

1. What is the current value of a bond that pays annual coupon payments at a rate of 3%, has a face value of \$1,000 and matures in 4 years if the discount rate is 4%.

$$\text{Coupon} = 1000 \times 0.03 = 30$$

$$\text{Bond value} = 30/(1.04)^1 + 30/(1.04)^2 + 30/(1.04)^3 + 1030/(1.04)^4$$

$$\text{Bond value} = 28.85 + 27.74 + 26.67 + 880.45$$

$$\text{Current value} = \$963.70$$

2. What is the current value of a bond that pays semi-annual coupon payments at a rate of 8% per year, has a face value of \$1,000, matures in 3 years and has a yield to maturity (in EAR terms) of 6%?

$$\text{Coupon} = (1000 \times 0.08)/2 = 40$$

$$\text{Bond value} = 40/(1.06)^{0.5} + 40/(1.06)^1 + 40/(1.06)^{1.5} + 40/(1.06)^2 + 40/(1.06)^{2.5} + 1040/(1.06)^3$$

$$\text{Current value} = \$1056.62$$

3. What is the current yield of a bond that has most recently traded for \$1040, has a face value of \$1,000 and coupon rate of 10% of its face value?

$$1000 \times 0.1 / 1040 = 9.62\%$$

4. What is the yield to maturity of a zero coupon bond which has a face value of \$1,000 and a maturity of 8 years if it has most recently traded for \$750?

$$\text{Value} = \text{FV} / (1 + \text{YTM})^8$$

$$750 = 1000 / (1 + \text{YTM})^8$$

$$750 \times (1 + \text{YTM})^8 = 1000$$

$$(1 + \text{YTM}) = \sqrt[8]{1000/750}$$

$$(1 + \text{YTM}) = 1.0366$$

$$\text{YTM} = 3.66\%$$

5. What is the yield to maturity of a bond that pays annual coupon payments at a rate of 7%, has a face value of \$1,000, matures in 2 years and has most recently traded at \$960

$$\text{If } a \times x^2 + b \times x + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$1000 \times 0.07 = 70$$

$$960 = 70 / (1 + \text{YTM}) + 1070 / (1 + \text{YTM})^2$$

$$= \$960 \times (1 + \text{YTM})^2 = \$70 \times (1 + \text{YTM}) + \$1070$$

$$0 = \$960 \times (1 + \text{YTM})^2 - \$70 \times (1 + \text{YTM}) - \$1070$$

$$\therefore a = 960; b = -70; c = -1070$$

$$(1 + YTM) = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$(1+YTM) = -(-70) \pm \sqrt{(-70)^2 - 4 \cdot 960 \cdot (-1070)} / (2 \cdot 960)$$

$$(1+YTM) = -(-70) \pm 2025.81 / (2 \cdot 960)$$

$$(1+YTM) = -(-70) - 2025.81 / (2 \cdot 960) = -1.019$$

$$(1+YTM) = -(-70) + 2025.81 / (2 \cdot 960) = 1.09$$

$$(1+YTM) = (1.0915..., -1.019)$$

$$YTM = 9.2\%$$

GOAL SEEK: 9.28%

6. What is the yield to maturity of the same bond outlined above if it matures in 5 years and not 2?

$$1000 \times 0.07 = 70$$

$$960 = 70 / (1+YTM) + 70 / (1+YTM)^2 + 70 / (1+YTM)^3 + 70 / (1+YTM)^4 + 1070 / (1+YTM)^5$$

Goal Seek: 8.0%

7. A firm has a measured level of systematic risk (equity β) of 0.8. The firm is an income firm and has a dividend policy \$0.2 per year with no future expected growth. Using the discounted dividend model what is the expected share price if the risk free rate is 1% and the return on the market is 6%?

$$E[r] = 0.01 + 0.8 \times (0.06 - 0.01) = 0.05$$

$$Sp = 0.2 / 0.05 = \$4$$