                               31
                                      6
                                         24.1 -97.5 hurrica~ 3
                                                                         100
                                                                                   963
##
  3 Belle
                1976
                         8
                                8
                                     18
                                         29.5 -75.3 hurrica~ 3
                                                                         100
                                                                                   958
  4 Belle
                                         30.9 -75.3 hurrica~ 3
##
                1976
                         8
                                9
                                      0
                                                                         105
                                                                                   957
## 5 Belle
                1976
                         8
                                9
                                         32.5 -75.2 hurrica~ 3
                                                                         105
                                                                                   959
                                      6
## 6 Anita
                1977
                         9
                                1
                                     18
                                         25.2 -95.5 hurrica~ 3
                                                                         110
                                                                                   945
```

0 24.6 -96.2 hurrica~ 5

6 24.2 -97.1 hurrica~ 5

140

150

931

926

7 Anita

8 Anita

9

9

1977

1977

2

2

```
## 9 Anita
                1977
                        9
                              2
                                    12 23.7 -98
                                                  hurrica~ 4
                                                                       120
                                                                                940
## 10 David
                1979
                         8
                              28
                                    0 12.2 -52.9 hurrica~ 4
                                                                                947
                                                                       115
## # ... with 769 more rows, and 3 more variables: ts diameter <dbl>,
## # hu_diameter <dbl>, distance_to_miami <dbl>
```

For each storm observation, use the function from the previous question to calculate the distance it moved since the previous observation.

```
#T0-D0
storms %<>%
  group_by(name)%>%
  mutate(dist_from_prev = ifelse(name != lag(name), 0, distance(lat, long, lag(lat), lag(long)))) %>%
 mutate(dist_from_prev = ifelse(is.na(dist_from_prev), 0, dist_from_prev))
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
```

Warning in sqrt(a): NaNs produced

- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced

- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(a): NaNs produced
- ## Warning in sqrt(1 a): NaNs produced

```
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
## Warning in sqrt(a): NaNs produced
## Warning in sqrt(1 - a): NaNs produced
storms
## # A tibble: 779 x 14
## # Groups:
               name [72]
##
      name
                year month
                             day hour
                                          lat long status
                                                             category wind pressure
               <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
##
      <chr>
                                                             <ord>
                                                                       <int>
                                                                                <int>
   1 Caroline 1975
                                        24
                                              -97
                                                    hurrica~ 3
                                                                         100
                                                                                  973
  2 Caroline 1975
                                        24.1 -97.5 hurrica~ 3
##
                         8
                              31
                                      6
                                                                         100
                                                                                  963
## 3 Belle
                                        29.5 -75.3 hurrica~ 3
                1976
                         8
                               8
                                    18
                                                                         100
                                                                                  958
                                        30.9 -75.3 hurrica~ 3
## 4 Belle
                1976
                         8
                               9
                                     0
                                                                         105
                                                                                  957
## 5 Belle
                1976
                         8
                               9
                                      6 32.5 -75.2 hurrica~ 3
                                                                         105
                                                                                  959
                                    18 25.2 -95.5 hurrica~ 3
## 6 Anita
                1977
                         9
                               1
                                                                         110
                                                                                  945
## 7 Anita
                1977
                         9
                               2
                                      0
                                        24.6 -96.2 hurrica~ 5
                                                                         140
                                                                                  931
                         9
                               2
                                        24.2 -97.1 hurrica~ 5
## 8 Anita
                1977
                                      6
                                                                         150
                                                                                  926
## 9 Anita
                1977
                         9
                               2
                                     12
                                        23.7 -98
                                                    hurrica~ 4
                                                                         120
                                                                                  940
## 10 David
                1979
                         8
                              28
                                      0
                                        12.2 -52.9 hurrica~ 4
                                                                         115
                                                                                  947
## # ... with 769 more rows, and 3 more variables: ts_diameter <dbl>,
       hu_diameter <dbl>, dist_from_prev <dbl>
```

Warning in sqrt(a): NaNs produced

For each storm, find the total distance it moved over its observations and its total displacement. "Distance" is a scalar quantity that refers to "how much ground an object has covered" during its motion. "Displacement" is a vector quantity that refers to "how far out of place an object is"; it is the object's overall change in position.

```
## # A tibble: 72 x 3
##
              Distance Displacement
      name
##
      <chr>
                 <dbl> <chr>
                16988. 2.3 / 4.7
##
   1 Alberto
##
   2 Alex
                25008. 2.3 / 6.4
   3 Alicia
                    0 0.2 / -0.1
##
   4 Andrew
               139302. 4 / -20.4
               17804. -1.5 / -2.5
##
   5 Anita
                17135. 3 / 0.1
##
   6 Belle
##
   7 Beta
                    0 0 / 0
   8 Bill
                50490. 10.9 / -14.3
   9 Bob
                    0 0 / 0
##
## 10 Bonnie
                84162. 9.3 / -6.3
## # ... with 62 more rows
```

For each storm observation, calculate the average speed the storm moved in location.

```
#TO-DO
storms %<>%
mutate(speed = dist_from_prev / 6)
```

For each storm, calculate its average ground speed (how fast its eye is moving which is different from windspeed around the eye).

```
#T0-D0
storms%>%
  group_by(name)%>%
 mutate(avg_speed = mean(speed))
## # A tibble: 779 x 16
## # Groups:
               name [72]
##
      name
                year month
                              day hour
                                          lat long status
                                                              category wind pressure
##
               <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dr>
      <chr>>
                                                              <ord>
                                                                        <int>
                                                                                 <int>
    1 Caroline 1975
                                      0
                                         24
                                               -97
                                                                          100
                                                                                   973
##
                          8
                               31
                                                     hurrica~ 3
                               31
                                      6
##
   2 Caroline 1975
                         8
                                         24.1 -97.5 hurrica~ 3
                                                                          100
                                                                                   963
##
   3 Belle
                1976
                         8
                                8
                                     18
                                         29.5 -75.3 hurrica~ 3
                                                                          100
                                                                                   958
   4 Belle
                1976
                         8
                                9
                                         30.9 -75.3 hurrica~ 3
                                                                          105
##
                                      0
                                                                                   957
##
   5 Belle
                1976
                         8
                                9
                                      6
                                         32.5 -75.2 hurrica~ 3
                                                                          105
                                                                                   959
##
   6 Anita
                         9
                                1
                                     18 25.2 -95.5 hurrica~ 3
                                                                                   945
                1977
                                                                          110
##
   7 Anita
                1977
                         9
                                2
                                      0
                                         24.6 -96.2 hurrica~ 5
                                                                          140
                                                                                   931
##
   8 Anita
                1977
                          9
                                2
                                      6
                                         24.2 -97.1 hurrica~ 5
                                                                          150
                                                                                   926
##
   9 Anita
                1977
                          9
                                2
                                     12
                                         23.7 -98
                                                     hurrica~ 4
                                                                          120
                                                                                   940
## 10 David
                1979
                          8
                               28
                                      0 12.2 -52.9 hurrica~ 4
                                                                          115
                                                                                   947
## # ... with 769 more rows, and 5 more variables: ts_diameter <dbl>,
       hu_diameter <dbl>, dist_from_prev <dbl>, speed <dbl>, avg_speed <dbl>
```

Is there a relationship between average ground speed and maximum category attained? Use a dataframe summary (not a regression).

```
#TO-DO
#cor(as.numeric(storms["speed"]), as.numeric(max(storms["category"])))
```

Now we want to transition to building real design matrices for prediction. This is more in tune with what happens in the real world. Large data dump and you convert it into X and y how you see fit.

Suppose we wish to predict the following: given the first three readings of a storm, can you predict its maximum wind speed? Identify the y and identify which features you need $x_1, ... x_p$ and build that matrix with dplyr functions. This is not easy, but it is what it's all about. Feel free to "featurize" as creatively as you would like. You aren't going to overfit if you only build a few features relative to the total 198 storms.

```
#T0-D0
storms_model = storms %>%
  group_by(name) %>%
  summarise(y = max(wind), avrage pressure = mean(pressure), avrage distance = mean(dist from prev)) %>%
  select(-name)
storms_model
## # A tibble: 72 x 3
##
          y avrage_pressure avrage_distance
##
      <int>
                       <dbl>
                                         <dbl>
##
    1
        110
                        956.
                                         4247.
                                         8336.
##
    2
        105
                        959.
##
    3
        100
                         962.
                                            0
##
    4
        150
                         940.
                                         7332.
                                         4451.
##
    5
        150
                         936.
##
    6
        105
                         958
                                         5712.
##
    7
        100
                         962
                                            0
    8
                                         4207.
##
        115
                         951.
    9
##
        100
                         950
                                            0
## 10
        100
                         961.
                                         6012.
## # ... with 62 more rows
Fit your model. #TO-DO Validate it.
mod = lm(y ~0 +., data = storms_model)
summary(mod)
```

```
## lm(formula = y ~ 0 + ., data = storms_model)
##
## Residuals:
      Min
               1Q Median
                                3Q
                                      Max
## -32.548 -12.920 -0.889 10.241
                                   39.401
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## avrage_pressure 0.1196206
                            0.0048119 24.860
                                                  <2e-16 ***
                                         2.228
                                                  0.0291 *
## avrage_distance 0.0016080 0.0007217
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 17.82 on 70 degrees of freedom
Multiple R-squared: 0.9799, Adjusted R-squared: 0.9793
F-statistic: 1705 on 2 and 70 DF, p-value: < 2.2e-16</pre>

##

```
n= nrow(storms)
K = 5

test_indices = sample(1 : n, 1 / K * n)
train_indices = setdiff(1 : n, test_indices)
X = select(storms_model, -y)
y = storms_model$y
X_train = X[train_indices, ]
y_train = y[train_indices]
X_test = X[test_indices, ]
y_test = y[test_indices]
modv = lm(y_train ~., data.frame(X_train))
yhat_oos = predict(mod, data.frame(X_test))
oos_residuals = y_test - yhat_oos
sd(modv$residuals) - sd(oos_residuals)
```

[1] NA

```
head(cbind(y_test, yhat_oos))
```

```
##
    y_test yhat_oos
## 1
       NA
## 2
        NA
                 NA
## 3
        NA
                 NA
## 4
        NA
                 NA
## 5
        NA
                 NA
## 6
        NA
                 NA
```

Assess your level of success at this endeavor.

#TO-DO

The Forward Stepwise Procedure for Probability Estimation Models

Set a seed and load the adult dataset and remove missingness and randomize the order.

```
set.seed(1)
pacman::p_load_gh("coatless/ucidata")
data(adult)
adult = na.omit(adult)
adult = adult[sample(1 : nrow(adult)), ]
```

Copy from the previous lab all cleanups you did to this dataset.

```
#TO-DO
adult$fnlwgt = NULL

adult$marital_status = as.character(adult$marital_status)
adult$marital_status = ifelse(adult$marital_status == "Married-AF-spouse" | adult$marital_status == "Ma adult$marital_status = as.factor(adult$marital_status)
```

```
adult$education = as.character(adult$education)
adult$education = ifelse(adult$education == "1st-4th" | adult$education == "Preschool", "<=4th", adult$
adult$education = as.factor(adult$education)
adult$education = NULL
tab = sort(table(adult$native_country))
adult$native_country = as.character(adult$native_country)
adult$native_country= ifelse(adult$native_country %in% names(tab[tab<50]), "Other", adult$native_countr
adult$native_country= as.factor(adult$native_country)
adult$worktype = paste(adult$occupation, adult$workclass, sep = ":")
tab_worktype = sort(table(adult$worktype))
adult$occupation = NULL
adult$workclass = NULL
adult$worktype = as.character(adult$worktype)
adult$worktype = ifelse(adult$worktype %in% names(tab_worktype[tab_worktype<100]), "Other", adult$worktype
adult$worktype = as.factor(adult$worktype)
adult$status = paste(as.character(adult$relationship), as.character(adult$marital_status), sep = ":")
adult$status = as.character(adult$status)
tab_status = sort(table(adult$status))
adult$relationship = NULL
adult$marital_status = NULL
adult$status = as.factor(adult$status)
```

We will be doing model selection. We will split the dataset into 3 distinct subsets. Set the size of our splits here. For simplicitiy, all three splits will be identically sized. We are making it small so the stepwise algorithm can compute quickly. If you have a faster machine, feel free to increase this.

```
Nsplitsize = 1000
```

Now create the following variables: Xtrain, ytrain, Xselect, yselect, Xtest, ytest with Nsplitsize observations. Binarize the y values.

```
Xtrain = adult[1 : Nsplitsize, ]
Xtrain$income = NULL
ytrain = ifelse(adult[1 : Nsplitsize, "income"] == ">50K", 1, 0)
Xselect = adult[(Nsplitsize + 1) : (2 * Nsplitsize), ]
Xselect$income = NULL
yselect = ifelse(adult[(Nsplitsize + 1) : (2 * Nsplitsize), "income"] ==">50K", 1, 0)
Xtest = adult[(2 * Nsplitsize + 1) : (3 * Nsplitsize), ]
Xtest$income = NULL
ytest = ifelse(adult[(2 * Nsplitsize + 1) : (3 * Nsplitsize), "income"] == ">50K", 1, 0)
```

Fit a vanilla logistic regression on the training set.

```
logistic_mod = glm(ytrain ~ ., Xtrain, family = "binomial")
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

and report the log scoring rule, the Brier scoring rule.

```
#TO-DO
p_hat_train = predict(logistic_mod, Xtrain, type = 'response')

## Warning in predict.lm(object, newdata, se.fit, scale = 1, type = if (type == :
## prediction from a rank-deficient fit may be misleading

#in sample log scoring rule
mean(ytrain * log(p_hat_train) + (1 - ytrain) * log(1 - p_hat_train))

## [1] -0.2671121

#in sample Brier scoring rule
mean(-(ytrain - p_hat_train)^2)
```

[1] -0.08715781

We will be doing model selection using a basis of linear features consisting of all first-order interactions of the 14 raw features (this will include square terms as squares are interactions with oneself).

Create a model matrix from the training data containing all these features. Make sure it has an intercept column too (the one vector is usually an important feature). Cast it as a data frame so we can use it more easily for modeling later on. We're going to need those model matrices (as data frames) for both the select and test sets. So make them here too (copy-paste). Make sure their dimensions are sensible.

```
#TO-DO

Xmm_train = data.frame(model.matrix( ~ . * . , Xtrain))
Xmm_select = data.frame(model.matrix( ~ . * . , Xselect))
Xmm_test = data.frame(model.matrix( ~ . * . , Xtest))
dim(Xmm_train)

## [1] 1000 3104
dim(Xmm_select)

## [1] 1000 3104
```

[1] 1000 3104

Write code that will fit a model stepwise. You can refer to the chunk in the practice lecture. Use the negative Brier score to do the selection. The negative of the Brier score is always positive and lower means better making this metric kind of like s_e so the picture will be the same as the canonical U-shape for oos performance.

Run the code and hit "stop" when you begin to the see the Brier score degrade appreciably oos. Be patient as it will wobble.

```
pacman::p_load(Matrix)
p_plus_one = ncol(Xmm_train)
predictor_by_iteration = c() #keep a growing list of predictors by iteration
in_sample_brier_by_iteration = c() #keep a growing list of briers by iteration
oos_brier_by_iteration = c() #keep a growing list of briers by iteration
i = 1
repeat {
  #get all predictors left to try
  all_brier = array(NA, p_plus_one) #record all possibilities
  for (j_try in 1 : p_plus_one){
    if (j_try %in% predictor_by_iteration){
     next
   }
   Xmm_sub = Xmm_train[, c(predictor_by_iteration, j_try), drop = FALSE]
   logistic_mod = suppressWarnings(glm(ytrain ~ ., Xmm_sub, family = "binomial"))
   phat_train = suppressWarnings(predict(logistic_mod, Xmm_sub, type = 'response'))
   all_brier[j_try] = mean(-(ytrain - phat_train)^2)
  }
  j_star = which.max(all_brier)
  predictor_by_iteration = c(predictor_by_iteration, j_star)
  in_sample_brier_by_iteration = c(in_sample_brier_by_iteration, all_brier[j_star])
  #now let's look at oos
  Xmm_sub = Xmm_train[, predictor_by_iteration, drop = FALSE]
    logistic_mod = suppressWarnings(glm(ytrain ~ ., Xmm_sub, family = "binomial"))
   phat_train = suppressWarnings(predict(logistic_mod, Xmm_sub, type = 'response'))
   all_brier[j_try] = mean(-(ytrain - phat_train)^2)
   phat_select = suppressWarnings(predict(logistic_mod, Xmm_select[, predictor_by_iteration, drop = FA
   oos_brier = mean(-(yselect - phat_select)^2)
   oos_brier_by_iteration = c(oos_brier_by_iteration, oos_brier)
  cat("i =", i, "in-sample_brier =", all_brier[j_star], "oos_brier =", oos_brier, "\n predictor added
  i = i + 1
  if (i > 10){
   break
  }
}
## i = 1 in-sample_brier = -0.1481517 oos_brier = -0.1543828
     predictor added: age.education_num
## i = 2 in-sample_brier = -0.1346776 oos_brier = -0.1472043
     predictor added: age.capital_gain
## i = 3 in-sample_brier = -0.1244369 oos_brier = -0.1362633
     predictor added: education num.sexMale
## i = 4 in-sample_brier = -0.1165644 oos_brier = -0.1291617
     predictor added: age.statusWife.Married
```

```
## i = 5 in-sample_brier = -0.1116817 oos_brier = -0.1279595
## predictor added: hours_per_week.statusNot.in.family.Never.married
## i = 6 in-sample_brier = -0.1087885 oos_brier = -0.1269657
## predictor added: age.statusNot.in.family.Divorced
## i = 7 in-sample_brier = -0.1058228 oos_brier = -0.1282639
## predictor added: statusNot.in.family.Married.spouse.absent
## i = 8 in-sample_brier = -0.1031665 oos_brier = -0.1278538
## predictor added: raceWhite.capital_loss
## i = 9 in-sample_brier = -0.1008492 oos_brier = -0.1270625
## predictor added: sexMale.worktypeOther.service.Private
## i = 10 in-sample_brier = -0.09941457 oos_brier = -0.1256182
## predictor added: education_num.worktypeFarming.fishing.Self.emp.not.inc
```

Plot the in-sample and oos (select set) Brier score by p. Does this look like what's expected?

```
#TO-DO

simulation_results = data.frame(
   iteration = 1 : length(in_sample_brier_by_iteration),
   in_sample_brier_by_iteration = in_sample_brier_by_iteration,
   oos_brier_by_iteration = oos_brier_by_iteration
)

pacman::p_load(latex2exp)

ggplot(simulation_results) +
   geom_line(aes(x = iteration, y = in_sample_brier_by_iteration), color = "red") +
   geom_line(aes(x = iteration, y = oos_brier_by_iteration), color = "blue") +
   #ylim(0, max(c(simulation_results$in_sample_brier_by_iteration, simulation_results$cos_brier_by_iteration, simulation_results$cos_brier_by_iteration
```

