

Asignatura	Sintaxis y Semántica de Lenguajes
Carrera	Ingeniería en Sistemas de Información
Alumno	

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Evaluación Final

P1	Construya la TAS correspondiente a la siguiente CFG [60 pts]
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$$\begin{aligned}
 W &\rightarrow WF \mid KM \mid CM \mid MW@W \mid MDM \mid W^*H \\
 H &\rightarrow C \mid D \mid [W] \\
 K &\rightarrow [W] \mid C \\
 P &\rightarrow P \mid Pa \mid E \mid (P) \\
 F &\rightarrow FP \mid aL \mid \varepsilon \\
 E &\rightarrow EbG \mid GaW \mid aPb \\
 D &\rightarrow \#D \mid D/ \mid \# \\
 M &\rightarrow \varepsilon \mid MG \\
 C &\rightarrow Cg \mid Mg \mid aB \mid uC
 \end{aligned}$$

P2 (40 pts)	En base a la CFG de P1 : [15 pts] A. Construya una gramática equivalente en CNF [20 pts] B. Construya una gramática equivalente en GNF [5 pts] C. Construya un PDA equivalente
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Limpiamos la gramática

$W \rightarrow [W] \mid C \mid W@W \mid D \mid W^*H$
 $H \rightarrow C \mid D \mid [W]$
 $D \rightarrow \#D \mid D \mid \# \quad \text{#####D} \quad D/////$
 $C \rightarrow Cg \mid g \mid uC$

Sacamos ambigüedad de W, D, C

$W \rightarrow W@H \mid W^*H \mid H$
 $H \rightarrow C \mid D \mid [W]$
 $D \rightarrow \text{NB}$
 $N \rightarrow \#N \mid \#$
 $B \rightarrow /B \mid \text{eps}$
 $C \rightarrow UG$
 $U \rightarrow uU \mid \text{eps}$
 $G \rightarrow gG \mid g$

Sacamos RI de W

fórmula de RI

$A \rightarrow A \text{ alfa} \mid \text{beta}$

$A \rightarrow \text{beta } W$

$W \rightarrow \text{alfa } W \mid \text{epsilon}$

Gramática en LL1 sacar ambigüedad, RI y debe estar factorizada

$W \rightarrow HZ$
 $Z \rightarrow @HZ \mid *HZ \mid \text{eps}$
 $H \rightarrow C \mid D \mid [W]$
 $D \rightarrow \text{NB}$
 $N \rightarrow \#M$
 $M \rightarrow N \mid \text{eps}$
 $B \rightarrow /B \mid \text{eps}$
 $C \rightarrow UG$
 $U \rightarrow uU \mid \text{eps}$
 $G \rightarrow gL$
 $L \rightarrow G \mid \text{eps}$

Para $W \rightarrow HZ$

$\text{prim}(HZ) = \{u, g, \#, []\}$
 $\text{prim}(H) = \{u, g, \#, []\}$
 $\text{prim}(C) = \{u, g\}$
 $\text{prim}(D) = \{\#\}$
 $\text{prim}([W]) = \{[]\}$

Para $Z \rightarrow @HZ$

$\text{prim}(@HZ) = \{@\}$

Para $Z \rightarrow *HZ$

$\text{prim}(*HZ) = \{*\}$

Para $Z \rightarrow \text{eps}$
 $\text{prim}(\text{eps}) = \{\text{eps}\}$
 $\text{sig}(Z) = \{\$, \}$
 $\text{sig}(W) = \{\$, \}$

Para $H \rightarrow C$
 $\text{prim}(C) = \{u, g\}$

Para $H \rightarrow D$
 $\text{prim}(D) = \{\#\}$

Para $H \rightarrow [W]$
 $\text{prim}([W]) = \{\}$

Para $D \rightarrow \text{NB}$
 $\text{prim}(\text{NB}) = \{\#\}$

Para $N \rightarrow \#M$
 $\text{prim}(\#M) = \{\#\}$

Para $M \rightarrow N$
 $\text{prim}(N) = \{\#\}$

Para $M \rightarrow \text{eps}$
 $\text{prim}(\text{eps}) = \{\text{eps}\}$
 $\text{sig}(M) = \{\$, \, , \, @, *, /\}$
 $\text{sig}(N) = \{\$, \, , \, @, *, /\}$
 $\text{prim}(B) = \{/, \text{eps}\}$
 $\text{sig}(B) = \{\$, \, , \, @, *\}$
 $\text{sig}(D) = \{\$, \, , \, @, *\}$
 $\text{sig}(H) = \{\$, \, , \, @, *\}$
 $\text{prim}(Z) = \{@, *, \text{eps}\}$
 $\text{sig}(Z) = \{\$, \}$
 $\text{sig}(W) = \{\$, \}$

Para $B \rightarrow /B$
 $\text{prim}(/B) = \{/\}$

Para $B \rightarrow \text{eps}$
 $\text{prim}(\text{eps}) = \{\text{eps}\}$
 $\text{sig}(B) = \{\$, \, , \, @, *\}$

Para $C \rightarrow \text{UG}$
 $\text{prim}(\text{UG}) = \{u, g\}$

Para $U \rightarrow uU$
 $\text{prim}(uU) = \{u\}$

Para $U \rightarrow \text{eps}$
 $\text{prim}(\text{eps}) = \{\text{eps}\}$
 $\text{sig}(U) = \{g\}$

Para $G \rightarrow gL$
 $\text{prim}(gL) = \{g\}$

Para $L \rightarrow G$
 $\text{prim}(G) = \{g\}$

Para $L \rightarrow \text{eps}$
 $\text{prim}(\text{eps}) = \{\text{eps}\}$
 $\text{sig}(L) = \{\$,], @, *\}$
 $\text{sig}(G) = \{\$,], @, *\}$
 $\text{sig}(C) = \{\$,], @, *\}$
 $\text{sig}(H) = \{\$,], @, *\}$

	@	*	[]	#	/	u	g	\$
W			HZ		HZ		HZ	HZ	
Z	@HZ	*HZ		eps					eps
H			[W]		D		C	C	
D					NB				
N					#M				
M	eps	eps		eps	N	eps			eps
B	eps	eps		eps		/B			eps
C							UG	UG	
U							uU	eps	
G								gL	
L	eps	eps		eps				G	eps

CNF, GNF y PDA

Limpiamos la gramática

$W \rightarrow [W] \mid C \mid W@W \mid D \mid W^*H$
 $H \rightarrow C \mid D \mid [W]$
 $D \rightarrow \#D \mid D/ \mid \#$
 $C \rightarrow Cg \mid g \mid uC$

CNF (2 variables o 1 terminal)

$W \rightarrow XZ \mid WA \mid WE \mid ND \mid DV \mid \# \mid CG \mid g \mid UC$
 $X \rightarrow [$
 $Z \rightarrow WY$
 $Y \rightarrow]$
 $A \rightarrow BW$
 $B \rightarrow @$
 $E \rightarrow FH$
 $F \rightarrow *$
 $H \rightarrow XZ \mid ND \mid DV \mid \# \mid CG \mid g \mid UC$
 $D \rightarrow ND \mid DV \mid \#$
 $N \rightarrow \#$
 $V \rightarrow /$
 $C \rightarrow CG \mid g \mid UC$
 $G \rightarrow g$
 $U \rightarrow u$

GNF (1 terminal seguido de cero o más variables)

$W \rightarrow [W] \mid C \mid W@W \mid D \mid W^*H$
 $H \rightarrow C \mid D \mid [W]$
 $D \rightarrow \#D \mid D/ \mid \#$
 $C \rightarrow Cg \mid g \mid uC$

Eliminamos RI de W y epsilon de la nueva variable //cálculo auxiliar

$W \rightarrow [W] \mid C \mid W@W \mid D \mid W^*H$

$W \rightarrow [W]Z \mid CZ \mid DZ \mid [W] \mid C \mid D$

$Z \rightarrow @WZ \mid ^*HZ \mid @W \mid ^*H$

Eliminamos RI de D //cálculo auxiliar

$D \rightarrow \#D \mid D/ \mid \#$

$D \rightarrow \#DX \mid \#X \mid \#D \mid \#$

$X \rightarrow /X \mid /$

Eliminamos RI de C //cálculo auxiliar

$C \rightarrow Cg \mid g \mid uC$

$C \rightarrow gU \mid uCU \mid g \mid uC$

$U \rightarrow gU \mid g$

Armo la gramática original a partir de la gramática limpia y de los cálculos auxiliares

$W \rightarrow [W PZ \mid gUZ \mid uCUZ \mid gZ \mid uCZ \mid \#DXZ \mid \#XZ \mid \#DZ \mid \#Z \mid [W P \mid gU \mid uCU \mid g$
 $\mid uC \mid \#DX \mid \#X \mid \#D \mid \#$
 $Z \rightarrow @WZ \mid ^*HZ \mid @W \mid ^*H$
 $H \rightarrow gU \mid uCU \mid g \mid uC \mid \#DX \mid \#X \mid \#D \mid \# \mid [W P$
 $D \rightarrow \#DX \mid \#X \mid \#D \mid \#$
 $X \rightarrow /X \mid /$
 $C \rightarrow gU \mid uCU \mid g \mid uC$
 $U \rightarrow gU \mid g$
 $P \rightarrow]$

PDA

Q	SIGMA U EPS	GAMMA	2**QXGAMMA*
0	[W	{{(0,WPZ), (0,WP)}}
0	g	W	{{(0,UZ),(0,Z), (0,U), (0,EPS) }}
0	u	W	{{(0,CUZ),(0,CZ), (0,CU), (0,C) }}
0	#	W	{{(0,DXZ),(0,XZ), (0,DZ), (0,Z) ,(0,DX),(0,X), (0,D), (0,EPS)}}
0	@	Z	{{(0,WZ),(0,W)}}
0	*	Z	{{(0,HZ),(0,H)}}
0	g	H	{{(0,U),(0,EPS)}}
0	u	H	{{(0,CU),(0,C)}}
0	#	H	{{(0,DX),(0,X), (0,D), (0,EPS) }}
0	[H	{{(0,WP)}}
0	#	D	{{(0,DX),(0,X), (0,D), (0,EPS) }}
0	/	X	{{(0,X),(0,EPS)}}
0	g	C	{{(0,U),(0,EPS)}}
0	u	C	{{(0,CU),(0,C)}}
0	g	U	{{(0,U),(0,EPS)}}
0]	P	{{(0,EPS)}}