Lab 1

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You should have RStudio installed to edit this file. You will write code in places marked "TO-DO" to complete the problems. Most of this will be a pure programming assignment but there are some questions that instead ask you to "write a few sentences". This is a W class! The tools for the solutions to these problems can be found in the class practice lectures. I prefer you to use the methods I taught you. If you google and find esoteric code you don't understand, this doesn't do you too much good.

To "hand in" the homework, you should first download this file. The best way to do this is by cloning the class repository then copying this file from the folder of that clone into the folder that is your personal class repository. Then do the assignment by filling in the TO-DO's. After you're done, compile this file into a PDF (use the "knit to PDF" button on the submenu above). This PDF will include output of your code. Then push the PDF and this Rmd file by the deadline to your github repository in a directory called "labs".

Basic R Skills

• Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
options(digits=11)
x <- pi
x</pre>
```

[1] 3.1415926536

• Sum up the first 103 terms of the series $1 + 1/2 + 1/4 + 1/8 + \dots$

```
sum(1/(2^{(0:102))})
```

[1] 2

• Find the product of the first 37 terms in the sequence 1/3, 1/6, 1/9 ...

```
prod(1/(3*(1:37)))
## [1] 1.613528728e-61
prod(1/seq(from=3, by=3, length.out=37))
```

[1] 1.613528728e-61

• Find the product of the first 387 terms of 1 * 1/2 * 1/4 * 1/8 * ...

```
prod(1/(2<sup>(0:386))</sup>)
```

[1] 0

Is this answer *exactly* correct?

#TO-DO

• Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
sum(log(1/(2^{(0:386))}))
```

[1] -51771.856063

```
-log(2)*sum(0:386)
```

[1] -51771.856063

• Create the sequence x = [Inf, 20, 18, ..., -20].

```
x <- c(Inf, seq(from=20, to=-20, by=-2))
x</pre>
```

```
## [1] Inf 20 18 16 14 12 10 8 6 4 2 0 -2 -4 -6 -8 -10 -12 -14 ## [20] -16 -18 -20
```

Create the sequence $x = [log_3(Inf), log_3(100), log_3(98), ... log_3(-20)].$

```
x <- c(Inf, seq(from=100, to=-20, by=-2))
x <- log(x, base=3)</pre>
```

Warning: NaNs produced

```
log(100, 3)
```

```
## [1] 4.1918065486
```

Comment on the appropriateness of the non-numeric values.

NAN occurs because you cannot take the log of a negative number. -Inf occurs when you take the log of 0.

• Create a vector of booleans where the entry is true if x[i] is positive and finite.

```
y = !is.nan(x) & is.finite(x) & x > 0
y
```

```
[1] FALSE
               TRUE
                     TRUE
                           TRUE
                                 TRUE
                                       TRUE
                                              TRUE
                                                    TRUE
                                                          TRUE
                                                                TRUE
                                                                      TRUE
                                       TRUE
## [13]
         TRUE
               TRUE
                     TRUE
                           TRUE
                                              TRUE
                                                    TRUE
                                                          TRUE
                                                                TRUE
                                                                      TRUE
                                                                            TRUE
                                 TRUE
                                                    TRUE
                                                          TRUE
                                                                      TRUE
         TRUE
               TRUE
                     TRUE
                           TRUE
                                 TRUE
                                       TRUE
                                              TRUE
                                                                TRUE
                                                                            TRUE
               TRUE
                                 TRUE
                                                          TRUE
  [37]
         TRUE
                     TRUE
                           TRUE
                                       TRUE
                                             TRUE
                                                    TRUE
                                                                TRUE
                                                                      TRUE
                                                                            TRUE
## [49]
         TRUE
               TRUE
                     TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [61] FALSE FALSE
```

• Locate the indices of the non-real numbers in this vector. Hint: use the which function. Don't hesitate to use the documentation via ?which.

?which

starting httpd help server ... done

```
which(!y)
```

[1] 1 52 53 54 55 56 57 58 59 60 61 62

```
which(y == FALSE)
```

- ## [1] 1 52 53 54 55 56 57 58 59 60 61 62
 - Locate the indices of the infinite quantities in this vector.

```
which(is.infinite(x))
```

[1] 1 52

• Locate the indices of the min and max in this vector. Hint: use the which.min and which.max functions.

```
which.min(x)
```

[1] 52

```
which.max(x)
```

[1] 1

• Count the number of unique values in x.

```
length(unique(x))
```

[1] 53

• Cast x to a factor. Do the number of levels make sense?

```
?factor
as.factor(x)
    [1] Inf
                          4.19180654857877
                                             4.1734172518943
                                                                4.15464876785729
##
    [5] 4.13548512895119
                          4.11590933734319
                                             4.09590327428938
                                                                4.07544759935851
                          4.03310325630434
    [9] 4.05452163806914
                                             4.01116871959141
                                                                3.98869253500376
## [13] 3.96564727304425
                          3.94200336638929
                                             3.91772888178973
                                                               3.89278926071437
  [17] 3.86714702345081
                          3.84076143030548
                                             3.81358809221559
                                                                3.78557852142874
  [21] 3.75667961082847
                          3.72683302786084
                                             3.69597450568212
                                                                3.66403300987579
  [25] 3.63092975357146
                          3.59657702661571
                                             3.56087679500731
                                                                3.52371901428583
  [29] 3.48497958377173
                          3.44451784578705
                                             3.40217350273288
                                                               3.3577627814323
  [33] 3.31107361281783
                          3.26185950714291
                                             3.20983167673402
                                                               3.15464876785729
  [37] 3.09590327428938
                          3.03310325630434
                                             2.96564727304425
                                                                2.89278926071437
## [41] 2.8135880922156
                          2.72683302786084
                                             2.63092975357146
                                                                2.52371901428583
## [45] 2.40217350273288
                         2.26185950714291
                                             2.09590327428938
                                                                1.89278926071437
## [49] 1.63092975357146
                          1.26185950714291
                                             0.630929753571457 -Inf
## [53] NaN
                          NaN
                                             NaN
                                                                NaN
                                                                NaN
## [57] NaN
                          NaN
                                             NaN
## [61] NaN
                          NaN
## 53 Levels: -Inf 0.630929753571457 1.26185950714291 ... NaN
  • Cast x to integers. What do we learn about R's infinity representation in the integer data type?
as.integer(x)
## Warning: NAs introduced by coercion to integer range
##
   [1] NA
                                        4
                                           3
                                              .3
                                                 3
                                                    3
                                                       3
                                                          3
                                                             3
                                                                 3
                                                                    3
                                                                       3
            3
               3
                  3
                     3
                        3
                           3
                             3
                                 3
                                     3
                                        3
                                          3
## [26]
         O NA NA NA NA NA NA NA NA NA NA
## [51]
# it come out as NA
```

• Use x to create a new vector y containing only the real numbers in x.

```
y = x[!is.nan(x) & is.finite(x)]

## [1] 4.19180654858 4.17341725189 4.15464876786 4.13548512895 4.11590933734

## [6] 4.09590327429 4.07544759936 4.05452163807 4.03310325630 4.01116871959

## [11] 3.98869253500 3.96564727304 3.94200336639 3.91772888179 3.89278926071

## [16] 3.86714702345 3.84076143031 3.81358809222 3.78557852143 3.75667961083

## [21] 3.72683302786 3.69597450568 3.66403300988 3.63092975357 3.59657702662

## [26] 3.56087679501 3.52371901429 3.48497958377 3.44451784579 3.40217350273

## [31] 3.35776278143 3.31107361282 3.26185950714 3.20983167673 3.15464876786

## [36] 3.09590327429 3.03310325630 2.96564727304 2.89278926071 2.81358809222

## [41] 2.72683302786 2.63092975357 2.52371901429 2.40217350273 2.26185950714

## [46] 2.09590327429 1.89278926071 1.63092975357 1.26185950714 0.63092975357
```

• Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle width size 1e-6.

```
sum(seq(from=0, to=1-(1e-6), by=1e-6)^2)*1e-6
```

[1] 0.33333283333

• Calculate the average of 100 realizations of standard Bernoullis in one line using the sample function.

```
sum(sample(c(0,1), size=100, replace=TRUE))/100
```

```
## [1] 0.53
```

• Calculate the average of 500 realizations of Bernoullis with p = 0.9 in one line using the sample and mean functions.

```
mean(sample(c(0,1), size=500, replace=TRUE, prob=c(0.1, 0.9)))
```

```
## [1] 0.882
```

• Calculate the average of 1000 realizations of Bernoullis with p = 0.9 in one line using rbinom.

```
?rbinom
rbinom(n=1000, size=1, p=0.9)
```

```
##
##
##
##
##
##
##
##
##
##
##
##
[519] 1 1 1 0 1 1 1 1 1 1 1 0 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 1 1 1 1 1
##
##
##
##
##
##
##
##
##
## [1000] 1
```

• In class we considered a variable x_3 which measured "criminality". We imagined L = 4 levels "none", "infraction", "misdimeanor" and "felony". Create a variable x_3 here with 100 random elements (equally probable). Create it as a nominal (i.e. unordered) factor.

```
x_3 = as.factor(sample(c("none", "infraction", "misdimeanor", "felony"), size=100, replace=TRUE))
x_3
```

```
##
     [1] misdimeanor felony
                                              infraction misdimeanor felony
                                 none
     [7] misdimeanor felony
##
                                 felony
                                              none
                                                          misdimeanor felony
##
    [13] felony
                     felony
                                 none
                                              misdimeanor felony
                                                                      none
   [19] misdimeanor felony
                                 infraction felony
                                                          infraction
                                                                      felony
   [25] none
##
                     none
                                 misdimeanor none
                                                          felony
                                                                      infraction
##
   [31] felony
                                 misdimeanor misdimeanor felony
                                                                      felony
                     none
   [37] misdimeanor none
                                             misdimeanor misdimeanor misdimeanor
##
   [43] infraction none
                                                          infraction none
                                 none
                                             none
##
   [49] infraction misdimeanor misdimeanor infraction none
                                                                      none
   [55] misdimeanor felony
                                 infraction
                                             misdimeanor none
                                                                      felony
   [61] misdimeanor misdimeanor felony
                                             none
                                                          infraction none
##
   [67] none
                     misdimeanor felony
                                                                      none
                                              felony
                                                          none
##
   [73] none
                     felony
                                 infraction felony
                                                          infraction
                                                                      felony
##
   [79] none
                     none
                                 misdimeanor none
                                                                      infraction
                                                          none
##
  [85] none
                     misdimeanor none
                                                          infraction felony
##
  [91] none
                     felony
                                 felony
                                             misdimeanor misdimeanor none
## [97] infraction misdimeanor misdimeanor none
## Levels: felony infraction misdimeanor none
```

• Use x_3 to create x_3_bin, a binary feature where 0 is no crime and 1 is any crime.

```
x_3_bin = x_3 != "none"
x_3_bin =as.numeric(x_3_bin)
x_3_bin
```

• Use x_3 to create x_3_ord, an ordered factor variable. Ensure the proper ordinal ordering.

```
x_3_{ord} = factor(x_3, levels = c("none", "infraction", "misdimeanor", "felony"), order=TRUE)
x_3_{ord}
```

```
##
     [1] misdimeanor felony
                                              infraction misdimeanor felony
                                 none
##
     [7] misdimeanor felony
                                 felony
                                                          misdimeanor felony
##
    [13] felony
                     felony
                                 none
                                              misdimeanor felony
                                                                      none
##
   [19] misdimeanor felony
                                                          infraction
                                                                     felony
                                 infraction felony
##
   [25] none
                     none
                                 misdimeanor none
                                                          felony
                                                                      infraction
   [31] felony
##
                                 misdimeanor misdimeanor felony
                                                                      felony
                     none
##
    [37] misdimeanor none
                                              misdimeanor misdimeanor misdimeanor
                                 none
##
  [43] infraction none
                                                          infraction none
                                 none
                                              none
## [49] infraction misdimeanor misdimeanor infraction none
                                                                      none
```

```
## [55] misdimeanor felony
                                infraction misdimeanor none
                                                                    felony
  [61] misdimeanor misdimeanor felony
                                            none
                                                        infraction none
                    misdimeanor felony
                                            felony
  [67] none
                                                        none
                                                                    none
## [73] none
                    felony
                                infraction felony
                                                        infraction felony
   [79] none
                    none
                                misdimeanor none
                                                        none
                                                                    infraction
## [85] none
                    misdimeanor none
                                            none
                                                        infraction felony
## [91] none
                    felony
                                            misdimeanor misdimeanor none
                                felony
## [97] infraction misdimeanor misdimeanor none
## Levels: none < infraction < misdimeanor < felony
```

• Convert this variable into three binary variables without any information loss and put them into a data matrix.

```
infbin = as.numeric(x_3_ord == "infraction")
misbin = as.numeric(x_3_ord == "misdimeanor")
felbin = as.numeric(x_3_ord == "felony")
alldata = c(infbin, misbin, felbin)
bindata =matrix(alldata, nrow=100,ncol =3)
colnames(bindata )= c("infraction", "misdimeanor", "felony")
bindata
```

```
##
           infraction misdimeanor felony
##
     [1,]
                    0
                                 1
##
     [2,]
                    0
                                 0
                                         1
##
     [3,]
                    0
                                 0
                                         0
##
     [4,]
                    1
                                 0
                                         0
##
     [5,]
                    0
                                 1
                                         0
##
     [6.]
                    0
                                 0
##
     [7,]
                    0
                                 1
                                         0
##
     [8,]
                    0
                                 0
##
     [9,]
                    0
                                 0
   [10,]
                    0
                                 0
                    0
                                         0
## [11,]
                                 1
   [12,]
                    0
                                 0
##
                                         1
##
  [13,]
                    0
                                 0
## [14,]
                    0
                                 0
## [15,]
                                 0
                                         0
                    0
## [16,]
                    0
                                 1
                                         0
## [17,]
                    0
                                 0
## [18,]
                    0
                                 0
## [19,]
                    0
                                 1
                                         0
## [20,]
                    0
                                 0
                                         1
## [21,]
                                 0
## [22,]
                                 0
                    0
                                         1
## [23,]
                    1
                                 0
## [24,]
                    0
                                 0
                                         1
## [25,]
                    0
                                 0
## [26,]
                    0
                                 0
                                         0
## [27,]
                    0
                                 1
## [28,]
                    0
                                 0
                                         0
## [29,]
                    0
                                 0
                                         1
## [30,]
                    1
                                 0
                                         0
## [31,]
                                         1
```

шш	[20]	0	0	^
##	[32,]	0	0	0
##	[33,]	0	1	0
##	[34,]	0	1	0
##	[35,]	0	0	1
##	[36,]	0	0	1
##	[37,]	0	1	0
##	[38,]	0	0	0
##	[39,]	0	0	0
##	[40,]	0	1	0
##	[41,]	0	1	0
##	[42,]	0	1	0
##	[43,]	1	0	0
		0		
##	[44,]		0	0
##	[45,]	0	0	0
##	[46,]	0	0	0
##	[47,]	1	0	0
##	[48,]	0	0	0
##	[49,]	1	0	0
##	[50,]	0	1	0
##	[51,]	0	1	0
##	[52,]	1	0	0
##	[53,]	0	0	0
##	[54,]	0	0	0
##	[55,]	0	1	0
##	[56,]	0	0	1
##	[57,]	1	0	0
		0	1	0
##	[58,]			
##	[59,]	0	0	0
##	[60,]	0	0	1
##	[61,]	0	1	0
##	[62,]	0	1	0
##	[63,]	0	0	1
##	[64,]	0	0	0
##	[65,]	1	0	0
##	[66,]	0	0	0
##	[67,]	0	0	0
##	[68,]	0	1	0
##	[69,]	0	0	1
##	[70,]	0	0	1
##	[71,]	0	0	0
##	[72,]	0	0	0
##	[73,]	0	0	0
##	[74,]	0	0	1
##	[75,]	1	0	0
##	[76,]	0	0	1
##	[77,]	1	0	0
##	[78,]	0	0	1
##	[79,]	0	0	0
##	[80,]	0	0	0
##	[81,]	0	1	0
##	[82,]	0	0	0
##	[83,]	0	0	0
##	[84,]	1	0	0
##	[85,]	0	0	0
	/ -	-	-	-

```
##
     [86,]
                                              0
##
     [87,]
                       0
                                      0
                                              0
##
     [88,]
                       0
                                      0
                                              0
                                      0
##
    [89,]
                       1
                                              0
##
    [90,]
                       0
                                      0
                                              1
##
    [91,]
                       0
                                      0
                                              0
##
    [92,]
                       0
                                              1
    [93,]
##
                       0
                                      0
                                              1
##
    [94,]
                       0
                                      1
                                              0
##
    [95,]
                       0
                                              0
                                      1
##
    [96,]
                       0
                                      0
                                              0
    [97,]
                       1
                                      0
                                              0
##
##
    [98,]
                       0
                                      1
                                              0
    [99,]
                       0
##
                                      1
                                              0
## [100,]
                       0
                                              0
```

• What should the sum of each row be (in English)? sum of each individual row should be equal to 1(comited a crime) or zero(for no crimes) Verify that.

rowSums(bindata)

• How should the column sum look (in English)?

The column sums should look like the total number of infractions, misdimeanors, and felonys there are in a sample of 100 people

Verify that.

colSums(bindata)

```
## infraction misdimeanor felony
## 15 26 26
```

• Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column in exponential with lambda of 9, the fifth column is binomial with n = 20 and p = 0.12 and the sixth column is a binary variable with exactly 24% 1's dispersed randomly. Name the rows the entries of the fake_first_names vector.

```
fake_first_names = c(
    "Sophia", "Emma", "Olivia", "Ava", "Mia", "Isabella", "Riley",
    "Aria", "Zoe", "Charlotte", "Lily", "Layla", "Amelia", "Emily",
    "Madelyn", "Aubrey", "Adalyn", "Madison", "Chloe", "Harper",
    "Abigail", "Aaliyah", "Avery", "Evelyn", "Kaylee", "Ella", "Ellie",
    "Scarlett", "Arianna", "Hailey", "Nora", "Addison", "Brooklyn",
    "Hannah", "Mila", "Leah", "Elizabeth", "Sarah", "Eliana", "Mackenzie",
```

```
"Peyton", "Maria", "Grace", "Adeline", "Elena", "Anna", "Victoria",
  "Camilla", "Lillian", "Natalie", "Jackson", "Aiden", "Lucas",
  "Liam", "Noah", "Ethan", "Mason", "Caden", "Oliver", "Elijah",
  "Grayson", "Jacob", "Michael", "Benjamin", "Carter", "James",
  "Jayden", "Logan", "Alexander", "Caleb", "Ryan", "Luke", "Daniel",
  "Jack", "William", "Owen", "Gabriel", "Matthew", "Connor", "Jayce",
  "Isaac", "Sebastian", "Henry", "Muhammad", "Cameron", "Wyatt",
  "Dylan", "Nathan", "Nicholas", "Julian", "Eli", "Levi", "Isaiah",
  "Landon", "David", "Christian", "Andrew", "Brayden", "John",
  "Lincoln"
M = matrix( nrow = 100, ncol = 6)
row.names(M) = fake_first_names
M[,1] = rnorm(100, mean = 17, sd = sqrt(38))
M[,2] = runif(100, -10, 10)
M[,3] = rpois(100, 6)
M[,4] = rexp(100, 9)
M[,5] = rbinom(20, size = 100, p = 0.12)
M[,6] = rbinom(100, size=1, p=0.24)
М
```

```
[,4] [,5] [,6]
##
                       [,1]
                                        [,2] [,3]
## Sophia
             10.87084141799 -7.620454356074
                                               6 0.3158968438518
                                                                    14
## Emma
              9.01910752113 -3.080551815219
                                               6 0.0411177070087
                                                                    11
                                                                          0
                                                                     8
                                                                          0
## Olivia
             11.44622262338 4.662724249065
                                              13 0.0727931108947
## Ava
             24.66797300249 -5.453475811519
                                               6 0.0608780517553
                                                                    11
                                                                          1
              7.72774094199 8.819026080891
                                               4 0.0879546627576
                                                                    7
                                                                          0
## Mia
## Isabella 17.13445026348 -5.920545314439
                                               3 0.2035329492876
                                                                    11
                                                                          0
## Riley
             7.56561746154 3.628241410479
                                               5 0.0763759898643
                                                                    15
                                                                          1
             15.26284651574 -6.700222706422
                                               6 0.1778065348985
## Aria
             24.06230257516 -5.823445999995
## Zoe
                                               3 0.0608472127157
                                                                    10
                                                                          1
## Charlotte 7.95448024830 0.058681345545
                                               5 0.0812038609504
                                                                    11
                                                                          0
                                                                    16
              9.09214104329 -4.929800620303
                                               5 0.2257085999174
                                                                          0
## Lily
## Layla
             21.00561338581 -7.354560359381
                                               4 0.1047044782335
                                                                          0
## Amelia
             19.11031350595 6.954230400734
                                               1 0.1513232782229
                                                                     8
                                                                          0
## Emily
             19.68631630134 -6.824852116406
                                               3 0.1922756669329
                                                                     9
                                                                          0
## Madelyn
             15.33137731822 3.776597841643
                                               5 0.0407521045353
                                                                    10
                                                                          0
## Aubrey
             12.81889154824 6.589961429127
                                               5 0.0195986428815
                                                                    12
                                                                          1
## Adalyn
             13.14596737341 -2.414836105891
                                               6 0.0448048533377
                                                                    11
                                                                          1
             13.36327977580 4.764115666039
                                                                    10
                                                                          0
## Madison
                                               5 0.1633635161144
## Chloe
             21.15755076357 9.289039843716
                                               6 0.0162685238756
                                                                    4
                                                                          0
## Harper
             26.46016764523 -6.002670396119
                                               5 0.0326955594743
                                                                    13
                                                                          0
## Abigail
             9.48110521721 -1.349963890389
                                               4 0.0084524795723
                                                                    14
                                                                          1
             14.86423973612 6.437963875942
## Aaliyah
                                              11 0.0383363361470
                                                                          0
                                                                    11
## Avery
                                               2 0.0777795538278
             18.93548647398 7.668207157403
                                                                     8
             13.87579940832 7.415770813823
## Evelyn
                                               4 0.0014052161173
                                                                    11
                                                                          0
## Kaylee
             17.02912913672 0.332856560126
                                               6 0.2179170844776
                                                                    7
                                                                          0
## Ella
             19.89998460088 0.083455503918
                                               5 0.0594544003765
                                                                    11
                                                                          1
## Ellie
             35.69396598183 -5.127922683023
                                               8 0.0510944587489
                                                                          0
## Scarlett 22.33953051095 9.959339150228
                                               8 0.0908047791731
                                                                    12
                                                                          0
```

```
## Arianna
              13.98329974549 -1.460459162481
                                                  4 0.3518035320585
                                                                       10
                                                                             0
                                                                             0
## Hailey
              7.91268056707 -1.526307961904
                                                  7 0.0820721346424
                                                                       11
## Nora
              19.90100248103
                              7.616754793562
                                                  3 0.0330518703879
                                                                       16
                                                                             0
                                                                        9
                                                                             0
##
   Addison
              12.99710325401
                              6.894308910705
                                                  9 0.2243959597322
##
  Brooklyn
             13.68086646996
                              0.398240662180
                                                  4 0.0991076346854
                                                                        8
                                                                             1
                                                                        9
                                                                             0
##
  Hannah
              14.55562563593
                              2.217311360873
                                                  5 0.0798462334385
## Mila
              13.11906331942 -5.545412516221
                                                  4 0.0899440039730
                                                                       10
                                                                             0
## Leah
              8.54522009216
                              5.488408012316
                                                  7 0.1645920748419
                                                                       12
                                                                             0
  Elizabeth 22.57449760610
                               6.929300175980
                                                 10 0.0488816974167
                                                                       11
                                                                             0
                                                                             0
##
   Sarah
              21.97616712740
                               6.341303661466
                                                  9 0.0876847888400
                                                                       10
   Eliana
              9.36987070849
                               0.881463713013
                                                  8 0.2631478195663
                                                                        4
                                                                             0
                                                                             0
   Mackenzie 21.21113618199
                             -9.860677756369
                                                  6 0.0836610563260
                                                                       13
                              5.145861022174
              7.80729428842
                                                  7 0.0505291940644
                                                                       14
                                                                             0
##
   Peyton
              13.25616247233
                              7.504017390311
                                                  6 0.0693305971929
##
  Maria
                                                                       11
                                                                             1
                                                                             0
##
  Grace
              9.56905150487
                               6.447297907434
                                                  5 0.0734409693525
                                                                        8
   Adeline
              9.93866135629
                               3.624987038784
                                                   0.1895421221759
                                                                       11
                                                                             1
                                                                        7
                                                                             0
##
                                                  7 0.3667980755182
  Elena
             20.06677521241
                               6.774886930361
##
              26.78164299802
                               9.052430847660
                                                  7 0.0084414238938
                                                                             1
   Anna
                                                                       11
##
  Victoria
             26.14308201779
                              7.173992232420
                                                  7 0.2909327614912
                                                                             0
                                                                       15
  Camilla
              16.37993345482
                              5.069515649229
                                                  9 0.0308073195111
                                                                       12
                                                                             0
## Lillian
              16.79185476205 -8.359192721546
                                                  3 0.0168902855791
                                                                       10
                                                                             0
## Natalie
              13.65098980719 -0.532937231474
                                                                             0
                                                  8 0.0585427002774
                                                                       11
## Jackson
             20.46575833753
                              5.321074989624
                                                  6 0.0622402181228
                                                                       16
                                                                             0
  Aiden
             23.10060108612
                              4.002433624119
                                                  7 0.1335706651785
                                                                        9
                                                                             0
## Lucas
              16.05161402103
                              9.459243966267
                                                  2 0.0172625056778
                                                                        8
                                                                             0
## Liam
             29.27413915820 -1.576540041715
                                                  4 0.1578349338764
                                                                        9
                                                                             0
##
                                                                             0
  Noah
             24.09678310803 -6.893312651664
                                                  6 0.0233764042043
                                                                       10
##
   Ethan
              7.66450443516 -4.731625430286
                                                  7 0.0792276647102
                                                                       12
                                                                             1
                                                                             0
##
  Mason
              10.11846607273 -5.962017434649
                                                 11 0.1555491626437
                                                                       11
  Caden
##
                              4.323527077213
                                                  5 0.3518182480500
                                                                       10
              13.87187977154
                                                                             1
##
   Oliver
              18.65044277317
                               9.860089290887
                                                   0.0207857384553
                                                                        4
                                                                             0
##
   Elijah
              18.91858234852
                              4.652845626697
                                                   0.1094852114484
                                                                       13
                                                                             1
   Grayson
              13.92786869115 -5.620933263563
                                                  3 0.4539050118143
                                                                       14
                                                                             0
              13.56372670866 -9.131066505797
##
   Jacob
                                                  9 0.3227558798073
                                                                             1
                                                                       11
  Michael
              7.78072736517
                              1.340793697163
                                                  8 0.0960077589538
                                                                        8
                                                                             0
                                                                             0
##
  Benjamin
             18.30850220536 -6.515653911047
                                                  6 0.1556799113657
                                                                       11
   Carter
              22.22022519097 -6.859387597069
                                                 10 0.0062162677808
                                                                        7
                                                                             0
   James
                                                  3 0.0950268757379
                                                                       11
                                                                             0
##
              0.33323385491
                              3.812437984161
                                                                             0
##
   Jayden
              16.24591865017
                              0.599678074941
                                                  8 0.0400629003222
                                                                       15
                                                                       12
                                                                             0
##
  Logan
              7.27015969619 -2.688242504373
                                                  9 0.0774234554994
  Alexander 20.92682966676 -1.733264103532
                                                  7 0.0204314275438
                                                                       10
                                                                             0
             23.76034776396 -3.956183134578
                                                                             0
##
   Caleb
                                                  9 0.0696721594884
                                                                       11
##
  Ryan
              25.18421311662
                              9.088041279465
                                                  0 0.3335359601324
                                                                       16
                                                                             0
##
                                                                        9
                                                                             1
   Luke
              10.15601348683 -5.593545245938
                                                   0.1744167601803
                                                                        8
## Daniel
              16.31270833126 -6.367807150818
                                                  5 0.0883252564771
                                                                             0
                                                                        9
                                                                             0
##
  Jack
              18.95423230802 -4.656140538864
                                                 13 0.0864841146348
##
  William
              20.13370294199 -4.164668023586
                                                  5 0.0211014518858
                                                                       10
                                                                             0
                                                                             0
##
   Owen
              19.83702824609
                              4.233120372519
                                                 11 0.0535048055980
                                                                       12
   Gabriel
             21.40789811685 -4.070856231265
                                                  6 0.3417137793084
                                                                       11
                                                                             0
##
   Matthew
              9.30637367080 -1.557856593281
                                                  7 0.0642879630129
                                                                       10
                                                                             0
                                                                        4
                                                                             0
##
              15.02971830895 -7.007462903857
                                                  2 0.0115809219682
   Connor
   Jayce
             21.06128846817 -0.144637399353
                                                  4 0.3121867568770
                                                                       13
                                                                             0
## Isaac
              14.24035991810
                              5.557890934870
                                                  6 0.0870648394810
                                                                       14
                                                                             1
## Sebastian 19.50766159519 -2.031480432488
                                                  4 0.0427045901631
                                                                       11
                                                                             0
```

```
## Henry
             16.07004916881
                             6.469997386448
                                                4 0.2159702510790
                                                                           1
## Muhammad 12.71670515862
                             3.401311584748
                                                4 0.0891963266203
                                                                     11
                                                                           1
## Cameron
                             4.242849601433
             20.61835820478
                                                6 0.0749697014689
                                                                      7
                                                                           0
## Wyatt
              9.17180600559 -9.333013338037
                                                5 0.0161639255858
                                                                     11
                                                                           1
## Dylan
             14.70698678311
                             4.070609072223
                                                5 0.0283224839821
                                                                     15
                                                                           0
## Nathan
             15.89140973647
                             5.647488473915
                                                4 0.0205113710992
                                                                     12
                                                                           0
## Nicholas 22.32440656593
                             0.182815603912
                                                7 0.2602150562183
                                                                           0
## Julian
             18.12855819962
                             1.398699372075
                                                8 0.1277651011207
                                                                     11
                                                                           1
## Eli
             20.88922197537
                             4.924859735183
                                                6 0.1809852905478
                                                                     16
                                                                           0
## Levi
             26.65567127924
                             2.952253725380
                                                2 0.0155583824445
                                                                      9
                                                                           0
## Isaiah
             13.66860922049 -8.088558637537
                                                6 0.0722097356079
                                                                           0
                                                                      9
                                                                           0
## Landon
             18.32423158644 -9.978384855203
                                                2 0.2240862997362
## David
             25.96945596297
                             3.999251746573
                                                4 0.0843861837721
                                                                     10
                                                                           0
## Christian 14.44793940824 -0.012656985782
                                                7 0.0029853850914
                                                                     12
                                                                           0
                                                5 0.0077320177495
                                                                           0
## Andrew
             22.90249187247
                             3.712495137006
                                                                     11
## Brayden
             19.38309573633 -8.291223808192
                                                5 0.5553177977689
                                                                     10
                                                                           0
                                                                      4
                                                                           0
## John
                             2.007378139533
                                                9 0.0195076676706
             15.26325604311
## Lincoln
             22.03513479619
                             4.988092295825
                                                4 0.0404746037076
                                                                     13
                                                                           1
```

• Create a data frame of the same data as above except make the binary variable a factor "DOMESTIC" vs "FOREIGN" for 0 and 1 respectively. Use RStudio's View function to ensure this worked as desired.

```
df <- data.frame(M)
df$X6 <- factor(df$X6, labels =c ("DOMESTIC", "FOREIGN") , levels = c(0,1))
View(df)</pre>
```

• Print out a table of the binary variable. Then print out the proportions of "DOMESTIC" vs "FOREIGN".

```
##
## DOMESTIC FOREIGN
## 78 22

table(df$X6)/100

##
## DOMESTIC FOREIGN
## 0.78 0.22
```

Print out a summary of the whole dataframe.

```
##
   Min.
          : 0.33323386
                                 :-9.97838486
                                                Min.
                                                      : 0.0
                          Min.
   1st Qu.:13.08857330
                          1st Qu.:-4.97933114
                                                1st Qu.: 4.0
##
##
   Median :16.27931349
                          Median: 0.74057089
                                                Median: 6.0
                                 : 0.55394762
   Mean
          :16.66063320
                          Mean
                                                Mean
                                                      : 5.9
                          3rd Qu.: 5.18966451
   3rd Qu.:20.94652560
                                                3rd Qu.: 7.0
```

```
##
    Max.
            :35.69396598
                            Max.
                                    : 9.95933915
                                                    Max.
                                                            :13.0
##
          Х4
                                    Х5
                                                     Х6
                                     : 4.0
##
    Min.
            :0.0014052161
                             Min.
                                             DOMESTIC:78
    1st Qu.:0.0403716779
                             1st Qu.: 9.0
                                             FOREIGN :22
##
##
    Median : 0.0795369491
                             Median:11.0
##
    Mean
            :0.1158018789
                             Mean
                                     :10.6
##
    3rd Qu.:0.1636706558
                             3rd Qu.:12.0
##
    Max.
            :0.5553177978
                             Max.
                                     :16.0
```

• Let n = 50. Create a n x n matrix R of exactly 50% entries 0's, 25% 1's 25% 2's. These values should be in random locations.

```
#multi =rmultinom(50, size =2, prob= c(0.5,0.25,0.25))
#R = matrix( multi , nrow = 50, ncol = 50)
#R

n<- 50
x<- sample(c(rep(0,n*n/2), rep(1,n*n/4), rep(2,n*n/4))) # sample randomizes
R<- matrix(x, nrow= n, ncol =n)
head(R)</pre>
```

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
##
##
   [1,]
                    0
                                 0
                                              0
                                                     2
                                                                  1
                                                                         2
##
   [2,]
              2
                           2
                                        0
                                              2
                                                                  0
                                                                         2
                                                                                         2
                                                                                                 2
                                                                                                         0
                    0
                                 1
                                                     1
                                                           0
                                                                                 1
   [3,]
              1
                    0
                           0
                                 0
                                        0
                                              0
                                                     0
                                                           0
                                                                  2
                                                                         0
                                                                                 0
                                                                                         0
                                                                                                 1
                                                                                                         0
##
## [4,]
              0
                           2
                                        2
                                              2
                                                           0
                                                                         0
                                                                                 2
                                                                                                 0
                    0
                                 1
                                                     1
                                                                  1
                                                                                         1
                                                                                                         1
                                 2
                                        2
                                                                                                         2
## [5,]
              0
                    2
                           0
                                              1
                                                     0
                                                           2
                                                                  0
                                                                          1
                                                                                 2
## [6,]
              0
                    1
                           0
                                 0
                                        1
                                              1
                                                     0
                                                           0
                                                                  1
                                                                         0
                                                                                 1
                                                                                         0
                                                                                                 0
##
          [,15]
                  [,16]
                          [,17]
                                 [,18] [,19]
                                                 [,20]
                                                         [,21]
                                                                 [,22]
                                                                        [,23]
                                                                                [,24]
                                                                                        [,25]
                                                                                                [,26]
                       2
                                                              0
##
   [1,]
               2
                                      0
                                              0
                                                      2
                                                                      1
                                                                             0
                                                                                     0
                                                                                             0
                                                                                                     0
                               1
## [2,]
                                                              2
                                                                      0
                                                                                                     2
               1
                       0
                               0
                                      0
                                              1
                                                      0
                                                                             0
                                                                                     0
                                                                                             0
               2
                                              2
                                                              2
                                                                                     2
   [3,]
                       0
                                                      0
                                                                                                     0
##
                               0
                                      1
                                                                      1
                                                                             1
                                                                                             1
                                              0
                                                              0
                                                                                     2
## [4,]
               0
                       1
                               0
                                      0
                                                      0
                                                                      1
                                                                             0
                                                                                             0
                                                                                                     1
                                              2
## [5,]
               1
                       0
                               2
                                      1
                                                      0
                                                              0
                                                                      1
                                                                             2
                                                                                     1
                                                                                                     0
## [6,]
               2
                       1
                               0
                                      0
                                              0
                                                      0
                                                              0
                                                                      1
                                                                             1
          [,27]
                          [,29]
                                 [,30]
                                         [,31]
                                                 [,32]
                                                         [,33]
                                                                 [,34]
                                                                        [,35]
                                                                                [,36]
                                                                                        [,37]
##
                  [,28]
## [1,]
                       0
                               0
                                      0
                                              0
                                                              0
                                                                      0
                                                                             2
                                                                                     0
               0
                                                      0
                                              2
## [2,]
                                      2
                                                              2
                                                                             2
                                                                                             2
               0
                       1
                               0
                                                      0
                                                                      1
                                                                                     0
                                                                                                     1
## [3,]
               2
                       1
                               2
                                      2
                                              1
                                                      0
                                                              0
                                                                      1
                                                                             1
                                                                                     0
                                                                                             2
                                                                                                     1
## [4,]
               0
                       1
                               2
                                      0
                                              1
                                                      0
                                                              1
                                                                      0
                                                                             0
                                                                                     2
                                                                                             1
                                                                                                     0
## [5,]
               0
                       1
                               0
                                      0
                                              0
                                                      0
                                                              0
                                                                      0
                                                                             0
                                                                                     0
                                                                                             0
                                                                                                     1
## [6,]
               2
                       0
                               2
                                      0
                                              2
                                                      2
                                                              0
                                                                      2
                                                                             1
                  [,40]
                          [,41]
                                 [,42]
                                         [,43]
                                                         [,45]
                                                                 [,46]
                                                                                [,48]
                                                                                                [,50]
##
          [,39]
                                                 [,44]
                                                                        [,47]
                                                                                        [,49]
## [1,]
               0
                       0
                               0
                                      0
                                              2
                                                      0
                                                              0
                                                                      1
                                                                             0
                                                                                     1
## [2,]
               0
                       2
                               0
                                              2
                                                      0
                                                              2
                                                                      2
                                                                                     0
                                                                                             2
                                                                                                     2
                                      1
                                                                             1
## [3,]
               2
                       2
                               0
                                      1
                                              0
                                                      0
                                                              1
                                                                      0
                                                                             0
                                                                                     1
                                                                                             0
                                                                                                     0
                                      2
                                                                      0
                                                                                             0
## [4,]
               0
                       0
                               2
                                              1
                                                              1
                                                                             0
                                                                                     0
                                                                                                     1
                                                      1
## [5,]
               0
                       0
                                      0
                                                      2
                                                              0
                                                                      0
                                                                                     0
                                                                                             2
                                                                                                     2
                               0
                                              1
                                                                             1
                                                              0
                                                                                             2
## [6,]
               0
                       1
                               0
                                      1
                                              1
                                                      0
                                                                      0
                                                                             0
                                                                                     0
                                                                                                     1
```

• Randomly punch holes (i.e. NA) values in this matrix so that an each entry is missing with probability 30%.

```
for(i in 50*50){
  if(rbinom(1,1,p = 0.3) == 0) {R[i] <- NA}

# R[i] == "NA"
}
head(R)</pre>
```

```
##
          [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
   [1,]
##
             2
                          2
                                0
                                       1
                                             0
                                                   2
                                                         1
                                                                1
                                                                       2
##
   [2,]
             2
                    0
                          2
                                1
                                      0
                                             2
                                                         0
                                                                0
                                                                       2
                                                                                      2
                                                                                              2
                                                                                                     0
                                                   1
                                                                               1
## [3,]
                                             0
                                                                2
             1
                          0
                                0
                                      0
                                                         0
                                                                       0
                                                                                              1
                                                                                                     0
## [4,]
             0
                    0
                          2
                                1
                                      2
                                             2
                                                         0
                                                                1
                                                                       0
                                                                               2
                                                                                              0
                                                                                                     1
                                                   1
                                                                                      1
## [5,]
             0
                    2
                          0
                                2
                                       2
                                             1
                                                   0
                                                         2
                                                                0
                                                                       1
                                                                                                     2
   [6,]
             0
                    1
                          0
                                0
                                       1
                                             1
                                                   0
                                                         0
                                                                1
                                                                       0
                                                                                              0
                                                                                                     0
##
                                                                               1
          [,15]
                 [,16]
##
                         [,17] [,18] [,19]
                                               [,20]
                                                       [,21]
                                                              [,22]
                                                                      [,23]
                                                                              [,24]
                                                                                     [,25]
                                                                                             [,26]
##
   [1,]
               2
                                     0
                                             0
                                                    2
                                                            0
                      2
                              1
                                                                   1
                                                                           0
                                                                                  0
   [2,]
                                     0
                                                            2
                                                                   0
                                                                                                  2
##
               1
                      0
                              0
                                             1
                                                    0
                                                                           0
                                                                                  0
                                                                                          0
## [3,]
                                             2
                                                            2
                                                                                  2
               2
                      0
                              0
                                     1
                                                    0
                                                                   1
                                                                           1
                                                                                          1
                                                                                                 0
## [4,]
               0
                      1
                              0
                                     0
                                             0
                                                    0
                                                            0
                                                                   1
                                                                           0
                                                                                  2
                                                                                          0
                                                                                                  1
## [5,]
                                             2
                                                                           2
               1
                      0
                              2
                                                    0
                                                            0
                                                                                          0
                                                                                                  0
                                     1
                                                                   1
                                                                                  1
               2
##
   [6,]
                      1
                              0
                                     0
                                             0
                                                    0
                                                            0
                                                                   1
                                                                                          2
                                                                                                  0
                                                                           1
##
                 [,28]
                         [,29]
                                [,30] [,31] [,32]
                                                       [,33]
                                                              [,34]
                                                                      [,35]
                                                                             [,36]
                                                                                     [,37] [,38]
          [,27]
##
   [1,]
                      0
                              0
                                     0
                                             0
                                                    0
                                                            0
                                                                   0
                                                                           2
                                                                                                  2
##
   [2,]
               0
                      1
                              0
                                     2
                                             2
                                                    0
                                                            2
                                                                   1
                                                                           2
                                                                                  0
                                                                                          2
                                                                                                  1
## [3,]
               2
                              2
                                     2
                                             1
                                                            0
                                                                                  0
                                                                                          2
                      1
                                                    0
                                                                   1
                                                                           1
                                                                                                  1
                                                                                  2
## [4,]
               0
                      1
                              2
                                     0
                                             1
                                                            1
                                                                   0
                                                                           0
                                                                                          1
                                                                                                  0
## [5,]
               0
                              0
                                     0
                                             0
                                                    0
                                                            0
                                                                   0
                                                                           0
                                                                                  0
                                                                                                  1
                      1
                                             2
## [6,]
               2
                      0
                              2
                                     0
                                                    2
                                                            0
                                                                   2
##
                                                                      [,47]
          [,39]
                 [,40]
                         [,41]
                                [,42] [,43]
                                               [,44]
                                                       [,45]
                                                              [,46]
                                                                             [,48]
                                                                                     [,49] [,50]
## [1,]
                                                                   1
## [2,]
                                             2
               0
                      2
                              0
                                                    0
                                                            2
                                                                   2
                                                                                  0
                                                                                          2
                                                                                                  2
                                     1
                                                                           1
## [3,]
               2
                      2
                              0
                                             0
                                                    0
                                                            1
                                                                   0
                                                                           0
                                                                                          0
                                                                                                  0
                                     1
                                                                                  1
## [4,]
                      0
                              2
                                     2
                                             1
                                                                   0
                                                                                          0
               0
                                                    1
                                                            1
                                                                           0
                                                                                  0
                                                                                                  1
## [5,]
               0
                      0
                              0
                                     0
                                             1
                                                    2
                                                            0
                                                                   0
                                                                           1
                                                                                  0
                                                                                          2
                                                                                                  2
## [6,]
               0
                      1
                              0
                                     1
                                             1
                                                    0
                                                            0
                                                                   0
                                                                           0
                                                                                  0
                                                                                          2
                                                                                                  1
```

• Sort the rows in matrix R by the largest row sum to lowest. Be careful about the NA's!

```
#TO-DO
sort(rowSums(R))
```

```
## [1] 25 28 30 31 31 32 32 32 33 33 33 34 34 34 34 34 34 35 35 36 36 36 37 38 ## [26] 38 38 38 38 39 39 40 40 40 41 41 41 41 41 41 41 41 43 44 45 46 46 47 48 49
```

• We will now learn the apply function. This is a handy function that saves writing for loops which should be eschewed in R. Use the apply function to compute a vector whose entries are the standard deviation of each row. Use the apply function to compute a vector whose entries are the standard deviation of each column. Be careful about the NA's! This should be one line.

```
sqrt(apply(R,2, var ))
## [1] 0.80913155763 0.82832508653 0.85714285714 0.70450445748 0.84006802446
## [6] 0.82536324718 0.82338276863 0.83397254396 0.79897894023 0.87037406924
```

```
## [6] 0.82536324718 0.82338276863 0.83397254396 0.79897894023 0.87037406924
## [11] 0.90913729010 0.80533932511 0.77222181439 0.77748941853 0.80330948111
## [16] 0.77958649427 0.81215259449 0.77617586898 0.87691481447 0.80812203564
## [21] 0.83029377638 0.85332482989 0.77222181439 0.84370417487 0.84176684929
## [26] 0.79385394225 0.80025506138 0.76371808026 0.85714285714 0.91160320763
## [31] 0.88063057185 0.89647837084 0.85714285714 0.88063057185 0.80913155763
## [36] 0.82709227578 0.83909572318 0.80533932511 0.70681810725 0.86307471240
## [41] 0.86307471240 0.79179465489 0.81441101793 0.78480466828 0.85260704636
## [46] 0.78869564239 0.87341693529 0.84006802446 0.89191378736 NA
```

• Use the apply function to compute a vector whose entries are the count of entries that are 1 or 2 in each column. This should be one line.

```
apply(R,2, sum)
## [1] 36 37 40 22 39 41 33 36 44 38 45 31 33 37 37 31 28 32 46 30 31 46 33 34 42
```

[26] 34 41 39 40 42 40 41 40 50 36 32 55 31 26 45 45 42 35 29 37 26 41 39 51 NA

• Use the split function to create a list whose keys are the column number and values are the vector of the columns. Look at the last example in the documentation ?split.

```
split(R, col(R) )
```

```
## $'1'
    [1] \ 2 \ 2 \ 1 \ 0 \ 0 \ 0 \ 2 \ 1 \ 0 \ 2 \ 0 \ 0 \ 1 \ 1 \ 2 \ 0 \ 0 \ 0 \ 1 \ 2 \ 2 \ 1 \ 1 \ 1 \ 0 \ 2 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 1 \ 1
## [39] 0 1 1 0 0 0 0 0 0 2 2 0
##
## $'2'
## [39] 1 0 0 0 1 0 2 0 0 0 2 2
##
## $'3'
    [1] \ 2 \ 2 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 2 \ 1 \ 1 \ 2 \ 0 \ 0 \ 0 \ 2 \ 1 \ 2 \ 2 \ 2 \ 0 \ 0 \ 0 \ 0 \ 2 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 0 \ 2 \ 1 \ 2 \ 2
## [39] 0 0 0 0 0 1 2 0 0 0 0 1
##
## $'4'
## [39] 0 0 0 1 0 2 1 0 0 0 0 2
##
## $'5'
    [1] \ 1 \ 0 \ 0 \ 2 \ 2 \ 1 \ 1 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 2 \ 2 \ 0 \ 1 \ 0 \ 1 \ 2 \ 0 \ 2 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0 \ 2 \ 0 \ 1 \ 1
## [39] 0 2 2 2 0 1 0 0 0 0 1 2
##
## $'6'
     \begin{smallmatrix} [1] \end{smallmatrix} 0 & 2 & 0 & 2 & 1 & 1 & 0 & 2 & 1 & 0 & 0 & 1 & 1 & 2 & 0 & 0 & 2 & 1 & 0 & 0 & 2 & 0 & 2 & 1 & 0 & 2 & 0 & 1 & 1 & 2 & 1 & 0 & 2 & 2 & 0 \\ \end{smallmatrix} 
## [39] 1 0 0 1 2 1 0 0 0 0 1
## $'7'
```

```
## [39] 0 0 1 1 0 0 0 0 1 0 0 1
##
## $'8'
## [39] 2 2 0 0 0 0 0 1 1 0 2 0
## $'9'
## [39] 1 2 0 0 1 0 2 0 0 0 1 0
## $'10'
## [39] 2 2 0 0 0 2 0 0 0 0 0
##
## $'11'
## [39] 0 2 2 1 0 0 2 0 2 2 0 0
##
## $'12'
## [39] 0 0 0 0 1 0 2 0 0 1 1 0
##
## $'13'
## [39] 0 2 0 0 2 0 0 0 1 0 1 0
##
## $'14'
## [39] 1 2 2 1 0 1 0 2 0 2 0 1
##
## $'15'
## [39] 2 0 0 1 0 1 0 2 0 0 0 0
##
## $'16'
## [39] 2 1 2 0 2 2 0 0 1 1 0 1
##
## $'17'
## [39] 1 0 0 0 1 0 0 0 0 0 1 0
## $'18'
## [39] 1 0 0 0 2 0 0 0 1 0 2 0
##
## $'19'
 \hbox{ \#\# } \quad \hbox{ [1] } \hbox{ 0 } \hbox{ 1 } \hbox{ 2 } \hbox{ 0 } \hbox{ 2 } \hbox{ 0 } \hbox{ 2 } \hbox{ 2 } \hbox{ 2 } \hbox{ 0 } \hbox{ 1 } \hbox{ 0 } \hbox{ 1 } \hbox{ 2 } \hbox{ 2 } \hbox{ 0 } \hbox{ 2 } \hbox{ 0 } \hbox{ 2 } \hbox{ 0 } \hbox{ 1 } \hbox{ 2 } \hbox{ 2 } \hbox{ 0 } \hbox{ 2 } \hbox{ 0 } \hbox{ 1 } \hbox{ 2 } \hbox{ 2 } \hbox{ 1 } \hbox{ 2 } \hbox{ 0 } \hbox{ 1 } \hbox{ 2 } \hbox{ 2 } \hbox{ 1 } \hbox{ 2 } \hbox{ 0 } \hbox{ 1 } \hbox{ 0 } \hbox{ 1 } \hbox{ 2 } \hbox{ 2 } \hbox{ 0 } \hbox{ 1 } \hbox{ 0 } \hbox{ 1 } \hbox{ 2 } \hbox{ 2 } \hbox{ 1 } \hbox{ 2 } \hbox{ 1 } \hbox{ 1 } \hbox{ 1 } \hbox{ 1 } \hbox{ 2 } \hbox{ 1 } \hbox{ 2 } \hbox{ 0 } \hbox{ 0 } \hbox{ 2 } \hbox{ 2 } \hbox{ 2 } \hbox{ 1 } \hbox{ 1 } \hbox{ 1 } \hbox{ 1 } \hbox{ 2 } \hbox
## [39] 2 2 1 0 0 1 0 1 0 0 0 0
##
## $'20'
## [39] 0 1 2 0 2 0 1 1 1 1 0 0
```

```
##
## $'21'
## [39] 0 2 2 1 0 0 0 1 0 0 0 0
## $'22'
## [39] 1 0 2 2 0 2 1 2 1 1 2 1
##
## $'23'
## [39] 0 0 1 0 1 2 0 0 1 0 0 0
## $'24'
## [39] 0 0 0 0 0 0 0 1 2 2 0 1
##
## $'25'
## [39] 1 0 2 1 1 0 2 2 2 1 1 0
##
## $'26'
## [39] 2 0 0 2 1 0 1 1 1 0 2 0
##
## $'27'
## [39] 1 2 1 2 1 2 0 1 0 0 2 1
##
## $'28'
## [39] 0 0 1 0 1 1 1 0 2 0 0 1
##
## $'29'
## [39] 1 0 0 1 0 1 2 0 1 1 0 2
##
## $'30'
## [39] 2 0 1 2 2 0 1 2 1 2 2 2
## $'31'
## [39] 2 1 1 2 2 0 0 0 2 0 0 1
## $'32'
## [39] 1 1 0 2 2 2 2 2 2 0 1 0
##
## $'33'
## [39] 1 0 0 1 1 0 1 2 1 0 1 0
##
## $'34'
```

```
## [39] 1 0 1 2 2 2 2 2 2 1 0 0
##
## $'35'
## [39] 1 1 1 0 0 1 0 2 1 0 0 1
## $'36'
## [39] 0 0 0 1 2 0 1 0 2 0 0 2
## $'37'
## [39] 2 1 1 2 2 1 0 1 1 0 2 1
##
## $'38'
## [1] 2 1 1 0 1 1 0 0 0 0 0 0 0 0 0 1 2 2 2 0 0 0 1 1 0 0 1 2 0 0 0 2 2 2 0 0 0
## [39] 0 0 0 1 1 0 1 0 0 0 2 2
##
## $'39'
## [39] 2 0 0 1 0 1 0 2 0 1 0 0
##
## $'40'
## [39] 1 2 2 0 2 2 0 0 0 2 1 0
##
## $'41'
## [39] 2 2 0 1 0 0 2 2 0 2 0 2
##
## $'42'
## [39] 2 0 0 0 0 0 1 0 0 1 2 1
##
## $'43'
## [39] 0 0 1 2 0 0 0 2 1 1 1 0
##
## $'44'
## [39] 0 2 1 0 0 0 0 0 0 1 0 1
## $'45'
## [39] 0 0 1 0 0 1 0 2 0 1 0 1
##
## $'46'
 \hbox{ \#\# } \quad \hbox{ [1] } 1 \ 2 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 2 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 0 \ 2 \ 0 \ 0 \ 1 \ 0 \ 0 \\ 
## [39] 0 0 1 0 0 0 2 2 0 0 0 0
##
## $'47'
## [39] 0 1 2 0 2 0 0 0 0 2 1 1
```

```
##
## $'48'
 [39] 0 0 0 0 1 1 2 0 0 0 1 2
##
## $'49'
 ## [39] 0 0 1 2 2 2 2 0 1 2 2 2
##
## $'50'
 [1]
      2
          2
               2
                0
                  0
                   0
                                   2
         1
                     1
                      1
                        0
## [26]
    2
                  1
                   0
                     0
                      0
                          0
                           0
             0
               0
                1
                                       1 NA
```

• In one statement, use the lapply function to create a list whose keys are the column number and values are themselves a list with keys: "min" whose value is the minimum of the column, "max" whose value is the maximum of the column, "pct_missing" is the proportion of missingness in the column and "first_NA" whose value is the row number of the first time the NA appears.

```
#a<-lapply(R,min)
#b<-lapply(R, max)
#lapply(R,if( is.na == TRUE) print )

#c<- matrix(c(a,b) ,50*50,2)

#c
```

 Set a seed and then create a vector v consisting of a sample of 1,000 iid normal realizations with mean -10 and variance 100.

```
#TO-DO
set.seed(10)
v = as.vector(rnorm(1000, -10, 10))
v
```

```
##
      [1]
          -9.8125382905817 -11.8425254206906 -23.7133054992251 -15.9916771578372
##
          -7.0545487343249 -6.1020569929983 -22.0807617542949 -13.6367601747086
##
      [9] -26.2667268170309 -12.5647839412399
                                                1.0177950308713
                                                                  -2.4421849197266
     [13] -12.3823355601872 -0.1255529658661 -2.5860987161618
##
                                                                  -9.1065273350418
##
     [17] -19.5494385615238 -11.9515038466724 -0.7447873790592
                                                                  -5.1702147516339
##
     [21] -15.9631063672021 -31.8528683816953 -16.7486593787512 -31.1906119191017
##
     [25] -22.6519802153090 -13.7366155515470 -16.8755543038792 -18.7215882671769
     [29] -11.0176100622482 -12.5378053010246 -28.5374045447914 -10.7794606607537
##
##
     [33]
           -0.3143365947546 -8.1507404000969 -23.7994357833758 -24.3551436236037
##
     [37]
           -6.3791277139339 -27.5908675375971 -13.2454400957233 -16.5156298854466
##
            0.8655139944051 -17.6254488003129 -18.2866253500109
     [41]
                                                                  -1.6552609691155
##
     [45] -19.6765198675991 -10.2881533547586 -7.6747484742461 -13.0120868150418
##
      \begin{bmatrix} 49 \end{bmatrix} \ -16.7761458314933 \ \ -3.4477236376478 \ -14.0063754703174 \ -13.3455656507335 
     [53]
            3.6795395319196 11.3776710365012 -4.9418073547097 -2.1365761576084
##
                                                                  -7.0901251157023
     [57] -19.0221194417864 -4.6710300767167 -16.4589425354921
##
     [61] -22.3759446887722 -14.5617627511781 -18.3032265472473
                                                                  -6.5988435632574
##
##
     [65]
            0.6637639568217
                               2.1612583807980 -2.6430934236695 -14.8120861731558
          -4.3725523714188 -22.4631971188920 -6.1907778737432 -24.3042725279669
##
     [69]
     [73] -20.4844550487860 -12.1850355053459 -24.8993623673554
##
                                                                  1.7270628121431
```

```
##
     [77] -24.7982702157166 -14.3038781607722 -20.5163864204345
                                                                 5.2258634405410
##
          -4.0717194541392 -12.2266150901927 -2.8710572375154
     [81]
                                                                -2.8339916625895
##
          -5.5975813561586 -8.4116937868190 -3.4023586166805 12.2051966293556
##
     [89] -21.8394507406540 -10.7395583449749 -14.1635467488652 -11.9148234375263
##
     [93]
          -9.3045521859260
                             1.5534831801052
                                              -4.0504265304951 -24.1964510835699
     [97] -26.0667724535804
                           -1.0707410043682 -8.5183204481227
##
                                                                 2.2702839010139
##
    [101] -17.6180433917803
                           -5.8062459411009 -20.3994336463235
                                                               -2.8842603400737
##
    [105] -16.3321301496783
                            -4.3682533554985
                                             -3.3901331416840 -26.5805085732545
##
    Γ1097
            0.2816797701792
                             1.2795361401459 -22.8015460342218
                                                                 1.2886822740957
##
    [113] -14.6413452716498 -13.1576020953137
                                              -0.7570685316505
                                                                -9.2285527601422
    [117]
            0.3992360511188
                            -2.5811379326182
                                               2.5554485828951
                                                                -0.4908103354382
                           -7.9711822203016 -10.3173974383773 -21.9558030033457
##
    [121] -14.8136560727329
##
    [125]
          -3.7631876315157 -19.1480448366691 -7.5124199229190 -20.6262279318038
    [129] -13.6398224719576 -22.0699485337827
##
                                               4.2921278138977
                                                                -3.6656410901717
##
    [133] -29.9681561765642 -16.8183217309621 -14.6005547931070 -19.8306919414776
##
    [137]
          -5.0466828711166
                            -2.7418249976747 -3.3270126810708
                                                                -0.4521356353341
    [141] -26.7533217929194 -22.0518539249191 -29.6325248922053
##
                                                                 4.7075230981397
##
    [145]
          -6.2752766144940
                             0.6587933403768 -4.6935013164268
                                                                -8.9801655411587
    Γ1497
           3.3778246578648 -9.1276523150887 -13.9110420740045 -12.4986748459556
##
##
    Γ153]
            1.5510474589615 -18.6472723983100 -18.6667834236831 -33.2101703034786
##
    Γ157]
          -3.9116983108215
                             1.5000604820099 -21.9959767173686 -25.8000075454988
          -3.4683380635781 -15.4940848512297 -4.7894547468747 -16.9940306640950
##
    [161]
    ##
          -8.1623610733187 -24.3514718265180 -21.3739989812347 -14.1464532687800
##
    [169]
##
    [173]
          -8.5606571184864
                             0.6202433069828 -15.7079390273540
                                                                 2.7718137641215
    Γ177]
          -7.7171067945992 -13.0881306450274 -0.4017086940442 -4.5117762518792
##
                            -3.5649996487183 -23.6030614350351 -11.9850610640319
    [181]
          -5.7448690622802
##
    [185]
          -3.8069732312462 10.6820960503683 -13.0528475419725
                                                                -7.1875438777014
##
          -3.0868266329410 -9.5363856185668 -8.8697063837404 -0.0466812571087
    [189]
##
    [193] -16.8115136132165 -22.7705724668769 -24.6869774983108 -13.1347406653587
##
    [197] -27.0365949266331 -23.5051465613771 -21.0209367720916 -20.9954301452935
##
    [201]
            2.1551377619565
                            -6.6912351489586
                                               3.9027511927468
                                                                -1.2795301497889
##
    [205] -20.8081702266027
                            -5.0417840855346
                                               0.5262755621631 -22.7464995015128
    [209] -11.9366672842338 -22.9508364255337
##
                                              -8.5811971532135
                                                                 2.6171505198662
##
    [213] -14.3150032806965 -28.2271258950182
                                              -6.4745604124689 -23.4845144147378
          -2.9231168209257 -14.1089093679878 -14.4604517992225 -20.4115630166875
##
    [217]
##
    [221] -13.2922471615401 -12.8282162413235
                                              -5.6757087450465 -13.0760709506342
##
    [225] -10.5663630788932 -2.6648457979973 -9.0268838033482
                                                                 6.3089173658816
                             3.2956476445216 -12.7882349563446 -22.6673154414092
##
    [229]
          -4.3938930099780
    [233] -12.4914839404027 -9.8201158543120
                                             -6.2292727288967
                                                                -2.0399144247256
##
    [237] -18.4067741709857 -32.0547175082621 -21.2805599106249 -23.4130995880245
    [241]
            6.0511404288097 -2.5557627151146 -1.3791779404662 -6.0484418452380
##
##
    [245]
          -4.9088130366967 -11.2255012583063 -9.0741535282172 -13.5787991433363
##
    [249] -13.5965522434701
                             0.2857072088428
                                               0.7789259245098
                                                               -0.6821878476750
    [253] -24.6079386697760 -19.0607557624934 -16.8034783139241
                                                                 0.6316603678904
    [257] -16.9241315212615 -21.3362826529090 -20.9461543379722 -20.1290361883673
##
##
    [261]
          -5.8972267411411
                            -5.2225955807321 -33.2987954506654
                                                                -9.8374453482326
##
    [265]
          -0.1964647685352 -1.9365173518264 -8.8039911110870 -34.3661560431758
##
    [269]
          -9.6897752387761 -13.3574669799984 -12.6377616192376 -13.5585246088020
##
    [273] -14.8115479829018
                            -7.7726453218213 14.2991031869739
                                                                 4.9629811873421
    [277] -17.1720820275909 -14.6705390018763
                                              -3.3707654714059
##
                                                                13.0017689094660
##
    [281]
          -6.7248985878341 -9.3613651838309 -21.3956093996767
                                                                 1.8041020362035
##
    [285]
          -9.5861152296685 -22.1359356338470 -9.2680422337219 -12.5732459434554
##
    [289]
          -7.3319358905787
                            3.8772432571642 -8.0692036497606 -4.0768337739957
```

```
[293] -18.2997452691578 -6.0742671835751 -6.1513238931919
                                                                   0.5104466572565
##
            1.5579748458375 -20.3443795894203 -12.5446806580427
    [297]
                                                                   2.7368426608477
##
    [301]
            5.0254463898139
                            -4.0959053285336 -16.3068545138345
                                                                 -2.0765046270573
    [305]
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          -9.4617851897070 -13.8956188390521
##
    [961]
                                                8.7782555336490 -24.5760672674387
          -2.7614462162304 -22.1807626153914 -13.0575886988837
##
    [965]
                                                                 -9.7560228337793
                                                                  2.9563746444499
##
    [969]
          -6.4773389881232 -1.7621024448896 -4.0221343890048
##
    [973] -15.7806617916108 -8.2702501953435 -15.8119624600776 -17.8259059633484
##
    [977] -26.6682920426637 -17.1347324830373 -15.0667582780123 -16.9518394411486
    [981]
          -4.5839218883509 -15.8107729636208 -5.6916794897939
                                                                 -3.2829881041342
    [985] -14.3350730550368 -17.8098342889453 -5.8370181762388 -18.2162059963196
##
##
    [989]
          -7.8892410964089 -2.4517683025882
                                              7.8010975268365
                                                                -3.3405231809554
##
    [993] -10.1073381954854 -22.0105460642858 -16.4339778448903 -2.0270768952201
         -4.7175172561890 -7.1633026119330 -10.1213930489634 -11.9191377747732
##
    [997]
```

• Repeat this exercise by resetting the seed to ensure you obtain the same results.

```
#TO-DO

set.seed(10)
v = as.vector(rnorm(1000, -10, 10))
v
```

```
##
      [1]
          -9.8125382905817 -11.8425254206906 -23.7133054992251 -15.9916771578372
##
          -7.0545487343249 -6.1020569929983 -22.0807617542949 -13.6367601747086
##
      [9] -26.2667268170309 -12.5647839412399
                                               1.0177950308713
                                                                -2.4421849197266
##
      \begin{bmatrix} 13 \end{bmatrix} \ -12.3823355601872 \ \ -0.1255529658661 \ \ -2.5860987161618 \ \ -9.1065273350418 
##
     [17] -19.5494385615238 -11.9515038466724 -0.7447873790592 -5.1702147516339
     ##
##
     [25] -22.6519802153090 -13.7366155515470 -16.8755543038792 -18.7215882671769
##
     ##
          -0.3143365947546 -8.1507404000969 -23.7994357833758 -24.3551436236037
     [33]
##
     [37]
          -6.3791277139339 -27.5908675375971 -13.2454400957233 -16.5156298854466
##
     [41]
           0.8655139944051 -17.6254488003129 -18.2866253500109 -1.6552609691155
##
     [45] -19.6765198675991 -10.2881533547586 -7.6747484742461 -13.0120868150418
##
      \left[ 49 \right] \; \text{-}16.7761458314933 \quad \text{-}3.4477236376478 \; \text{-}14.0063754703174 \; \text{-}13.3455656507335} 
##
     [53]
            3.6795395319196
                            11.3776710365012 -4.9418073547097
                                                                -2.1365761576084
##
     [57] -19.0221194417864 -4.6710300767167 -16.4589425354921
                                                                -7.0901251157023
      \begin{bmatrix} 61 \end{bmatrix} \ -22.3759446887722 \ -14.5617627511781 \ -18.3032265472473 \ -6.5988435632574 
##
##
     Γ651
                              2.1612583807980 -2.6430934236695 -14.8120861731558
           0.6637639568217
##
     [69]
          -4.3725523714188 -22.4631971188920 -6.1907778737432 -24.3042725279669
##
     [73] -20.4844550487860 -12.1850355053459 -24.8993623673554
                                                                 1.7270628121431
##
     [77] -24.7982702157166 -14.3038781607722 -20.5163864204345
                                                                  5.2258634405410
     [81]
          -4.0717194541392 -12.2266150901927
                                              -2.8710572375154
                                                                -2.8339916625895
##
##
     [85]
          -5.5975813561586 -8.4116937868190 -3.4023586166805
                                                                12.2051966293556
##
     [89] -21.8394507406540 -10.7395583449749 -14.1635467488652 -11.9148234375263
##
     [93]
          -9.3045521859260
                            1.5534831801052 -4.0504265304951 -24.1964510835699
##
     [97] -26.0667724535804
                            -1.0707410043682
                                              -8.5183204481227
                                                                  2.2702839010139
    [101] -17.6180433917803
                            -5.8062459411009 -20.3994336463235
##
                                                                -2.8842603400737
##
    [105] -16.3321301496783
                            -4.3682533554985 -3.3901331416840 -26.5805085732545
##
    Γ1097
           0.2816797701792
                            1.2795361401459 -22.8015460342218
                                                                 1.2886822740957
    [113] -14.6413452716498 -13.1576020953137 -0.7570685316505 -9.2285527601422
```

```
[117]
            0.3992360511188 - 2.5811379326182 2.5554485828951 - 0.4908103354382
    [121] -14.8136560727329 -7.9711822203016 -10.3173974383773 -21.9558030033457
##
           -3.7631876315157 -19.1480448366691 -7.5124199229190 -20.6262279318038
    [129] -13.6398224719576 -22.0699485337827
                                                4.2921278138977 -3.6656410901717
##
##
    [133] -29.9681561765642 -16.8183217309621 -14.6005547931070 -19.8306919414776
           -5.0466828711166 -2.7418249976747 -3.3270126810708 -0.4521356353341
##
    [137]
    [141] -26.7533217929194 -22.0518539249191 -29.6325248922053
                                                                   4.7075230981397
           -6.2752766144940
##
    [145]
                              0.6587933403768 -4.6935013164268
                                                                 -8.9801655411587
##
    Γ1497
            3.3778246578648
                             -9.1276523150887 -13.9110420740045 -12.4986748459556
##
    [153]
            1.5510474589615 -18.6472723983100 -18.6667834236831 -33.2101703034786
    [157]
           -3.9116983108215
                              1.5000604820099 -21.9959767173686 -25.8000075454988
           -3.4683380635781 -15.4940848512297 -4.7894547468747 -16.9940306640950
##
    [161]
##
    [165] -14.3890931479220 -16.7731929611669 -0.4085880522465 -24.6817332946240
           -8.1623610733187 -24.3514718265180 -21.3739989812347 -14.1464532687800
##
    [169]
##
    [173]
                              0.6202433069828 -15.7079390273540
                                                                   2.7718137641215
           -8.5606571184864
##
    [177]
           -7.7171067945992 -13.0881306450274 -0.4017086940442
                                                                  -4.5117762518792
                             -3.5649996487183 -23.6030614350351 -11.9850610640319
##
    [181]
           -5.7448690622802
##
    [185]
           -3.8069732312462 10.6820960503683 -13.0528475419725
                                                                  -7.1875438777014
                             -9.5363856185668 -8.8697063837404
##
    Г1897
           -3.0868266329410
                                                                 -0.0466812571087
##
    [193] -16.8115136132165 -22.7705724668769 -24.6869774983108 -13.1347406653587
##
     \left[ 197 \right] -27.0365949266331 -23.5051465613771 -21.0209367720916 -20.9954301452935 
            2.1551377619565
                             -6.6912351489586
                                                 3.9027511927468
                                                                 -1.2795301497889
##
                                                 0.5262755621631 -22.7464995015128
                             -5.0417840855346
##
    [205] -20.8081702266027
    [209] -11.9366672842338 -22.9508364255337
##
                                               -8.5811971532135
                                                                   2.6171505198662
##
    [213] -14.3150032806965 -28.2271258950182
                                              -6.4745604124689 -23.4845144147378
    [217]
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##
    [221] -13.2922471615401 -12.8282162413235
                                               -5.6757087450465 -13.0760709506342
##
    [225] -10.5663630788932
                             -2.6648457979973 -9.0268838033482
                                                                   6.3089173658816
##
          -4.3938930099780
                              3.2956476445216 -12.7882349563446 -22.6673154414092
##
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                                               -6.2292727288967
                                                                  -2.0399144247256
##
    [237] -18.4067741709857 -32.0547175082621 -21.2805599106249 -23.4130995880245
##
    [241]
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                             -2.5557627151146
                                               -1.3791779404662
                                                                  -6.0484418452380
##
    [245]
           -4.9088130366967 -11.2255012583063
                                               -9.0741535282172 -13.5787991433363
                              0.2857072088428
                                                0.7789259245098
##
    [249] -13.5965522434701
                                                                  -0.6821878476750
##
    [253] -24.6079386697760 -19.0607557624934 -16.8034783139241
                                                                   0.6316603678904
##
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##
           -5.8972267411411
                             -5.2225955807321 -33.2987954506654
                                                                  -9.8374453482326
##
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           -0.1964647685352 \quad -1.9365173518264 \quad -8.8039911110870 \quad -34.3661560431758
           -9.6897752387761 -13.3574669799984 -12.6377616192376 -13.5585246088020
##
    [269]
    [273] -14.8115479829018 -7.7726453218213
                                              14.2991031869739
##
                                                                   4.9629811873421
    [277] -17.1720820275909 -14.6705390018763
                                               -3.3707654714059
                                                                  13.0017689094660
    [281]
                            -9.3613651838309 -21.3956093996767
                                                                   1.8041020362035
##
           -6.7248985878341
##
    [285]
           -9.5861152296685 -22.1359356338470
                                               -9.2680422337219 -12.5732459434554
                                                                  -4.0768337739957
##
          -7.3319358905787
                              3.8772432571642
                                              -8.0692036497606
    [289]
##
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                            -6.0742671835751 -6.1513238931919
                                                                   0.5104466572565
##
    [297]
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                                                                   2.7368426608477
##
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                             -4.0959053285336 -16.3068545138345
                                                                  -2.0765046270573
##
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                                                                  -2.3315606553862
##
    [309] -24.0350302182772 -21.7604677961141 -4.8840353081520
                                                                   3.1676526377830
##
    [313]
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                                                                   9.9643445216969
##
            5.4321779434101 -22.2833762626182 16.4448799222478
    [317]
                                                                  -2.4298629172563
##
    [321]
            0.5534519215293
                            -0.4205510469419 -1.6612094235735 -11.6927557001864
##
    [325] -14.0443364307844 -7.0439842629709 -12.3187450723486 -14.4807823162639
           -9.7768920342761 -9.5553270276387 -5.1927883470936 -3.6438014483043
##
    [329]
```

```
[333] -30.0074239307650 -16.9065550376296 -11.3064518930652 -13.4425178302364
##
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                                                                -4.4520652472126
            2.3544587854851
                           -7.1486661869311 -14.5879292777288
##
                                                                -3.7652197813763
    [345] -17.2399509164038
                             6.1941870348572 -16.1667341021694
##
                                                                -6.1545894255312
##
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                                                                 2.7114600133104
                             1.2227338293318 11.5843864176903
##
    [353] -26.0508544127984
                                                                -5.7175338697736
##
    [357]
            2.0117869045970
                             0.3169011615184 -3.4612574728974
                                                                10.1208177317955
##
    [361]
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                           -2.7359064591801 -23.9965713658319 -22.8779516329080
##
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##
    [369]
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                                                                -5.9963827138848
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                                                               12.1977624873515
          -6.8573019208592 -15.6378507451632 -24.8569615831883
##
    [377]
                                                                -5.8470140690619
##
    [381] -15.2806368267859 -13.5047061745097 -2.6937806270378 -15.5662416507982
    [385] -24.4976053616599 -20.5199642811248 -16.8283861878505 -16.1294117857592
##
##
           8.9078003505454 \ -11.4541053359420 \ -16.3942372058860 \ -14.1117604522169
    [389]
##
    [393]
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                                                                -9.6200023403604
          -0.7893525245555 11.3496563845849 -15.9982693155619
##
    [397]
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##
    [401] -10.7945701712045
                             1.8175154981561 11.8614406267608
                                                                -5.9382506929464
    [405] -17.3835910458486 -29.5648670291891 -29.5004570159855 -19.4099781569260
##
##
    [409]
            1.9778676862693 -16.2423939035829 -11.3286965510209 -10.1722092219131
##
    [413] -14.5962928217906
                             4.7293679052688 11.6931961261593 -40.0143130631433
    [417] -27.7198558305170 -13.6483922283578 -6.2546621931091 -22.3407792667110
##
                              2.3305745705665 -15.9312865679849
                                                                -2.4773756067248
##
    [421]
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          -3.8795449311322 -12.2865736527439 -17.0483934989938
##
    [425]
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##
    [429]
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                             3.4509418039941 -11.2369152893043
                                                                -0.6609754644998
    [433]
          -9.8050315437978 -1.6914789025703 -13.0449466799607 -10.5928127710359
##
    [437]
           ##
    [441]
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                                               0.0679265745540
                                                                -7.2578508365171
##
    [445] -10.8038236456008 -19.0355249532682
                                             -5.2685489702804
                                                                  3.8848897790595
##
    [449]
          -9.6525390623583 -22.9258502807925
                                              1.6396750490781 -25.2338459706839
##
    [453] -35.1833505361223 -17.0752923056637 -12.8743288270911 -14.3530831147691
##
    [457] -13.4307877074330 -10.3931088400990 -1.1303401227621 -13.5994840081589
##
    [461] -17.2895427063139
                             7.5174561927189 -10.8603859023211
                                                                  1.0636301587614
    [465] -10.1917783723957 -24.9346017845903 17.0063662306933 -17.4369442224344
##
##
    [469]
            0.6519498093684 -10.3208173166496 -15.3995968933919 -29.2564356755388
##
           0.0783137615909 -12.7923479676676 -22.4956585528460
                                                                 2.4849112786506
    [473]
##
    [477] -11.9221337656587 -0.8802376891256 -31.5826968002626
                                                                  2.8961053233286
##
    [481] -14.2810996555383 -12.5500289297295
                                               3.2715823880373 -1.6130987938999
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                                             -8.9389416059358 -28.4401675772715
##
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##
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    [493]
    [497]
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##
##
    [501]
          -1.3052495509230 -16.8000959781380 -8.2678546129149 -11.5943803907549
##
    [505]
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                             6.9435049142761
                                               2.3996868635003
                                                               -9.7056325685223
##
    [509]
           6.5721449904792
                             1.3122314018687 -24.0241063212584
                                                                -8.4322953888707
##
    [513]
          -1.3249140356862 -10.3323515710174 -0.4593544367399
                                                                 1.3009672517014
##
    [517]
          -6.0630268791701
                            -6.2319167203290 -12.5174290704864
                                                                -4.9590510917322
##
    [521] -23.2980347134830 -11.1829945251477 -16.3324846660885
                                                                -3.2230865528305
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##
    [525] -12.9788176477430
                            -3.7207775287270
##
    [529] -23.4984288507140
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                                               2.9384271937366 -10.5959434618245
##
    [533] -16.8506234517232 -24.5343930439156
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                                                                  1.7616908935200
##
          -1.3595492182401 -32.9673252346068 -23.9181001193225 -23.8587674502157
##
    [541] -20.7304684391546 -19.4142550319634 -15.8643430972218
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         -5.4103779330522 -21.9344507199800 -2.0811072832840 -27.7230491079952
##
    [545]
```

```
[549] -15.8772242199909 -22.8237031255411 -13.1213466098008 -16.9877530062472
##
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##
           -0.7343058916559 -12.1869186057380 -0.0686650257996 -29.2333434248037
    [561] -20.5271518447267
                            -1.0960223807401 25.4114027762577 -2.5848925731212
##
##
    [565] -12.0747125409922
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                                                4.2636484940947 -14.4316678948262
          -6.3281001334818 -3.0417830388934 -0.6655527138822
                                                                   4.9188908255981
##
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##
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##
    [577]
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##
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    [589]
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                            -7.6366740733879 10.6167415943736 -22.9005998583527
##
    [593]
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##
    [597]
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                             7.8539022670878 -7.8705975690789 -1.1530785394932
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##
##
            3.9571911930986 -22.1122381679601 -12.0414166079742 -25.5245132607939
    [605]
##
    [609]
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           -5.0196626493359 \ -16.7386820519833 \ -18.8698139561134 \ -27.3137735086099
##
    [613]
##
    [617]
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    [621] -11.1722237431415 -9.0177706141557 -16.7685722184453 -10.4924635492814
##
##
    [625] -15.6071975993502 13.9915486524696 -10.8987210159804 -18.2164841778561
##
    [629] -12.8696176159712 -8.6872112602923 -20.6208395043809
                                                                 -2.6641896427090
           -6.7730780152115 -13.4897977134871
                                                 2.8352566424672 -20.1448804888177
##
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```

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```

```
## [981] -4.5839218883509 -15.8107729636208 -5.6916794897939 -3.2829881041342

## [985] -14.3350730550368 -17.8098342889453 -5.8370181762388 -18.2162059963196

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## [993] -10.1073381954854 -22.0105460642858 -16.4339778448903 -2.0270768952201

## [997] -4.7175172561890 -7.1633026119330 -10.1213930489634 -11.9191377747732
```

• Find the average of v and the standard error of v.

```
#average <- mean
average <- function(x) sum(x)/length(x)
standard_error <- function(x) sd(x)/sqrt(length(x))

Av= average(v)
Av

## [1] -9.8862525833
standard_error(v)</pre>
```

[1] 0.31364801174

• Find the 5%ile of v and use the qnorm function to compute what it theoretically should be. Is the estimate about what is expected by theory?

```
#TO-DO
quantile(v, 0.05)

## 5%
## -26.189131915
```

• What is the percentile of v that corresponds to the value 0? What should it be theoretically? Is the estimate about what is expected by theory?

```
#TO-DO

print("Theoreticall percentile of 'v'")

## [1] "Theoreticall percentile of 'v'"

z=pnorm(0,-10, 100)
print(z)

## [1] 0.53982783728

print("Percentile of 'v' that corresponds to the value ~ 0")
```

[1] "Percentile of 'v' that corresponds to the value ~ 0"

```
for(i in 1:100){
y= i/100
x= quantile(v, y)
if(x<1 && x>-1) { print(x)}
##
             81%
## -0.82111960301
             82%
## -0.48021788347
##
            83%
## -0.12930762607
           84%
## 0.23869179684
##
            85%
## 0.62104299086
           86%
## 0.87489344693
```