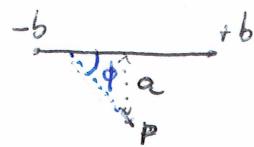
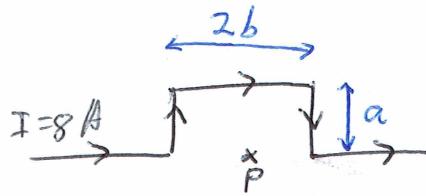


FFT: Maratón Navidad

①



$$B_1 = \frac{M_0 \cdot I}{4\pi} \cdot \int_{-b}^b \frac{d\vec{l} \times \vec{r}}{r^3} = \frac{M_0 \cdot I \cdot a}{4\pi} \cdot \int_{-b}^b \frac{dl}{(\sqrt{a^2 + l^2})^3} = \frac{M_0 \cdot I \cdot a}{4\pi} \left[\frac{L}{a \sqrt{b^2 + a^2}} \right]_{-b}^b =$$

$$d\vec{l} \times \vec{r} = d\vec{l} \cdot \sin \phi \cdot |\vec{r}|$$

$$d\vec{l} \times \vec{r} = d\vec{l} \frac{a}{\sqrt{a^2 + l^2}}$$

$$= \frac{M_0 \cdot I}{4\pi \cdot a} \cdot \frac{2b}{\sqrt{b^2 + a^2}} = \boxed{\frac{M_0 \cdot I}{2\pi \sqrt{b^2 + a^2}} \cdot \frac{b}{a}}$$

$$\frac{dl}{\sqrt{a^2 + l^2}}$$

$$B_2 = \frac{M_0 \cdot I \cdot b}{4\pi} \int_0^a \frac{1}{(\sqrt{b^2 + l^2})^3} dl = \frac{M_0 \cdot I \cdot b}{4\pi \cdot b^2} \left[\frac{L}{\sqrt{b^2 + L^2}} \right]_0^a =$$

$$d\vec{l} \times \vec{r} = d\vec{l} \cdot \sin \alpha \cdot |\vec{r}|$$

$$d\vec{l} \times \vec{r} = d\vec{l} \cdot \frac{b}{\sqrt{b^2 + l^2}}$$

$$= \boxed{\frac{M_0 \cdot I \cdot a}{4\pi \cdot b \cdot \sqrt{b^2 + a^2}}}$$

$$|B_+| = B_1 + 2B_2 = \frac{M_0 \cdot I}{2\pi \sqrt{b^2 + a^2}} \left(\frac{a}{b} + \frac{b}{a} \right)$$

Entrante
en el papel

②



$$|B| = \int \frac{M_0 \cdot I \cdot d\vec{l}}{R^2} = \frac{M_0 \cdot I}{4\pi R^2} \cdot L = \frac{M_0 \cdot I}{4\pi R^2} \cdot \pi \cdot R = \boxed{\frac{M_0 \cdot I}{4R}}$$

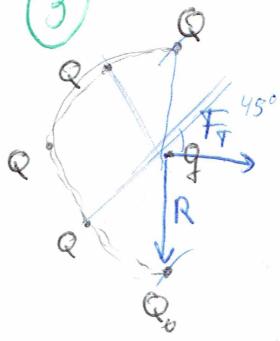
Entrante en el papel.

$$*\quad \sin \alpha = \frac{b}{\sqrt{R^2 + b^2}}$$

$$\sin \phi = \frac{a}{\sqrt{R^2 + a^2}}$$

③

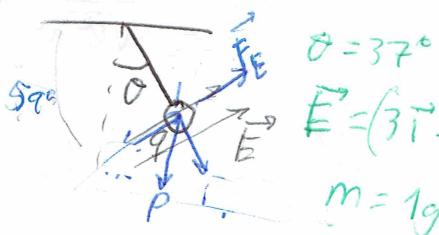
$$|F_Q| = \frac{k \cdot Q \cdot q}{R^2}$$



$$\vec{F}_T = \frac{kQq}{R^2} \left(\vec{i} + \frac{\sqrt{2}}{2} \vec{i} + \frac{\sqrt{2}}{2} \vec{j} + \frac{\sqrt{2}}{2} \vec{i} - \frac{\sqrt{2}}{2} \vec{j} + \vec{j} - \vec{j} \right)$$

$$\boxed{\vec{F}_T = \frac{k \cdot Q \cdot q}{R^2} (1 + \sqrt{2}) \vec{i}} \quad N$$

④



$$\theta = 37^\circ$$

$$\vec{E} = (3\vec{i} + 5\vec{j}) \cdot 10^5 \text{ N/C}$$

$$m = 1g$$

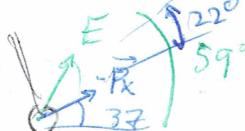
$$\vec{F}_E = q \cdot (3\vec{i} + 5\vec{j}) \cdot 10^5$$

$$|\vec{F}_E| = 5'831 \cdot 10^5 \cdot q$$

$$\vec{F}_E = 5'831 \cdot 10^5 \cdot q (\cos(59)\vec{i} + \sin(59)\vec{j})$$

$$|P_k| = |P| \cdot \sin(\theta) = 9'8 \cdot 10^{-3} \cdot \sin(37) = 5'8978 \cdot 10^{-3}$$

$$\vec{P}_x = 5'8978 \cdot 10^{-3} (-\cos(37)\vec{i} + \sin(37)\vec{j})$$



$$|\vec{F}_E| \cdot \cos(22) = |\vec{P}_x| \Rightarrow 5'831 \cdot 10^5 \cdot q \cdot 0'927 = 5'8978 \cdot 10^{-3}$$

$$q = \frac{5'8978 \cdot 10^{-3}}{10^5 \cdot 5'831 \cdot 0'927}$$

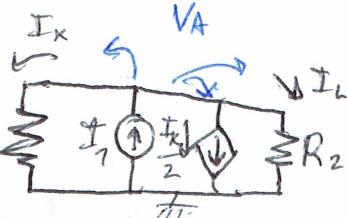
$$\boxed{q = 1'09 \cdot 10^{-8} \text{ C}}$$

$$|P_y| = 9'8 \cdot 10^{-3} \cos(37) = 7'83 \cdot 10^{-3} \text{ N}$$

$$F_{EY} = -|\vec{F}_E| \cdot \sin(22) = -2'388 \cdot 10^{-3} \text{ N} = 5'831 \cdot 10^5 \cdot q \cdot \sin(22)$$

$$\boxed{T = 5'45 \cdot 10^{-3} \text{ N}}$$

⑤



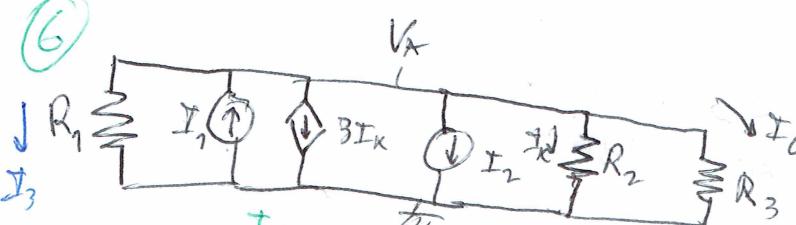
$$\begin{aligned} I_1 &= 6 \text{ mA} \\ R_1 &= 2 \text{ k}\Omega \\ R_2 &= 4 \text{ k}\Omega \end{aligned}$$

$$I_L = \frac{V_A}{4} = \frac{6}{4} = 1.5 \text{ mA}$$

$$I_1 = I_x + \frac{I_x}{2} + I_L$$

$$6 = \frac{2V_A}{2 \cdot 2} + \frac{V_A}{4} + \frac{V_A}{4} \Rightarrow 6 = \frac{4V_A}{4} \Rightarrow V_A = 6V$$

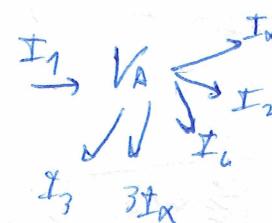
⑥



$$I_1 = \frac{V_A}{R_2} + \frac{V_A}{R_3} + \frac{V_A}{R_1} + I_2 + 3 \cdot \frac{V_A}{R_2}$$

$$6 = \frac{V_A}{2} + \frac{V_A}{3} + \frac{V_A}{6} + 3 + \frac{3V_A}{2} \Rightarrow 3 = \frac{3V_A + 2V_A + V_A + 9V_A}{6} = \frac{25}{6} V_A$$

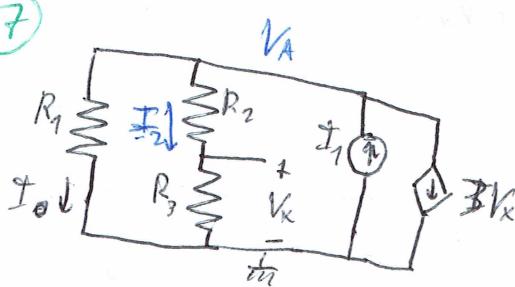
$$V_A = \frac{18}{15} = 1.2V$$



$$\begin{aligned} I_1 &= 6 \text{ mA} \\ I_2 &= 3 \text{ mA} \\ R_1 &= 6 \text{ k}\Omega \\ R_2 &= 2 \text{ k}\Omega \\ R_3 &= 3 \text{ k}\Omega \end{aligned}$$

$$I_L = \frac{V_A}{R_3} = \frac{1.2}{3} = 0.4 \text{ mA}$$

⑦



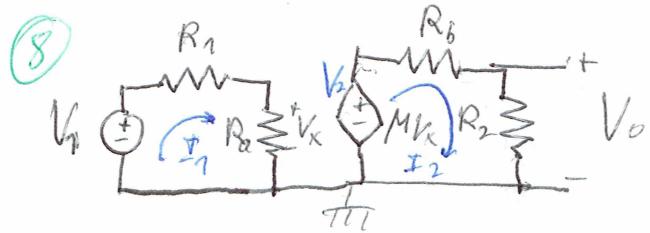
$$\begin{aligned} I_1 &= 5A \\ R_1 &= 6\Omega \\ R_2 &= 8\Omega \\ R_3 &= 4\Omega \end{aligned}$$

$$I_1 = I_2 + I_0 + 3V_K$$

$$5 = \frac{V_A}{R_2 + R_3} + \frac{V_A}{R_1} + 3(I_2 \cdot R_3)$$

$$5 = \frac{V_A}{12} + \frac{V_A}{6} + 3 \left(\frac{V_A}{12} \cdot 4 \right) \Rightarrow 5 = \frac{V_A + 2V_A + 12V_A}{12} \Rightarrow V_A = 4$$

$$I_0 = \frac{V_A}{R_1} = \frac{4}{6} = \frac{2}{3} A$$



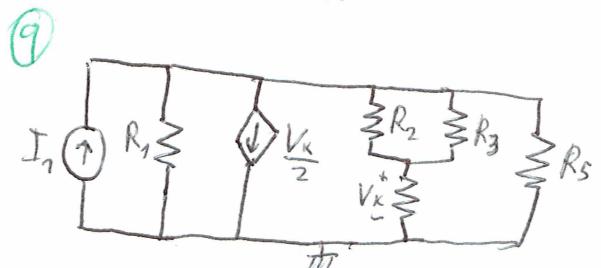
$$V_o = I_2 \cdot R_2$$

$$I_2 = M \cdot V_k = M \cdot I_1 \cdot R_a$$

$R_a \uparrow \Rightarrow I_2 \uparrow \Rightarrow V_o \uparrow$

($R_a \rightarrow \infty$)

$$V_2 = I_2 \cdot R_b + R_2 \cdot I_2 \quad \Rightarrow \quad V_o = V_2 - I_2 \cdot R_b \Rightarrow R_b \downarrow \Rightarrow V_o \uparrow \Rightarrow R_b \rightarrow 0$$



$$I_1 = 11 \text{ mA}$$

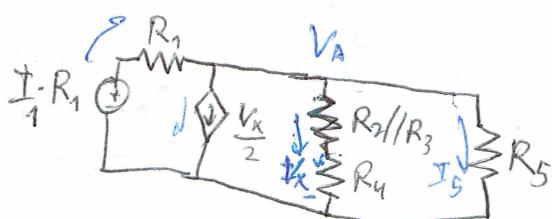
$$R_1 = 2 \text{ k}\Omega$$

$$R_2 = 4 \text{ k}\Omega$$

$$R_3 = 4 \text{ k}\Omega$$

$$R_4 = 3 \text{ k}\Omega$$

$$R_5 = 10 \text{ k}\Omega$$



$$R_2/R_3 = 2 \text{ k}\Omega \quad I_1 \cdot R_1 = 22 \text{ V}$$

$$\frac{1}{4} + \frac{1}{4} = \frac{2}{4}$$

$$\frac{22 - V_A}{R_1} = \frac{V_k}{2} + \frac{V_A}{2+3} + \frac{V_A}{10}$$

$$I_k = \frac{V_A}{5} \quad V_k = R_4 \cdot I_k = 3 \cdot \frac{V_A}{5}$$

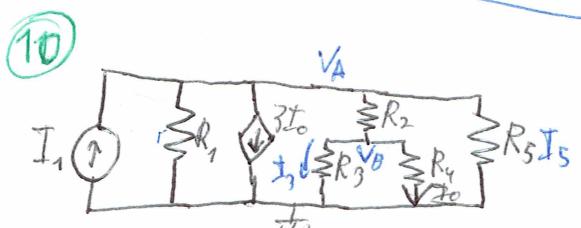
$$\frac{22 - V_A}{2} = \frac{3 V_A}{10} + \frac{V_A}{5} + \frac{V_A}{10} \Rightarrow 110 - 5 V_A = 3 V_A + 2 V_A + V_A$$

$$I_s = \frac{V_A}{10} = 1 \text{ V}$$

$$110 = 14 \text{ V}_A$$

$$V_A = 10 \text{ V}$$

$$P_s = I_s^2 \cdot R_5 = 1.10 \text{ mW}$$



$$I_1 = 6 \text{ mA}$$

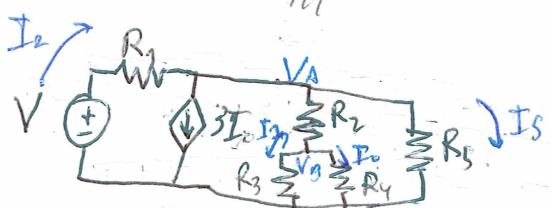
$$R_1 = 6 \text{ k}\Omega$$

$$R_2 = 4 \text{ k}\Omega$$

$$R_3 = 6 \text{ k}\Omega$$

$$R_4 = 3 \text{ k}\Omega$$

$$R_5 = 12 \text{ k}\Omega$$



$$V = I_1 \cdot R_1 = 36 \text{ V}$$

$$I_2 = 3I_0 + I_3 + I_0 + I_s$$

$$\frac{36 - V_A}{6} = 3I_0 + \frac{V_B}{6} + \frac{V_B}{3} + \frac{V_A}{72} \Rightarrow 72 - 6V_B = 72V_B + 2V_B + 4V_B$$

$$\frac{V_A - V_B}{4} = (I_0 + I_3)$$

$$V_A = V_B + \frac{4}{3}V_B + \frac{4}{6}V_B = 3V_B$$

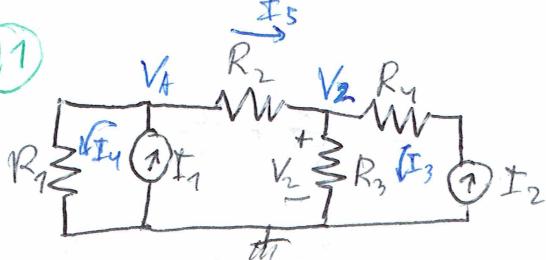
$$72 = 27V_B \Rightarrow V_B = \frac{8}{3} \text{ V}$$

$$V_A = 3V_B = 8V$$

$$I_S = \frac{V_A}{72} = \frac{2}{3}$$

$$P_{R_5} = \left(\frac{2}{3}\right)^2 \cdot 12 = 5.33 \text{ mW}$$

(11)



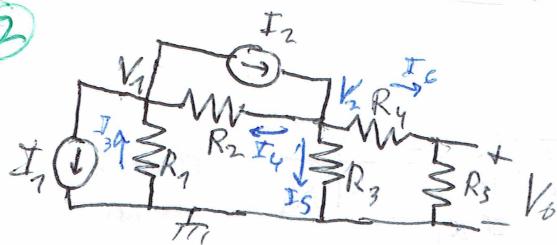
$$\begin{aligned} I_1 &= 4 \text{ mA} \\ I_2 &= 6 \text{ mA} \\ R_1 &= 2 \text{ k}\Omega \\ R_2 &= 4 \text{ k}\Omega \\ R_3 &= 6 \text{ k}\Omega \\ R_4 &= 2 \text{ k}\Omega \end{aligned}$$

$$\begin{aligned} I_1 &= I_4 + I_5 \\ I_2 + I_3 &= I_3 \\ V_A &= \frac{16 + V_2}{3} \\ I_1 &= \frac{5V_2 - 72}{3} \end{aligned} \quad \begin{aligned} 4 &= \frac{V_A}{2} + \frac{V_A - V_2}{4} \\ 6 + \frac{V_A - V_2}{4} &= \frac{V_2}{6} \end{aligned} \quad \begin{aligned} 16 &= 2V_A + V_A - V_2 \\ 72 + 3V_A - 3V_2 &= 2V_2 \end{aligned} \quad \begin{aligned} 16 &= 3V_A - V_2 \\ 72 &= 5V_2 - 3V_A \end{aligned}$$

$$\frac{16 + V_2}{3} = \frac{5V_2 - 72}{3}$$

$$88 = 4V_2 \Rightarrow V_2 = 22 \text{ V}$$

(12)



$$\begin{aligned} I_1 &= 4 \text{ mA} \\ I_2 &= 2 \text{ mA} \\ R_1 &= 3 \text{ k}\Omega \\ R_2 &= 6 \text{ k}\Omega \\ R_3 &= 12 \text{ k}\Omega \\ R_4 &= 2 \text{ k}\Omega \\ R_5 &= 2 \text{ k}\Omega \end{aligned}$$

$$\begin{aligned} I_3 + I_4 &= I_1 + I_2 \\ I_2 &= I_4 + I_5 + I_6 \end{aligned} \quad \begin{aligned} -\frac{V_1}{3} + \frac{V_2 - V_1}{6} &= 4 + 2 \\ 2 &= \frac{V_2 - V_1}{6} + \frac{V_2}{12} + \frac{V_2}{2+2} \end{aligned}$$

$$-2V_1 + V_2 - V_1 = 36$$

$$V_2 - 3V_1 = 36$$

$$V_2 = 36 + 3V_1$$

$$36 + 3V_1 = 4 + \frac{1}{3}V_1$$

$$32 = -\frac{8}{3}V_1$$

$$V_1 = -12 \text{ V}$$

$$I_6 = \frac{V_2}{R_4 + R_5}$$

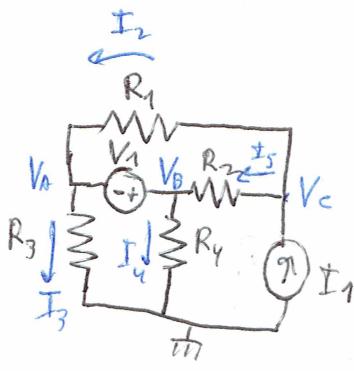
$$I_6 = 0$$

$$V_o = I_6 \cdot R_5 = 0 \text{ V}$$

$$6V_2 = 24 + 2V_1 \Rightarrow V_2 = 4 + \frac{1}{3}V_1$$

$$V_2 = 4 - 4 = 0 \text{ V}$$

(13)



$$V_A = 12 \text{ V} \quad R_1 = R_2 = R_3 = R_4 = 6 \text{ k}\Omega$$

$$I_1 = 2 \text{ mA}$$

$$I_1 = I_S + I_2$$

$$V_B = V_A + 12$$

$$I_5 = 0$$

$$I_1 = I_2 = I_3 + I_4$$

$$2 = \frac{V_A}{R_3} + \frac{V_E}{R_4}$$

$$2 = \frac{V_c - V_B}{6} + \frac{V_c - V_A}{6}$$

$$I_2 = I_1$$

$$2 = \frac{V_A}{6} + \frac{V_c}{6}$$

$$12 = V_c - V_B + V_c - V_A$$

$$12 = V_A + V_c$$

$$12 = V_c - (V_A + 12) + V_c - V_A$$

$$V_c = 12 - V_A$$

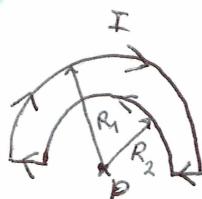
$$24 = V_c - V_A + V_c - V_A$$

$$12 + V_A = 12 - V_A$$

$$V_A = 0$$

$$\boxed{V_c = 12 \text{ V}}$$

(14)



1^{er} cable (tramo):

$$B_1 = \frac{\mu_0}{4\pi} \frac{I}{R_1^2} \int dl = \frac{\mu_0 I}{4\pi R_1^2} \left[\frac{L}{R_1} \right] = \frac{\mu_0 I L}{4\pi R_1^3}$$

Hacia dentro

2^{do} tramo:

$$B_2 = \frac{\mu_0}{4\pi} \frac{I}{R_2^2} \int dl = \frac{\mu_0 I}{4\pi R_2^2} \left[\frac{L}{R_2} \right] = \frac{\mu_0 I L}{4\pi R_2^3}$$

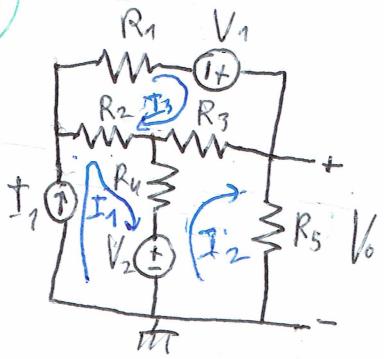
Hacia fuera

$$R_2 < R_1 \Rightarrow B_2 > B_1$$

$$B_T = B_2 - B_1 = \frac{\mu_0 I}{4} \left(\frac{1}{R_2} - \frac{1}{R_1} \right)$$

Hacia fuera

15



$$V_1 = 6V$$

$$V_2 = 12V$$

$$I_1 = 2mA$$

$$R_1 = R_2 = R_4 = R_5 = 1k\Omega$$

$$R_3 = 2k\Omega$$

$$V_0 = I_2 \cdot R_5 = I_2$$

$$V_{x1} = (I_1 - I_3) R_2 + (I_1 - I_2) R_4 + V_1$$

$$V_2 = (I_2 - I_1) R_4 + (I_2 - I_3) R_3 + I_2 \cdot R_5$$

$$V_1 = (I_3 - I_2) R_3 + (I_3 - I_1) R_2 + I_3 \cdot R_1$$

$$\left. \begin{aligned} V_{x1} &= 2 - I_3 + 2 - I_2 + 12 \\ 12 &= I_2 - 2 + 2I_2 - 2I_3 + I_2 \\ 6 &= 2I_3 - 2I_2 + I_3 - 2 + I_3 \end{aligned} \right\}$$

$$14 = 4I_2 - 2I_3 \Rightarrow 7 = 2I_2 - I_3 \Rightarrow I_3 = 2I_2 - 7$$

$$8 = 4I_3 - 2I_2 \Rightarrow 4 = 2I_3 - I_2 \Rightarrow I_3 = 2 + \frac{I_2}{2}$$

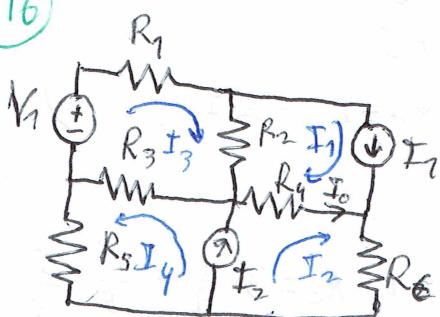
$$2I_2 - 7 = 2 + \frac{I_2}{2}$$

$$4I_2 - 14 = 4 + I_2$$

$$3I_2 = 18$$

$$I_2 = 6mA$$

16



$$V_1 = 12V$$

$$I_1 = 2mA$$

$$I_2 = 4mA \text{ Diferente a } I_1$$

$$R_1 = R_2 = R_3 = R_4 = R_5 = R_6 = 1k\Omega$$

$$V_1 = I_3 \cdot R_1 + (I_3 - I_1) R_2 + (I_3 + I_4) R_3$$

$$I_0 = I_2 - I_1 = I_2 - 2$$

$$I_2 + I_4 = 4$$

$$I_4 = 4 - I_2$$

$$V_{x1} = (I_1 - I_2) R_4 + (I_1 - I_3) R_2$$

$$V_{x2} = (I_2 - I_1) R_4 + I_2 \cdot R_6$$

$$V_{x2} = (I_3 + I_4) R_3 + I_4 \cdot R_5$$

$$12 = I_3 + I_4 - 2 + I_3 + 4 - I_2$$

$$V_{x1} = 2 - I_2 + 2 - I_3$$

$$V_{x2} = I_2 - 2 + I_2$$

$$V_{x2} = I_3 + 4 - I_2 + 4 - I_2$$

$$10 = 3I_3 - I_2 \Rightarrow I_3 = \frac{10 + I_2}{3}$$

$$4 = V_{x1} + I_2 + I_3$$

$$2 = 2I_2 - V_{x2}$$

$$+ 8 = V_{x2} - I_3 + 2I_2$$

$$10 = 4I_2 - I_3 \Rightarrow 10 = 4I_2 - \frac{10 + I_2}{3} - I_2$$

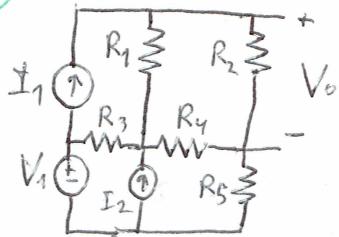
$$30 = 12I_2 - 10 - I_2$$

$$I_o = I_2 - I_1 = 3.64 - 2 = 1.64 \text{ mA}$$

$$40 = 11I_2$$

$$I_2 = 3.64 \text{ mA}$$

(17)



$$V_1 = 6V$$

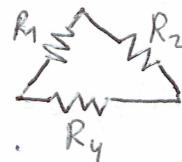
$$I_1 = 3 \text{ mA}$$

$$I_2 = 1 \text{ mA}$$

$$R_1 = R_5 = 2 \text{ k}\Omega$$

$$R_2 = R_3 = 4 \text{ k}\Omega$$

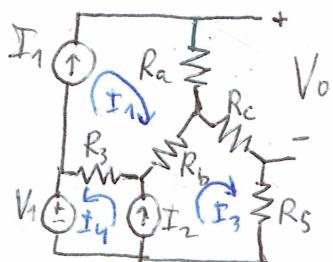
$$R_4 = 12 \text{ k}\Omega$$



$$R_a = \frac{R_2 \cdot R_1}{R_1 + R_2 + R_4} = \frac{8}{18} = \frac{4}{9} \text{ k}\Omega$$

$$R_b = \frac{R_1 \cdot R_4}{18} = \frac{24}{18} = \frac{4}{3} \text{ k}\Omega$$

$$R_c = \frac{R_2 \cdot R_4}{18} = \frac{48}{18} = \frac{8}{3} \text{ k}\Omega$$



$$I_3 + I_4 = I_2$$

$$I_3 = 1 - I_4 \Rightarrow I_4 = 1 - I_3$$

$$\left. \begin{aligned} V_{x1} &= I_1 R_a + (I_1 - I_3) R_b + (I_1 + I_4) R_3 \\ V_{x2} &= (I_1 + I_4) R_3 + V_1 \\ V_{x2} &= (I_3 - I_1) R_b + I_3 \cdot R_c + I_3 \cdot R_5 \end{aligned} \right\} \quad \left. \begin{aligned} V_{x1} &= 3 \cdot \frac{4}{9} + 3 \cdot \frac{4}{3} - \frac{4}{3} I_3 + 4 \cdot 3 + 4 - 4 I_3 \\ V_{x2} &= 12 + 4 - 4 I_3 + 6 \\ V_{x2} &= \frac{4}{3} I_3 - 3 \cdot \frac{4}{3} + \frac{8}{3} I_3 + 2 I_3 \end{aligned} \right\}$$

$$V_{x2} = 22 - 4I_3 \Rightarrow -V_{x2} = -22 + 4I_3$$

$$V_{x2} = 6I_3 - 4$$

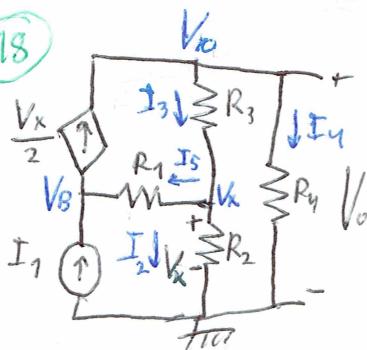
$$0 = -26 + 10I_3$$

$$I_3 = \frac{-26}{10} = \frac{13}{5} \text{ mA}$$

$$V_o = I_1 \cdot R_a + I_3 \cdot R_c = 3 \cdot \frac{4}{9} + \frac{13}{5} \cdot \frac{8}{3}$$

$$V_o = 8.27 \text{ V}$$

(18)



$$I_1 = 2 \text{ mA}$$

$$R_1 = 4 \text{ k}\Omega$$

$$R_2 = R_4 = 6 \text{ k}\Omega$$

$$R_3 = 2 \text{ k}\Omega$$

$$V_k = I_2 \cdot R_2$$

$$I_1 + I_s = \frac{V_k}{2} = \frac{I_2 \cdot R_2}{2}$$

$$I_3 = I_s + I_2$$

$$\frac{I_2 \cdot R_2}{2} = I_3 + I_4$$

$$2 + \frac{V_k - V_B}{4} = \frac{V_k}{2} \Rightarrow 8 + V_k - V_B = 2V_k$$

$$\frac{V_o - V_k}{2} = \frac{V_k - V_B}{4} + \frac{V_k}{6} \Rightarrow 6V_o - 6V_k = 3V_k - 3V_B + 2V_k$$

$$\frac{V_k}{2} = \frac{V_o - V_k}{2} + \frac{V_o}{6} \Rightarrow 3V_k = 3V_o - 3V_B + V_o$$

$$V_B = 8 - V_k$$

$$6V_o + 3V_B = 11V_k \Rightarrow 6V_o + 3(8 - V_k) = 11V_k$$

$$6V_o = 4V_o \Rightarrow V_o = \frac{3}{2} V_k$$

$$6 \cdot \frac{3}{2} V_x + 3(8 - V_x) = 11V_x$$

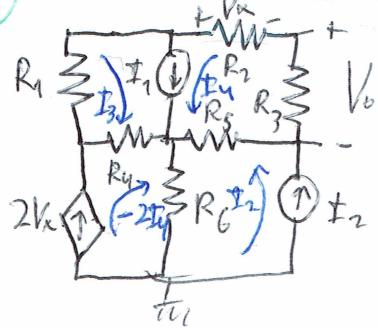
$$9V_x + 24 - 3V_x = 11V_x$$

$$24 = (11 - 9 + 3)V_x$$

$$V_x = \frac{24}{5}$$

$$V_o = \frac{3}{2} V_x = \frac{3}{2} \cdot \frac{24}{5} = \boxed{\frac{36}{5} V}$$

(19)



$$I_1 = 1 \text{ mA}$$

$$I_2 = 0.5 \text{ mA}$$

$$R_1 = R_6 = 2 \text{ k}\Omega$$

$$R_2 = R_3 = R_4 = R_5 = 1 \text{ k}\Omega$$

$$V_x = -I_4 \cdot R_2 = -I_4$$

$$I_3 + I_4 = 1 \Rightarrow I_3 = 1 - I_4$$

$$V_o = -I_4$$

$$V_{x1} = I_3 + 2I_4 + 2I_3$$

$$V_{x1} = I_4 - I_2 + I_4 + I_4$$

$$V_{x2} = -2I_4 - I_3 - 4I_4 + 2I_2$$

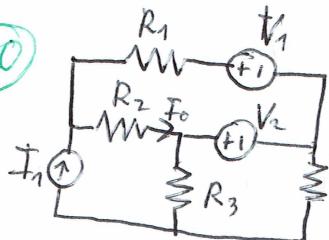
$$V_{x2} = I_2 - I_4 + 2I_2 - 4I_4$$

$$\left. \begin{aligned} V_{x1} &= 3 - 3I_4 + 2I_4 \\ -V_{x1} &= 3I_4 - 0.5 \end{aligned} \right\}$$

$$0 = 3.5 - 4I_4 \Rightarrow I_4 = \frac{3.5}{4} = \frac{7}{8}$$

$$\boxed{V_o = -I_4 = -\frac{7}{8}}$$

(20)

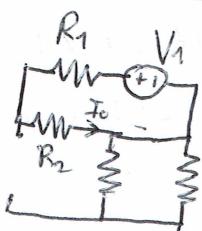


$$V_1 = 12 \text{ V}$$

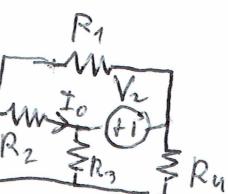
$$V_2 = 6 \text{ V}$$

$$I_1 = 2 \text{ mA}$$

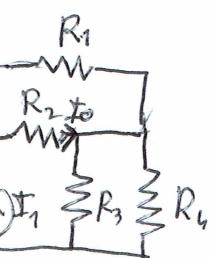
$$R_1 = R_2 = R_3 = R_4 = 2 \text{ k}\Omega$$



$$V_1 = I_{o1}(R_1 + R_2) \Rightarrow 12 = I_{o1}(4) \Rightarrow I_{o1} = 3 \text{ mA}$$



$$V_2 = (R_1 + R_2)(-I_{o2}) \Rightarrow 6 = 4(-I_{o2}) \Rightarrow I_{o2} = -\frac{3}{2} \text{ mA}$$



$$R_3 // R_4 = 1 \text{ k}\Omega$$

$$I_1 = I_2 + I_{o2}$$

$$2 = \frac{V_A - V_B}{2} + \frac{V_A - V_B}{2}$$

$$2 = \frac{V_A - 2}{2} + \frac{V_A - 2}{2}$$

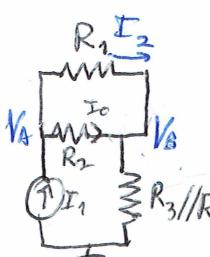
$$2 = V_A - 2 \Rightarrow V_A = 4$$

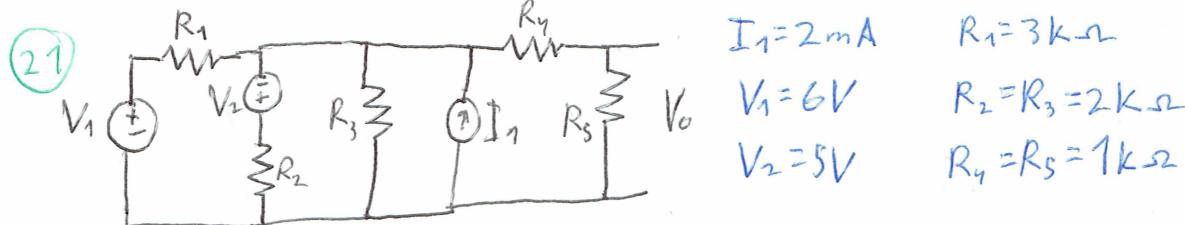
$$V_B = I_1 \cdot R_3 // R_4 = I_2 = 2$$

$$I_{o2} = 1 \text{ mA}$$

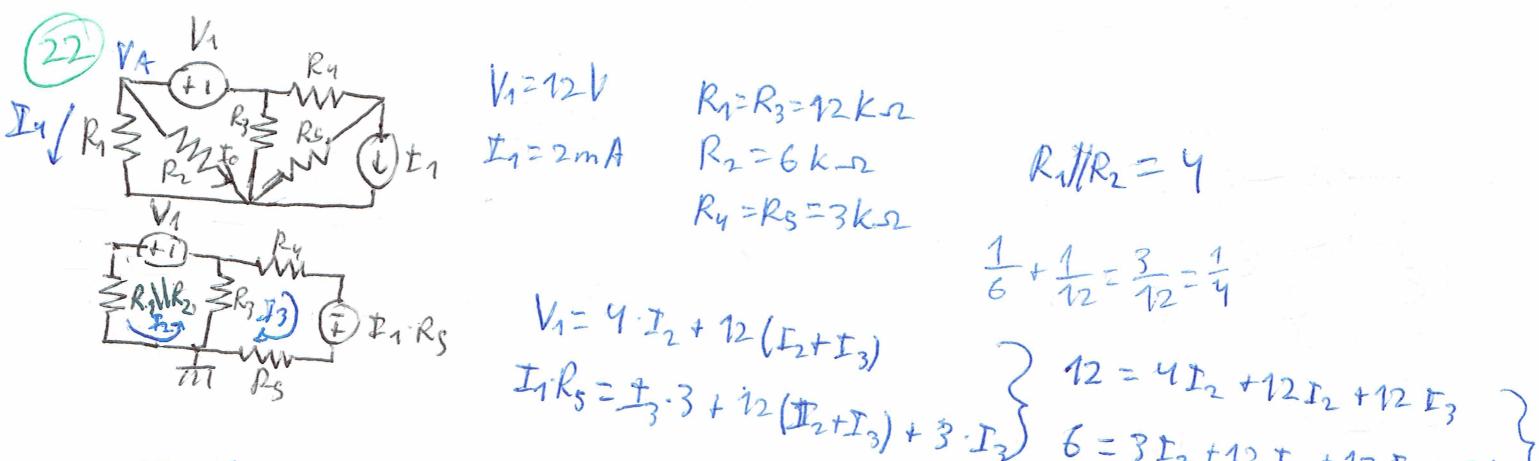
$$I_o = I_{o1} + I_{o2} + I_{o3} = 3 - \frac{3}{2} + 1$$

$$\boxed{I_o = 2.5 \text{ mA}}$$





$$\begin{aligned} &V_1/R_1 + V_2/R_2 + R_3 I_1 + R_4 I_1 = V_o \\ &\frac{V_1}{R_1} + \frac{V_2}{R_2} + R_3 I_1 + R_4 I_1 = V_o \\ &\frac{V_1 + I_1 R_1 - V_2}{R_2} + R_3 I_1 + R_4 I_1 = V_o \\ &R_1 // R_2 // R_3 + R_4 + R_5 = V_o \\ &I = I_2 + I_3 \\ &I = \frac{V_A}{\frac{3}{4}} + \frac{V_A}{2} \\ &1.5 = \frac{V_A}{\frac{3}{4}} + \frac{V_A}{2} \\ &V_o = I_3 \cdot R_5 = I_3 \\ &V_0 = I_3 \cdot R_5 = I_3 \\ &V_0 = I_3 \cdot \frac{1}{2} = \frac{9}{22} = 0.41 \text{ V} \\ &1.5 = \frac{9}{3} I_3 + \frac{9}{2} I_3 \Rightarrow 1.5 = \frac{11}{6} V_A \Rightarrow V_A = \frac{9}{71} \end{aligned}$$



$$\begin{aligned} &I_1 + I_3 = 1 \\ &\frac{V_A}{R_1} + \frac{V_A}{R_2} = 1 \Rightarrow \frac{V_A}{12} + \frac{V_A}{6} = 1 \Rightarrow V_A + 2V_A = 12 \Rightarrow V_A = 4 \end{aligned}$$

$$(23) \quad C = 25 \mu F \quad V_{initial} = -10V \quad t = 750s$$

\rightarrow

$$I = 25mA \quad Q_{initial} = V_{initial} \cdot C = -10 \cdot 25 = -250 \mu C$$

$$Q = I \cdot t \Rightarrow Q = 25 \cdot 150 = 375 \mu C$$

$$Q_{final} = Q_{initial} + Q = -250 + 375 = 125 \mu C$$

$$V_{final} = \frac{Q_{final}}{C} = \frac{125}{25} = 5V$$

$$(24) \quad E(t) = 12 \cdot \sin^2 377t \quad J$$

$$E = \int V \cdot dq = \int \frac{Q}{C} \cdot \frac{dq}{dt} = \frac{Q^2}{2C} = \frac{V^2 \cdot C^2}{2C} = \frac{C}{2} V^2$$

$$E = \frac{C}{2} V^2 \quad V = \frac{Q}{C}$$

$$E = \frac{C}{2} \frac{Q^2}{C^2} = \frac{Q^2}{2C} \quad Q = |Q| \cdot \sin 377t$$

$$Q = 0.0245 \sin 377t$$

$$\frac{|Q|^2}{2C} = 12 \Rightarrow |Q|^2 = 12 \cdot 50 = 6 \cdot 10^{-4} C^2$$

$$|Q| = 0.0245 C$$

$$i(t) = \frac{dQ(t)}{dt} = 0.0245 \cdot 377 \cdot \cos 377t$$

$$= 92365 \cdot \cos(377t) \quad (A)$$

$$(25) \quad C = 10 \mu F$$

$$i(t) = 10 \cos(377t) \quad (mA)$$

$$a) V? \quad V(t) = \frac{Q(t)}{C} = 10 \cdot \cos(377t) \quad (A)$$

$$i(t) = \frac{dQ(t)}{dt} = 10 \cdot \cos(377t)$$

$$= \frac{10 \cdot 10^{-6} \cdot \sin(377t)}{377} = 2.63 \cdot \sin(377t) \quad V$$

$$Q(t) = \int 10 \cdot \cos(377t) dt = 10 \cdot \frac{\sin(377t)}{377} = 26.53 \cdot 10^{-6} \sin(377t)$$

$$\textcircled{26} \quad L = 50 \text{ mH}$$

$$i(t) = \begin{cases} 0 & t < 0 \\ 2t e^{-4t} & t \geq 0 \end{cases} \quad (\text{A})$$

a) V ?

$$V(t) = L \cdot \frac{di(t)}{dt} = 50 \cdot 10^{-3} \cdot (2 - 8t) \cdot e^{-4t} = (0.1 - 0.8t) \cdot e^{-4t} \text{ V}$$

$$\frac{d(2t e^{-4t})}{dt} = 2e^{-4t} + 2t \cdot (-4) \cdot e^{-4t} = e^{-4t}(2 - 8t)$$

$$V(t) = \begin{cases} 0 & t < 0 \\ (0.1 - 0.8t) \cdot e^{-4t} & t \geq 0 \end{cases}$$

b) i_{\max}

$$e^{-4t}(2 - 8t) = 0 \Rightarrow 2 = 8t \Rightarrow \boxed{t = \frac{1}{4} \text{ s}}$$

0, 0'25	0'25	\rightarrow
+	-	
\nearrow	\searrow	

c) V_{\min}

$$V(t) = 0.1 e^{-4t} - 0.8t e^{-4t}$$

$$\frac{dV(t)}{dt} = 0.1 \cdot (-4) \cdot e^{-4t} - 0.8 \left(e^{-4t} + t \cdot (-4) \cdot e^{-4t} \right) = -0.4 \cdot e^{-4t} - 0.8 \cdot e^{-4t} + 3.2t \cdot e^{-4t} = (1.6t - 0.8) \cdot e^{-4t}$$

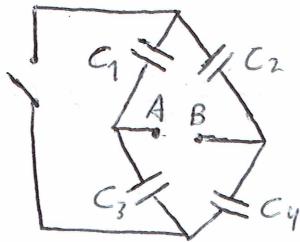
$$(1.6t - 0.8) e^{-4t} = 0$$

$$\boxed{1.6t = 0.8}$$

$$\boxed{t = 0.5 \text{ s}}$$

0, 0's	0's	\rightarrow
-	+	
\searrow	\nearrow	

(27)



$$C_1 = 3 \mu F$$

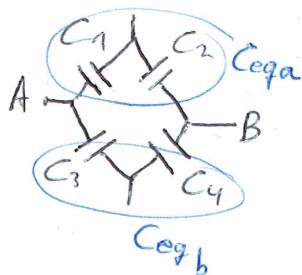
$$C_2 = 6 \mu F$$

$$C_3 = 6 \mu F$$

$$C_4 = 9 \mu F$$

Ceq. AB

a) Abierto.



$$C_{eq_a} | C_1, C_2 = 2$$

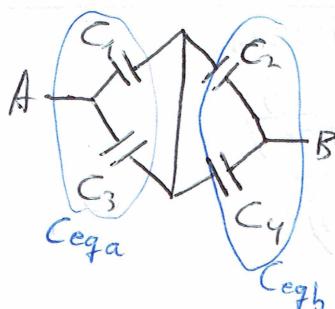
$$\frac{1}{3} + \frac{1}{6} = \frac{3}{6}$$

$$G = C_{eq_a} // C_{eq_b} = 2 + 4 = \boxed{6 \mu F}$$

$$C_{eq_b} | C_3, C_4 = 4$$

$$\frac{1}{6} + \frac{1}{12} = \frac{3}{12}$$

b) Cerrado.



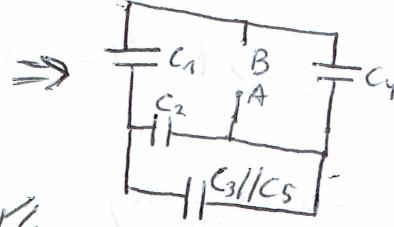
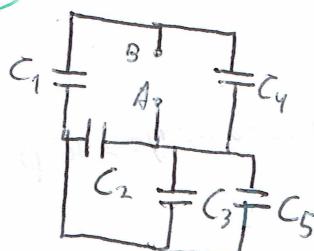
$$C_{eq_a} = C_1 + C_3 = 9 \mu F$$

$$C_{eq_b} = C_2 + C_4 = 18 \mu F$$

$$\frac{1}{9} + \frac{1}{18} = \frac{3}{18}$$

$$G = \boxed{C_{eq} = 6 \mu F}$$

(28)



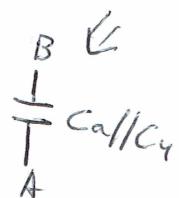
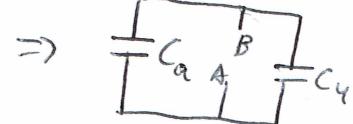
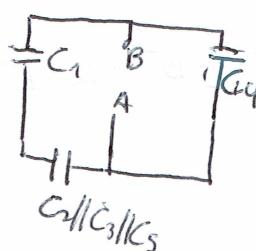
$$\begin{aligned} C_1 &= 4 \mu F & C_4 &= 6 \mu F \\ C_2 &= 1 \mu F & C_5 &= 3 \mu F \\ C_3 &= 8 \mu F \end{aligned}$$

$$C_3 // C_5 = 8 + 3 = 11 \mu F$$

$$C_2 // C_3 // C_5 = 1 + 11 = 12 \mu F$$

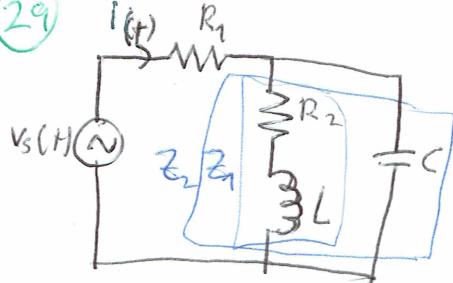
$$C_a = 3 \mu F$$

$$\frac{1}{12} + \frac{1}{4} = \frac{4}{12}$$



$$C_T = C_a // C_4 = 3 + 6 = \boxed{9 \mu F}$$

(29)



$$R_1 = 1 \Omega$$

$$R_2 = 2 \Omega$$

$$L = 10 \text{ mH} = 10^{-2} \text{ H}$$

$$C = 10 \text{ nF} = 10^{-9} \text{ F}$$

$$V_s(t) = 120 \cos(377t + \frac{\pi}{2}) \text{ V} \quad V_o(t) = 120 \cdot e^{j\omega t}$$

$$Z_L = j\omega L$$

$$Z_C = \frac{1}{j\omega C}$$

$$\omega = \frac{2\pi}{T} = 2\pi \cdot f$$

$$Z_1 = Z_{R_2} + Z_L = R_2 + j\omega L$$

$$Z_2 = Z_1 // Z_C$$

$$Z_{eq} = Z_{R_1} + Z_2$$

$$Z_{eq} = \frac{R_1 + R_2 + j\omega L}{1 - \omega^2 CL + j\omega CR_2}$$

$$\frac{1}{Z_2} = \frac{1}{R_2 + j\omega L} + \frac{1}{j\omega C} = \frac{1}{R_2 + j\omega L} + j\omega C$$

$$\frac{1}{Z_2} = \frac{j\omega C(R_2 + j\omega L) + 1}{R_2 + j\omega L}$$

$$Z_2 = \frac{R_2 + j\omega L}{1 - \omega^2 CL + j\omega CR_2}$$

$$Z_{eq} = \frac{R_1 + j\omega L + R_1(1 - \omega^2 CL + j\omega CR_2)}{1 - \omega^2 CL + j\omega CR_2} = \frac{2 + j\omega \cdot 10^{-2} + 1 - \omega^2 \cdot 10^{-5} \cdot 10^{-2} + j\omega \cdot 10^{-5} \cdot 2}{1 - \omega^2 \cdot 10^{-7} + j\omega \cdot 2 \cdot 10^{-5}}$$

$$Z_{eq} = \frac{3 + j\omega(10^{-2} + 2 \cdot 10^{-5}) - \omega^2 \cdot 10^{-7}}{1 - \omega^2 \cdot 10^{-7} + j\omega \cdot 2 \cdot 10^{-5}} = \boxed{E^{j\arctg\left(\frac{\omega(10^{-2} + 2 \cdot 10^{-5})}{3 - \omega^2 \cdot 10^{-7}}\right)} \cdot E^{j\arctg\left(\frac{2 \cdot 10^{-5} \cdot \omega}{1 - \omega^2 \cdot 10^{-7}}\right)}}$$

$$\arctg\left(\frac{\omega(10^{-2} + 2 \cdot 10^{-5})}{3 - \omega^2 \cdot 10^{-7}}\right) - \arctg\left(\frac{2 \cdot 10^{-5} \cdot \omega}{1 - \omega^2 \cdot 10^{-7}}\right) = 0$$

$$\frac{\omega(10^{-2} + 2 \cdot 10^{-5})}{3 - \omega^2 \cdot 10^{-7}} = \frac{2 \cdot 10^{-5} \cdot \omega}{1 - \omega^2 \cdot 10^{-7}} \Rightarrow (10^{-2} + 2 \cdot 10^{-5})(1 - \omega^2 \cdot 10^{-7}) = 2 \cdot 10^{-5}(3 - \omega^2 \cdot 10^{-7})$$

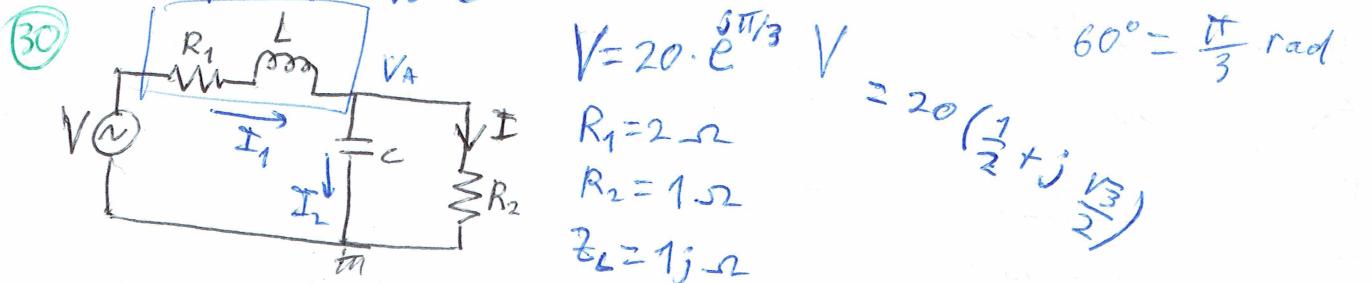
$$10^{-2} + 2 \cdot 10^{-5} - \omega^2 \cdot 10^{-9} - 2\omega^2 \cdot 10^{-12} = 6 \cdot 10^{-5} - 2\omega^2 \cdot 10^{-12}$$

$$1 + 2 \cdot 10^{-3} - \omega^2 \cdot 10^{-7} - 2\omega^2 \cdot 10^{-10} = 6 \cdot 10^{-3} - 2\omega^2 \cdot 10^{-10}$$

$$\omega = \sqrt{\frac{1 + 4 \cdot 10^{-3}}{10^{-2}}} = 3155.95 \quad \Rightarrow 1 + 2 \cdot 10^{-3} - 6 \cdot 10^{-3} = \omega^2 \cdot 10^{-7}$$

$$\boxed{f = \frac{\omega}{2\pi} = 502.3 \text{ Hz}}$$

$$\omega = 2\pi f \approx 100 \text{ rad/s}$$



$$I_1 = I_2 + I$$

$$\frac{V - V_A}{Z_1} = \frac{V_A}{Z_C} + \frac{V_A}{Z_{R_2}}$$

$$\frac{10 + 10\sqrt{3}j - V_A}{2+j} = \frac{V_A}{-2j} + V_A$$

$$(2+j)(-2j) = -4j + 2$$

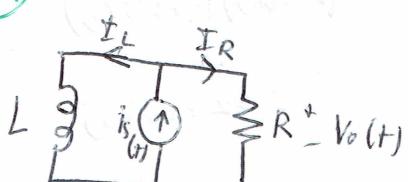
$$-2j[(10+10\sqrt{3}j) - V_A] = (2+j)V_A + (-4j)V_A$$

$$2jV_A - 20j + 20\sqrt{3} = (4 - 3j)V_A \Rightarrow 20\sqrt{3} - 20j = (4 - 3j)V_A$$

$$V_A = \frac{20\sqrt{3} - 20j}{4 - 3j} = \frac{40 \cdot e^{-j\frac{\pi}{6}}}{6.403e^{-j0.896}} = 6.247 e^{j0.3724}$$

$$I = V_A = 6.247 \cdot e^{j0.3724} \text{ A}$$

(31)



$$i_S(t) = 100 \cdot \cos(5000t + 0.142) \text{ mA}$$

$$L = 8 \text{ mH}$$

$$R = 30 \Omega$$

$$Z_L = j\omega L$$

$$I = 0.1 \cdot \cos(5000t + 0.142) \text{ A}$$

$$\frac{1}{Z_{eq}} = \frac{1}{Z_L} + \frac{1}{Z_R} = \frac{1}{j\omega L} + \frac{1}{R} = \frac{R + j\omega L}{j\omega LR}$$

$$Z_{eq} = \frac{j\omega LR}{j\omega L + R} = \frac{j5000 \cdot 8 \cdot 10^{-3} \cdot 30}{j5000 \cdot 8 \cdot 10^{-3} + 30} = \frac{1200 e^{j\frac{\pi}{2}}}{50 \cdot e^{j0.9273}} = 24 \cdot e^{j0.6435}$$

$$V_o = I \cdot Z_{eq} = 0.1 \cdot e^{j0.142} \cdot 24 \cdot e^{j0.6435}$$

$$= 2.4 \cdot e^{j0.786}$$

$$V_o(t) = 2.4 \cdot \cos(5000t + 0.786) \text{ V}$$

$$I_R = \frac{V_0}{Z_R} = \frac{2^4 \cdot e^{j0^\circ 786}}{30} = 0'08 \cdot e^{j0^\circ 786}$$

$$I_L = \frac{V_0}{Z_L} = \frac{2^4 \cdot e^{j0^\circ 786}}{5000 \cdot 8 \cdot 10^{-3} \cdot e^{j0^\circ 786}} = 0'06 \cdot e^{-j\pi/2}$$

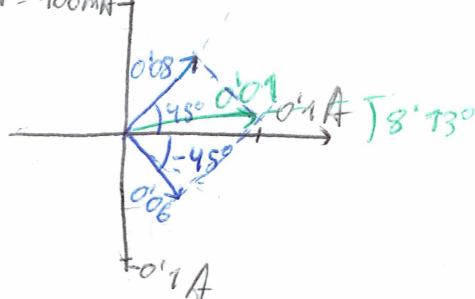
$$\sqrt{0'08^2 + 0'06^2} = 0'07$$

$$I: 0'1, 8'74^\circ$$

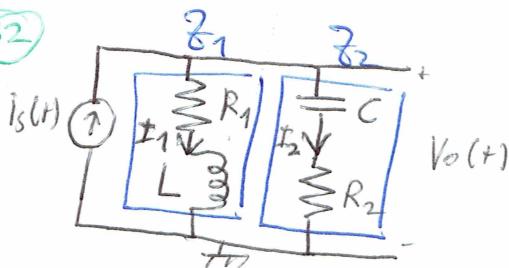
$$0'1A = 100mA \uparrow$$

$$I_R: 0'08, 45^\circ$$

$$I_L: 0'06, -45^\circ$$



(32)



$$Z_1 = R_1 + j\omega L \Rightarrow$$

$$C = 3'33 \mu F$$

$$Z_2 = R_2 + \frac{1}{j\omega C} \Rightarrow 10 + j \cdot 10^4 \cdot 6 \cdot 10^{-3} = 63'25 \cdot e^{j1'25}$$

$$I_s = I_1 + I_2$$

$$\frac{1 + 10 (j \cdot 3'33 \cdot 10^{-2})}{j 3'33 \cdot 10^{-2}} = \frac{1'054 \cdot e^{j0'321}}{3'33 \cdot 10^2 \cdot e^{j\pi/2}}$$

$$(20+60j)(1+0'333j)$$

$$0'02 + 66'66j$$

$$0'2196 - 0'2046j = \frac{V_0}{Z_1} + \frac{V_0}{Z_2} = \frac{V_0}{20+60j} + \frac{V_0 \cdot j 3'33 \cdot 10^{-2}}{1 + 3'33 \cdot 10^{-1} j}$$

$$(0'02 + 66'66j)(0'2196 - 0'2046j) = V_0(1 + 0'333j) + V_0 \cdot j 3'33 \cdot 10^{-2} (20+60j)$$

$$13'643 - 14'634j$$

$$= V_0 [1 + 0'333j + 0'666j - 1'998]$$

$$V_0 = \frac{13'643 - 14'634j}{-0'998 + 0'999j} = \frac{20 \cdot e^{-j0'82}}{1'412 \cdot e^{j2'356}} = 14'164 \cdot e^{-j3'176}$$

$$\approx 14'164 e^{-j\pi}$$

$$14'164 \cdot e^{j\pi}$$

$$V_0(t) = 14'164 \cdot \cos(10^4 t + \pi) V$$

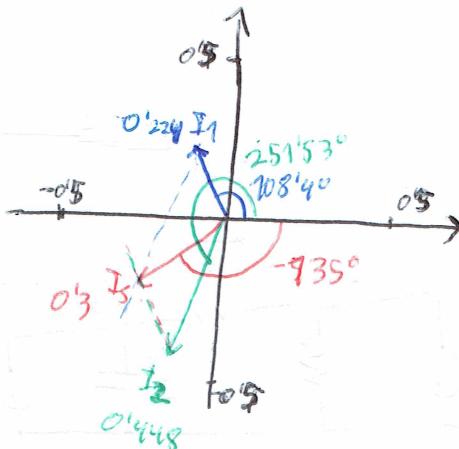
$$I_1 = \frac{V_o}{Z_1} = \frac{14'164 \cdot e^{j\pi}}{63'25 \cdot e^{-j125}} = 0'224 \cdot e^{j1'892}$$

$$I_2 = \frac{V_o}{Z_2} = \frac{14'164 \cdot e^{j\pi}}{31'65 \cdot e^{-j125}} = 0'448 \cdot e^{j4'39}$$

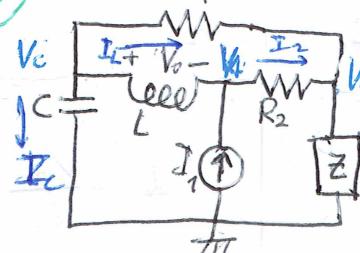
$$I_3: 0'3, -135^\circ$$

$$I_1: 0'224, 108'4^\circ$$

$$I_2: 0'448, 251'53^\circ$$



(33)



$$I_1 = 6 \cdot e^{j0^\circ} A$$

$$R_1 = 1 \Omega$$

$$R_2 = 1 \Omega$$

$$Z_L = 1j \Omega$$

$$Z_C = -1j \Omega$$

$$I_L = \frac{V_o}{Z_L} = \frac{2 e^{j\pi/4}}{e^{j\pi/2}} = 2 e^{-j\pi/4} = 2 \left(\frac{\sqrt{2}}{2} + j \frac{\sqrt{2}}{2} \right)$$

$$I_1 + I_L = I_2 = 6 + \sqrt{2} - j\sqrt{2} = 7'414 - \sqrt{2}j$$

$$I_1 = I_C + I_2$$

$$I_2 = I_3 + I_Z$$

$$I_3 = I_L + I_C$$

$$6 = I_C + I_Z$$

$$7'414 - \sqrt{2}j = I_3 + I_Z$$

$$I_3 = I_C + \sqrt{2} - \sqrt{2}j$$

$$I_C = -I_Z + 6$$

Necesito otra ecuación

$$I_C + \sqrt{2} - \sqrt{2}j = 7'414 - \sqrt{2}j - I_Z$$

$$I_C = 6 - I_Z$$

$$\Rightarrow I_C = 6 - 16'24 + \sqrt{2}j = -10'24 + \sqrt{2}j$$

$$V_C - V_o = V_A \Rightarrow V_C - V_o = V_B + 7'414 + \sqrt{2}j$$

$$V_A - I_2 \cdot R_2 = V_B \Rightarrow V_A = V_B + I_2 R_2$$

$$V_B - V_C = I_3$$

$$V_B - I_3 \cdot R_1 = V_C$$

$$V_B + I_2 = V_C - V_o \Rightarrow V_B - V_C = -I_2 - V_o$$

$$I_3 = -I_2 - V_o$$

$$I_3 = -7'414 + \sqrt{2}j - \sqrt{2} - \sqrt{2}j = -8'83$$

$$I_2 = I_3 + I_Z \Rightarrow 7'414 - \sqrt{2}j = -8'83 + I_Z \Rightarrow I_2 = 16'24 - \sqrt{2}j$$

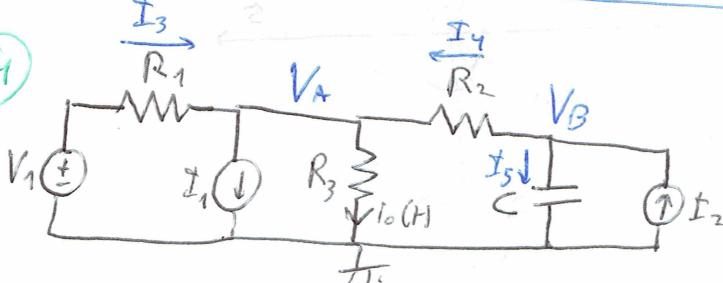
$$\frac{V_B}{Z} = I_2 \quad V_B = I_3 + V_C = 10'24j + \sqrt{2} - 8'83$$

$$\frac{V_C}{-j} = I_C = -10'24 + \sqrt{2}j \quad V_B = -7'416 + 10'24j$$

$$V_C = 10'24j + \sqrt{2}$$

$$Z = \frac{12'64 \cdot e^{j2'2}}{16'3 \cdot e^{-j0'09}} = 0'775 \cdot e^{j2'29}$$

(34)



$$V_1 = 12 \text{ V}$$

$$R_1 = R_3 = 2 \Omega$$

$$I_1 = 2 \text{ A}$$

$$R_2 = 1 \Omega$$

$$I_2 = 4 \text{ A}$$

$$Z_C = -1j \Omega$$

$$\begin{aligned} I_3 + I_4 &= I_1 + I_0 \\ I_2 &= I_4 + I_5 \end{aligned} \quad \left\{ \begin{aligned} I_3 + I_4 &= 2 + I_0 \\ 4 &= I_4 + I_5 \end{aligned} \right\}$$

$$I_0 = \frac{V_A}{R_3}$$

$$\frac{12 - V_A}{2} + \frac{V_B - V_A}{1} = 2 + \frac{V_A}{2} \Rightarrow 12 - V_A + 2V_B - 2V_A = V_A + 4 \Rightarrow V_B = \frac{4(V_A - 8)}{2}$$

$$4 = \frac{V_B - V_A}{1} + \frac{V_B + j}{-j \omega}$$

$$4 = (V_B - V_A) + jV_B \Rightarrow V_B(1+j) = 4 + V_A$$

$$V_A = \frac{16 + 8j}{2 + 9j} = \frac{17'89 \cdot e^{j0'646}}{\sqrt{20} \cdot e^{j2'29}}$$

$$V_A = 4 \cdot e^{j0'646}$$

$$\frac{4V_A - 8}{2} = \frac{4 + V_A}{1+j}$$

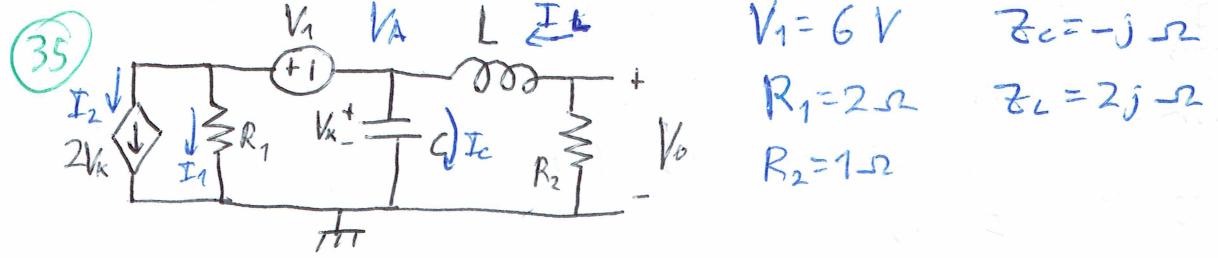
$$(4V_A - 8)(1+j) = 8 + 2V_A$$

$$2V_A + 4V_A j - 8 - 8j = 8$$

$$V_A(2+4j) = 16 + 8j$$

$$I_0 = \frac{4 \cdot e^{j0'646}}{2} = [2 \cdot e^{-j0'646}] \text{ A}$$

$$[i_0(t) = 2 \cos(\omega t - 0'644) \text{ A}]$$



$$I_L = I_2 + I_1 + I_c \quad V_A = V_L$$

$$\frac{-V_A}{2+j} = \frac{V_A + 6}{2} + \frac{V_A j}{-j} + 2V_A \quad V_o = -I_L \cdot R_2$$

$$\frac{-V_A}{\frac{1}{2}+j} = V_A + 6 + 2V_A j + 4V_A = 5V_A + 2V_A j + 6$$

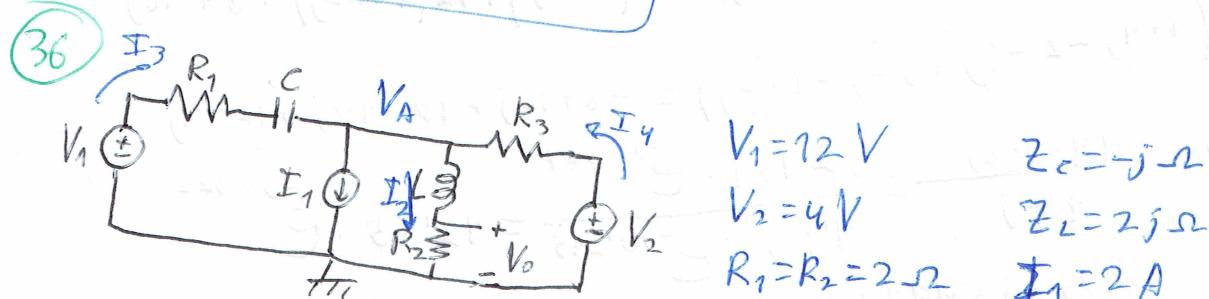
$$-V_A = (2+j)(5V_A + 2V_A j + 6) = \frac{5}{2}V_A + V_A j + 3 + 5jV_A - 2V_A + 6j$$

$$-\frac{3}{2}V_A - 7V_A j = 3 + 6j$$

$$V_A = \frac{3+6j}{\frac{-3-7j}{2}} = \frac{6+12j}{-3-14j} = \frac{13'42 \cdot e^{j111}}{14'32 \cdot e^{j136}} = 0'94 \cdot e^{-j0'25}$$

$$I_L = \frac{-V_A}{2+2j} = \frac{0'94 \cdot e^{-j0'25}}{\sqrt{5} \cdot e^{j111}} = 0'92 \cdot e^{-j1'36}$$

$V_o = -I_L = -0'92 \cdot e^{-j1'36}$



$$I_3 + I_4 = I_1 + I_2$$

$$\frac{12-V_A}{2-j} + \frac{4-V_A}{1} = 2 + \frac{V_A}{2+2j} \quad (2-j)(2+2j) = 6+2j$$

$$(12-V_A)(2+2j) + (2-V_A)(6+2j) = V_A(2-j)$$

$$24-2V_A + 24j - 2V_A j + 12 + 4j - 6V_A - 2V_A j = 2V_A - V_A j$$

$$36 + 28j = 10V_A + 3V_A j$$

$$V_A = \frac{36+28j}{10+3j} = \frac{45'61 \cdot e^{j0'66}}{10'44 \cdot e^{j0'29}} = 4'37 \cdot e^{j0'37}$$

$$V_1 = 6V \quad Z_C = -j\Omega$$

$$R_1 = 2\Omega \quad Z_L = 2j\Omega$$

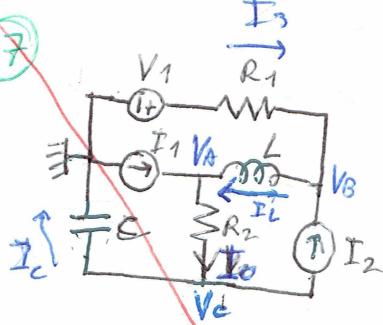
$$R_2 = 1\Omega$$

$$V_o = I_2 \cdot R_2$$

$$V_o = 2 \cdot 1'54 \cdot e^{-j0'42} \quad V$$

$V_o = 3'08 \cdot e^{-j0'42} \quad V$

37



$$\begin{aligned}
 V_1 &= 12 \text{ V} & I_1 &= 2 \text{ A} \\
 R_1 = R_2 &= 2 \Omega & I_2 &= 4 \text{ A} \\
 Z_L &= 1j\Omega \\
 Z_C &= -2j\Omega
 \end{aligned}$$

$$\left. \begin{aligned}
 I_1 + I_L &= I_0 \\
 I_2 + I_3 &= I_L \\
 I_0 &= I_2 + I_C
 \end{aligned} \right\} \quad \left. \begin{aligned}
 2 + \frac{V_B - V_A}{j} &= \frac{V_A - V_C}{2} \Rightarrow 4j + 2V_B - 2V_A = jV_A - jV_C \\
 4 + \frac{12 - V_B}{2} &= \frac{V_B - V_A}{j} \Rightarrow 8j + 12j - jV_B = 2V_B - 2V_A \\
 \frac{V_A - V_C}{2} &= 4 + \frac{V_C - j}{-2j} \Rightarrow V_A - V_C = 8 + V_Cj
 \end{aligned} \right\}$$

$$\begin{aligned}
 V_A - 8 &= V_C + V_Cj \Rightarrow V_C = \frac{V_A - 8}{1+j} \\
 2V_B + jV_B &= 2V_A + 20j \Rightarrow V_B = \frac{2V_A + 20j}{2+j} \\
 4j + 2\left(\frac{2V_A + 20j}{2+j}\right) - 2V_A &= jV_A - j\left(\frac{V_A - 8}{1+j}\right) \quad (2+j)(1+j) = +1+3j
 \end{aligned}$$

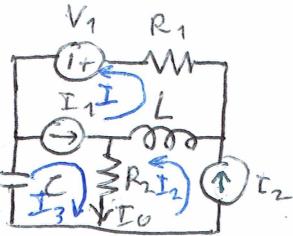
$$\begin{aligned}
 4j(1+3j) + (4V_A + 40j)(1+j) - 2V_A(1+3j) &= jV_A(1+3j) - (V_Aj - 8j)(2+j) \\
 4j - 12 + (4+4j)V_A + 40j - 40 - V_A(2+6j) &= V_A(-3+j) + V_A(+1-2j) - 8 + 16j
 \end{aligned}$$

$$V_A = \frac{44 - 28j}{4 - j} = \frac{52'154 \cdot e^{-j0'567}}{4'123 \cdot e^{-j0'245}} = 12'65 \cdot e^{-j0'322}$$

$$\begin{aligned}
 V_C &= \frac{V_A - 8}{1+j} = \frac{4'0175 - j3'9974}{1+j} = \frac{5'67 \cdot e^{-j0'783}}{\sqrt{2} \cdot e^{j\pi/4}} = 72'65(0'95 - j0'316) \\
 &\approx 4'01 \cdot e^{-j1'568} \approx 4 \cdot e^{-j\pi} = 4 \cdot e^{j\pi} = 4(-1) = -4
 \end{aligned}$$

$$I_0 = \frac{V_A - V_C}{2} = \frac{12'02 - 4j - (-4)}{2} = \frac{8 - 4j}{2} = 4 - 2j \quad A$$

(37)



$$V_1 = 12 \text{ V} \quad I_1 = 2 \text{ A}$$

$$R_1 = R_2 = 2 \Omega \quad I_2 = 4 \text{ A}$$

$$Z_L = j\omega L$$

$$Z_C = -j\omega C$$

$$I_0 = I_2 + I_3$$

$$I_1 = I + I_3 \Rightarrow I = 2 - I_3$$

$$V_{x1} = (I - I_2) Z_L + I \cdot R_1 + V_1$$

$$\left. \begin{array}{l} V_{x2} = (I_2 - I) Z_L + (I_2 + I_3) R_2 \\ V_{x3} = (I_2 + I_3) R_2 + I_3 \cdot Z_C \end{array} \right\} \begin{array}{l} V_{x1} = (I - 4) j + 2I + 12 \\ V_{x2} = (4 - I) j + (4 + I_3) \cdot 2 \\ V_{x3} = (4 + I_3) \cdot 2 + I_3 (-2j) \end{array}$$

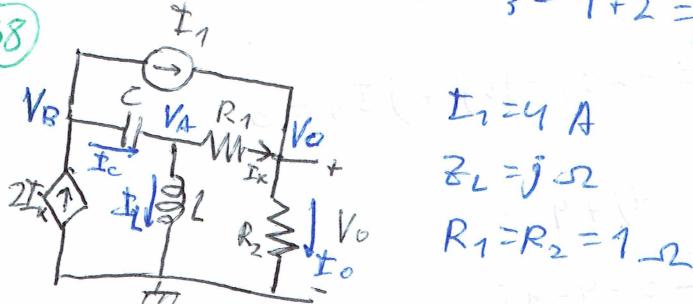
$$\left. \begin{array}{l} V_{x1} = j(2 - I_3) - 4j + 4 - 2I_3 + 12 \\ V_{x3} = 8 + 2I_3 - 2jI_3 \end{array} \right.$$

$$0 = 2j - I_3 j - 4j + 16 - 2I_3 - 8 - 2I_3 + 2jI_3$$

$$0 = -2j + 8 + jI_3 - 4I_3 \Rightarrow I_3 = \frac{-8 + 2j}{-4 + j} = 2 \text{ A}$$

$$I_0 = I_2 + I_3 = 4 + 2 = 6 \text{ A}$$

(38)



$$I_1 = 4 \text{ A}$$

$$Z_L = j\omega L$$

$$R_1 = R_2 = 1 \Omega$$

$$I_1 + I_K = I_0$$

$$2I_K = I_1 + I_C \quad \left. \begin{array}{l} 4 + V_A - V_0 = -V_0 \Rightarrow V_A = 2V_0 - 4 \\ 2V_A - 2V_0 = 4 + \frac{V_B - V_A}{Z_C} \end{array} \right\} 2V_A - 2V_0 = 4 + I_C$$

$$I_C = I_K + I_L$$

$$\frac{V_B - V_A}{Z_C} = V_A - V_0 + \frac{V_A}{j}$$

$$I_C = V_A - V_0 + \frac{V_A}{j}$$

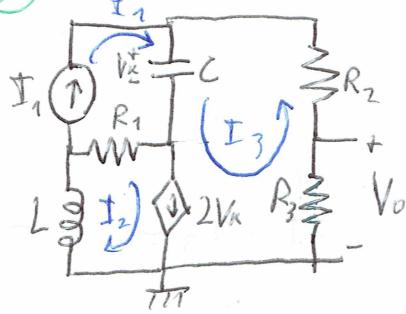
$$2V_A - 2V_0 - 4 = V_A - V_0 - jV_A$$

$$V_A(1+j) = 4 + V_0$$

$$(2V_0 - 4)(1+j) = 4 + V_0 \Rightarrow V_0(2+2j) - 4 - 4j = 4 + V_0 \Rightarrow V_0 = \frac{+8 + 4j}{1+2j} = \frac{8 + 4j}{\sqrt{5}} e^{j0^\circ 46^\circ} =$$

$$= \boxed{V_0 = 4 \cdot e^{-j0^\circ 65^\circ} \text{ V}}$$

(39)



$I_1 = 4 \text{ A}$

$R_1 = R_2 = R_3 = 1 \Omega$

$V_o = -I_3$

$Z_L = 1j \Omega$

$Z_C = -1j \Omega$

$V_x = (I_1 + I_3) Z_C = -4j - I_3 j$

$V_{x1} = -4j - I_3 j + 4 - I_2$

$V_{x2} = I_2 \cdot j + I_2 - 4$

$V_{x2} = I_3 + I_3 - 4j - I_3 j$

$I_2 + I_3 = 2V_x = -8j - 2I_3 j$

$I_2 + I_3 = -8j - 2I_3 j$

$I_3(1+2j) = -I_2 - 8j$

$I_3 = \frac{-I_2 - 8j}{1+2j}$

$I_2(1+j) - 4 = (2-j)I_3 - 4j$

$I_2 + jI_2 - 4 = (2-j) \cdot \frac{-I_2 - 8j}{1+2j} - 4j$

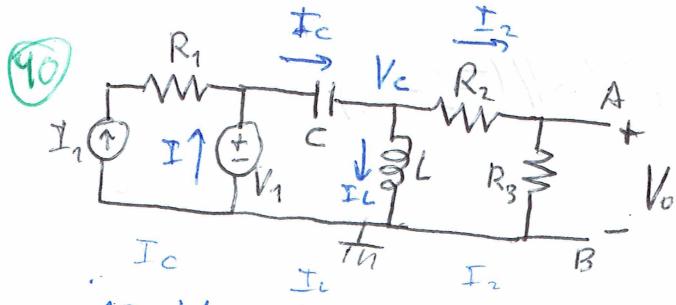
$(I_2 + jI_2 - 4 + 4j)(1+2j) = (2-j)(-I_2 - 8j)$

$I_2(1+j+2j-2+2-j) = -2I_2 - 16j + jI_2 - 8$

$I_2 = \frac{(4-12j)(1-2j)}{(1+2j)(1-2j)} = \frac{-20-20j}{5} = -4-4j$

$I_3 = \frac{4+4j-8j}{1+2j} = \frac{(4-4j)(1-2j)}{(1+2j)(1-2j)} = \frac{-4-12j}{5} = -0.8-2.4j$

$\boxed{V_o = -I_3 = 0.8 + 2.4j}$



$$\frac{12 - V_c}{-j} = \frac{V_c}{2j} + \frac{V_c}{3}$$

$$12j - V_c j = -\frac{V_c j}{2} + \frac{V_c}{3}$$

$$72j - 6V_c j = -3V_c j + 2V_c$$

$$72j = V_c (2 + 3j)$$

$$V_c = \frac{72j}{2 + 3j}$$

$$V_1 = 12V \quad Z_L = 2j\Omega$$

$$I_1 = 6A \quad Z_C = -j\Omega$$

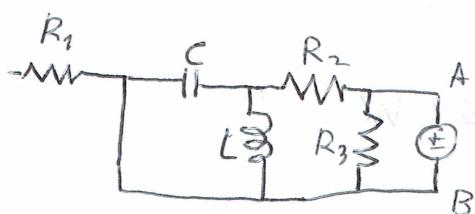
$$R_1 = R_2 = 2\Omega$$

$$R_3 = 1\Omega$$

$$V_o = V_{th} = R_3 \cdot I_2 = I_2 = \frac{V_c}{3}$$

$$V_o = \frac{1}{3} \cdot \frac{72j}{(2+3j)} = \frac{72 \cdot e^{j\pi/2}}{10.817 \cdot e^{j0.988}} =$$

$$= \boxed{6.66 \cdot e^{j0.988} V} = V_{th}$$



$$Z_{th} = Z_{R3} \parallel \left(Z_{R2} + (Z_L \parallel Z_C) \right) = 1 \parallel \left(2 + \frac{2j}{j-2} \right)$$

$$\frac{1}{2} - \frac{1}{j} = \frac{j-2}{2j} \quad \frac{(j-2)2 + 2j}{(j-2)} = \frac{2j-4 + 2j}{j-2} = \frac{4j-4}{j-2}$$

$$Z_L \parallel Z_C = \frac{2j}{j-2}$$

$$\frac{1}{Z_{th}} = 1 + \frac{j-2}{4j-4} = \frac{4j-4 + j-2}{4j-4} = \frac{5j-6}{4j-4}$$

$$Z_{th} = \frac{4j-4}{5j-6} = \frac{4V_2}{5j-6} \cdot e^{j2.356}$$

$$= \frac{4}{\sqrt{67}} \cdot e^{j2.447} = \boxed{0.72 \cdot e^{j0.091} \Omega}$$

(91)



$I_1 = 2 e^{j\pi/6} \text{ A}$

$R = 4 \Omega$

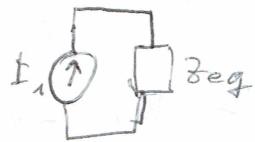
$Z_L = 2j \Omega$

$Z_C = -4j \Omega$

$Z_{eq} = Z_R // (Z_L + Z_C)$

$\frac{1}{Z_{eq}} = \frac{1}{4} + \frac{1}{2j-4j} = \frac{1}{4} + \frac{1}{-2j} = \frac{1}{4} + \frac{j}{2} = \frac{1+2j}{4}$

$Z_{eq} = \frac{4(1-2j)}{(1+4)(1-2j)} = \frac{4-8j}{5} = 0.8 - 1.6j = 1.79 \cdot e^{-j111}$



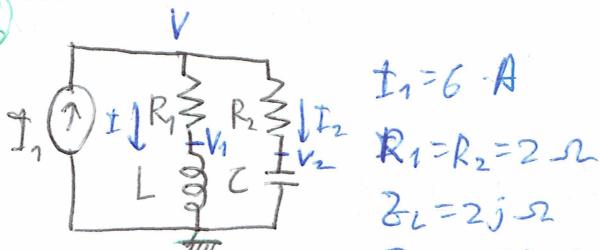
$V = I_1 \cdot Z_{eq} = 2 \cdot e^{j\pi/6} \cdot 1.79 \cdot e^{-j111} = 3.58 \cdot e^{-j0.58}$

$i(t) = 2 \cdot \cos(\omega t + \pi/6)$

$v(t) = 3.58 \cdot \cos(\omega t - 0.58)$

$\bar{P} = \frac{I \cdot V}{2} \cdot \cos\left(\frac{\pi}{6} + 0.58\right) = \frac{7.16 \cdot 0.45}{2} = 1.67 \text{ W}$

(92)



$I_1 = 6 \text{ A}$

$R_1 = R_2 = 2 \Omega$

$Z_L = 2j \Omega$

$Z_C = -4j \Omega$

$I_1 = I + I_2$

$6 = \frac{V}{2+2j} + \frac{V}{2-j} \quad (2+2j)(2-j) = 6 + 3j$

$36 + 12j = 2V - jV + 2V + 2jV$

$V = \frac{36 + 12j}{4+j} = \frac{37.93 \cdot e^{j0.322}}{4.123 \cdot e^{j0.245}} = 9.2 \cdot e^{j0.077}$

$I = \frac{V}{2+2j} = \frac{9.2 \cdot e^{j0.077}}{2.83 \cdot e^{j0.285}}$

$I = 3.25 \cdot e^{-j0.708} \text{ A}$

$I_2 = \frac{V}{2-j} = \frac{9.2 \cdot e^{j0.077}}{\sqrt{5} \cdot e^{-j0.460}}$

$I_2 = 4.11 \cdot e^{j0.542} \text{ A}$

$V_1 = I \cdot Z_L = 2 \cdot e^{j\pi/2} \cdot 3.25 \cdot e^{-j0.708} = 6.5 \cdot e^{j0.863}$

$V_2 = I_2 \cdot Z_C = e^{-j\pi/2} \cdot 4.11 \cdot e^{j0.542} = 4.11 \cdot e^{-j1.029}$

$V - V_1 = I \cdot Z_{R1} = 2 \cdot 3.25 \cdot e^{-j0.708} = 6.5 \cdot e^{-j0.708}$

$V - V_2 = I_2 \cdot Z_{R2} = 2 \cdot 4.11 \cdot e^{j0.542} = 8.22 \cdot e^{j0.542}$

$$\bar{P}_{R_1} = \frac{6'5 \cdot 3'25}{2} \cdot \cos(-0'708 + 0'708) = 10'56 \text{ W} \quad \text{Consumida}$$

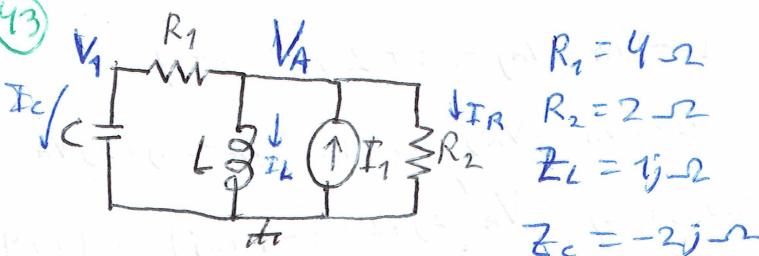
$$\bar{P}_{R_2} = \frac{8'22 \cdot 4'91}{2} \cdot \cos(0'542 - 0'542) = 16'89 \text{ W} \quad \text{Consumida}$$

$$\bar{P}_L = \frac{6'5 \cdot 3'25}{2} \cdot \cos(-0'708 - 0'863) = 0 \text{ W}$$

$$\bar{P}_C = \frac{8'22 \cdot 4'91}{2} \cdot \cos(0'542 + 1'029) = 0 \text{ W}$$

$$\bar{P}_{I_1} = \frac{6 \cdot 9'2}{2} \cdot \cos(0'077) = 27'52 \text{ W} \quad \text{Suministrada}$$

(43)



$$I_1 = 4 e^{j0} \text{ A}$$

$$R_1 = 4-j2$$

$$R_2 = 2-j2$$

$$Z_L = 1-j2$$

$$Z_C = -2j-j$$

$$I_1 = I_c + I_L + I_R$$

$$V_A = \frac{V_A}{4-j2} + \frac{V_A}{j} + \frac{V_A}{2}$$

$$8 = \frac{V_A}{2-j} - 2V_{A,j} + V_A$$

$$I_L = \frac{3'51 \cdot e^{j0'91}}{e^{j0'91}} = 3'51 \cdot e^{-j0'661} \quad | \quad V_A = 16 + 4V_{A,j} - 2V_A - 8j + 2V_A + V_{A,j}$$

$$I_R = \frac{3'51 \cdot e^{j0'91}}{2} = 1'76 \cdot e^{j0'91} \quad | \quad V_A(1-5j) = 16-8j$$

$$I_c = \frac{3'51 \cdot e^{j0'91}}{4'47 \cdot e^{-j0'464}} = 0'79 \cdot e^{j0'374} \quad | \quad V_A = \frac{16-8j}{1-5j} = \frac{17'89 \cdot e^{-j0'464}}{5'1 \cdot e^{-j1'373}}$$

$$V_1 = I_c \cdot Z_C = +2 \cdot e^{-j0'28} \cdot 0'79 \cdot e^{j0'374} = 1'58 \cdot e^{-j0'2} = 3'51 \cdot e^{j0'91}$$

$$V_A - V_1 = I_c \cdot R_1 = 4 \cdot 0'79 \cdot e^{j0'374} = 3'16 \cdot e^{j0'374}$$

$$\bar{P}_{R_2} = \frac{1'76 \cdot 3'51}{2} \cdot \cos(0'91 - 0'91) = [3'09 \text{ W}] (\text{consumida})$$

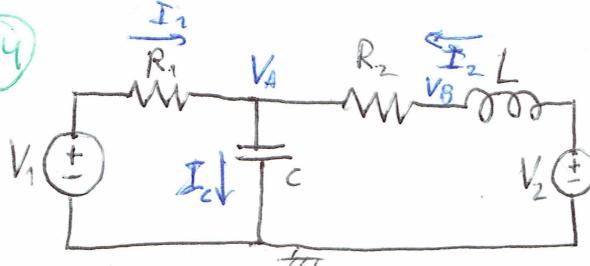
$$\bar{P}_{R_1} = \frac{0'79 \cdot 3'16}{2} \cdot \cos(1'374 - 1'374) = [1'25 \text{ W}] (\text{consumida})$$

$$\bar{P}_{I_1} = \frac{4 \cdot 3'51}{2} \cdot \cos(0'91) = [4'31 \cdot W] \text{ (suministrada)}$$

$$\bar{P}_C = \frac{0'79 \cdot 1'58}{2} \cdot \cos(1'374 + 0'2) = 0 \text{ W}_{\parallel}$$

$$\bar{P}_L = \frac{3'51 \cdot 3'51}{2} \cdot \cos(0'91 + 0'661) = 0 \text{ W}_{\parallel}$$

(44)



$$V_1 = 12 \text{ V}$$

$$Z_L = 1j \text{ ohm}$$

$$V_2 = 6 \text{ V}$$

$$Z_C = -2j \text{ ohm}$$

$$R_1 = 9 \text{ ohm}$$

$$R_2 = 2 \text{ ohm}$$

$$I_1 + I_2 = I_c$$

$$\frac{12 - V_A}{1} + \frac{6 - V_A}{2+j} = \frac{V_A}{-2j} = \frac{V_A j}{2}$$

$$12 - 2V_A = (V_A j - 24 + 2V_A)(2+j)$$

$$24 - 2V_A + \frac{12 - 2V_A}{2+j} = V_A j$$

$$12 + 48 + 24j = V_A(2j + 2 + 9 - 1 + 2j) = V_A(5 + 4j)$$

$$I_1 = 12 - 9'67 + j2'93 = 3'74 \cdot e^{j0'899}$$

$$V_A = \frac{64'62 \cdot e^{j0'381}}{6'4 \cdot e^{j0'675}} = 10'1 \cdot e^{j0'294}$$

$$I_2 = \frac{6 - 9'67 + j2'93}{2'23 \cdot e^{j0'464}} = \frac{4'75 \cdot e^{j2'47}}{2'23 \cdot e^{j0'464}} = 2'11 \cdot e^{j2'01}$$

$$9'67 - j2'93$$

$$I_c = \frac{10'1 \cdot e^{-j0'294}}{2 \cdot e^{-j1'11}} = 5'05 \cdot e^{j1'277}$$

$$V_B = V_A + I_2 \cdot R_2 = V_A + 4'22 \cdot e^{j0'281}$$

$$V_B = 9'67 - j2'93 - 1'79 + j3'82j$$

$$\bar{P}_{R_1} = \frac{3'74 \cdot 3'74}{2} \cdot \underbrace{\cos(0'899 - 0'894)}_{1} = 7 \text{ W consume}$$

$$V_B = 7'88 + 0'89j$$

$$\bar{P}_{R_2} = \frac{4'22 \cdot 2'11}{2} \cdot \underbrace{\cos(2'01 - 2'01)}_{1} = 4'45 \text{ W consume}$$

$$V_B - V_A = 4'22 \cdot e^{j2'01}$$

$$\bar{P}_L = \frac{2'11 \cdot 2'11}{2} \cdot \cos(3'581 - 2'01) = 0 \text{ W}$$

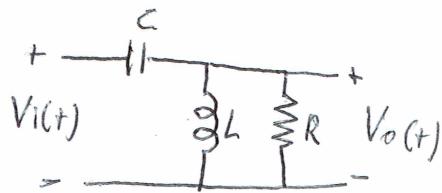
$$\bar{P}_C = \frac{9'67 \cdot 5'05}{2} \cdot \cos(1'277 + 0'294) = 0 \text{ W}$$

$$\bar{P}_{V_1} = \frac{12 \cdot 3'74}{2} \cdot \cos(0'899) = 13'97 \text{ W suministra}$$

$$2'11 \cdot e^{j2'01} \cdot e^{j\pi/2} \\ 2'11 \cdot e^{j3'581}$$

$$\bar{P}_{V_2} = \frac{6 \cdot 2'11}{2} \cdot \cos(2'01) = 2'69 \text{ W consume}$$

(95)



$$\frac{Vi - Vo}{Z_C} = \frac{Vo}{Z_L} + \frac{Vo}{Z_R}$$

$$Z_C = \frac{1}{j\omega C}$$

$$Z_L = j\omega L$$

$$Z_R = R$$

$$(Vi - Vo)j\omega C = \frac{Vo}{j\omega L} + \frac{Vo}{R} = Vo \left(\frac{1}{j\omega L} + \frac{1}{R} \right) \Rightarrow$$

$$\Rightarrow j\omega C Vi - j\omega C V_o = V_o \left(\frac{R + j\omega L}{j\omega LR} \right) \Rightarrow j\omega C Vi = V_o \left(\frac{R + j\omega L}{j\omega LR} + j\omega C \right) \Rightarrow$$

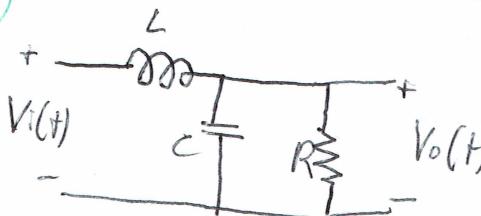
$$\Rightarrow V_o \left(\frac{R + j\omega L - \omega^2 CLR}{j\omega LR} \right) = j\omega C Vi \Rightarrow \frac{V_o}{Vi} = \frac{j\omega C j\omega L R}{R + j\omega L - \omega^2 CLR} = \boxed{\frac{-\omega^2 CLR}{R - \omega^2 CLR + j\omega L}}$$

$$\omega \rightarrow 0 \Rightarrow T(\omega) \rightarrow \frac{0}{R - 0} = 0$$

$$\omega \rightarrow \infty \Rightarrow T(\omega) \rightarrow \frac{-\omega^2 CLR}{-\omega^2 CLR} \rightarrow 1$$

Filtro de paso alta.

(96)



$$\frac{Vi - Vo}{Z_L} = \frac{Vo}{Z_C} + \frac{Vo}{Z_R}$$

$$Z_C = \frac{1}{j\omega C}$$

$$Z_L = j\omega L$$

$$Z_R = R$$

$$\frac{Vi - Vo}{j\omega L} = V_o \cdot j\omega C + \frac{V_o}{R} \Rightarrow$$

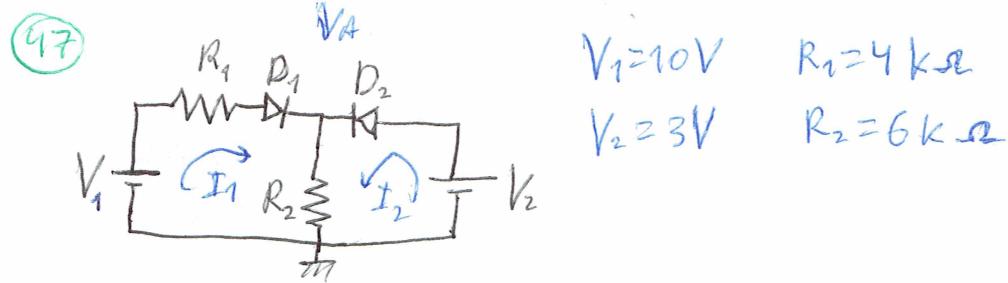
$$\Rightarrow \frac{Vi}{j\omega L} = V_o \left(\frac{1}{j\omega L} + j\omega C + \frac{1}{R} \right) \Rightarrow \frac{Vi}{j\omega L} = V_o \left(\frac{R + j\omega C \cdot j\omega L \cdot R + j\omega L}{j\omega L \cdot R} \right) \Rightarrow$$

$$\Rightarrow \frac{Vi}{j\omega L} = V_o \left(\frac{R - \omega^2 CLR + j\omega L}{j\omega L R} \right) \Rightarrow \frac{V_o}{Vi} = \frac{j\omega L R}{(R - \omega^2 CLR + j\omega L) j\omega L} = \boxed{\frac{R}{R - \omega^2 CLR + j\omega L}}$$

$$\omega \rightarrow 0 \Rightarrow T(\omega) \rightarrow \frac{R}{R} = 1$$

$$\omega \rightarrow \infty \Rightarrow T(\omega) \rightarrow \frac{R}{-\omega^2 CLR + j\omega L} \rightarrow 0$$

Filtro de paso baja



$D_1, D_2 \text{ OFF} \Rightarrow V_{D1} = 10V, V_{D2} = 3V$ Absurdo

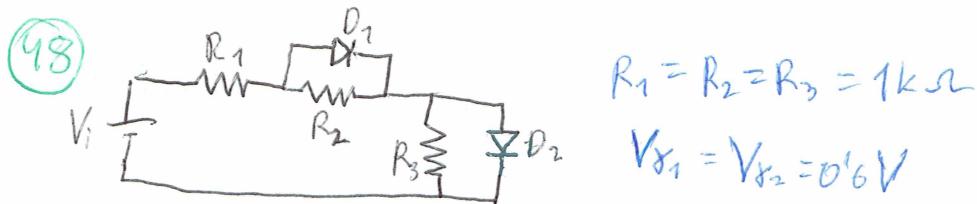
$D_1 \text{ OFF}, D_2 \text{ ON} \Rightarrow V_{D1} = 7V$ Absurdo $\Rightarrow D_1 \text{ ON}$

$D_2 \text{ OFF} \Rightarrow I_2 = 0, I_1 = \frac{V_1}{R_1 + R_2} = \frac{10}{10} = 1 \text{ mA}$

$V_A = I_1 \cdot R_1 = 6V > 3V \Rightarrow$ Suposición correcta, $D_2 \text{ OFF}$

$I_{R1} = I_1 = 1 \text{ mA}$

$I_{R2} = I_1 + I_2 = 1 + 0 = 1 \text{ mA}$



Ambos en conte: $I = \frac{V_1}{R_1 + R_2 + R_3} = \frac{V_1}{3}$

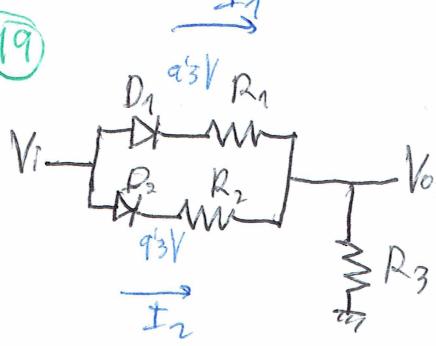
$V_{R2} = I \cdot R_2 = \frac{V_1}{3} \cdot 1$

$V_{R3} = I \cdot R_3 = \frac{V_1}{3} \cdot 1$

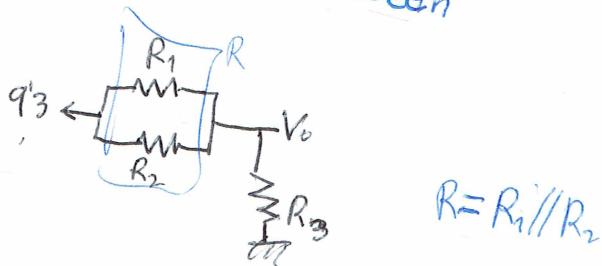
Ambos comenzarán a conducir a la vez,
Lo harán para:

$0.6 = \frac{V_1}{3} \Rightarrow V_1 = 1.8V$

(49)



$10 > 0'7 \Rightarrow$ ambos conduzam

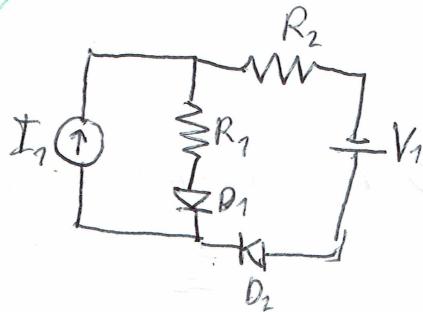


$$\frac{1}{R} = \frac{1}{2} + \frac{1}{0'7} = 10'5 \Rightarrow R = \frac{1}{10'5} = 0'09524 \text{ k}\Omega$$

$$I = \frac{q'3}{0'09524} = 4'44 \text{ mA}$$

$$V_0 = I \cdot R_3 = 8'88 \text{ V}$$

(50)



$$R_1 = 2 \text{ k}\Omega$$

$$R_2 = 1 \text{ k}\Omega$$

$$I_1 = 5 \text{ mA}$$

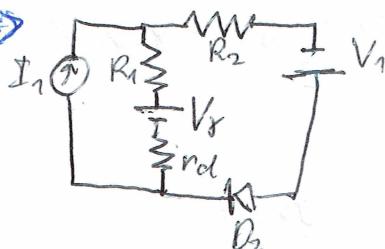
$$V_1 = 10 \text{ V}$$

$$V_0 = 0'7 \text{ V}$$

$$r_d = 20 \text{ }\Omega = 0'02 \text{ k}\Omega$$

Sup. D1, D2 OFF $\Rightarrow V_{D2} = 10 \text{ V}$ Absurdo

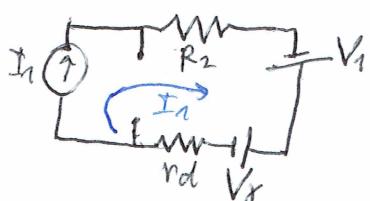
Sup. D1 ON, D2 OFF \Rightarrow



$$V_{D1} = I_1 (R_1 + r_d) + V_0$$

$V_{D2} = 10 \text{ V}$ Absurdo $\Rightarrow D_2 \text{ ON}$

Sup. D1 OFF, D2 ON

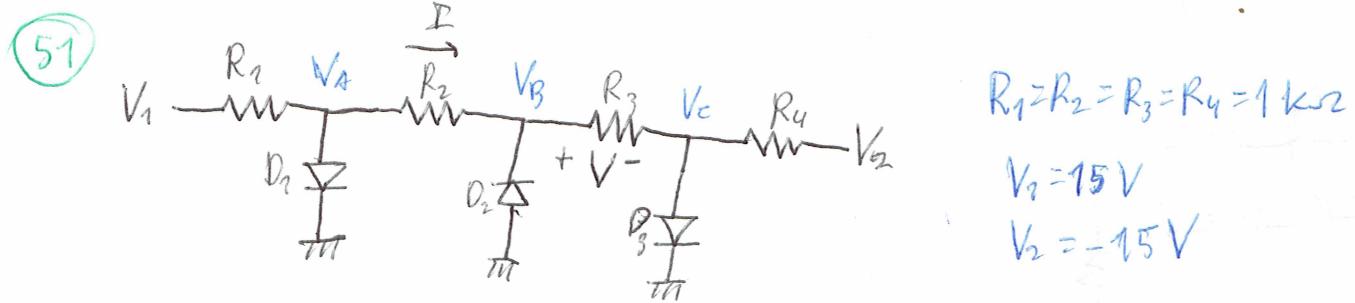


$$V_1 - V_r + V_{D1} = I_1 (R_2 + r_d) \Rightarrow V_{D1} + 9'3 = 5'1$$

$$V_{D1} = -4'2 \text{ V} \text{ (suspicion correcta)}$$

$$V_{D1} = -4'2 \text{ V}$$

$$I_{D1} = 0 \quad I_{D2} = 5 \text{ mA}$$



$$R_1 = R_2 = R_3 = R_4 = 1 \text{ k}\Omega$$

$$V_1 = 15 \text{ V}$$

$$V_2 = -15 \text{ V}$$

Sup D_1, D_2, D_3 OFF $\Rightarrow V_{D1} = 7'5 \text{ V}$, Absurdo $\Rightarrow D_1 \text{ ON}$

Sup $D_1 \text{ ON}, D_2, D_3 \text{ OFF} \Rightarrow V_{D2} = 5 \text{ V}$, Absurdo $\Rightarrow D_2 \text{ ON}$

Sup $D_1, D_2 \text{ ON}, D_3 \text{ OFF} \Rightarrow V_A = 0 \quad \left. \begin{array}{l} \\ V_B = 0 \end{array} \right\} \Rightarrow I_{R_2} = 0$

$$V_C = -7'5 \text{ V}$$

$$\Rightarrow V_{R_2} = 7'5 \text{ V}$$

(52) Sup D_1, D_2, D_3 OFF $\Rightarrow V_{D1} = 7'5 \text{ V}$, Absurdo $\Rightarrow D_1 \text{ ON}$

Sup $D_1 \text{ ON}, D_2, D_3 \text{ OFF}$

$$V_A = 0'7 \text{ V}$$

$$I = \frac{+15 + 0'7}{3} = 5'23 \text{ mA}$$

$$V_B = 0'7$$

Sup $D_1, D_2 \text{ ON}, D_3 \text{ OFF} \Rightarrow V_{D2} = 4'53 \text{ V}$, Absurdo $\Rightarrow D_2 \text{ ON}$

$$V_A = 0'7$$

$$V_B = -0'7$$

$$I_1 = \frac{-0'7 + 15}{2} = 7'15 \text{ mA}$$

$$V_{D3} = -7'85 \text{ V}$$

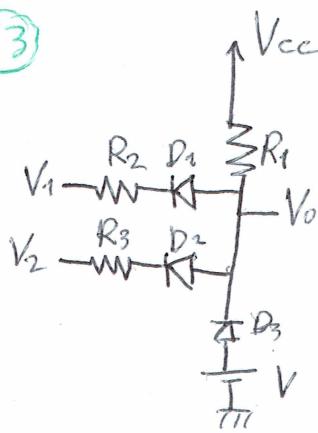
$$V_C = -0'7 - 7'85 = -7'85 \text{ V}$$

Suposición correcta,

$$I = V_A - V_B = 0'7 - (-0'7) = 1'4 \text{ mA}$$

$$V = V_B - V_C = -0'7 - (-7'85) = 7'15 \text{ V}$$

(53)



$$R_1 = 10 \text{ k}\Omega$$

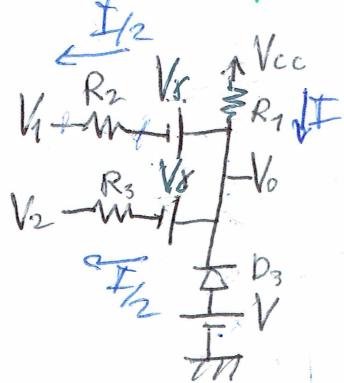
$$R_2 = R_3 = 0'47 \text{ k}\Omega$$

$$V = 3'7 \text{ V}$$

$$V_F = 0'7 \text{ V}$$

a) $V_1 = V_2 = 25 \text{ V}$

$$V_{cc} = 32 \text{ V}$$



$$I = \frac{I}{2} + \frac{I}{2}$$

$$\frac{V_{cc} - V_0}{R_1} = 2 \cdot \frac{V_0 - V_F - V_1}{R_2}$$

$$\frac{32 - V_0}{10} = 2 \cdot \frac{V_0 - 0'7 - 25}{0'47}$$

$$32 - 0'4 V_0 = 4'255 V_0 - 109'36$$

$$112'56 = 4'355 V_0$$

$$\boxed{V_0 = 25'846 \text{ V}}$$

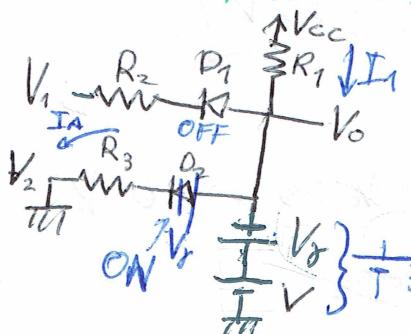
b) D_1 ON

D_2 ON

D_3 OFF

(54)

a) $V_1 = 25 \text{ V}, V_2 = 0 \text{ V}, V_0 = 3 \text{ V}$



$$I_A = \frac{3 - V_F}{R_3} = 4'894 \text{ V}$$

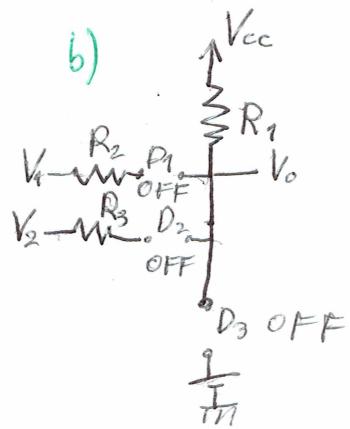
$$I_A = I_1$$

$$I_1 = \frac{V_{cc} - V_0}{R_1} = \frac{V_{cc} - 3}{10}$$

$$\frac{V_{cc} - 3}{10} = 4'894$$

$$V_{cc} = 51'94 \text{ V}$$

b)



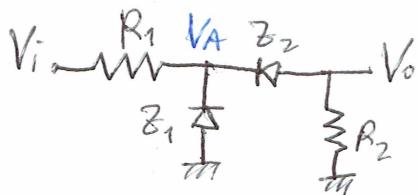
$$V_o = 10V$$

$$V_1 = V_2 = 25V$$

$$\boxed{V_{cc} = V_o = 10V}$$

$$10V \leq V_{cc} \leq 51'94V$$

(55)



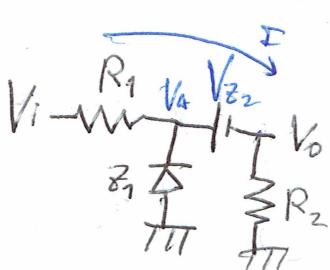
$$R_1 = 500\Omega$$

$$R_2 = 1k\Omega$$

$$V_i = 10V$$

$$V_{z1} = 12V$$

$$V_{z2} = 5V$$

Sup. Z_1, Z_2 OFF \Rightarrow 

$$V_A = V_i \quad \left. \begin{array}{l} \\ \end{array} \right\} Z_2 \text{ röto.}$$

$$I = \frac{10 - 3'33 - 5}{0'5} = 3'33 \text{ mA}$$

$$\frac{V_i - V_o - V_{z2}}{R_1} = \frac{V_o}{R_2}$$

$$\boxed{I_{z1} = 0 \text{ mA}}$$

$$\boxed{I_{z2} = 3'33 \text{ mA}}$$

$$\frac{10 - 5 - V_o}{0'5} = \frac{V_o}{1} \Rightarrow 10 - 2V_o = V_o$$

$$\boxed{V_o = 3'33V}$$

(56) Z_2 röto, sup. Z_1 OFF

$$\frac{V_i - V_o - V_{z2}}{R_1} = \frac{V_o}{R_2} \Rightarrow \frac{15 - V_o}{0'5} = V_o \Rightarrow 30 - 2V_o = V_o \Rightarrow V_o = 10V$$

$$V_A = V_o + V_{z2} = 15V > 12 = V_{z1} \text{ Absurdo. } Z_1 \text{ röto.}$$

$$V_o = V_{z1} - V_{z2} = 12 - 5 = \boxed{7V}$$

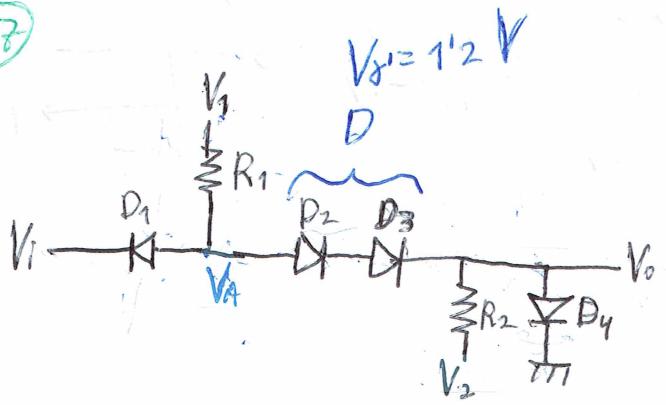
$$I = I_{z1} + I_{z2}$$

$$I = \frac{V_i - V_{z1}}{R_1} = \frac{20 - 12}{0'5} = 16 \text{ mA}$$

$$I_{z2} = \frac{V_o}{R_2} = \boxed{7 \text{ mA}}$$

$$I_{z1} = I - I_{z2} = \boxed{9 \text{ mA}}$$

(57)



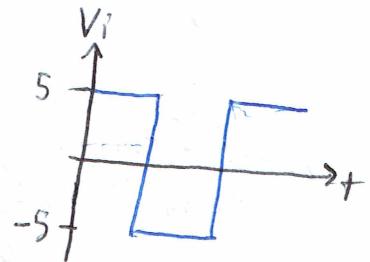
$$R_1 = 2 \text{ k}\Omega$$

$$R_2 = 3 \text{ k}\Omega$$

$$V_z = 0.6 \text{ V}$$

$$V_1 = 9 \text{ V}$$

$$V_2 = -1 \text{ V}$$



$$\underline{V_i = 5 \text{ V}}:$$

Sup. D ON, D₁ OFF, D₄ OFF

$$\frac{V_i - V_o - 1.2}{R_1} = \frac{V_o - V_2}{R_2} \Rightarrow \frac{9 - 1.2 - V_o}{2} = \frac{V_o + 1}{3}$$

$$3(7.8 - V_o) = 2V_o + 2$$

$$21.4 = 5V_o \Rightarrow V_o = 4.28 \text{ V}$$

Absurdo

D₄ ON.

$$V_o + 1.2 = 7.8 < V_i \text{ Suposición correcta.}$$

$$\underline{V_i = -5 \text{ V}}:$$

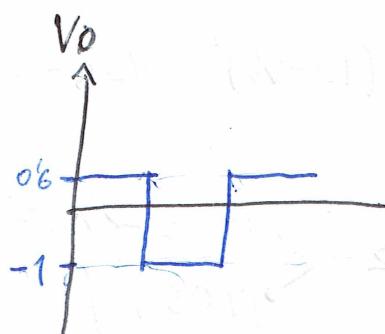
D₁ conduce, D₂, D₃, D₄ OFF

$$I_f = \frac{V_i - (5 + V_z)}{2} = 6.7 \text{ mA}$$

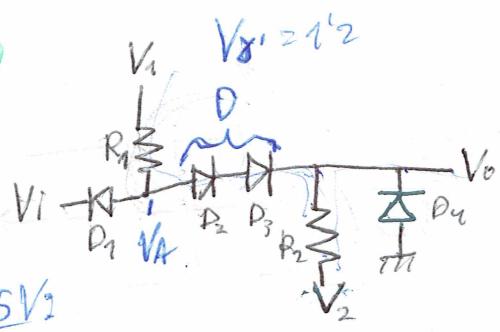
$$V_A = -5 + V_z = -4.4 \text{ V}$$

$$\boxed{V_o = -1 \text{ V}}$$

V_o > V_A \Rightarrow Suposición correcta



(58)



$$V_1 = 5V_2$$

Sup. D_1 OFF, D_3 ON, D_4 OFF

$$\frac{V_1 - V_o - 1.2}{R_1} = \frac{V_o - V_2}{R_2} \Rightarrow \frac{7.8 - V_o}{2} = \frac{V_o + 1}{3} \Rightarrow 21.4 = 5V_o \Rightarrow V_o = 4.28V$$

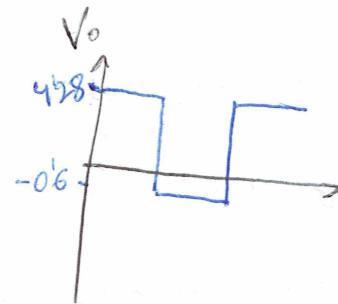
$$V_o + 1.2 = 5.48V < 5.6 \quad \left. \begin{array}{l} D_1 \text{ OFF} \\ 4.28 > 0.6 \Rightarrow D_2 \text{ OFF} \end{array} \right\}$$

Suposición correcta.

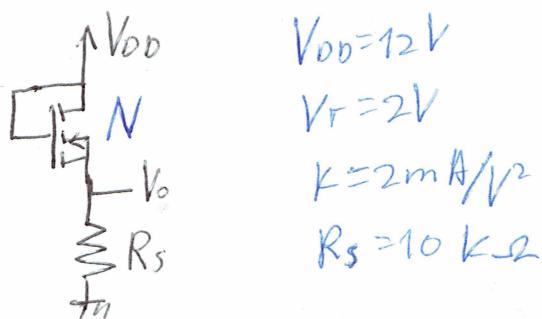
$$V_1 = -5V_2 \quad D_1 \text{ ON}, \quad D \text{ OFF}, \quad D_4 \text{ ON}$$

$$V_o = -0.6V = V_2$$

$$V_A = V_1 + V_2 = -4.4V < V_o \Rightarrow D \text{ OFF}$$



(59)



N MOSFET SAT:

$$I = \frac{k}{2} (V_{GS} - V_T)^2 = (12 - V_o - 2)^2$$

$$I = \frac{V_o}{R_S}$$

$$V_o = 1000 - 200V_o + 10V_o^2$$

$$0 = 1000 - 201V_o + 10V_o^2$$

$$\frac{V_o}{10} = (10 - V_o)^2 = 100 - 200V_o + V_o^2$$

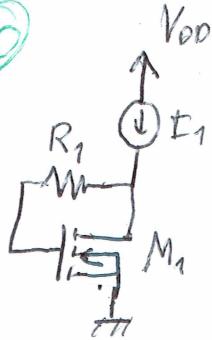
$$V_o = \frac{209 \pm \sqrt{209^2 - 4 \cdot 10000}}{20} = \frac{201 \pm 20.025}{20} \rightarrow 11.05 \Rightarrow V_{GS} = 0.95 < 2 = V_T$$

Absurdo.

$$I = \frac{9.05}{10} = 0.905 \text{ mA}$$

$$V_{DS} = V_{DD} - V_o = 2.95V$$

(60)



$$V_{D0} = 10V$$

$$R_1 = 100k\Omega$$

$$I_1 = 0.2mA$$

$$K = 0.1 mA/V^2$$

$$V_D < 5V$$

M_1 sat.

$$0.2 = \frac{0.1}{2} (V_G - V_T)^2$$

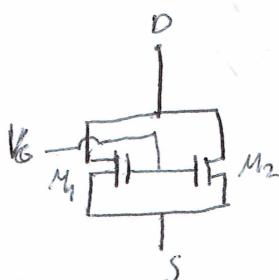
$$4 = (V_G - V_T)^2$$

$$2 = V_G - V_T \quad V_D = V_G$$

$$V_D = 2 + V_T \Rightarrow V_T < 3V$$

(61)

Meq.



$$K_1 = K_2 = 2 mA/V^2$$

$$V_{T1} = 1V$$

$$V_{GS1} = V_{GS2}$$

$$V_{T2} = 2V$$

$$S_1 \quad V_{T1} = V_{T2}$$

$$I_{eq} = I_1 + I_2$$

$$\frac{k}{2} (V_{GS} - V_T)^2 = \frac{k_1}{2} (V_{GS} - V_T)^2 + \frac{k_2}{2} (V_{GS} - V_T)^2$$

$$\frac{k}{2} = \frac{k_1}{2} + \frac{k_2}{2} \Rightarrow K = 4 mA/V^2$$

a) $V_{GS} = 1V \Rightarrow$ Circula intensidad $\Rightarrow V_{eq} = 1V$

b) $V_{GS} = 3V$

$$I_{D, \text{sat}} = I_{D, \text{lin}} \Rightarrow \frac{k}{2} (V_{GS} - V_T)^2 = \frac{k}{2} [2(V_{GS} - V_T)V_{GS} - V_{GS}^2]$$

$$(3-1)^2 = 2 \cdot 2 V_{GS} - V_{GS}^2$$

$$4 = 4V_{GS} - V_{GS}^2$$

$$V_{GS, \text{sat}} = 2V$$

c) $I_D(V_{GS})$ M_1, M_2 sat.

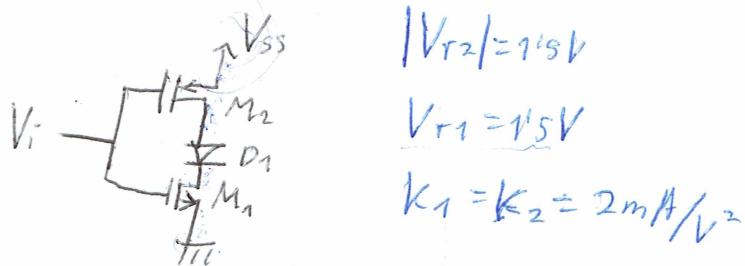
$$I = I_1 + I_2$$

$$I = \frac{k_1}{2} (V_{GS} - V_{T1})^2 + \frac{k_2}{2} (V_{GS} - V_{T2})^2$$

$$I = \frac{3}{2} (V_{GS} - 1)^2 + \frac{2}{2} (V_{GS} - 2)^2 = V_{GS}^2 - 2V_{GS} + 1 + V_{GS}^2 - 4V_{GS} + 4$$

$$\boxed{I = 2V_{GS}^2 - 6V_{GS} + 5 \quad \text{mA}}$$

⑥2



$$|V_{r2}| = 1.5V$$

$$V_{r1} = 1.5V$$

$$k_1 = k_2 = 2mA/V^2$$

$$V_{ss} = 10V$$

$$V_d = 2V$$

D_1 ON Supongo M_1, M_2 lin.

$$V_{D2} - V_{D1} = 2V$$

$$M_2: |V_{GS}|/2, V_{ss} - V_d \Rightarrow V_{ss} - V_i > 1.5V$$

$$|V_{GS2}| = V_{ss} - V_{D2} < V_{ss} - V_i - (V_{r2})$$

$$V_{D2} > V_i + 1.5 \quad \text{Lin.}$$

$$M_1: V_{GS} = V_i \Rightarrow V_i > 1.5V \quad \text{ON}$$

$$V_{D1} < V_i - 1.5 \quad \text{Lin.}$$

$$\left. \begin{aligned} V_i &< V_{D2} - 1.5 \\ V_i &> V_{D1} + 1.5 \end{aligned} \right\} \Rightarrow V_{D2} = 2 + V_{D1}$$

$$V_i < 2 + V_{D1} - V_s \quad \text{Contradiccion}$$

$$V_i < V_{D1} + 0.5$$

(63)

M₁, M₂ sat.D₁ ON

$$V_{D2} - V_{D1} = 2V$$

$$|V_{DS2}| = V_{SS} - V_{D2} > V_{SS} - V_i = |V_{T2}| = |V_{GS1}| - |V_{T2}|$$

$$V_{D2} < V_i + 1.5$$

$$V_{GS} - V_T = V_i - 1.5 < V_{D1}$$

$$V_{D1} + 2 = V_{D2}$$

$$V_i < V_{D1} + 1.5$$

$$V_{D1} + 2 < V_i + 1.5$$

$$\left. \begin{array}{l} V_{D1} + 0.5 < V_i \\ \end{array} \right\}$$

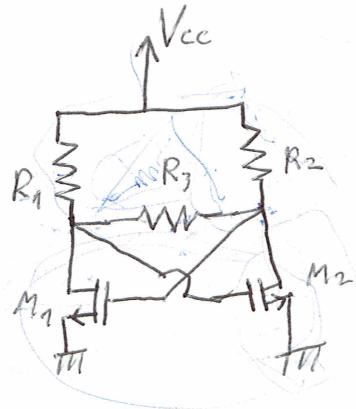
$$I_{m1} = I_{m2}$$

$$\frac{k_1}{2} (V_i - 1.5)^2 = \frac{k_2}{2} (V_{SS} - V_i - 1.5)^2 \quad k_1 = k_2$$

$$V_i - 1.5 = 10 - V_{SS} - V_i$$

$$\boxed{V_i = 5V}$$

(64)



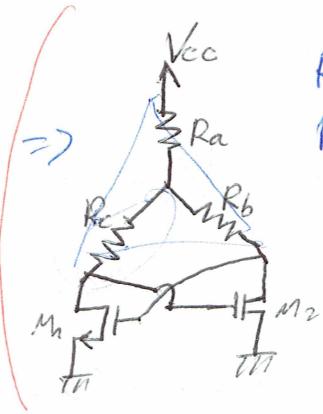
$$R_1 = R_2 = 0.5 \text{ k}\Omega$$

$$R_3 = 1 \text{ k}\Omega$$

$$V_{T1} = V_{T2} = 1 \text{ V}$$

$$k_1 = k_2 = 2 \text{ mA/V}^2$$

$$V_{cc} = 5 \text{ V}$$



$$Ra = 0.425 \text{ k}\Omega$$

$$Rb = 0.25 \text{ k}\Omega$$

$$Rc = 0.125 \text{ k}\Omega$$

$$V_{GS2} = V_{DS1}$$

$$V_{DS2} = V_{GS1}$$

M_1, M_2 sat.

$$V_{GS2} + V_T < V_{DS2} \Rightarrow V_{GS2} - 1 < V_{GS1}$$

$$V_{GS1} - V_T < V_{DS1} \Rightarrow V_{GS1} - 1 < V_{GS2}$$

$$V_{GS1} + 1 > V_{GS2} > V_{GS1} - 1$$

$$I = \frac{k}{2} (V_{GS} - V_T)^2$$

$$I = \frac{V_{cc} - V_{GS}}{0.5}$$

$$V_{DS} = V_{GS} = V$$

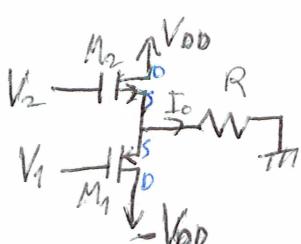
$$\frac{5-V}{0.5} = (V-1)^2$$

$$V_{GS1} = V_{GS2} = V_{DS1} = V_{DS2}$$

$$80 - 2V = V^2 - 2V + 1$$

$$0 = V^2 - 9 \Rightarrow V_{GS} = 3 \text{ V}$$

(65)



$$R = 1 \text{ k}\Omega$$

$$k_1 = k_2 = 2 \text{ mA/V}^2$$

$$|V_{T1}| = |V_{T2}| = 1 \text{ V}$$

$$I_2 = I_1 + I_o$$

$$M_1, M_2 \text{ sat.}$$

$$|V_{GS1}| - |V_T| < |V_{DS1}|$$

$$V_2 - I_o - V_T < V_{DS2}$$

$$\frac{k}{2} (V_2 - I_o - 1)^2 = \frac{k}{2} (I_o - V_1 - 1)^2 + I_o$$

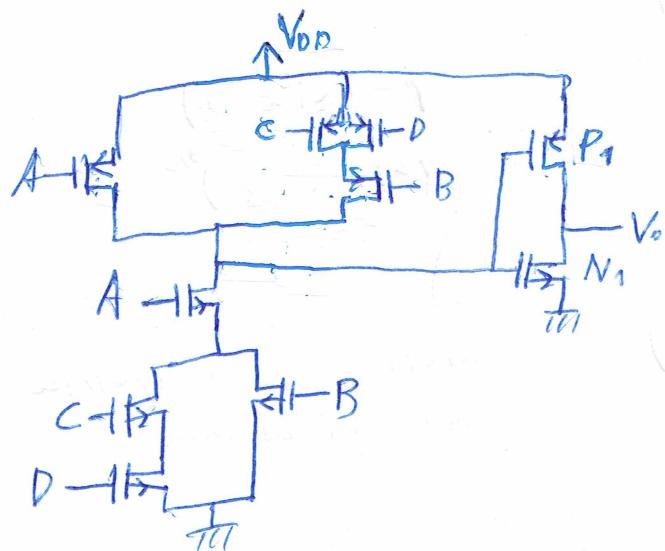
$$I_o = (V_2 - I_o - 1)^2 - (I_o - V_1 - 1)^2 = (V_2 - V_1 - 2)(V_2 + V_1 - 2I_o)$$

$$I_o = -2I_o(V_2 - V_1 - 2) + (V_2 + V_1)(V_2 - V_1 - 2)$$

$$I_o + 2I_o(V_2 - V_1 - 2) = (V_2 + V_1)(V_2 - V_1 - 2)$$

$$I_o (1 + 2(V_2 - V_1 - 2)) = (V_2 + V_1)(V_2 - V_1 - 2) \Rightarrow I_o = \frac{(V_2 + V_1)(V_2 - V_1 - 2)}{1 + 2(V_2 - V_1 - 2)}$$

⑥6) $Y = A(B + CD)$ CMOS



A	B	C	D
1	0	1	1

N_A: ON

N_B: OFF

P_A: OFF

P_B: ON

N_C: OFF

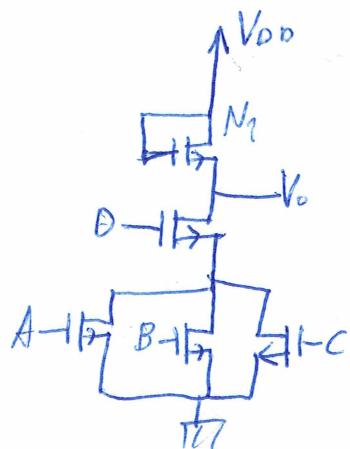
P_C: OFF

N_D: ON

P_D: OFF

$Y = 1$

⑥7) $Y = \overline{(A+B+C)} \cdot D$ NMOS



A	B	C	D
1	1	1	0

N_A: ON

N_B: ON

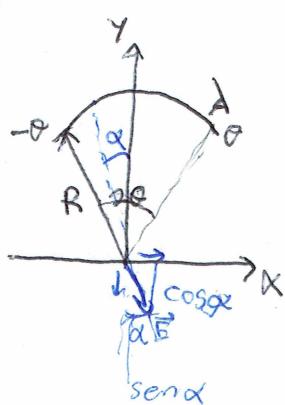
N_C: ON

N_D: OFF

N_D: SAT (ON)

$Y = 1$

⑥8)



$$E = \int_{-\theta}^{\theta} \frac{k \cdot dQ}{R^2} (\sin \alpha \vec{i} - \cos \alpha \vec{j})$$

$$dQ = \lambda \cdot d\vec{l} = \lambda \cdot R \cdot d\alpha$$

$$d\vec{l} = R \cdot d\alpha$$

$$E = \int_{-\theta}^{\theta} \frac{k \cdot \lambda \cdot R \cdot d\alpha}{R^2} (\sin \alpha \vec{i} - \cos \alpha \vec{j}) = \frac{1 \cdot \lambda}{4\pi \epsilon_0 R} \left[\int_{-\theta}^{\theta} \sin \alpha d\alpha \vec{i} - \int_{-\theta}^{\theta} \cos \alpha d\alpha \vec{j} \right]$$

$$\vec{E} = \frac{\lambda}{2\pi \epsilon_0 R} (-2 \sin \theta) \vec{j}$$

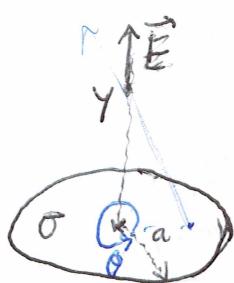
$$\vec{E} = -\frac{\lambda \sin \theta}{2\pi \epsilon_0 R} \vec{j}$$

$$\begin{aligned} & \left[-\cos \alpha \right]_{-\theta}^{\theta} \\ & -\cos \theta + \cos(-\theta) \\ & 2 \cdot \sin \theta \end{aligned}$$

$$\left[\sin \alpha \right]_{-\theta}^{\theta}$$

$$\sin \theta - \sin(-\theta)$$

(69)



$$\vec{E} = \int \frac{k \cdot \sigma \cdot ds}{r^3} \cdot \vec{r}$$

$$ds = dx \cdot x \cdot d\theta$$

$$\vec{r} = (x\hat{i} + y\hat{j})$$

$$r^3 = (x^2 + y^2)^{3/2}$$

$$\vec{E} = \int_0^a \int_0^{2\pi} \frac{k \cdot \sigma \cdot dx \cdot x \cdot d\theta}{(x^2 + y^2)^{3/2}} (x\hat{i} + y\hat{j})$$

Cada componente \hat{i} se anula por la simetría del problema.

$$\vec{E} = k \cdot \sigma \int_0^a \frac{x \cdot dx}{(x^2 + y^2)^{3/2}} \cdot \int_0^{2\pi} d\theta \cdot y\hat{j} = \frac{1 \cdot \sigma \cdot y}{2k\pi\epsilon_0} \cdot \frac{1}{2} \left[(x^2 + y^2)^{-1/2} \right]_0^a \cdot 2\pi \cdot \hat{j} =$$

$$= \frac{\sigma y}{\epsilon_0 \cdot 2} \left[\frac{1}{\sqrt{a^2 + y^2}} - \frac{1}{y} \right] = \boxed{\left[\frac{\sigma}{2\epsilon_0} \left[1 - \frac{y}{\sqrt{a^2 + y^2}} \right] \right] \hat{j}}$$

$$\lim_{a \rightarrow \infty} E = \frac{\sigma}{2\epsilon_0} \hat{j}$$