

Chapter 2: Exchange with production

Ch 32 in H. Varian 8th Ed.

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Inspired by [Michael D. Robinson](#), Mount Holyoke College

Exchange Economies (revisited)

So far...

- No production, only endowments, so no description of how resources are converted to consumables.
- General equilibrium: all markets clear simultaneously.
- 1st and 2nd Fundamental Theorems of Welfare Economics.

Now

- Add input markets, output markets, describe firms' technologies, the distributions of firms' outputs and profits ... **That's not easy!**

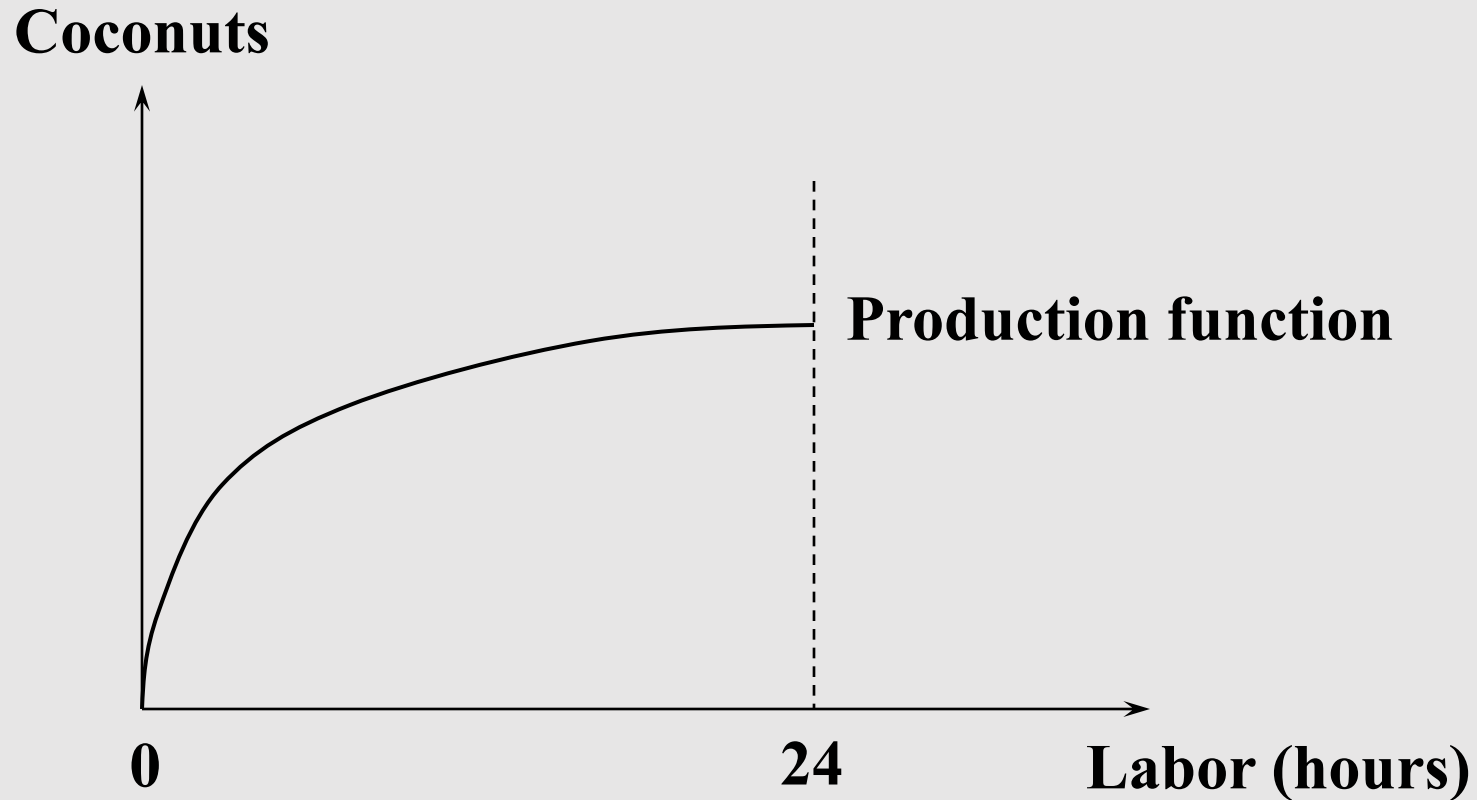
Robinson Crusoe's Economy

- One agent, RC.
- Endowed with a fixed quantity of one resource → 24 hours.
- Use time for labor (production) or leisure (consumption).
- Labor time = L . Leisure time = $24 - L$.
- What will RC choose?

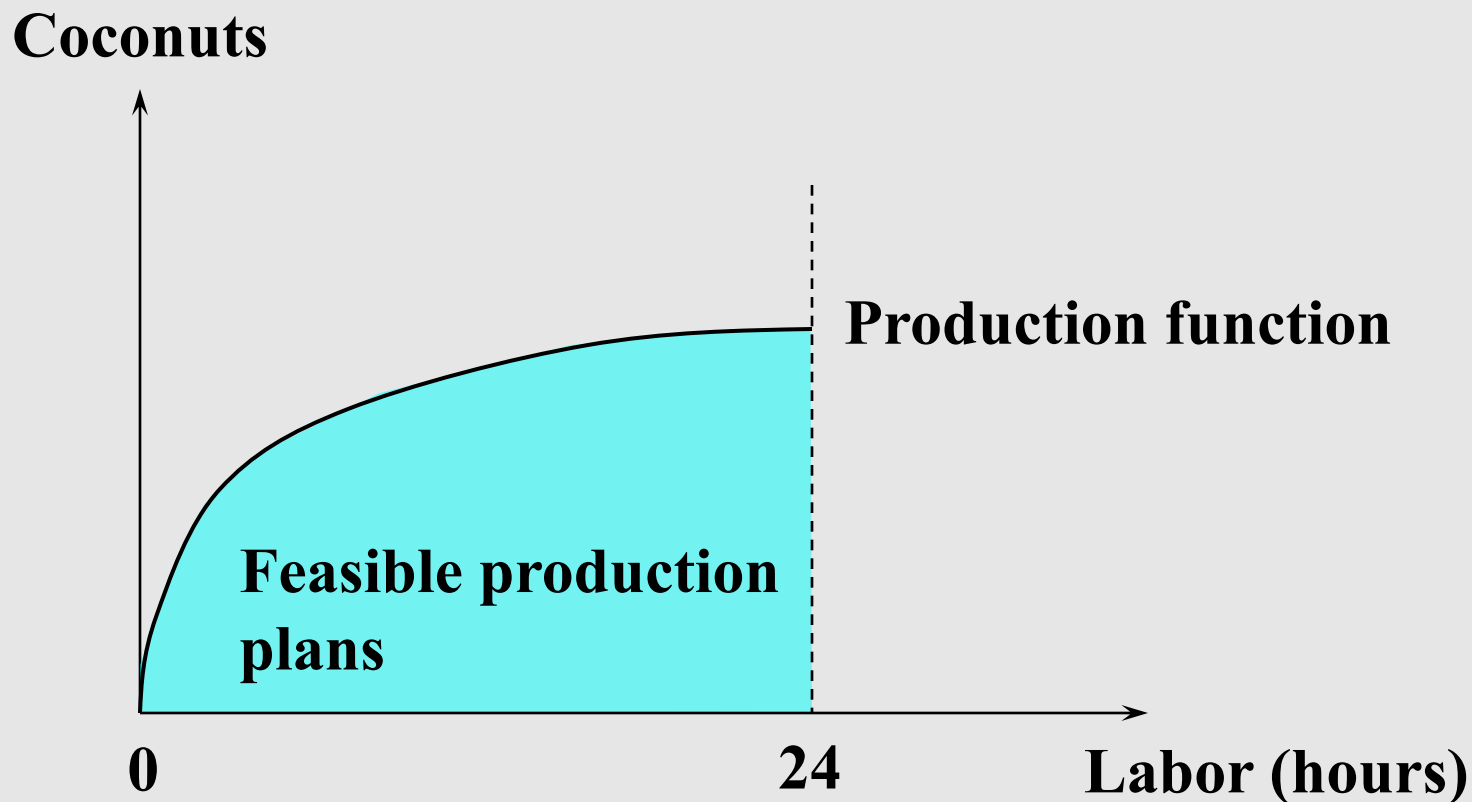
Robinson Crusoe's Technology

- Technology: Labor produces output (coconuts) according to a concave production function.

Robinson Crusoe's Technology



Robinson Crusoe's Technology

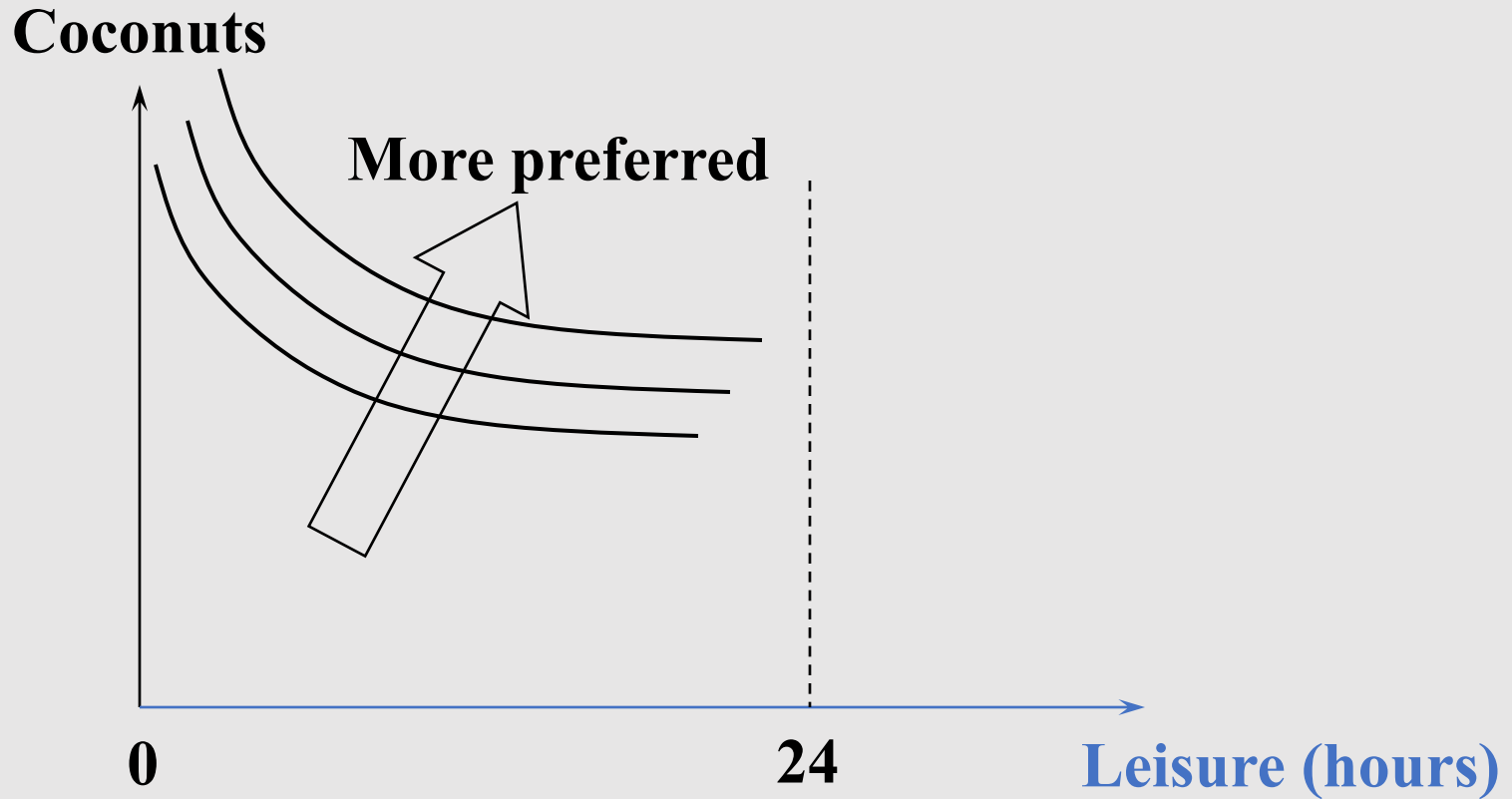


Robinson Crusoe's Preferences

→ RC's preferences:

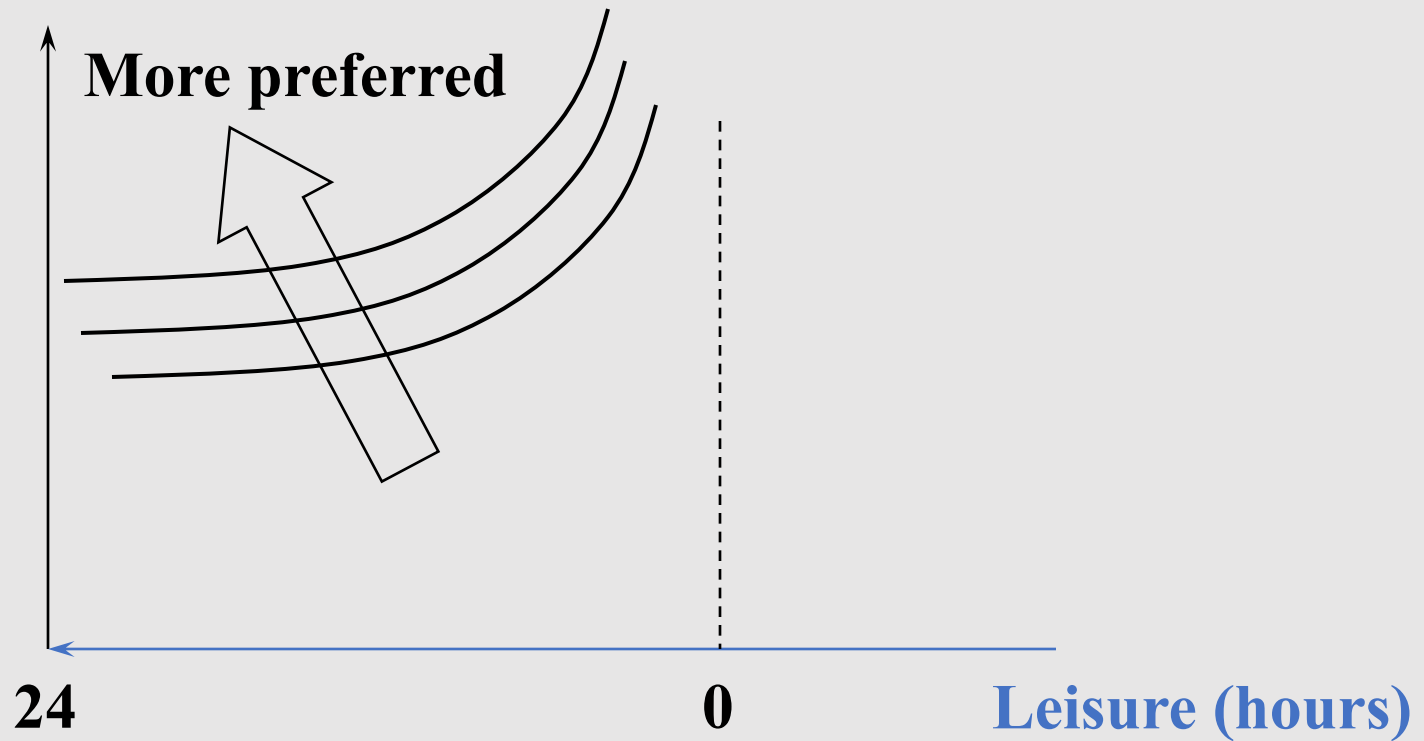
- coconut is a good
- leisure is a good

Robinson Crusoe's Preferences

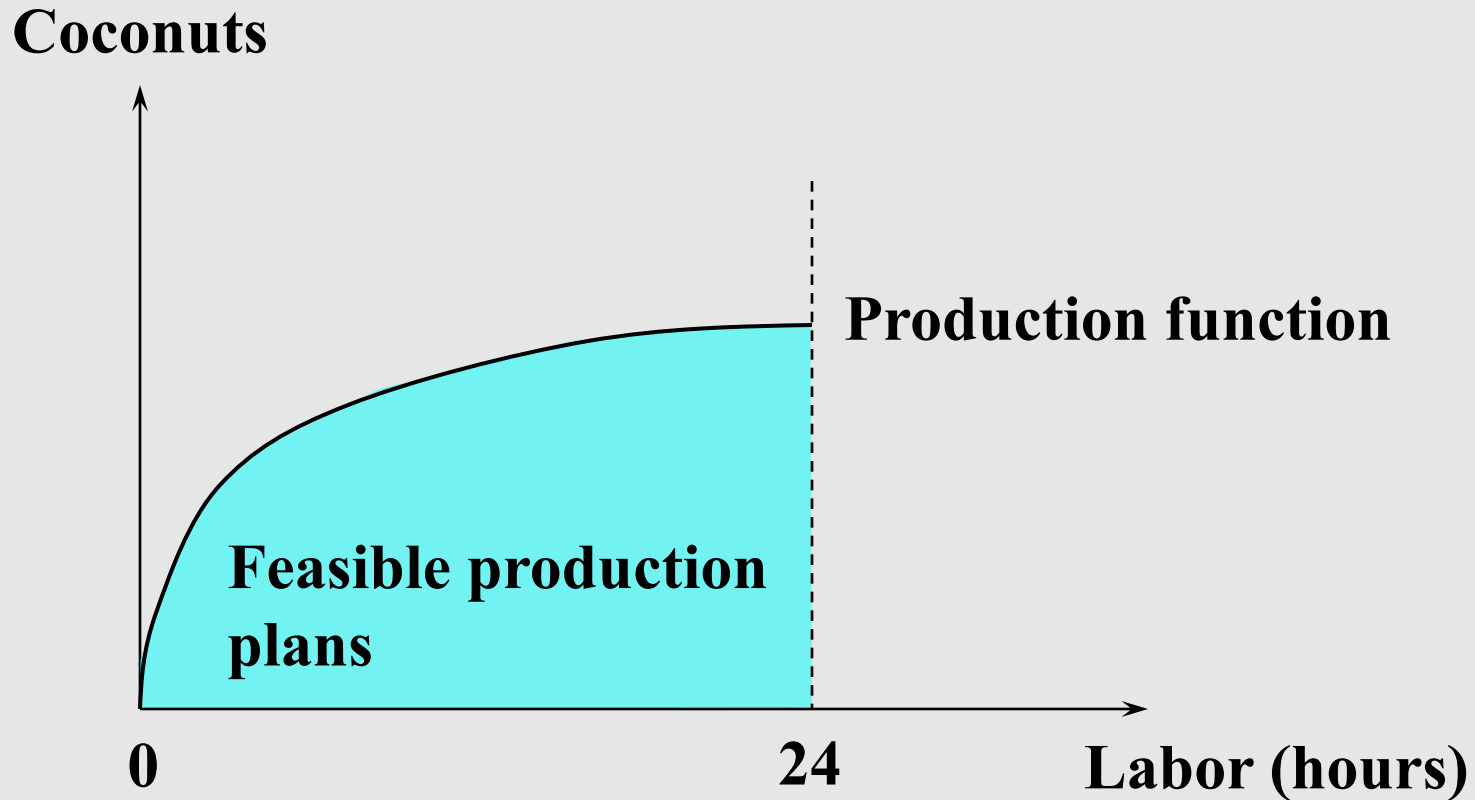


Robinson Crusoe's Preferences

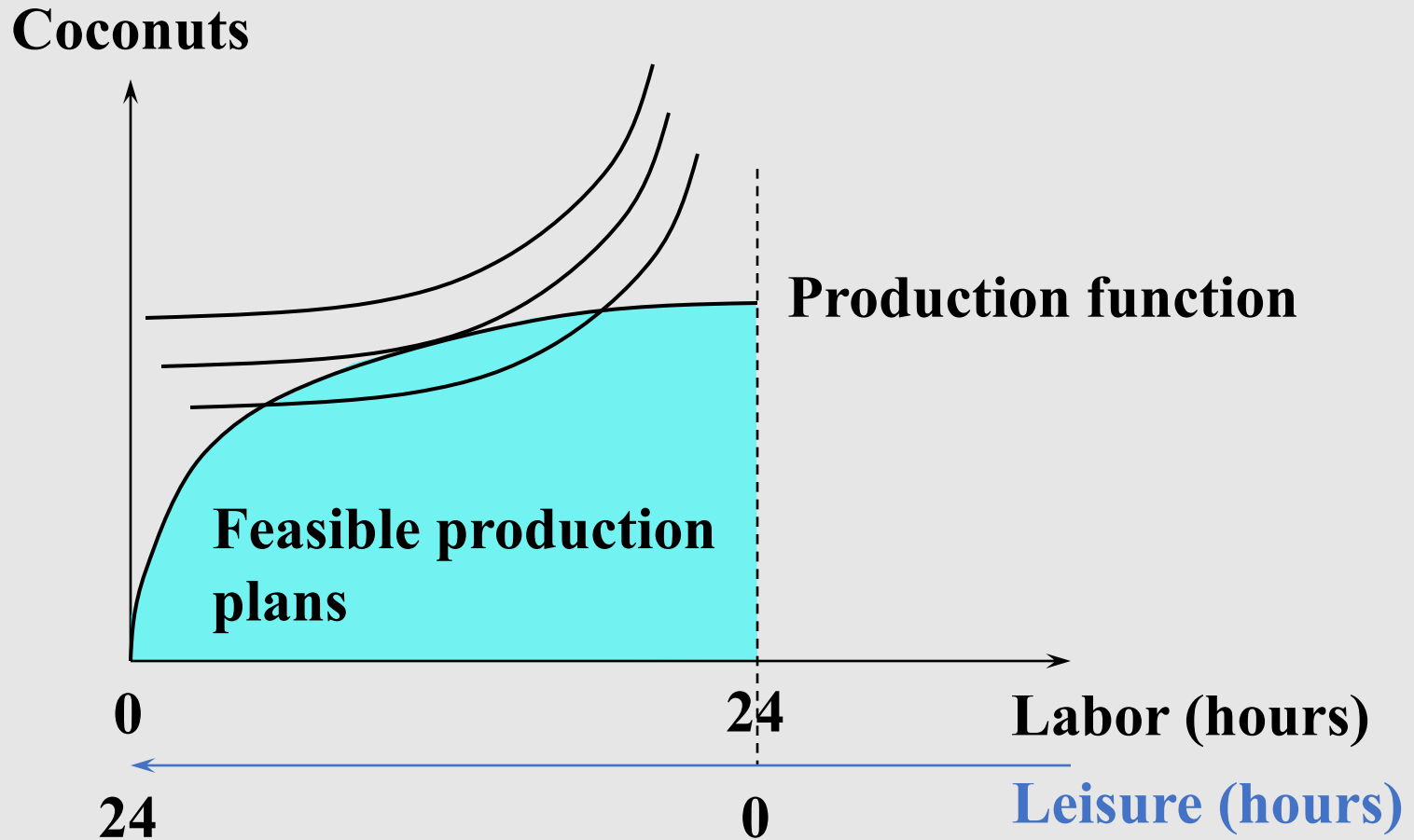
Coconuts



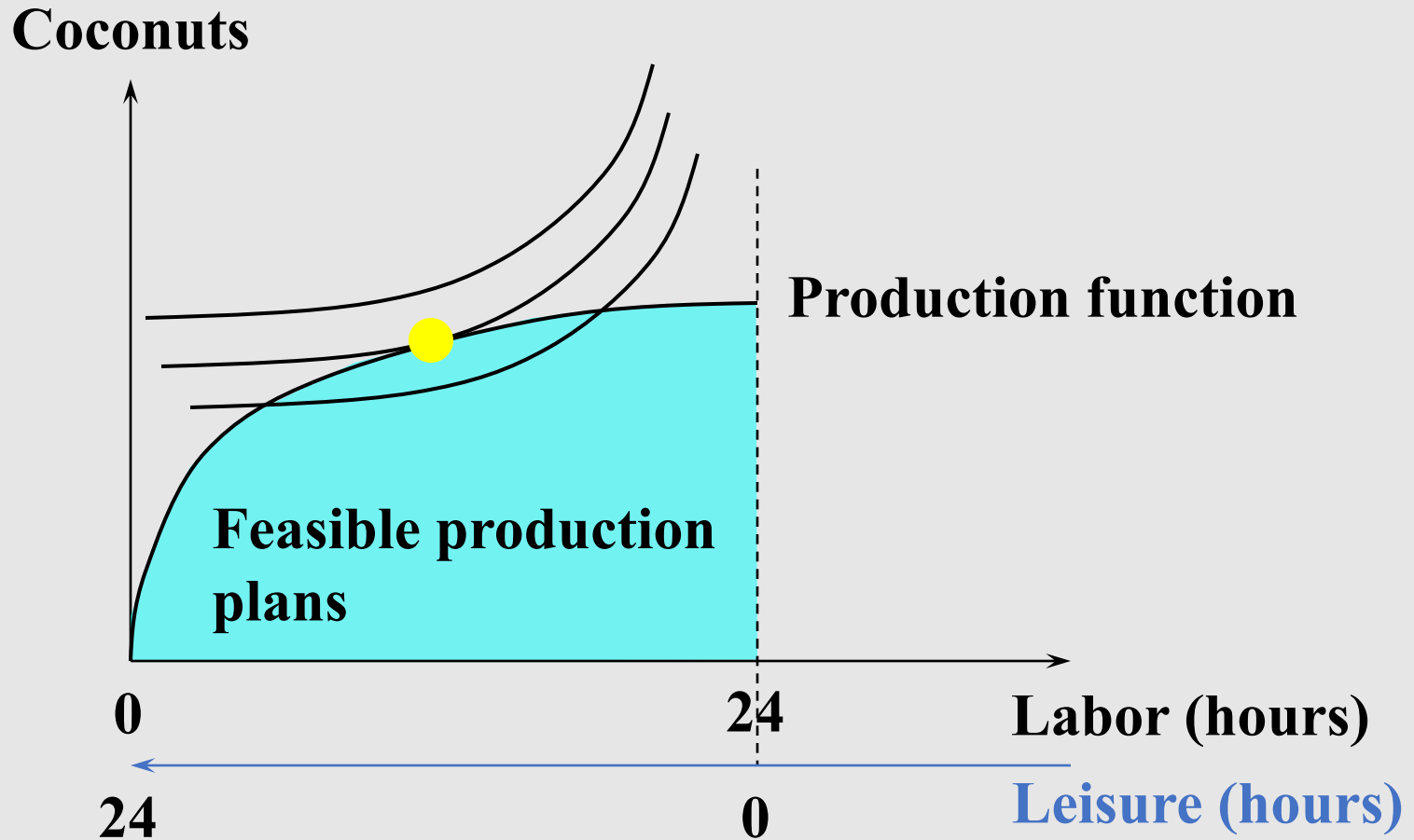
Robinson Crusoe's Choice



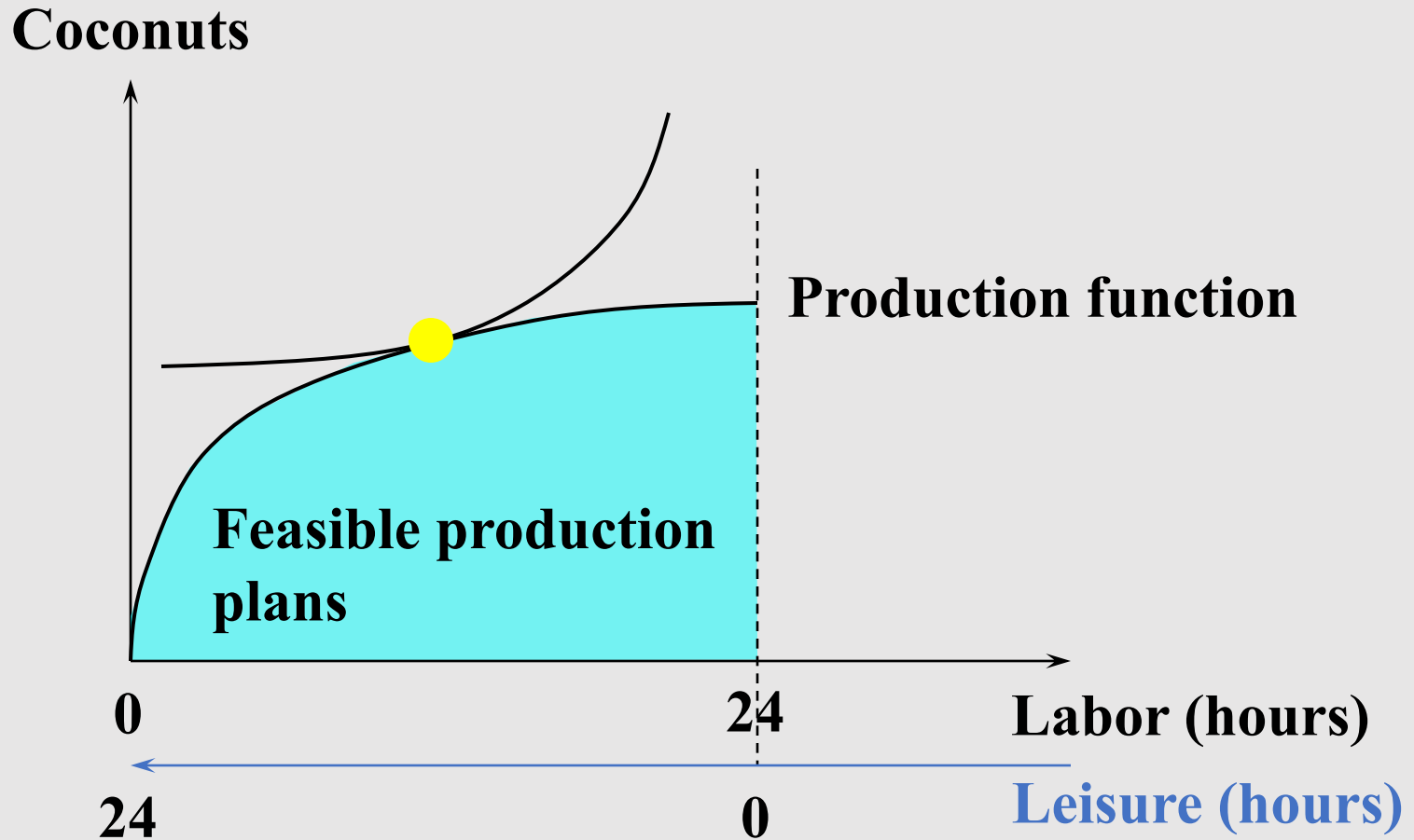
Robinson Crusoe's Choice



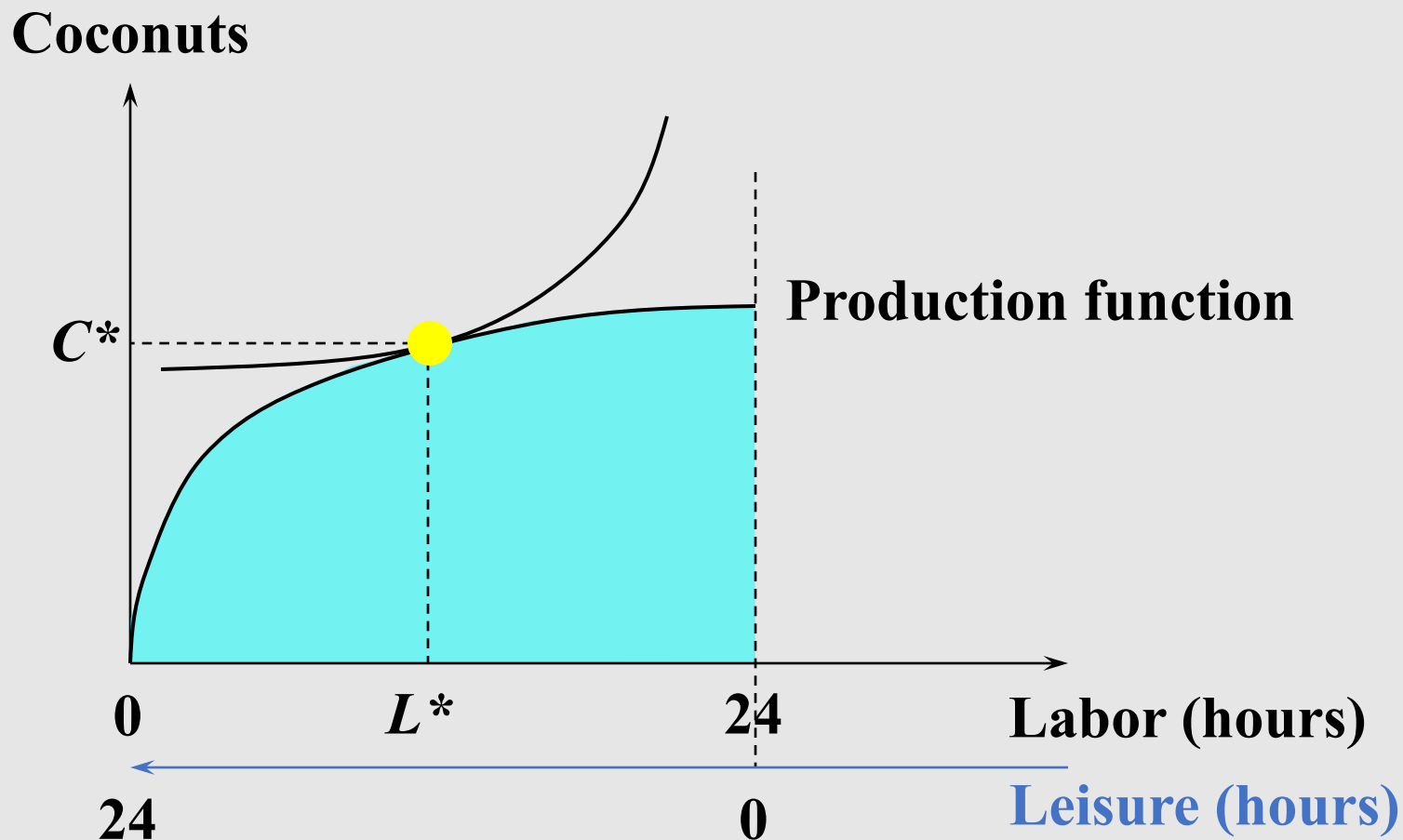
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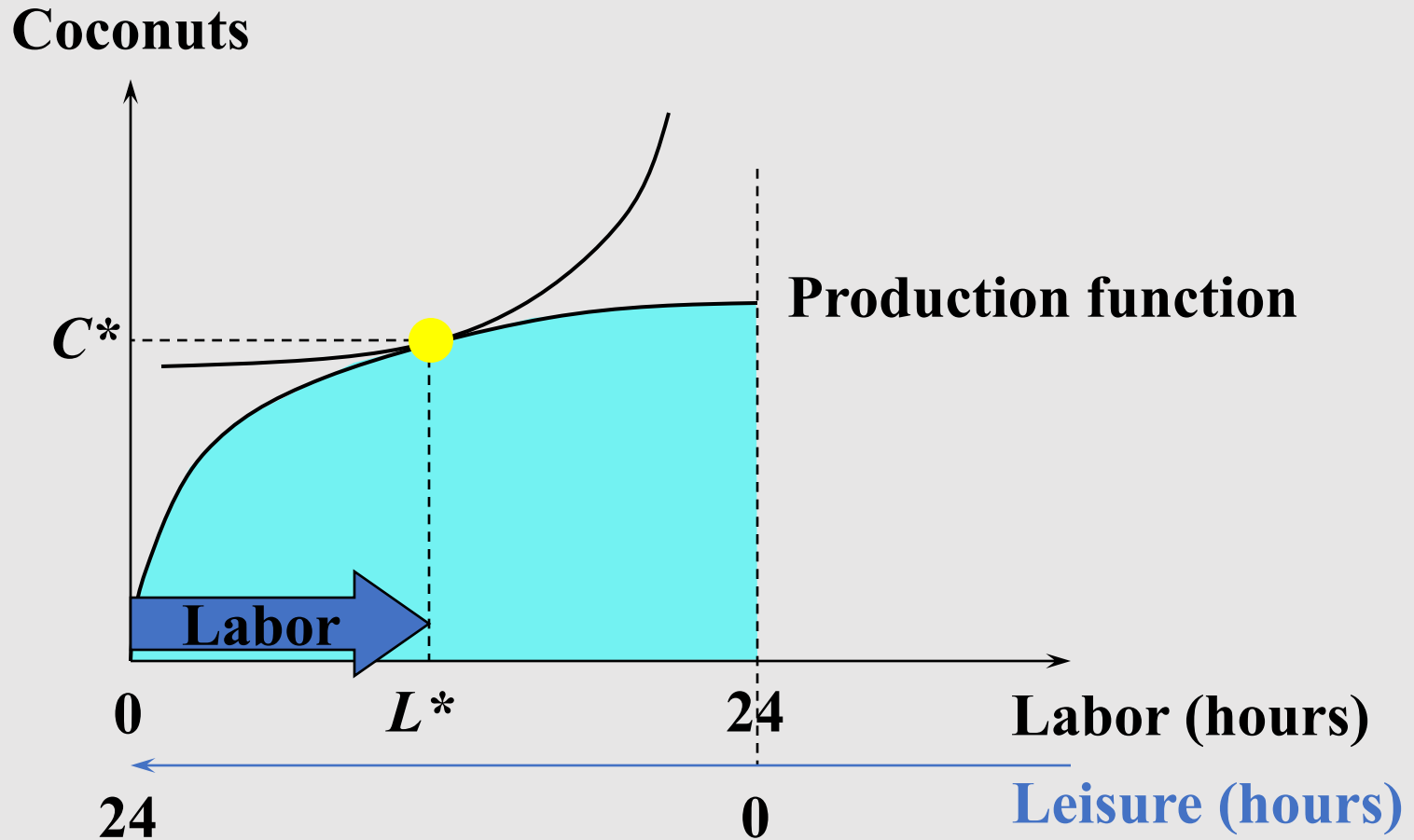
Robinson Crusoe's Choice



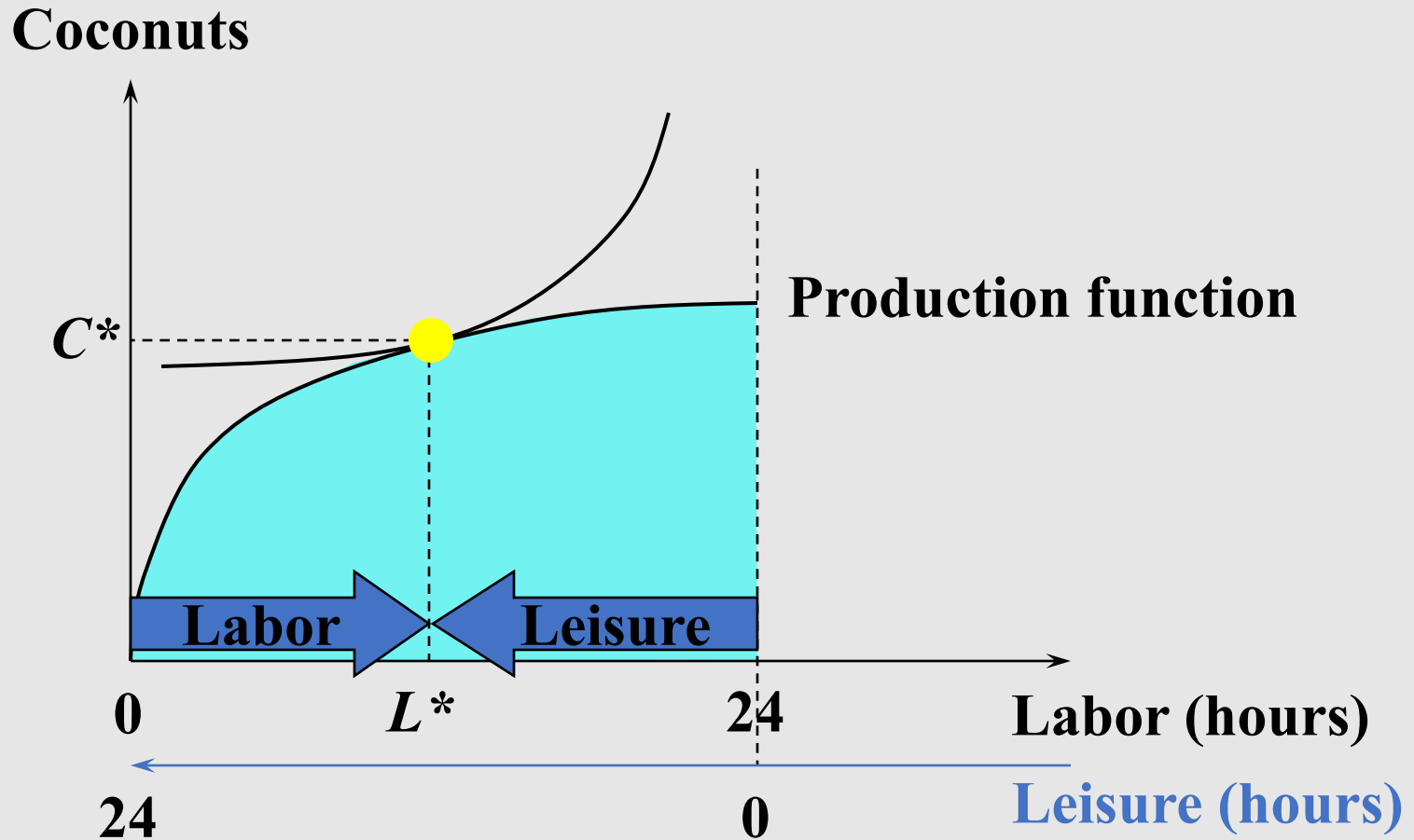
Robinson Crusoe's Choice



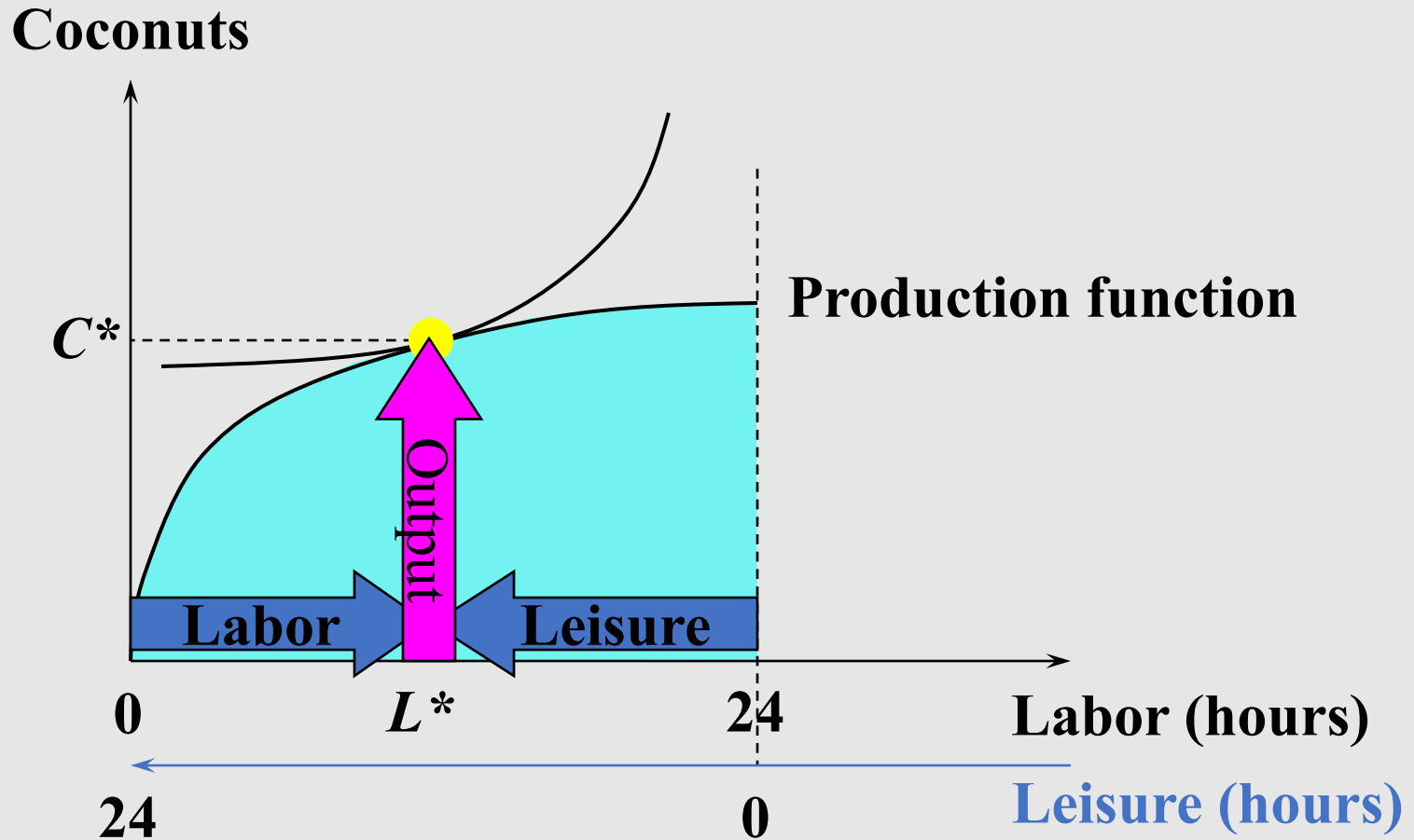
Robinson Crusoe's Choice



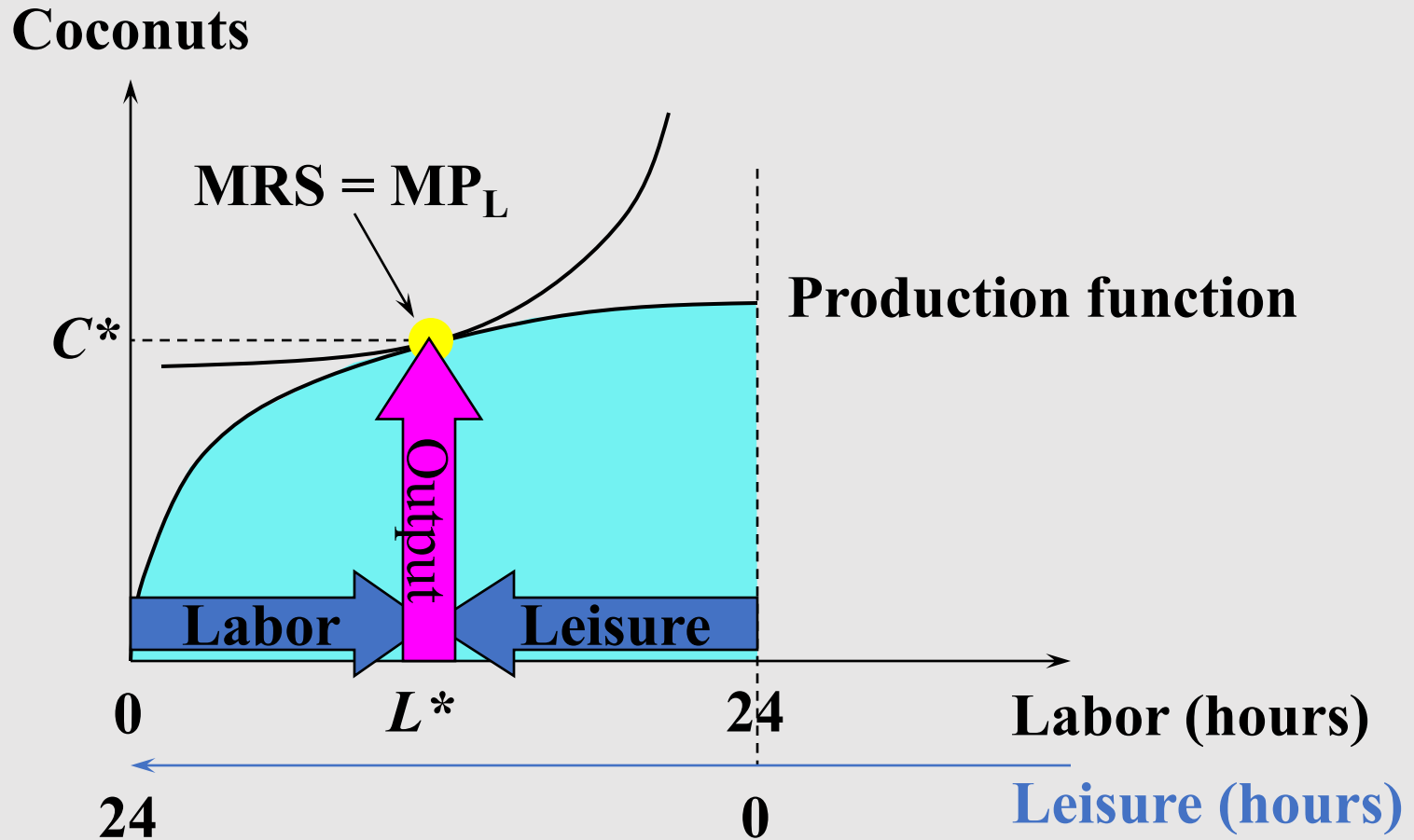
Robinson Crusoe's Choice



Robinson Crusoe's Choice



Robinson Crusoe's Choice



Robinson Crusoe as a Firm

- Now suppose RC is both a utility-maximizing consumer and a profit-maximizing firm.
- Use coconuts as the numeraire good; i.e. price of a coconut = \$1.
- RC's wage rate is w .
- Coconut output level is C .

Robinson Crusoe as a Firm

→ RC's firm's profit is $\pi = C - wL$.

→ $\pi = C - wL \Leftrightarrow C = \pi + wL$, the equation of an isoprofit line.

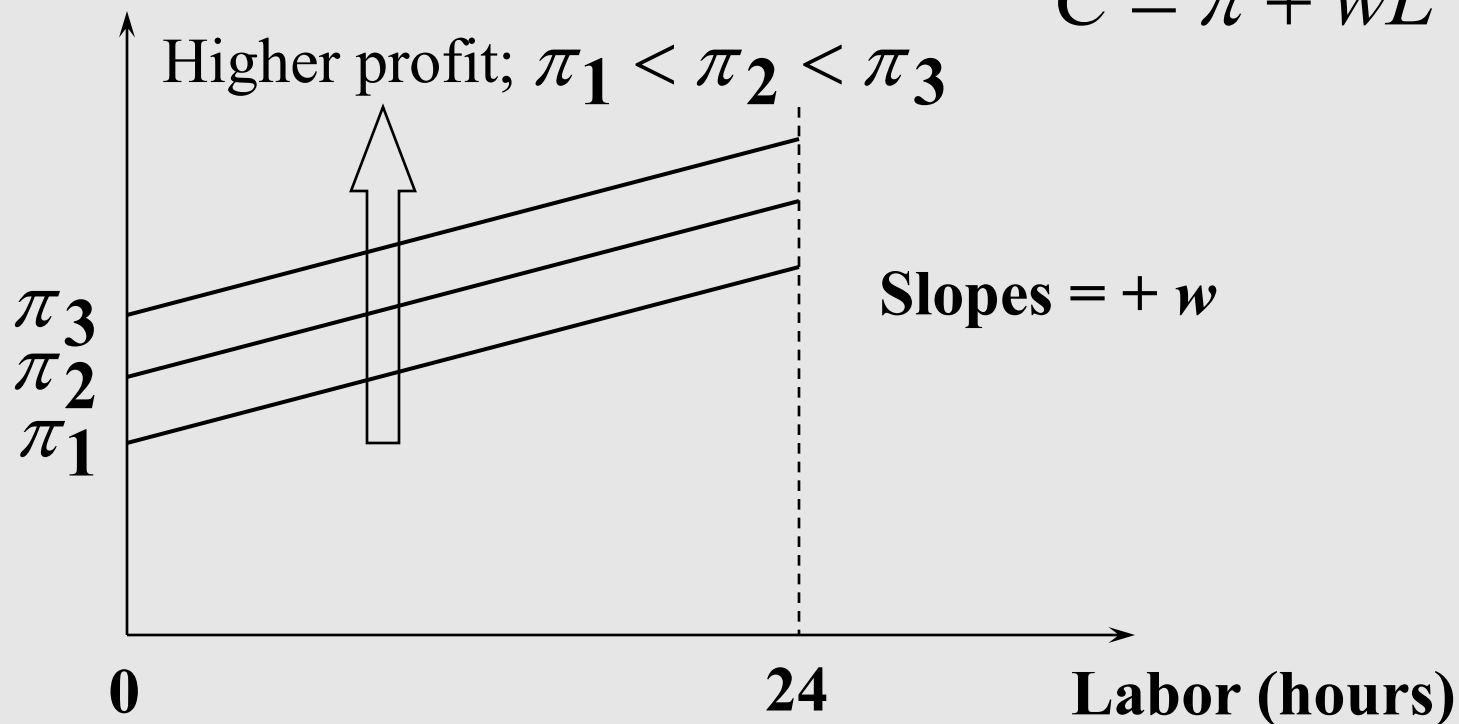
→ Slope = $+ w$.

→ Intercept = π .

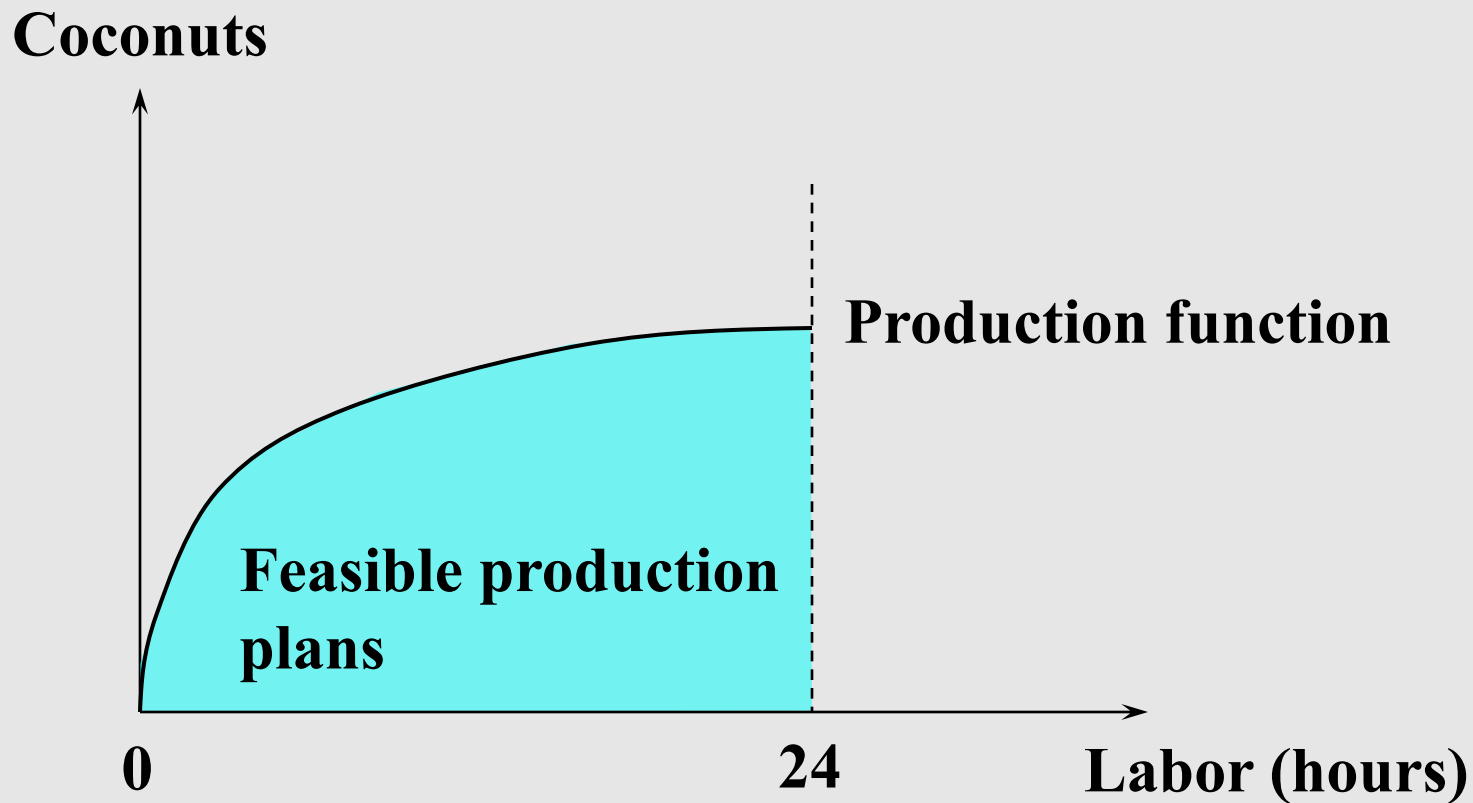
Isoprofit Lines

Coconuts

$$C = \pi + wL$$

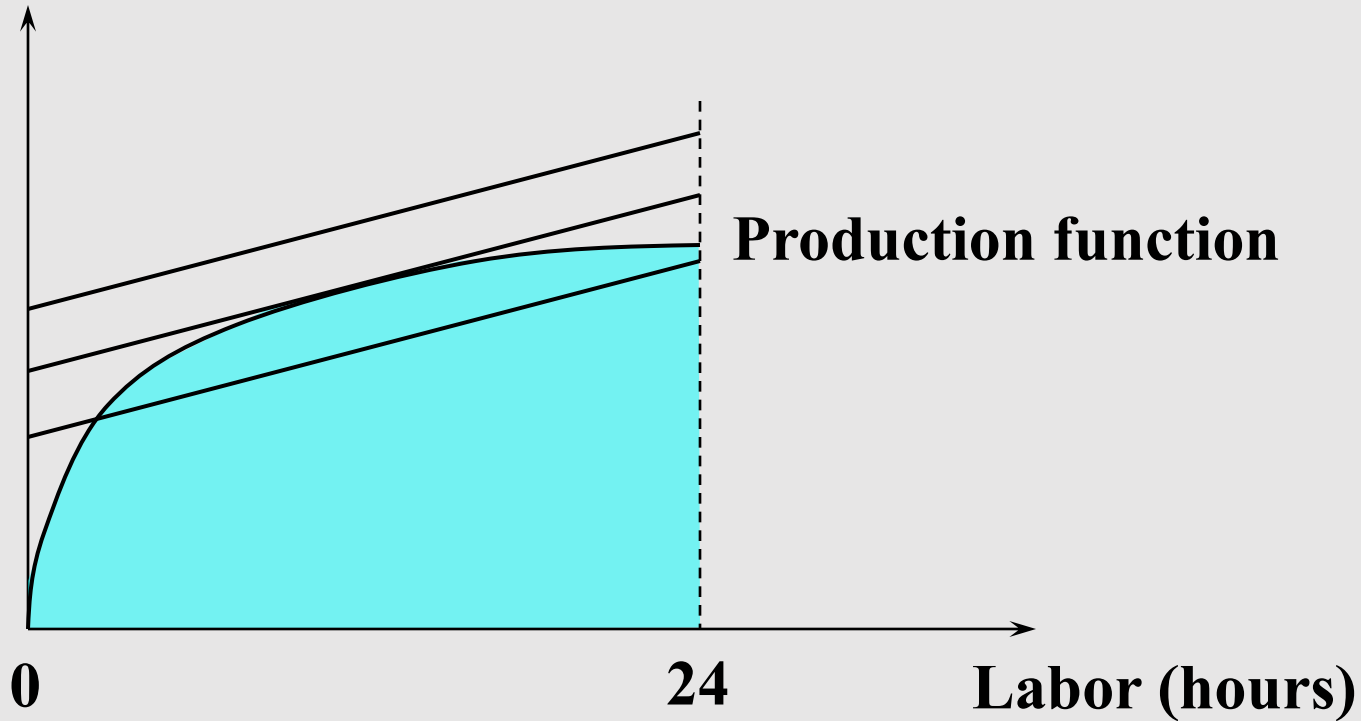


Profit-Maximization



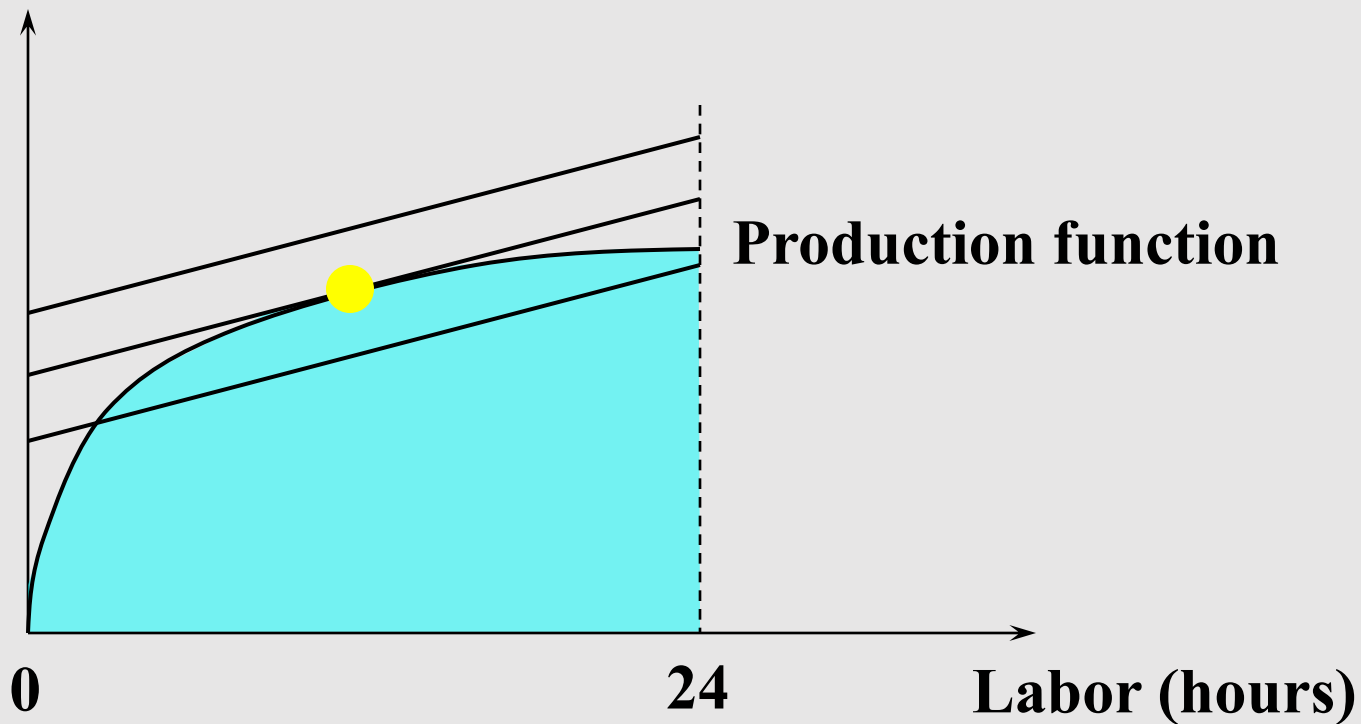
Profit-Maximization

Coconuts

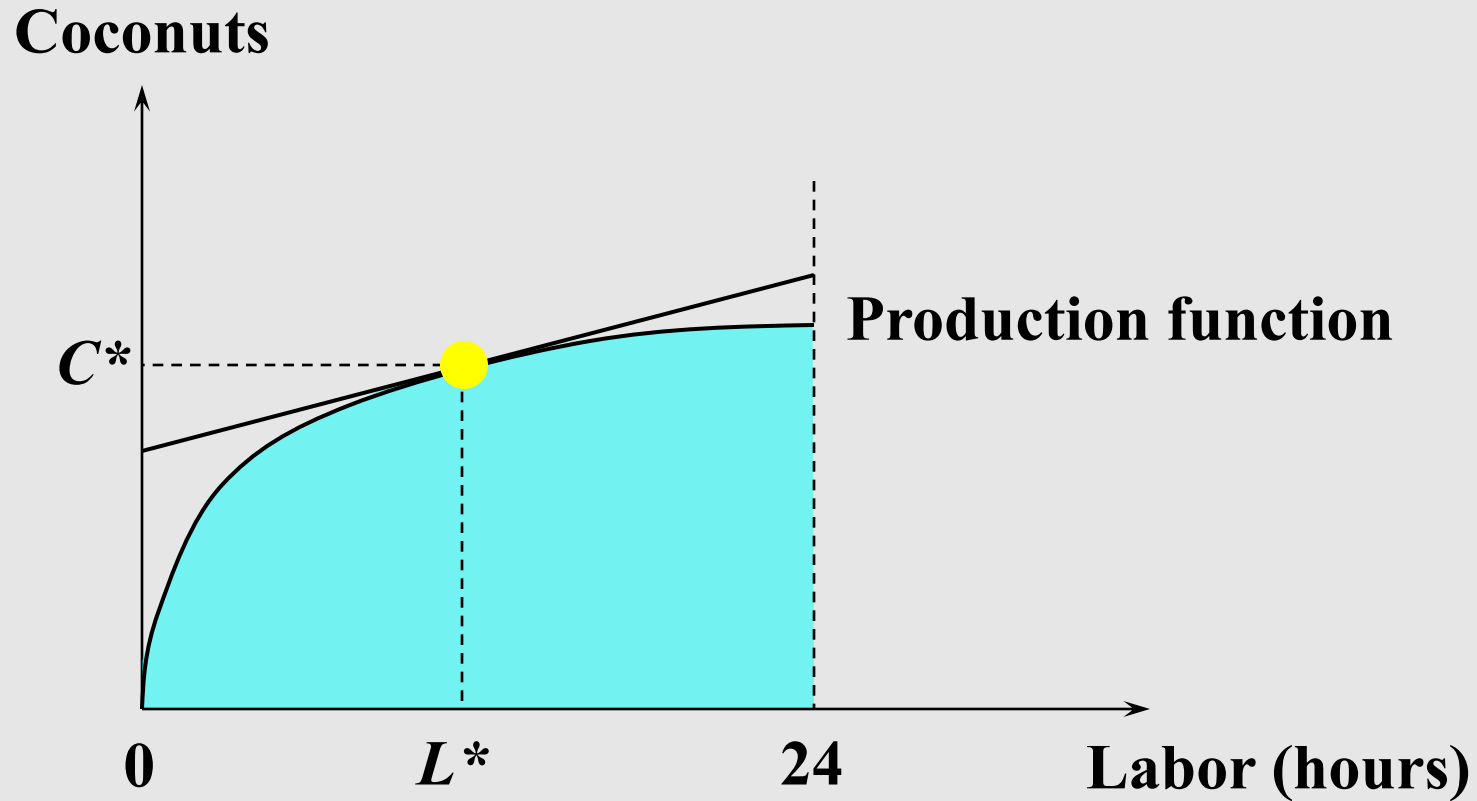


Profit-Maximization

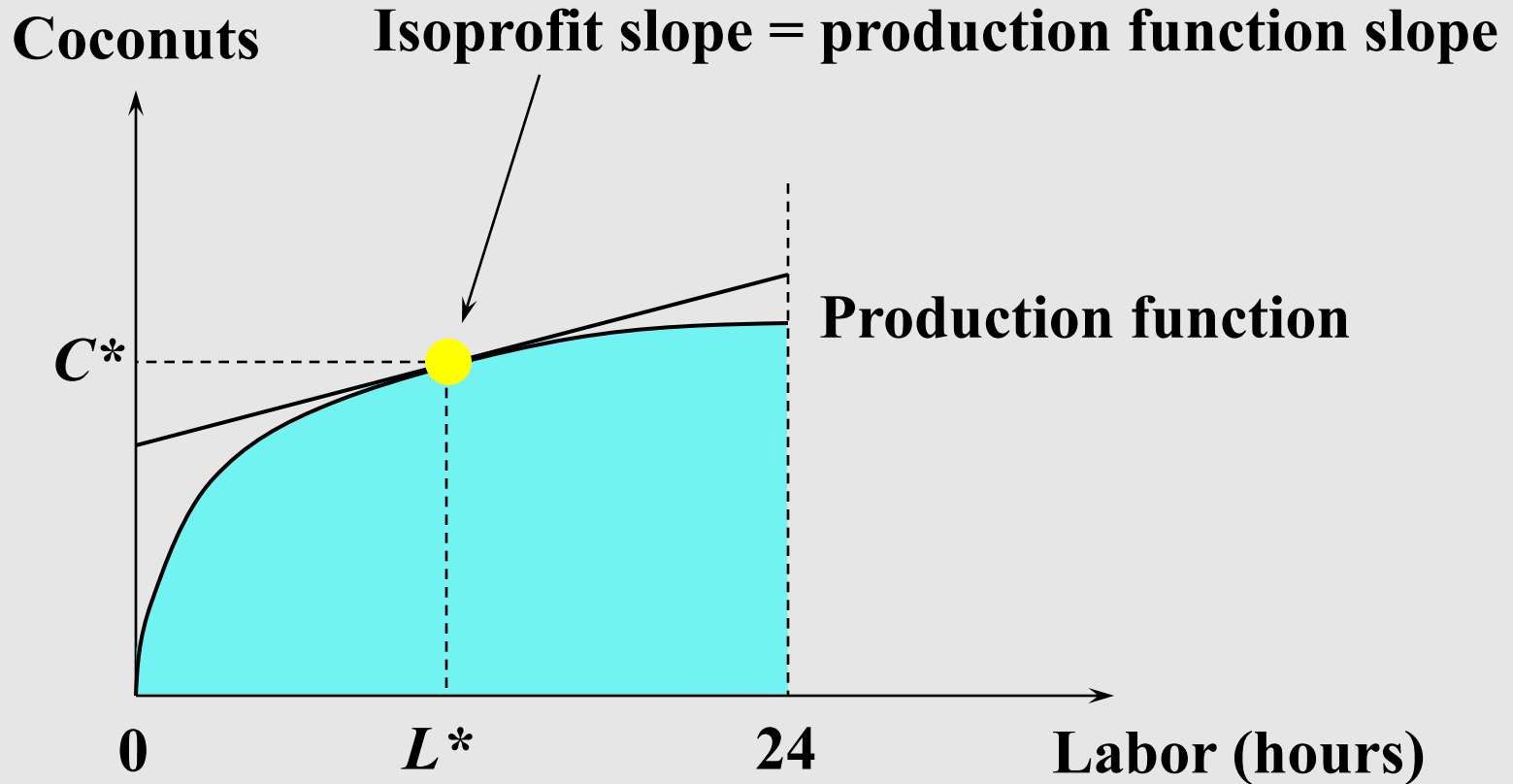
Coconuts



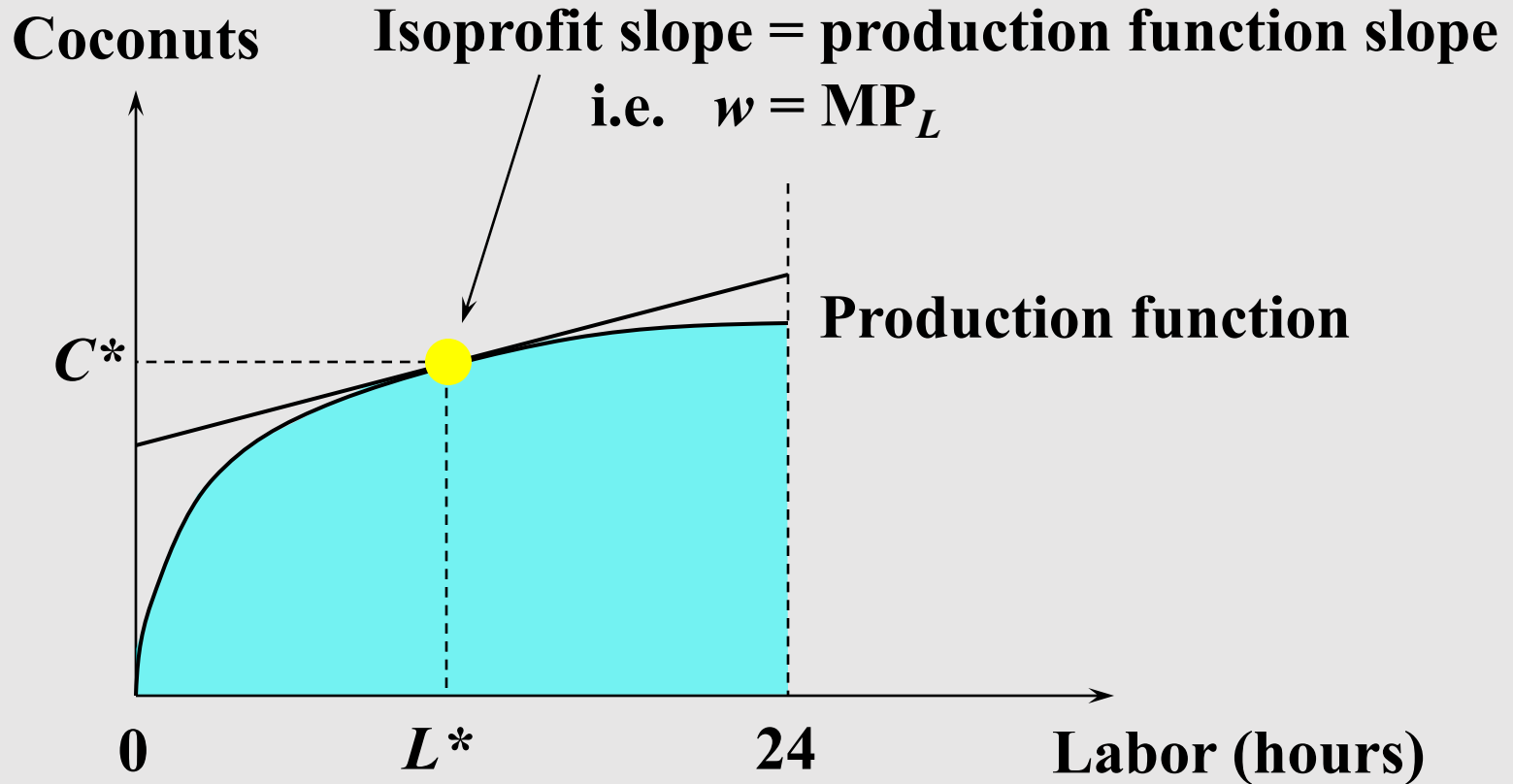
Profit-Maximization



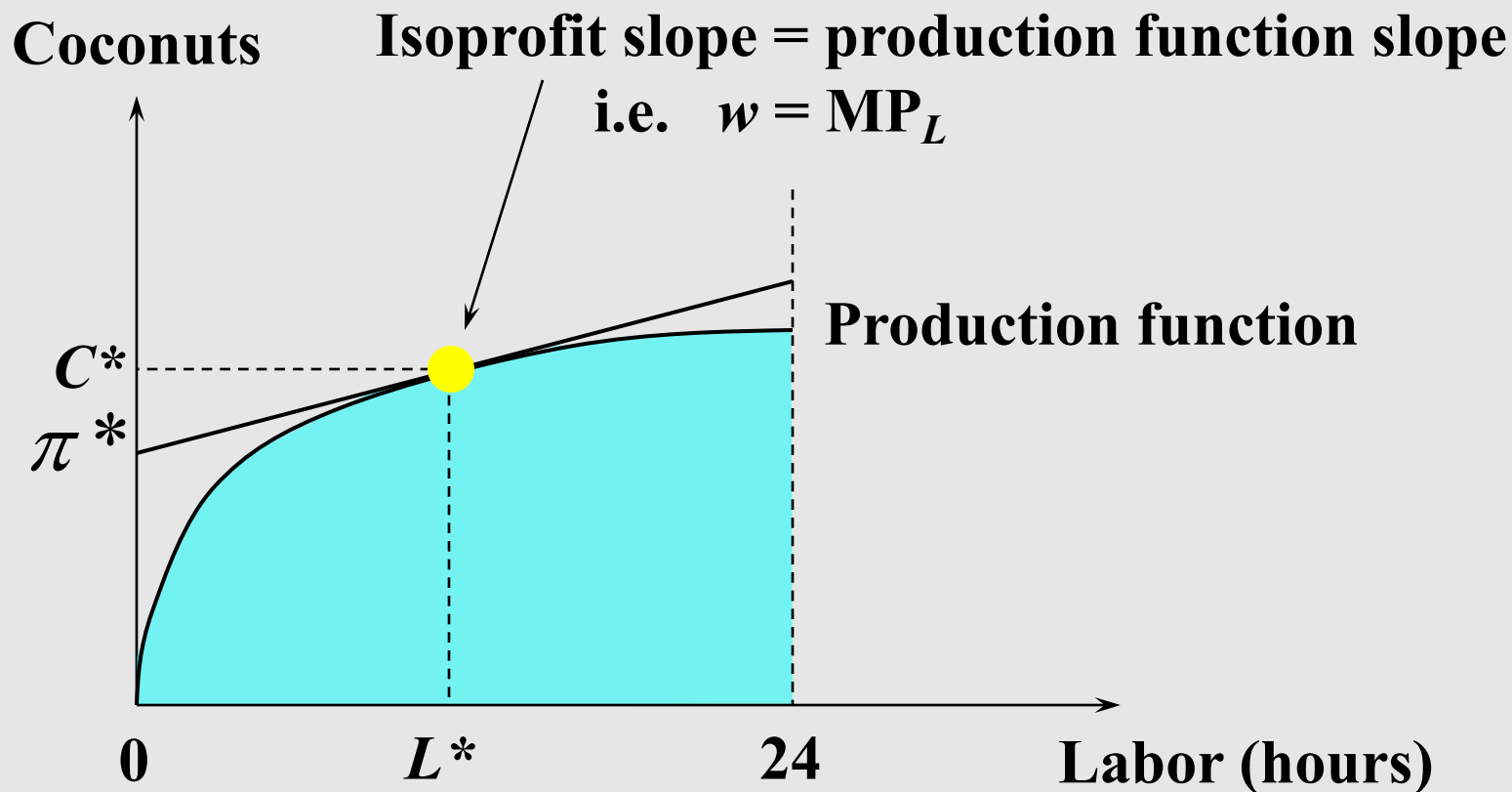
Profit-Maximization



Profit-Maximization

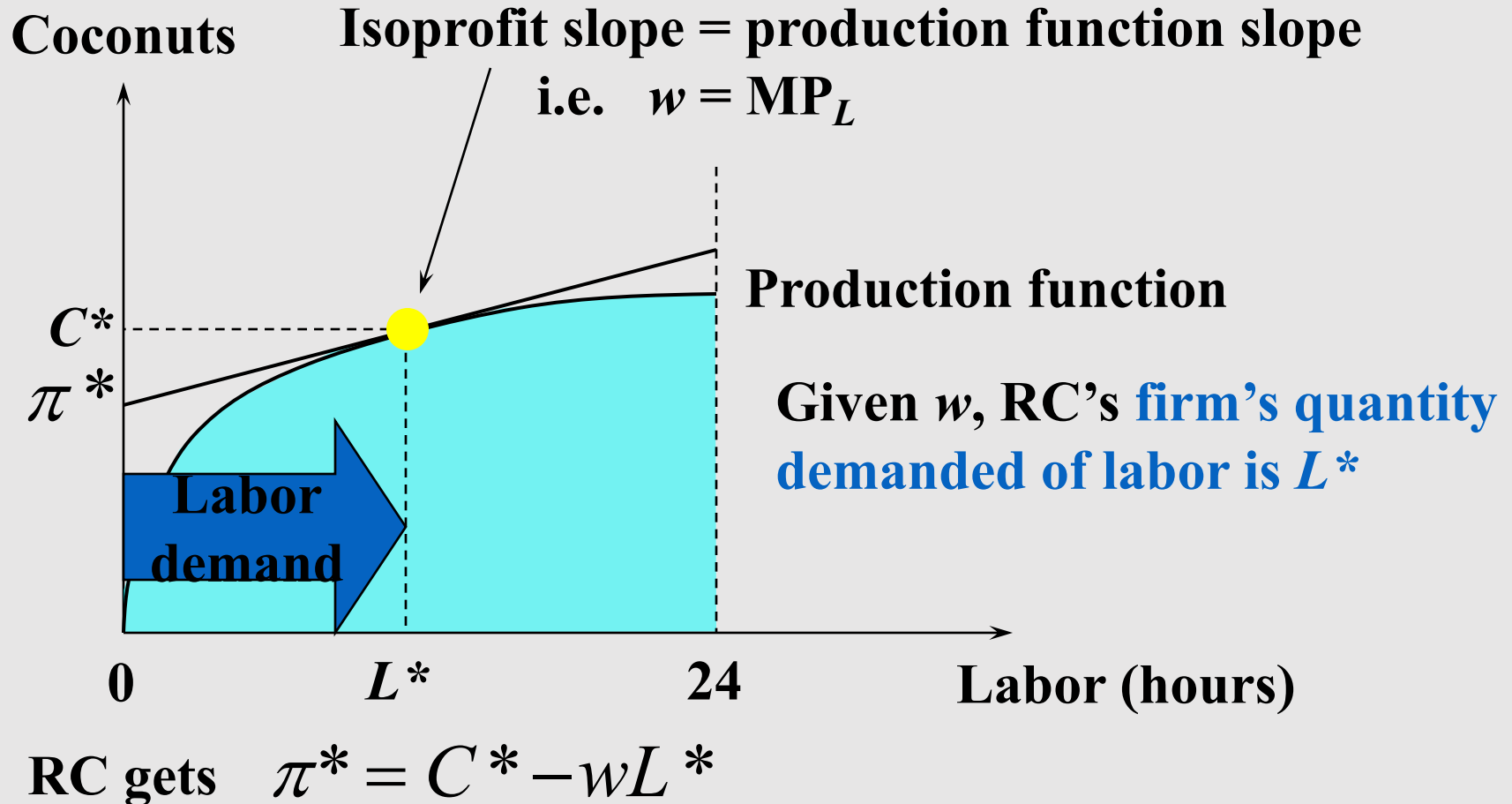


Profit-Maximization

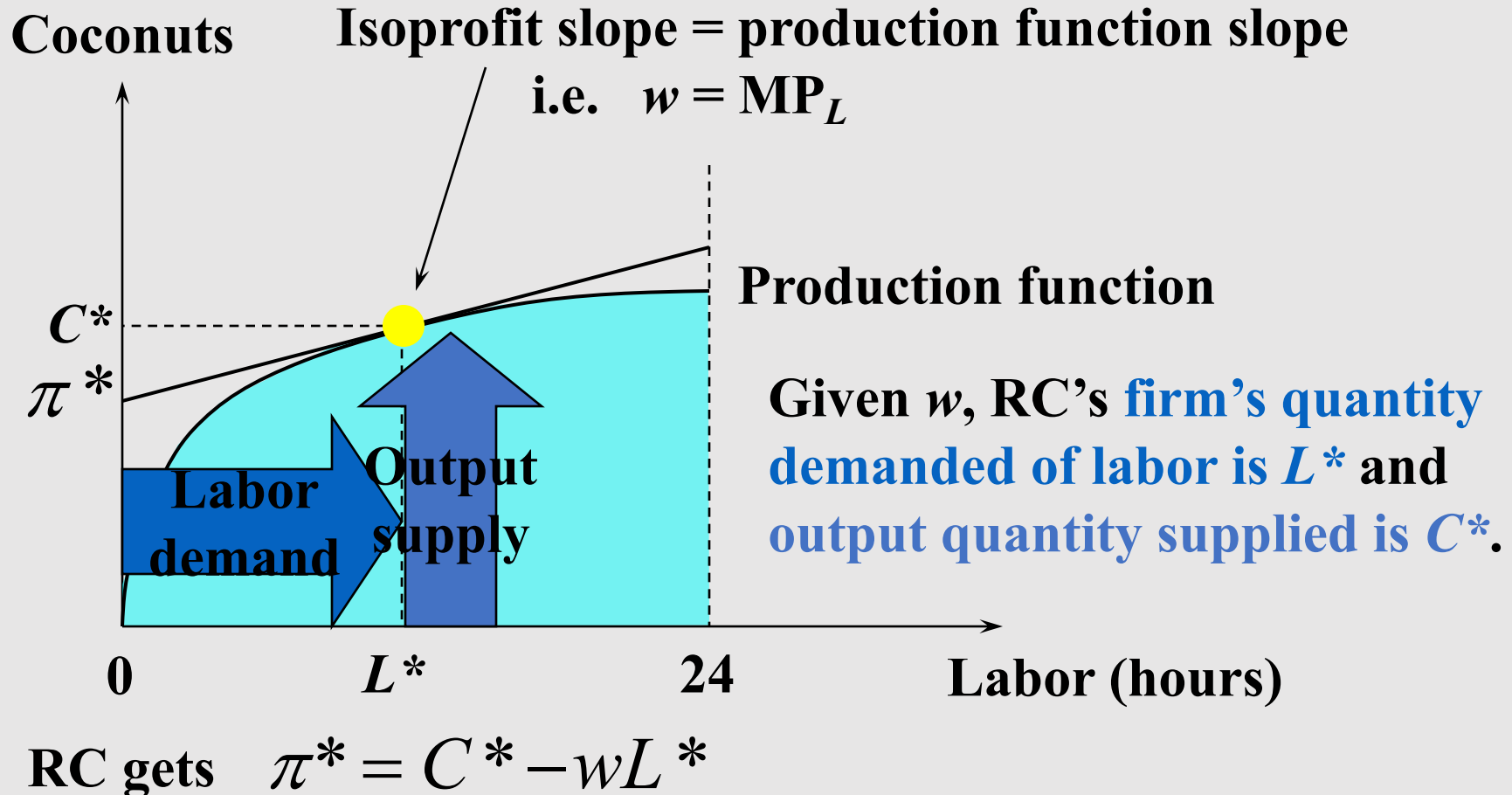


RC gets $\pi^* = C^* - wL^*$

Profit-Maximization



Profit-Maximization



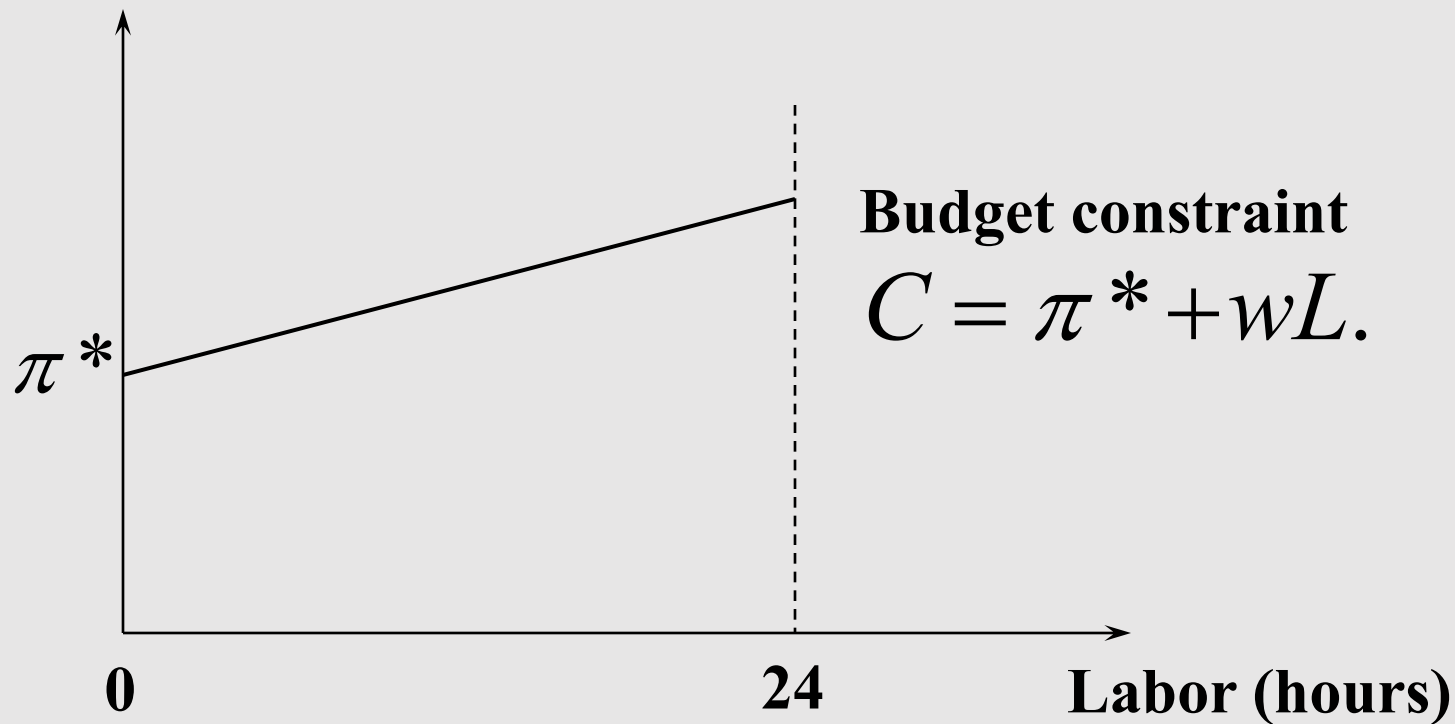
Utility-Maximization

- Now consider RC as a consumer endowed with π^* who can work for w per hour.
- What is RC's most preferred consumption bundle?
- Budget constraint is

$$C = \pi^* + wL.$$

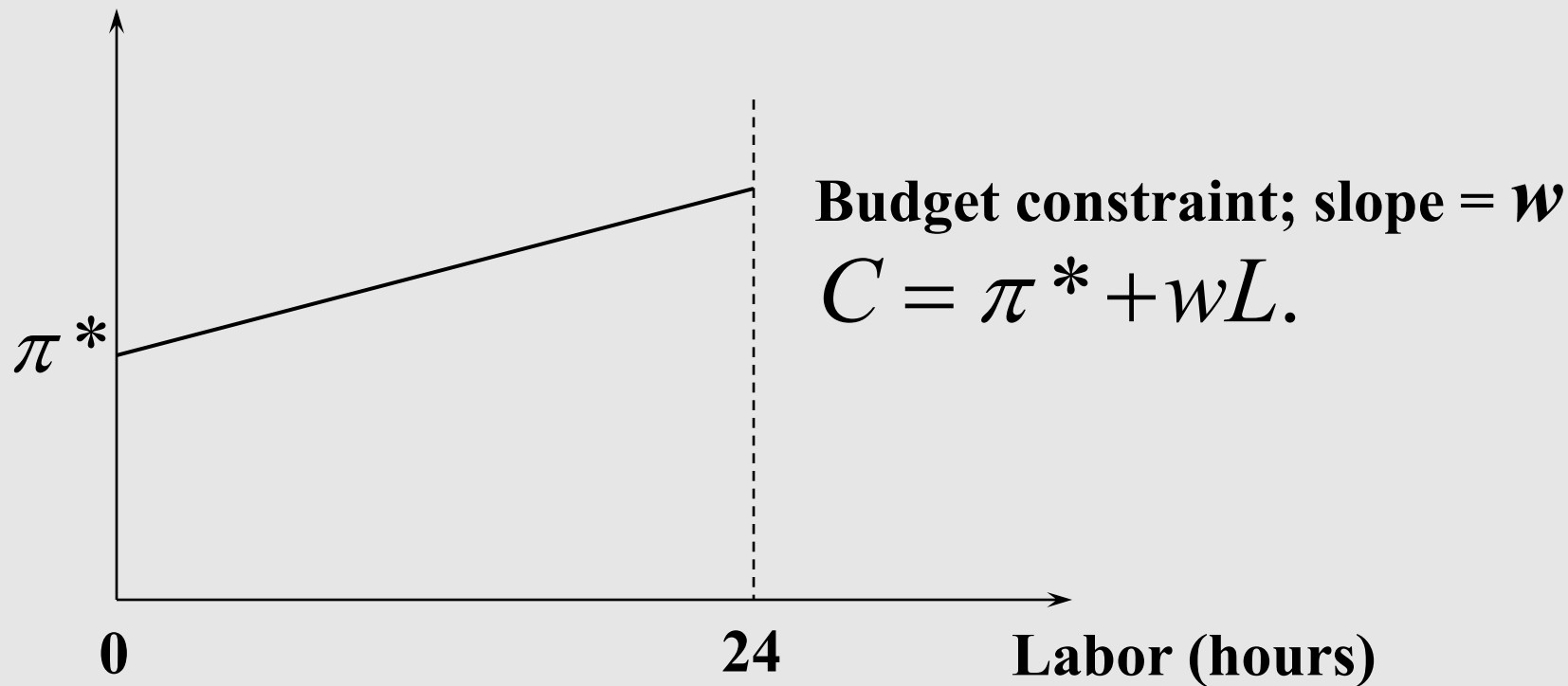
Utility-Maximization

Coconuts



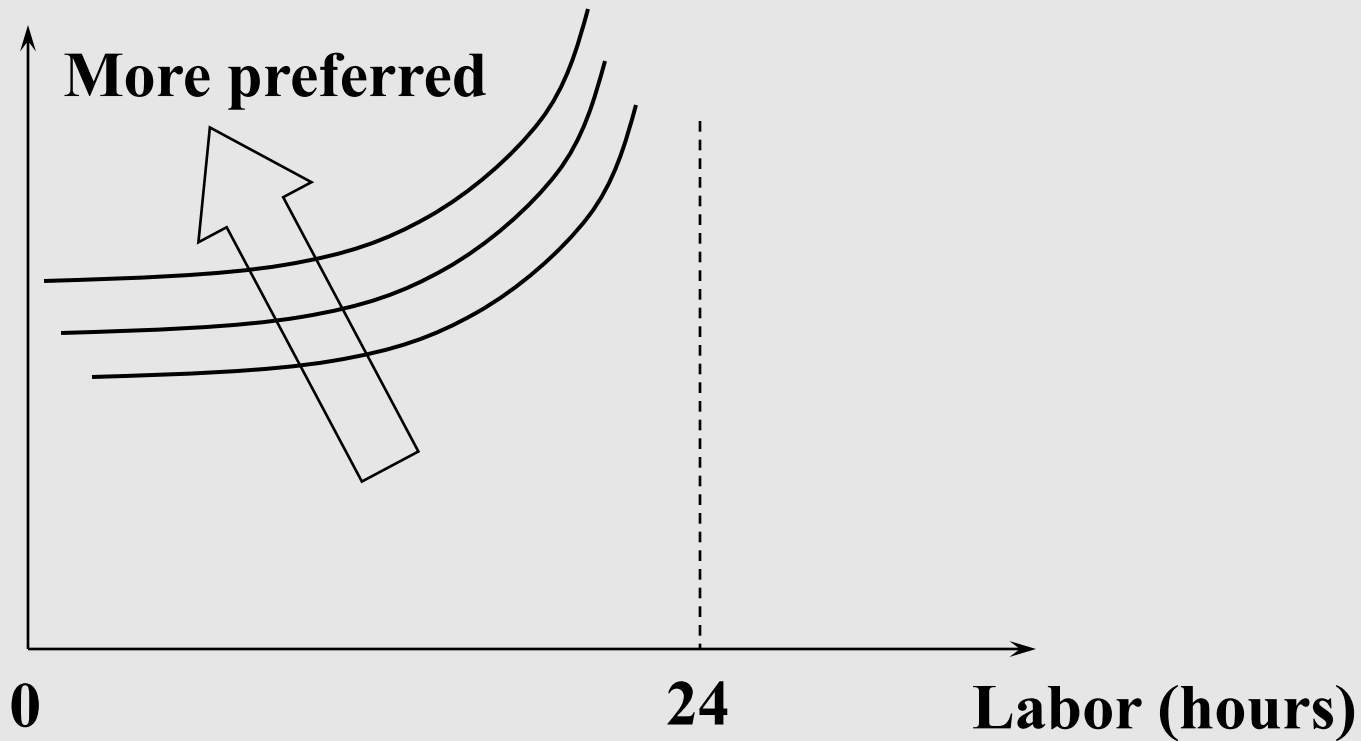
Utility-Maximization

Coconuts



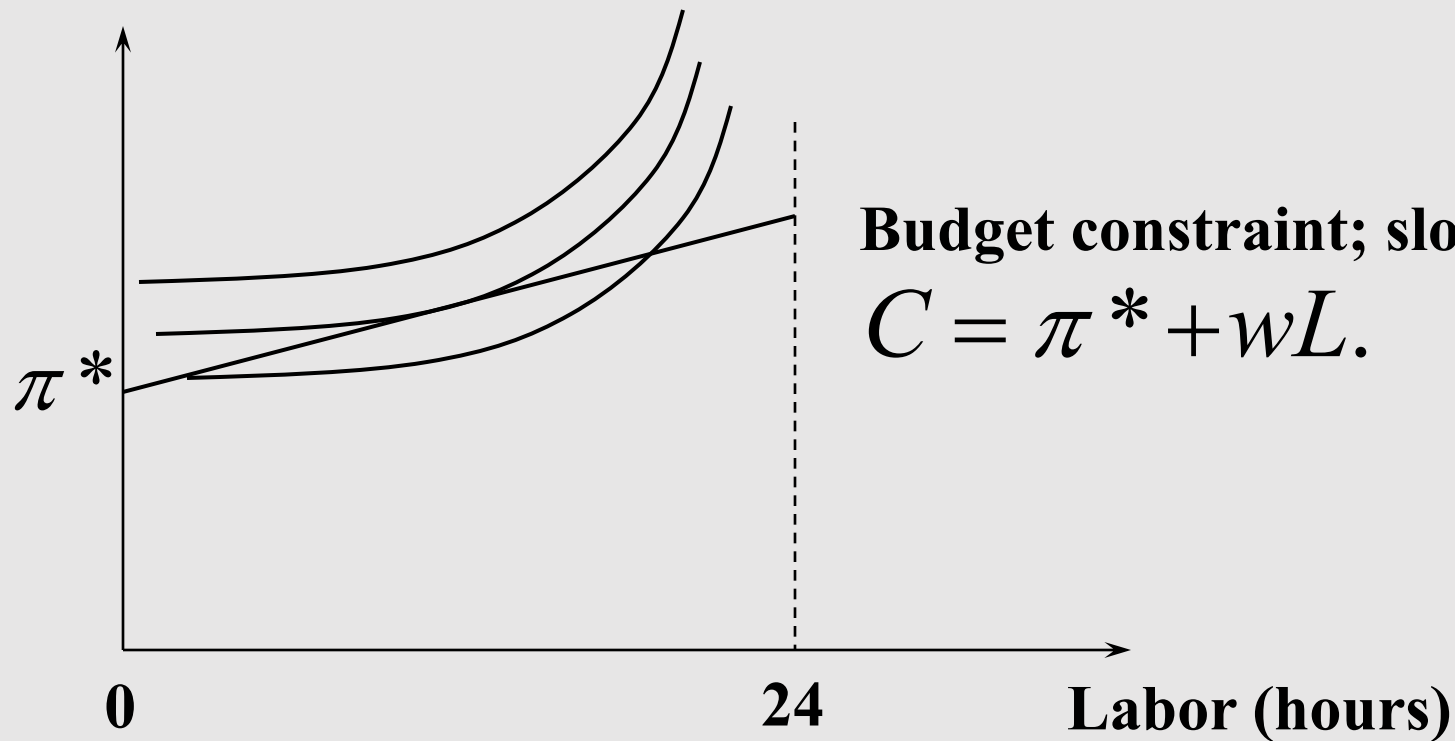
Utility-Maximization

Coconuts



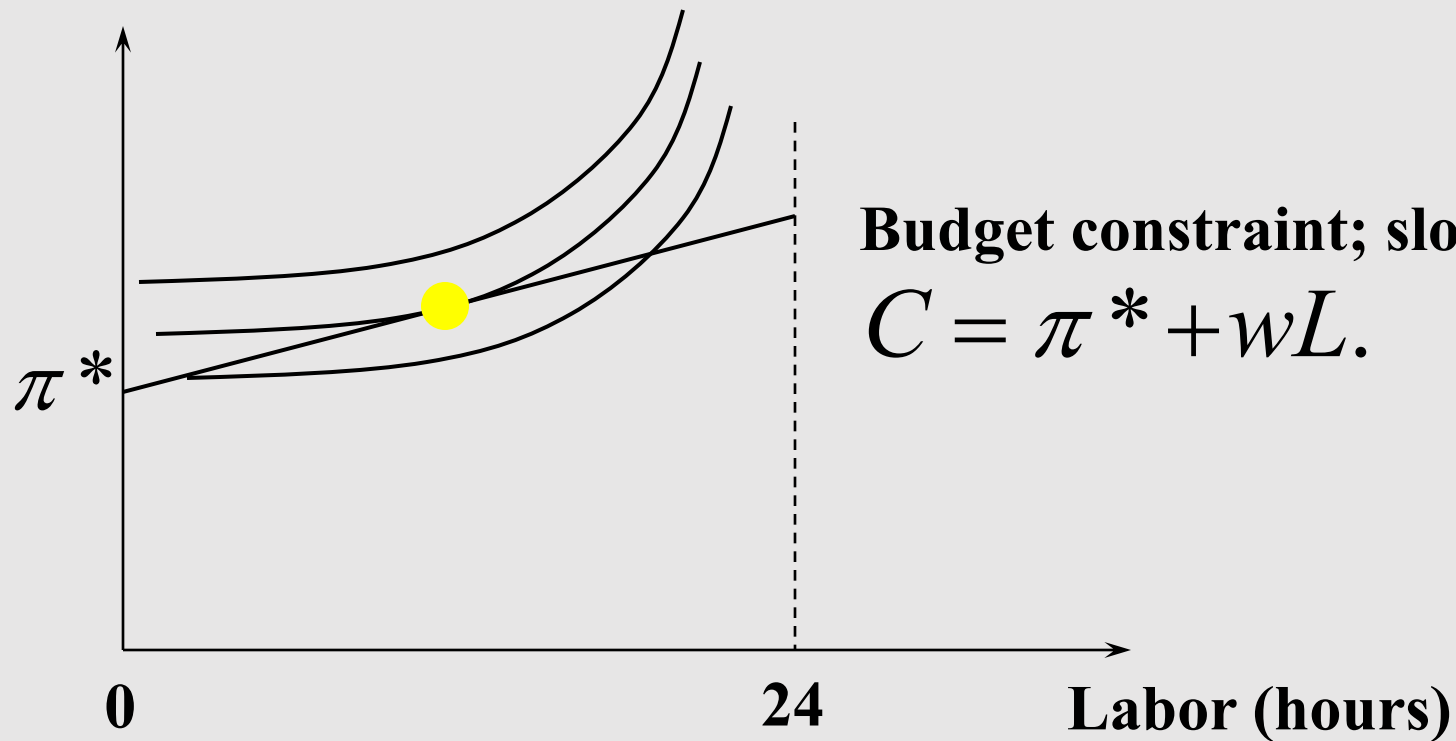
Utility-Maximization

Coconuts



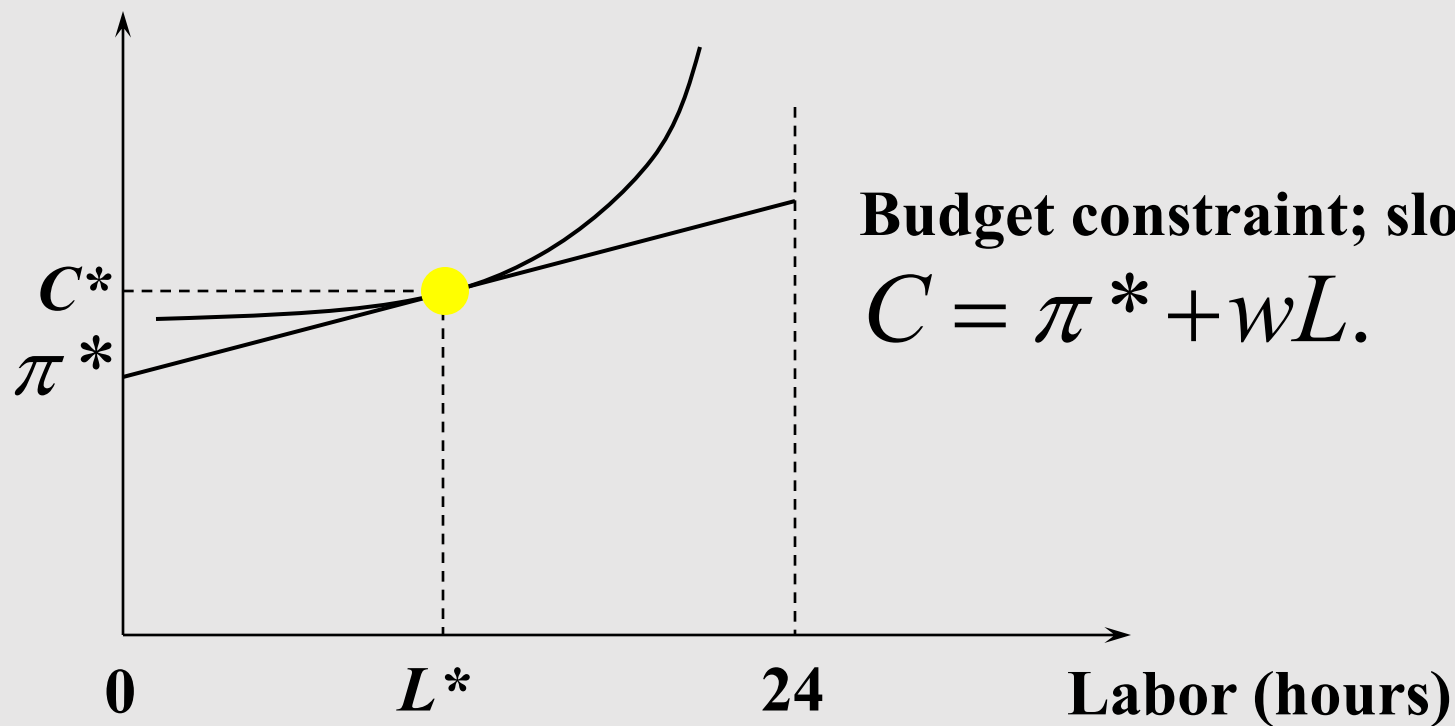
Utility-Maximization

Coconuts



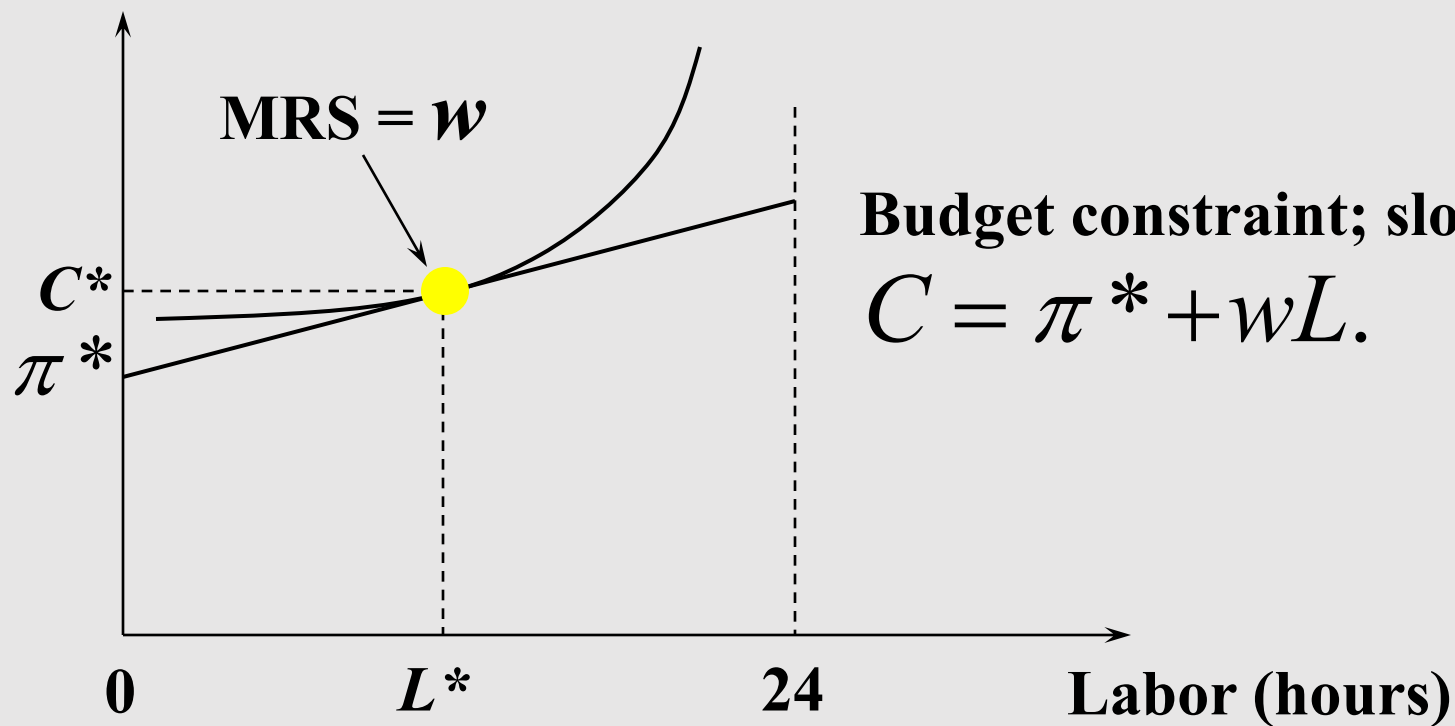
Utility-Maximization

Coconuts



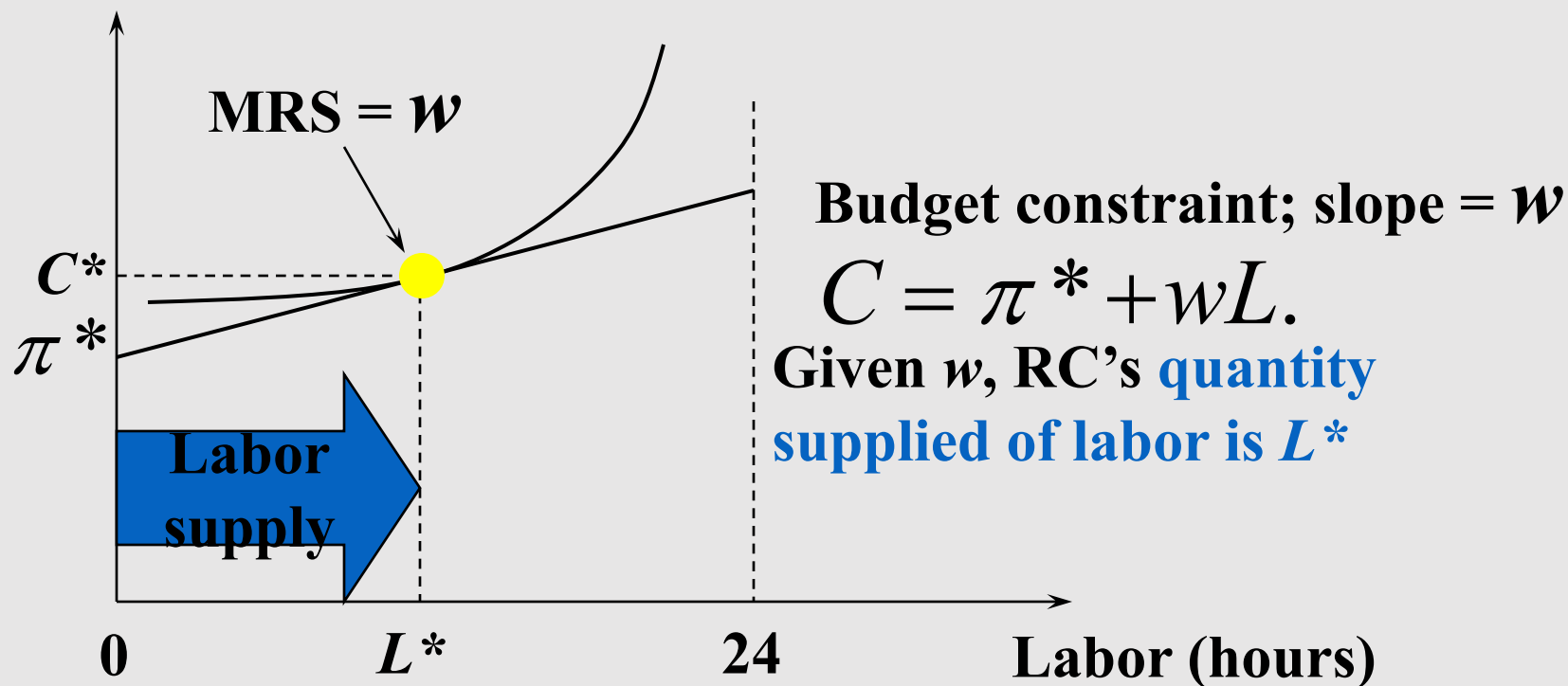
Utility-Maximization

Coconuts



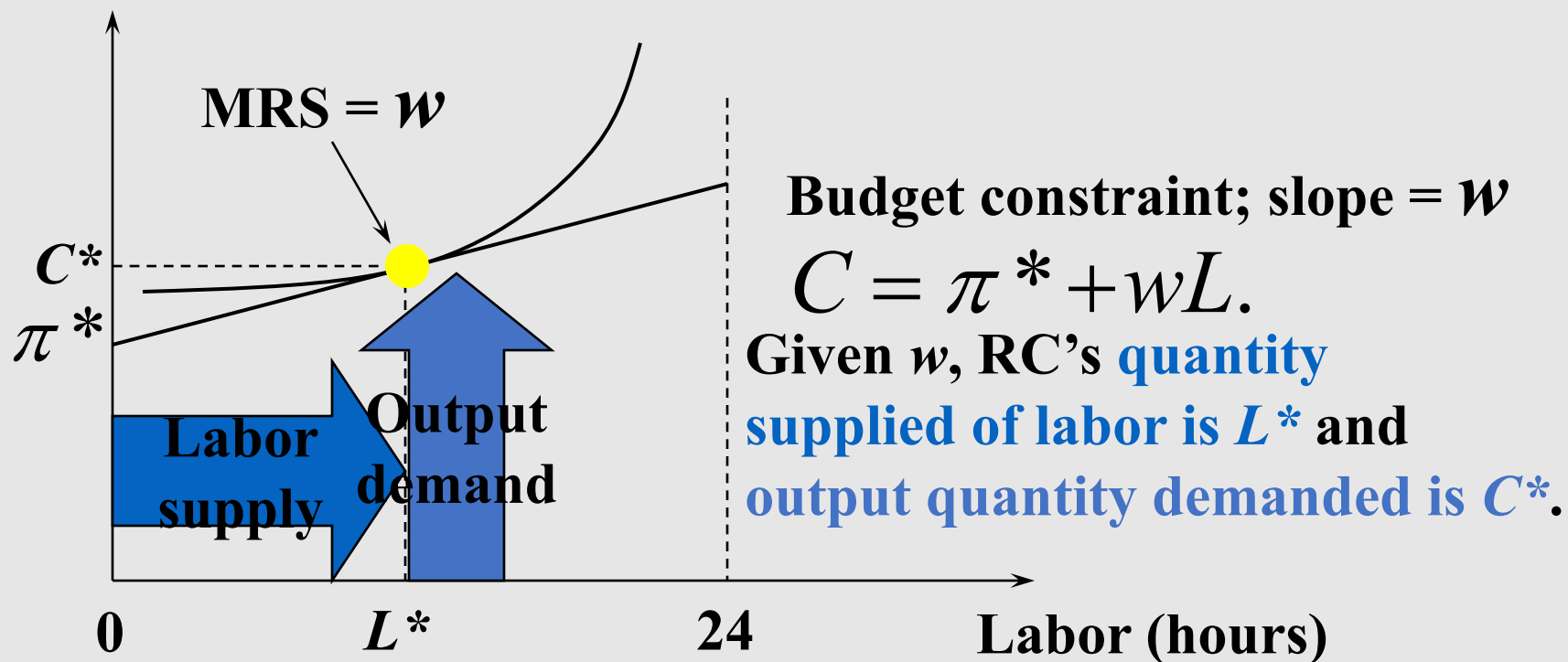
Utility-Maximization

Coconuts



Utility-Maximization

Coconuts



Utility-Maximization & Profit-Maximization

→ Profit-maximization:

- $w = MP_L$
- quantity of output supplied = C^*
- quantity of labor demanded = L^*

→ Utility-maximization:

- $w = MRS$
- quantity of output demanded = C^*
- quantity of labor supplied = L^*

Utility-Maximization & Profit-Maximization

→ Profit-maximization:

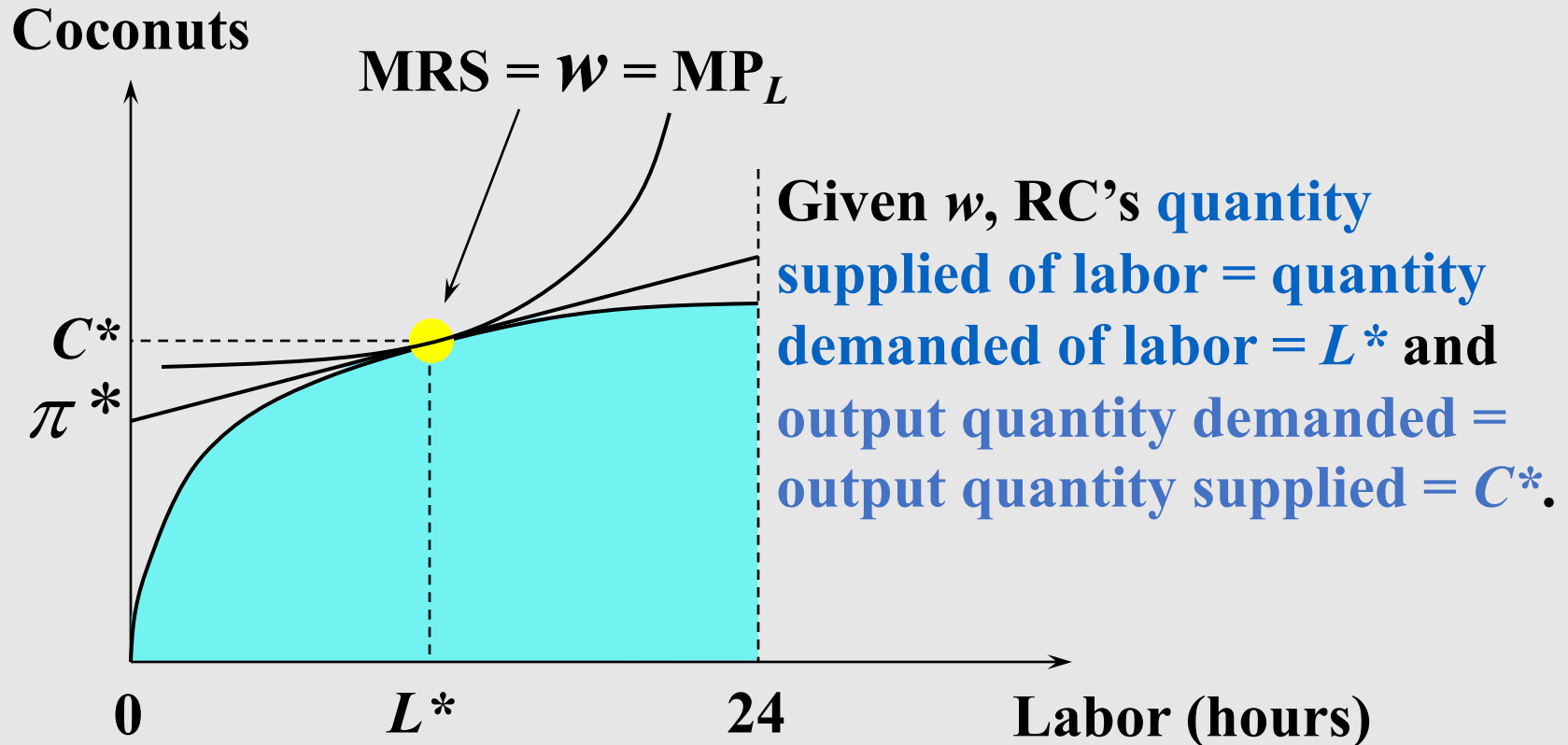
- $w = MP_L$
- quantity of output supplied = C^*
- quantity of labor demanded = L^*

→ Utility-maximization:

- $w = MRS$
- quantity of output demanded = C^*
- quantity of labor supplied = L^*

**Coconut and labor
markets both clear.**

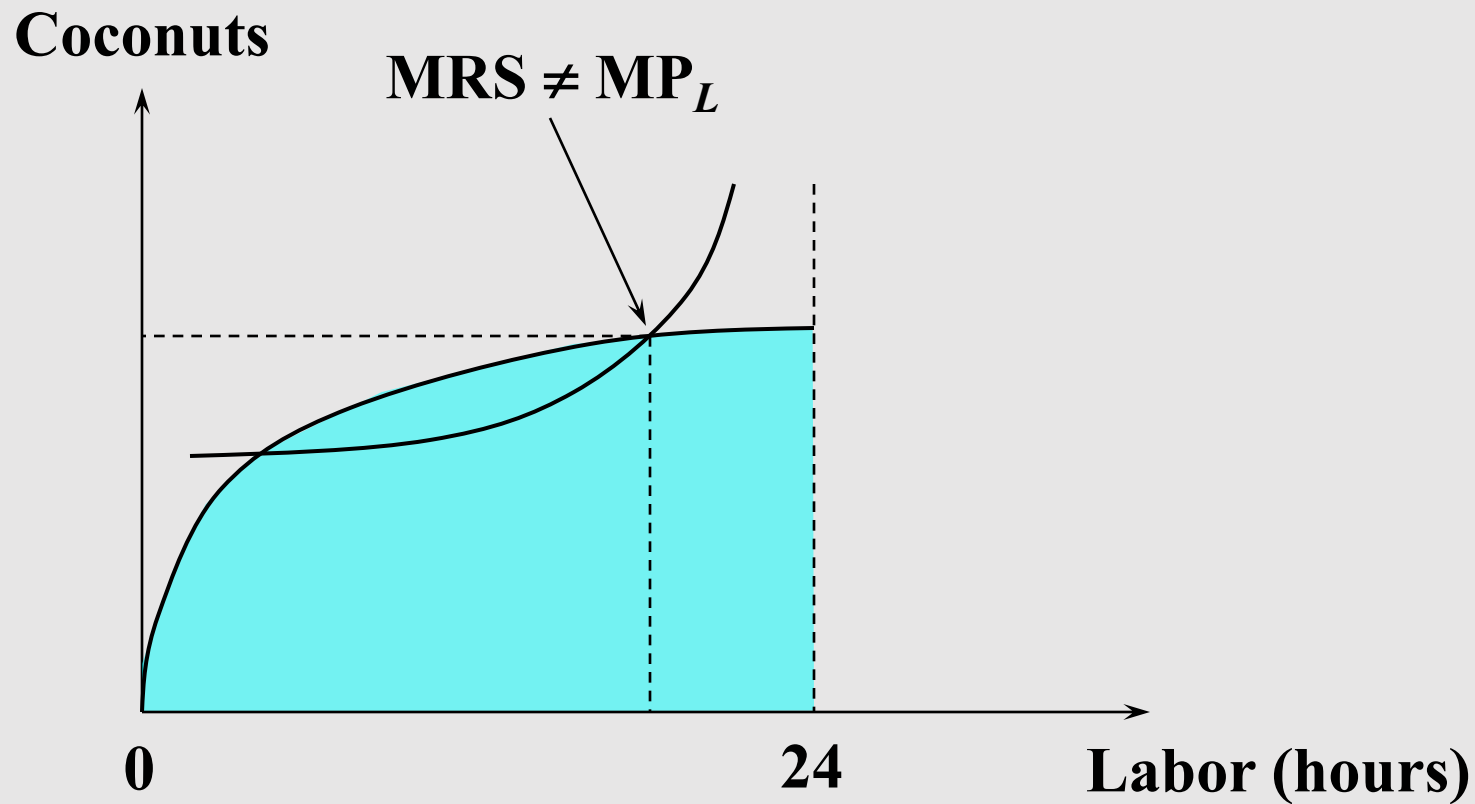
Utility-Maximization & Profit-Maximization



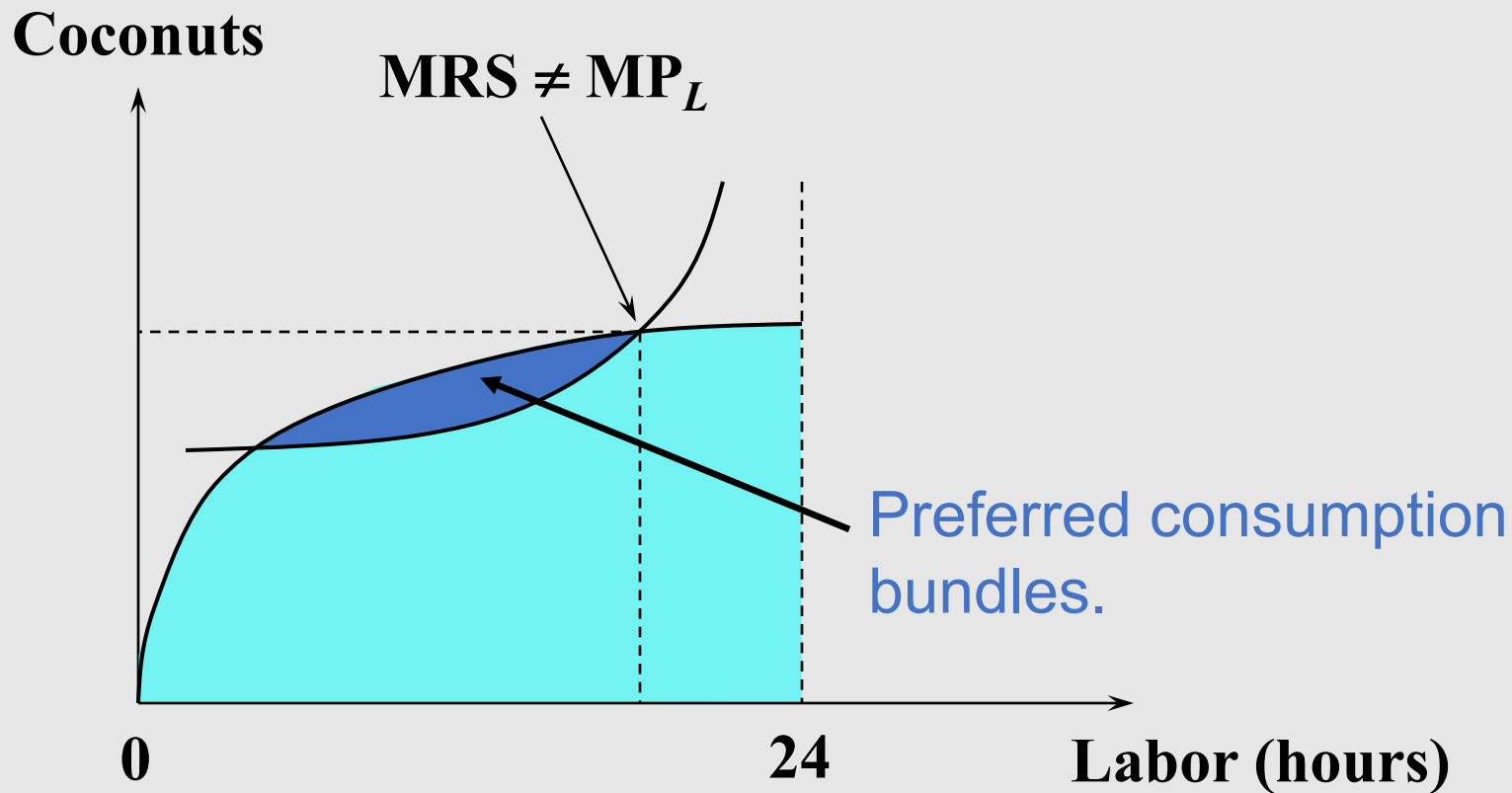
Pareto Efficiency

→ Must have $MRS = MP_L$.

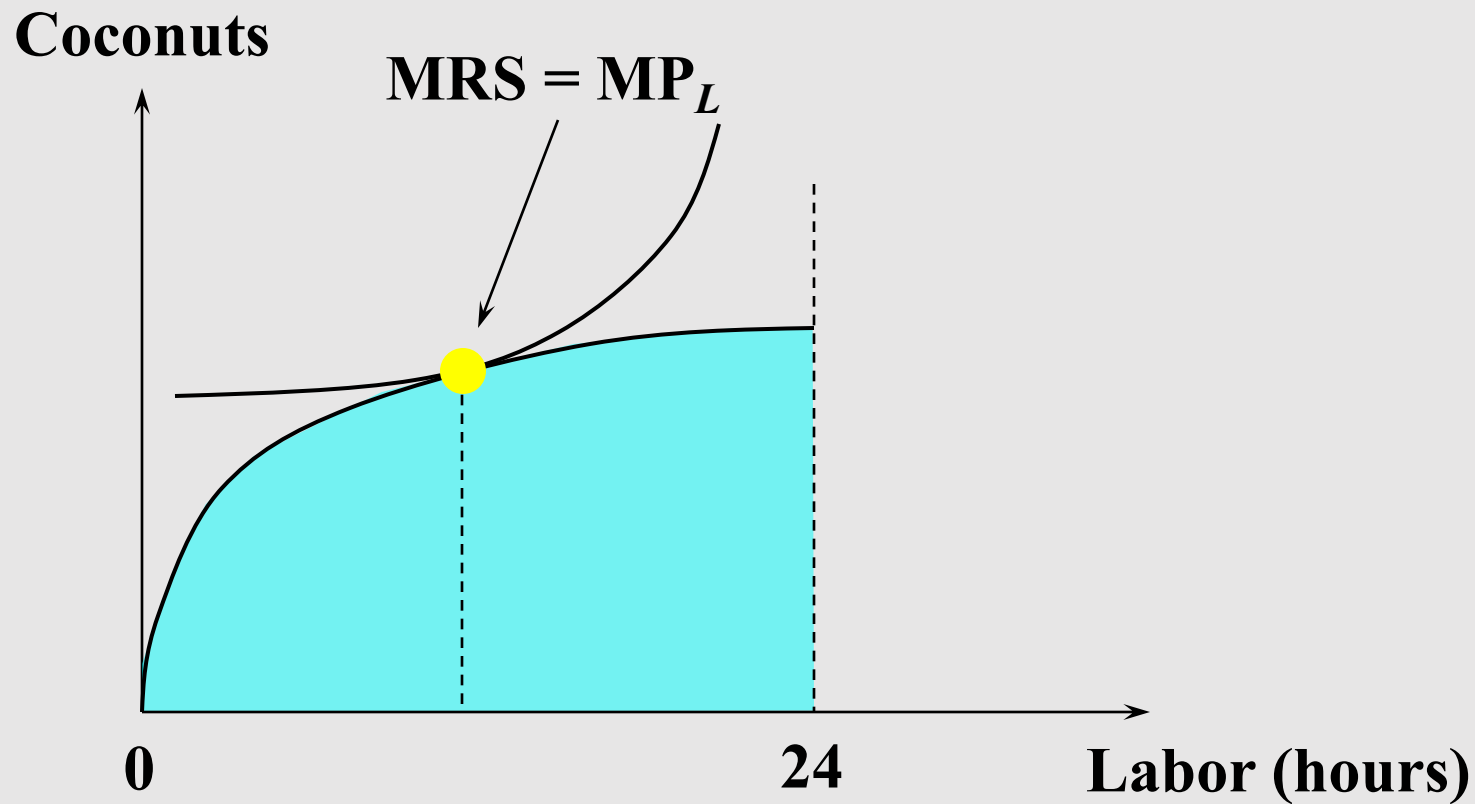
Pareto Efficiency



Pareto Efficiency



Pareto Efficiency



First Fundamental Theorem of Welfare Economics

- A competitive market equilibrium is Pareto efficient if
 - consumers' preferences are convex
 - there are no externalities in consumption or production.

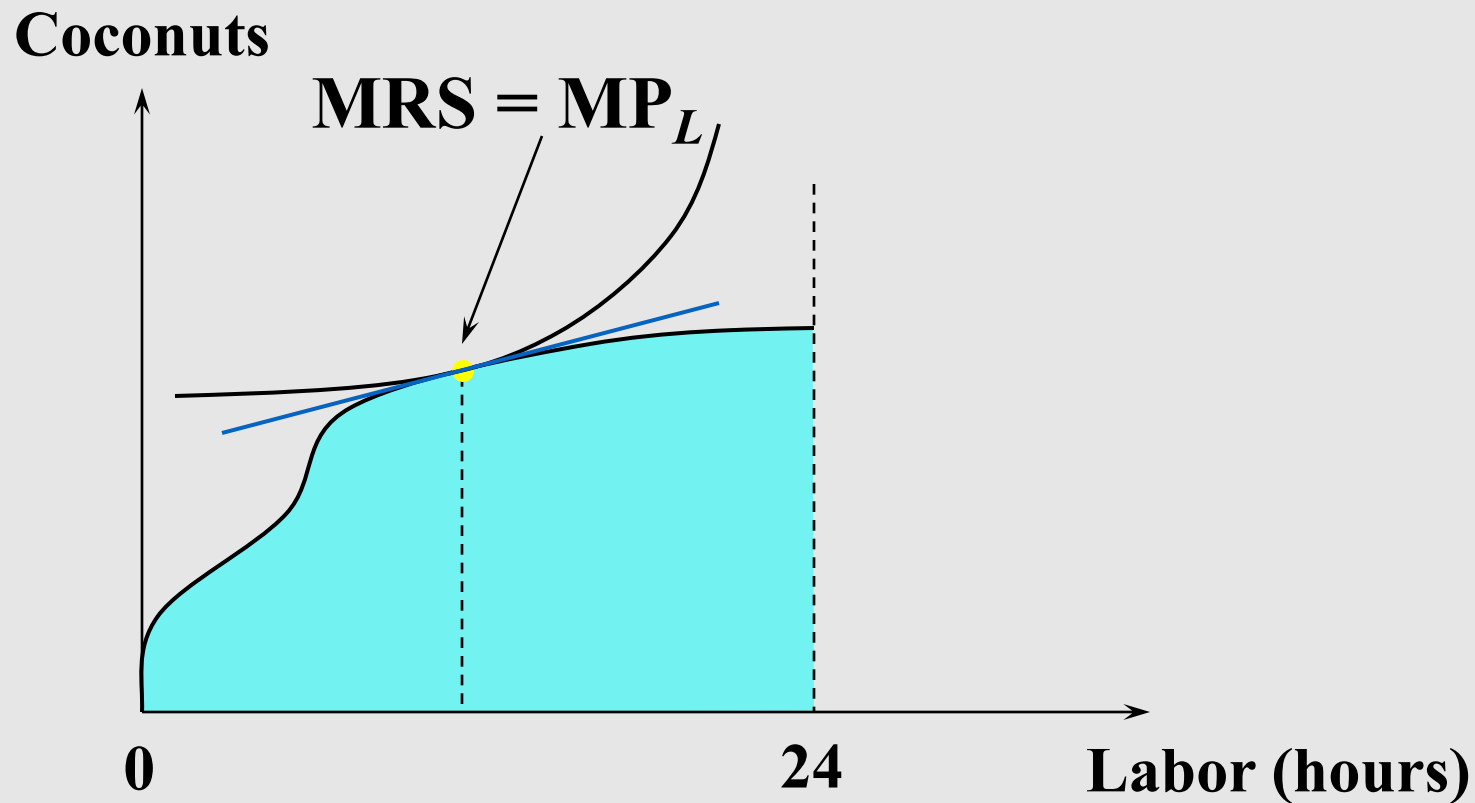
Second Fundamental Theorem of Welfare Economics

- Any Pareto efficient economic state can be achieved as a competitive market equilibrium if
 - consumers' preferences are convex
 - firms' technologies are convex
 - there are no externalities in consumption or production.

Non-Convex Technologies

- Do the Welfare Theorems hold if firms have non-convex technologies?
- The 1st Theorem does not rely upon firms' technologies being convex.

Non-Convex Technologies

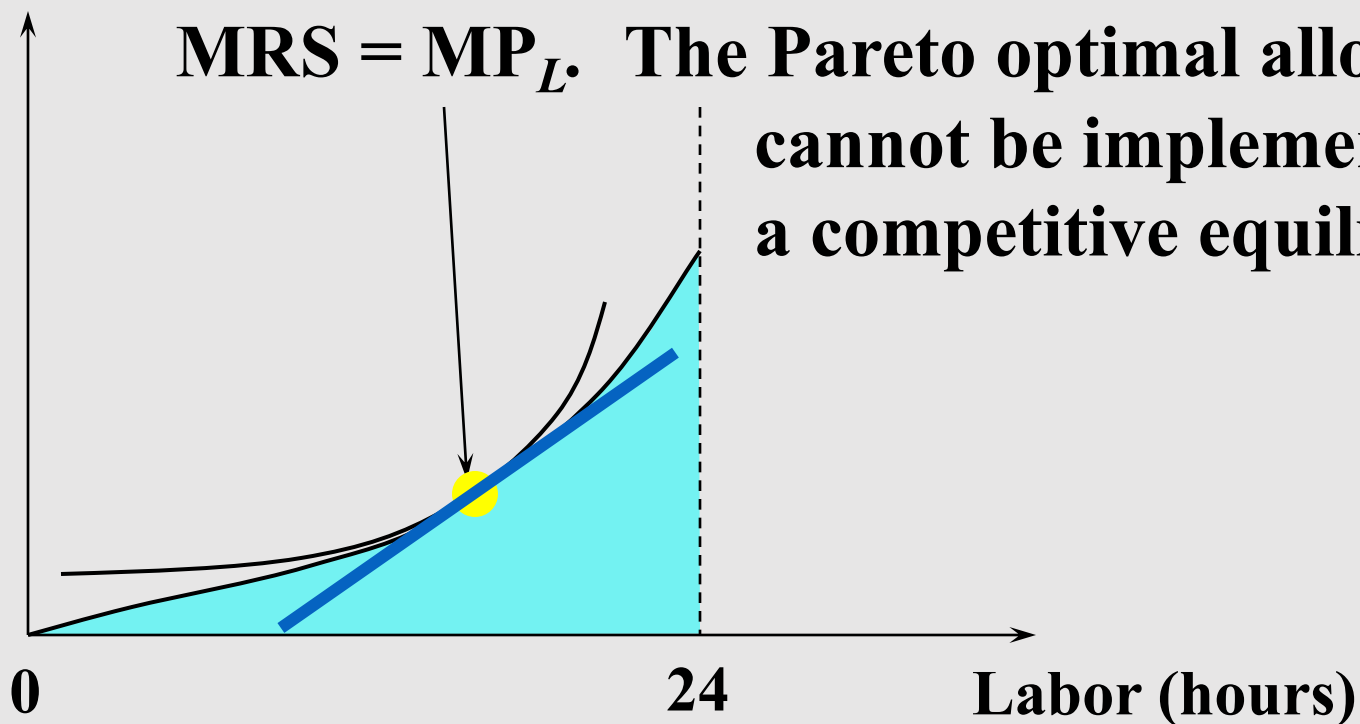


Non-Convex Technologies

- Do the Welfare Theorems hold if firms have non-convex technologies?
- The 2nd Theorem **does** require that firms' technologies be convex.
 - This means that all situations with increasing returns to scale are ruled out.

Non-Convex Technologies

Coconuts



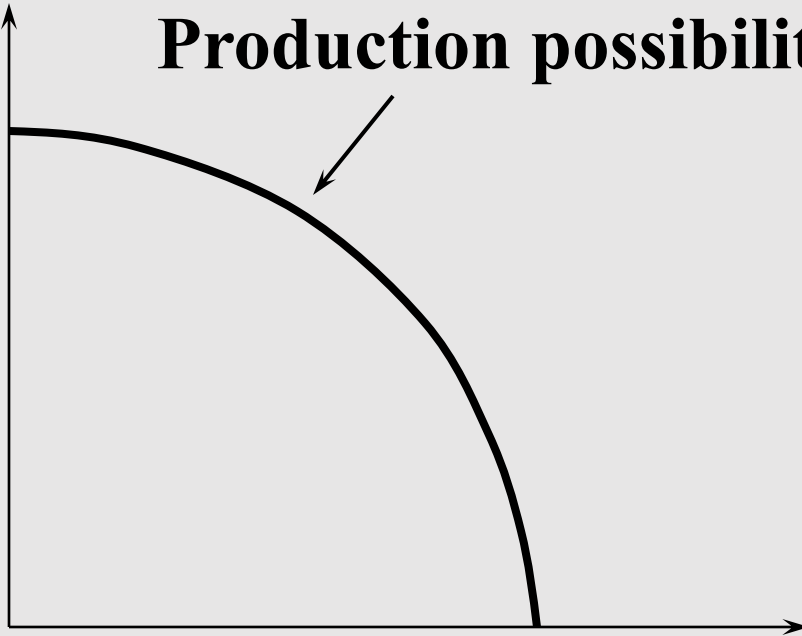
Production Possibilities

- Resource and technological limitations restrict what an economy can produce.
- The set of all feasible output bundles is the economy's production possibility set.
- The set's outer boundary is the production possibility frontier.

Production Possibilities

Coconuts

Production possibility frontier (ppf)



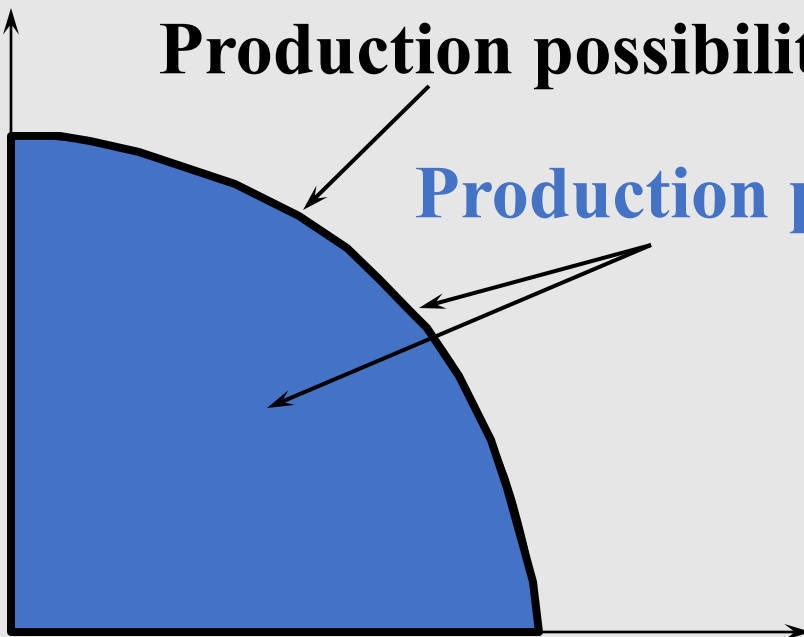
Fish

Production Possibilities

Coconuts

Production possibility frontier (ppf)

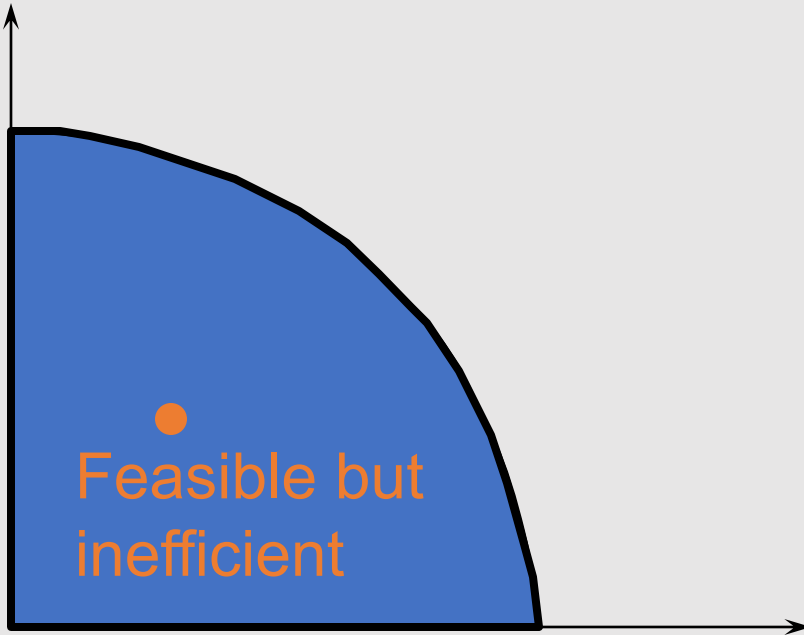
Production possibility set



Fish

Production Possibilities

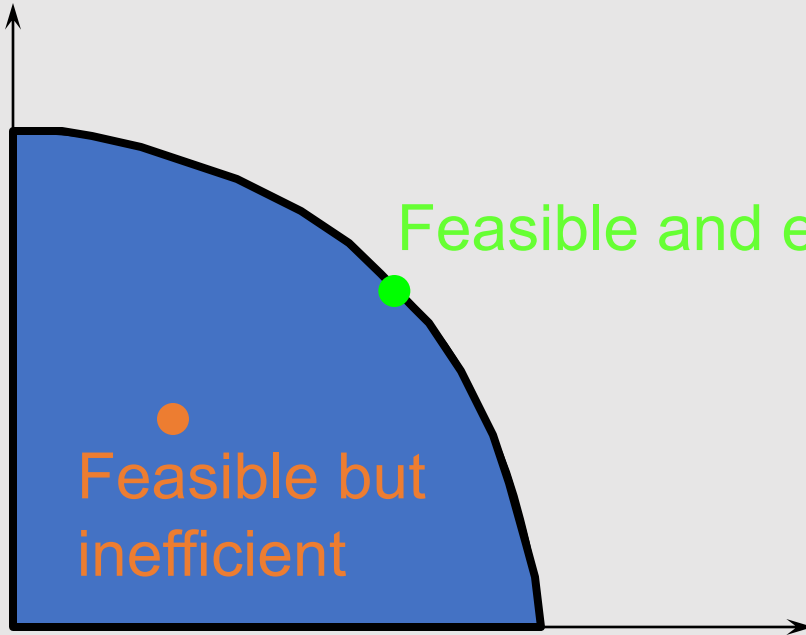
Coconuts



Fish

Production Possibilities

Coconuts



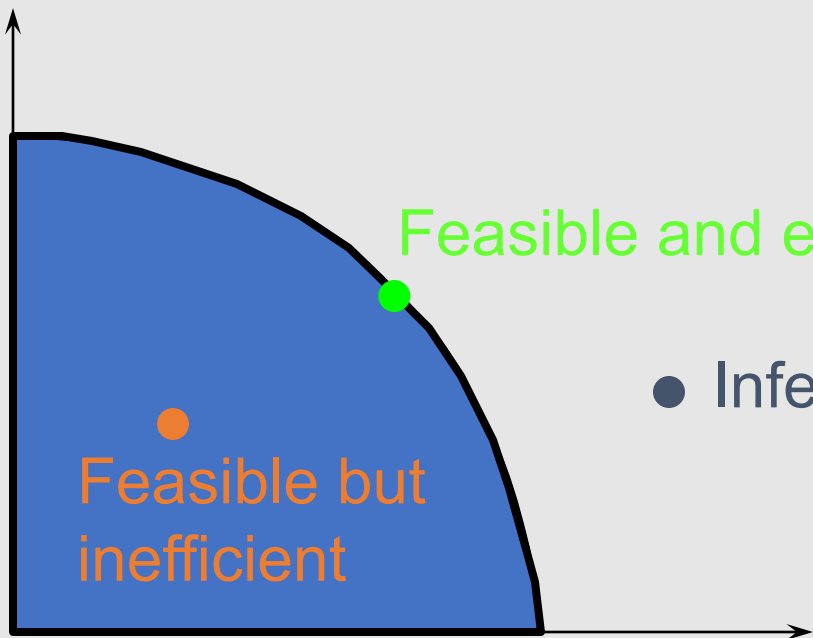
Feasible and efficient

Feasible but
inefficient

Fish

Production Possibilities

Coconuts



Feasible and efficient

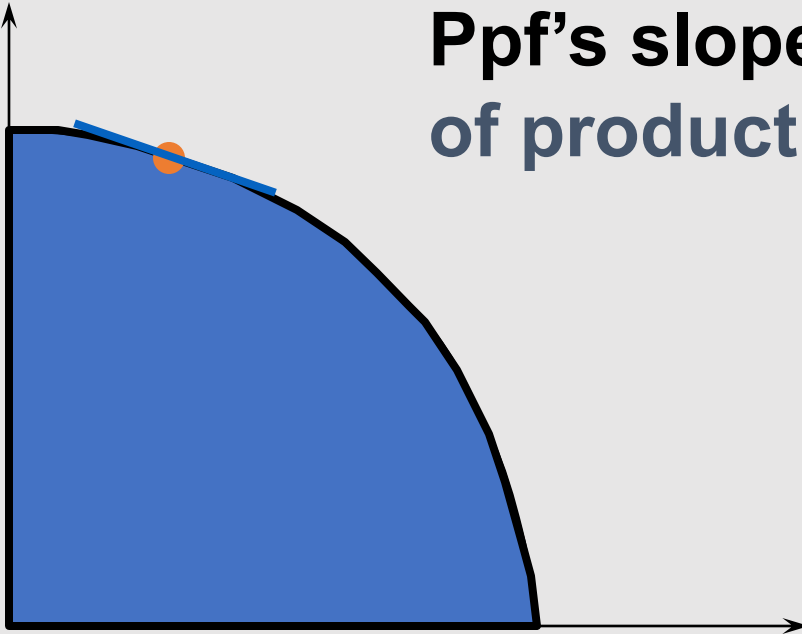
● Infeasible

Feasible but
inefficient

Fish

Production Possibilities

Coconuts

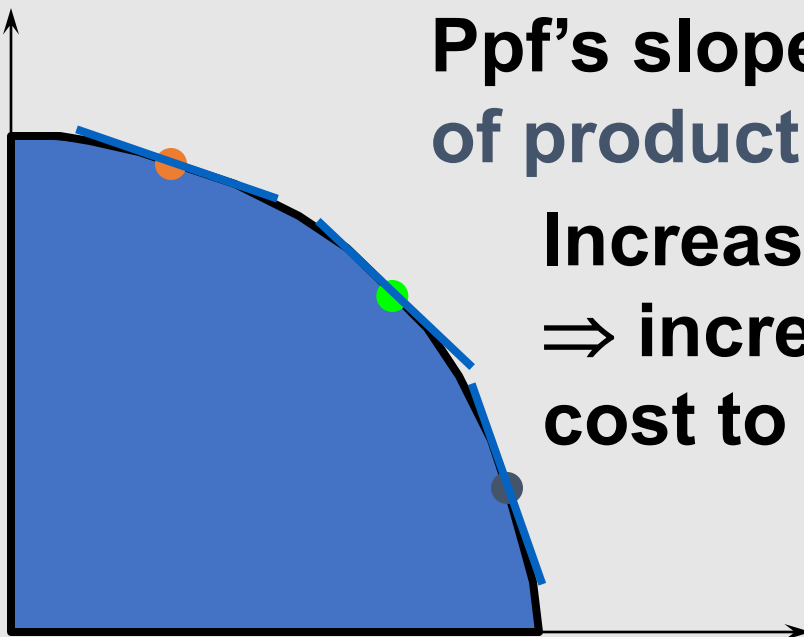


Ppf's slope is the marginal rate of product transformation.

Fish

Production Possibilities

Coconuts



Ppf's slope is the marginal rate of product transformation.

**Increasingly negative MRPT
⇒ increasing opportunity
cost to specialization.**

Fish

Production Possibilities

- If there are no production externalities then a ppf will be concave w.r.t. the origin.
- Why?

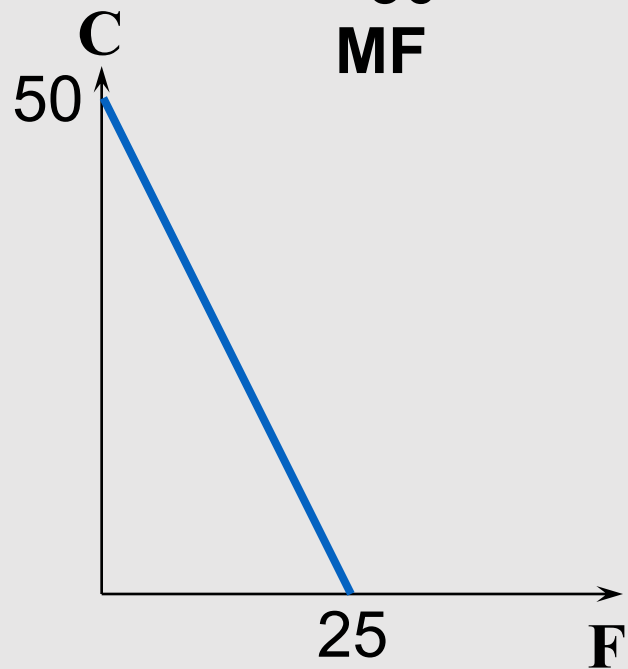
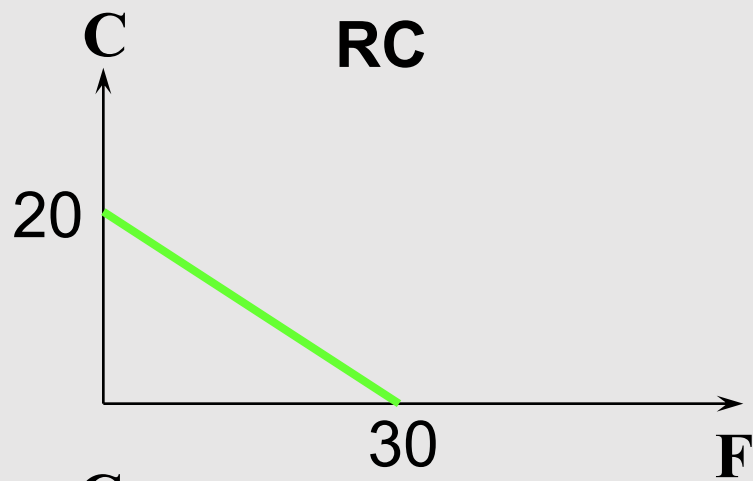
Production Possibilities

- If there are no production externalities then a ppf will be concave w.r.t. the origin.
- Why?
- Because efficient production requires exploitation of comparative advantages.

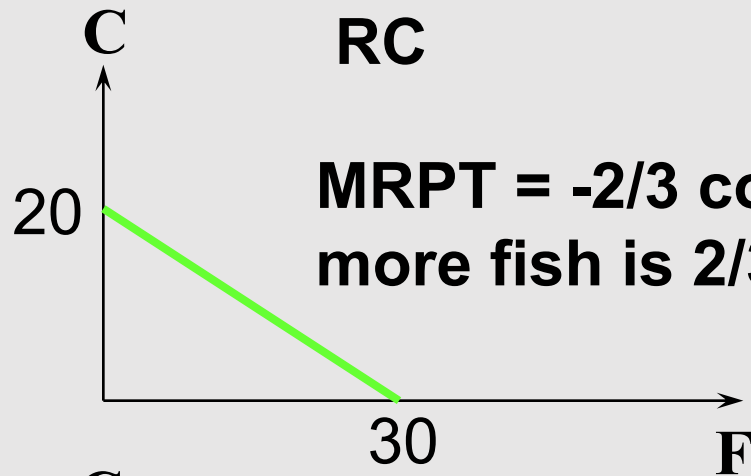
Comparative Advantage

- Two agents, RC and Man Friday (MF).
- RC can produce at most 20 coconuts or 30 fish.
- MF can produce at most 50 coconuts or 25 fish.

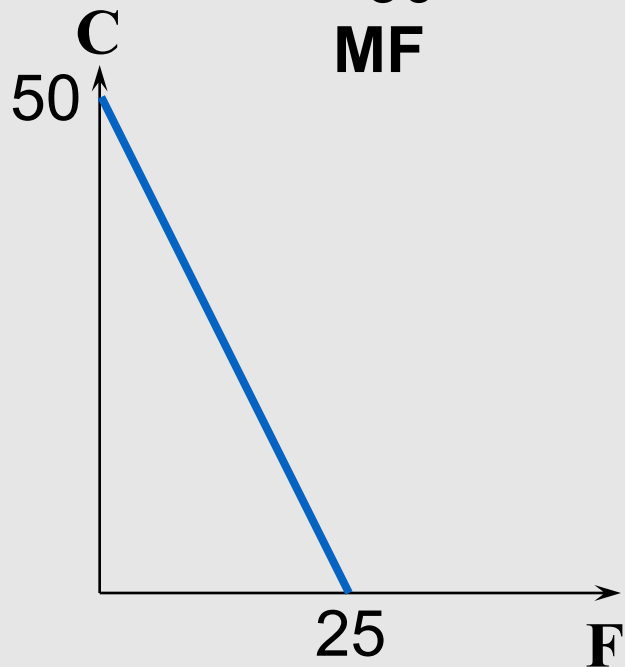
Comparative Advantage



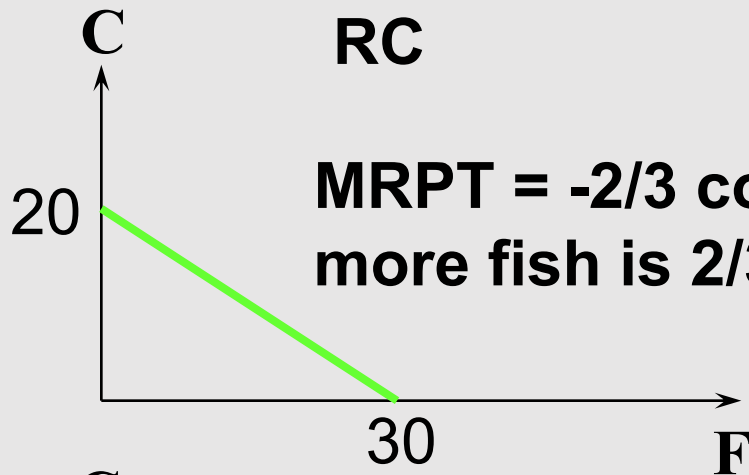
Comparative Advantage



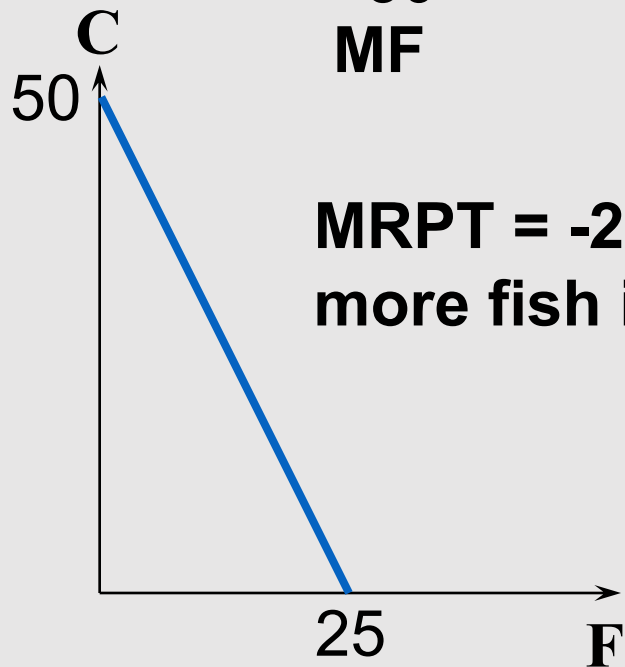
MRPT = $-2/3$ coconuts/fish so opp. cost of one more fish is $2/3$ foregone coconuts.



Comparative Advantage

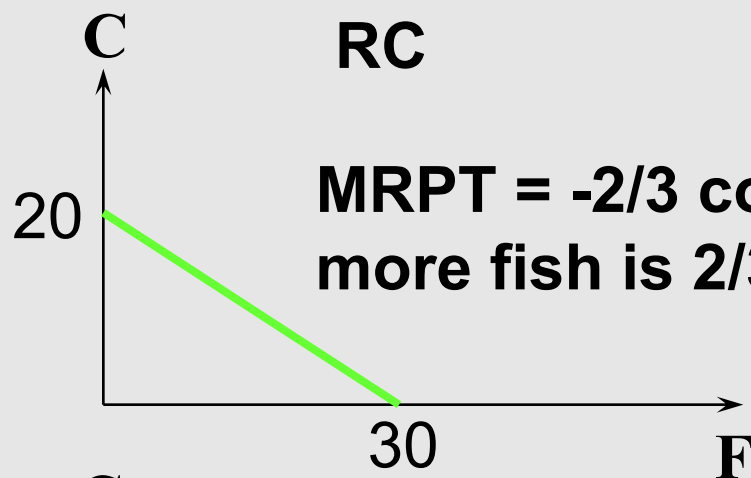


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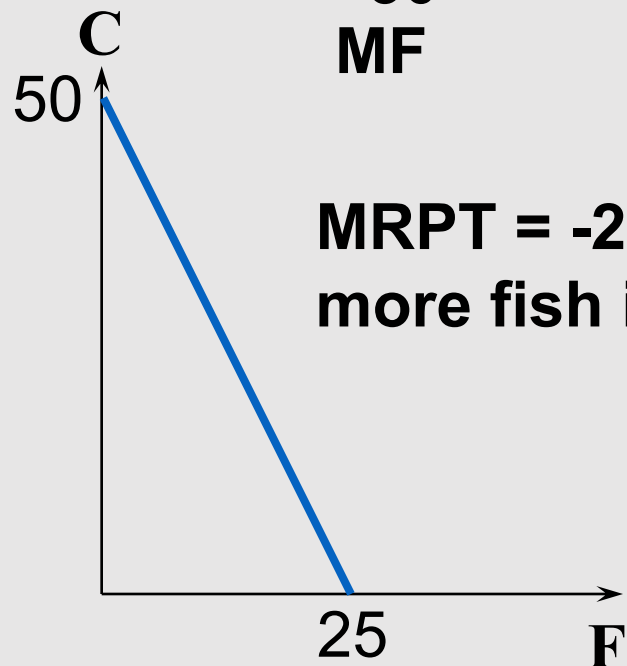
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Comparative Advantage



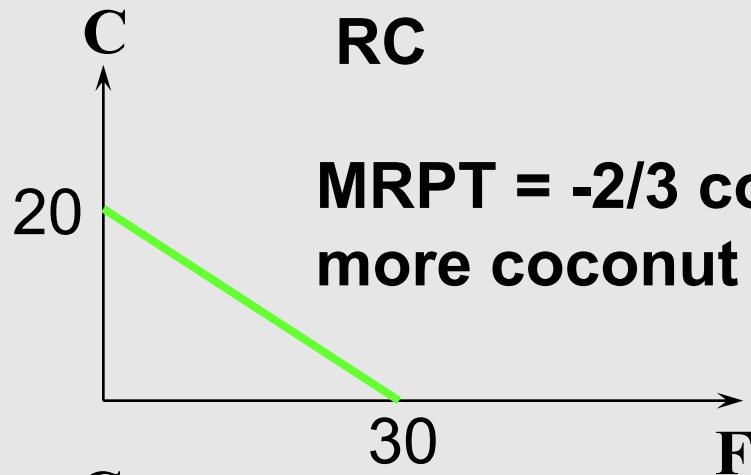
MRPT = $-2/3$ coconuts/fish so opp. cost of one more fish is $2/3$ foregone coconuts.

RC has the comparative opp. cost advantage in producing fish.

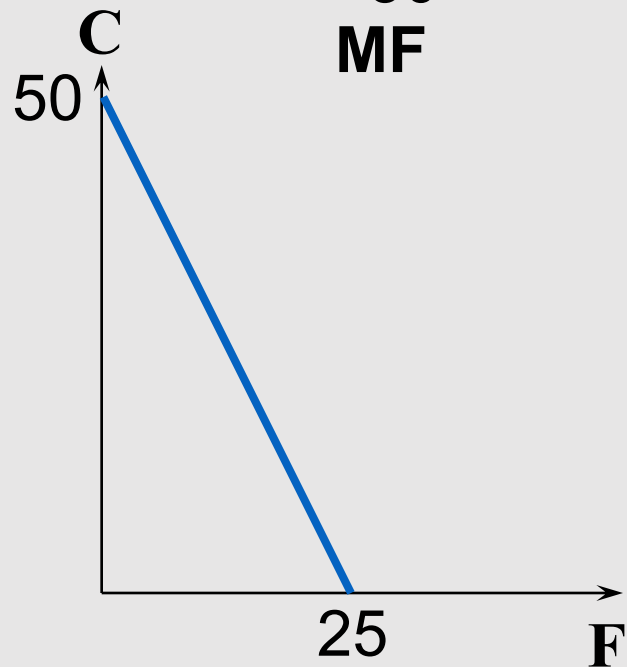


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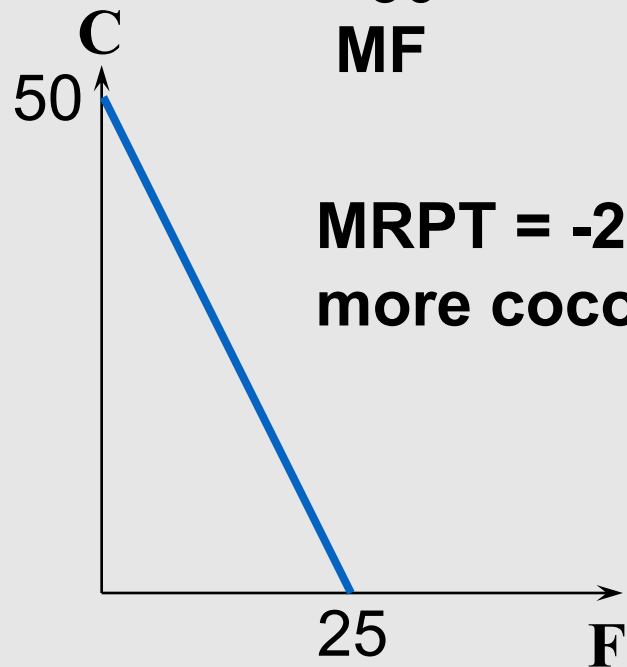
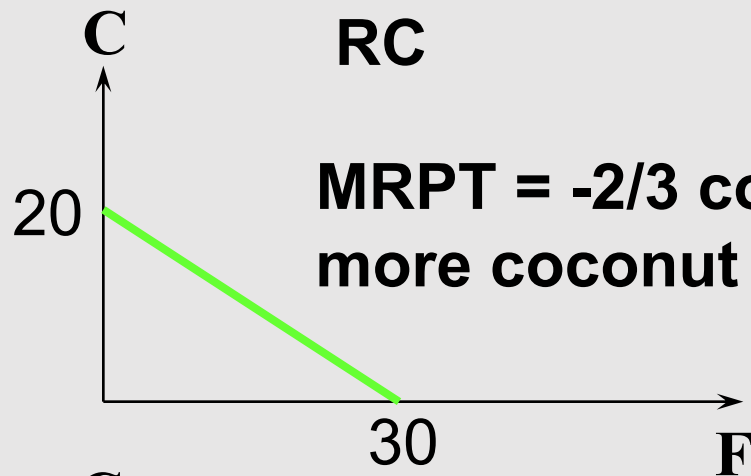
Comparative Advantage



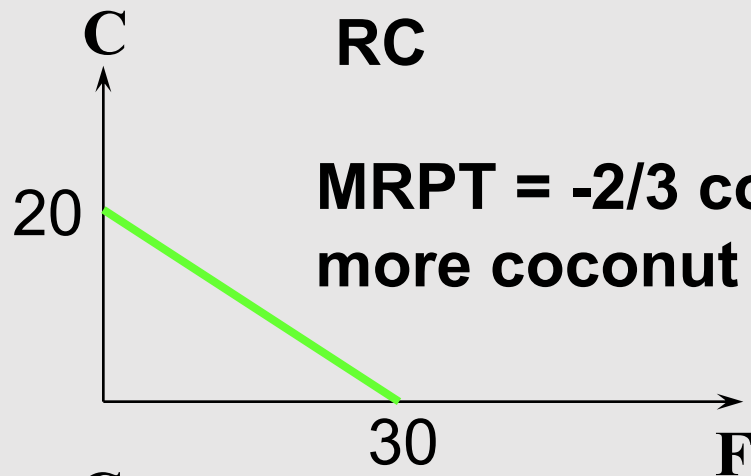
MRPT = $-2/3$ coconuts/fish so opp. cost of one more coconut is $3/2$ foregone fish.



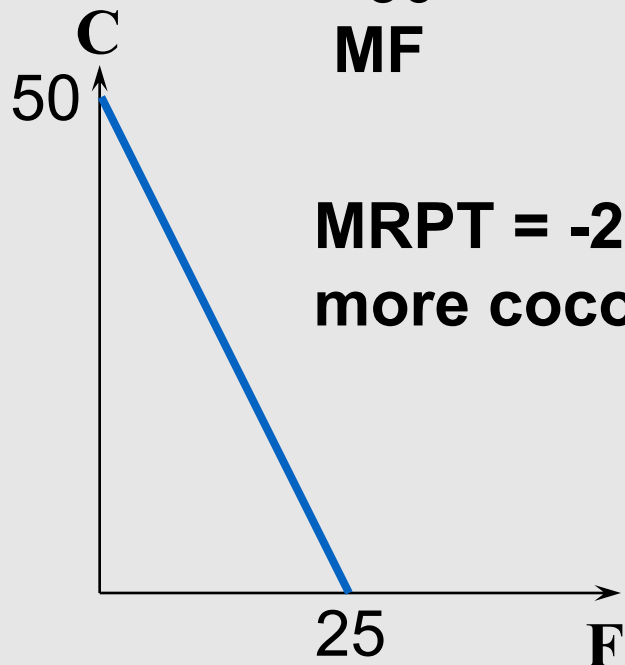
Comparative Advantage



Comparative Advantage



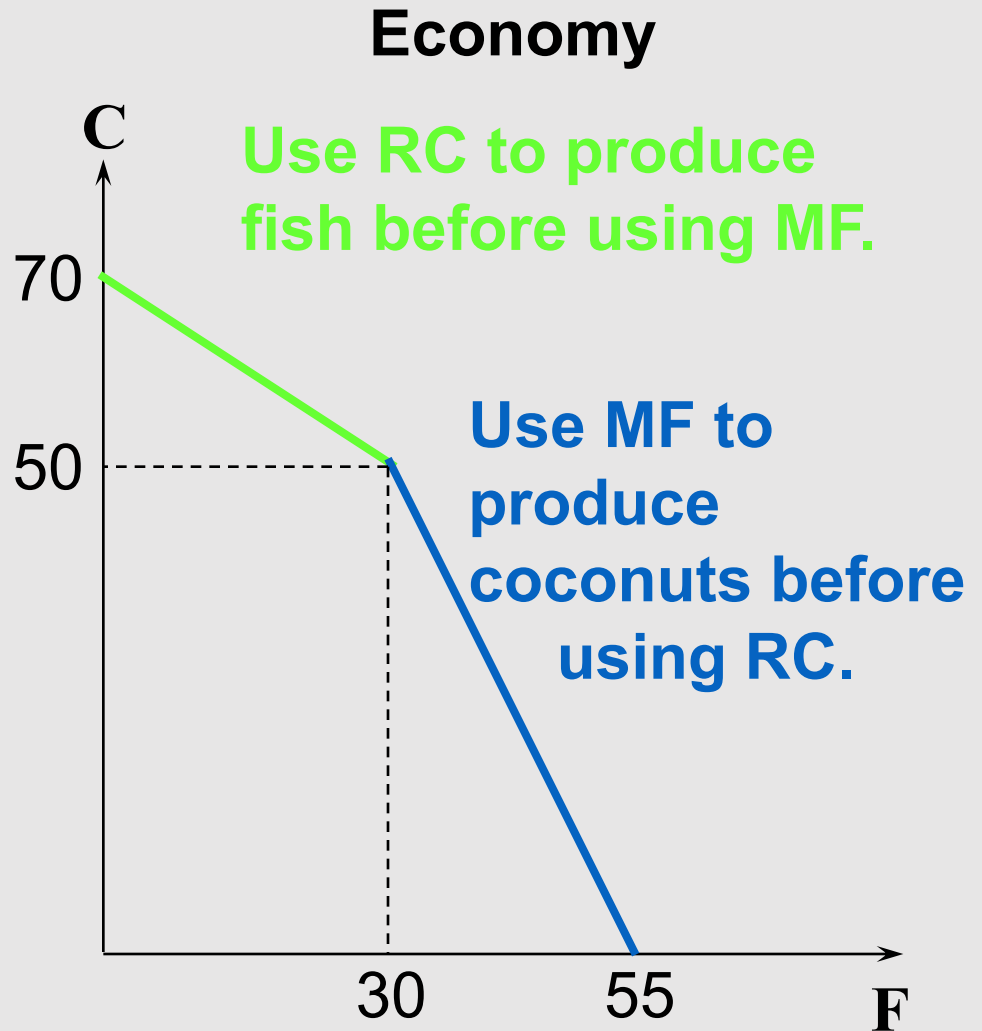
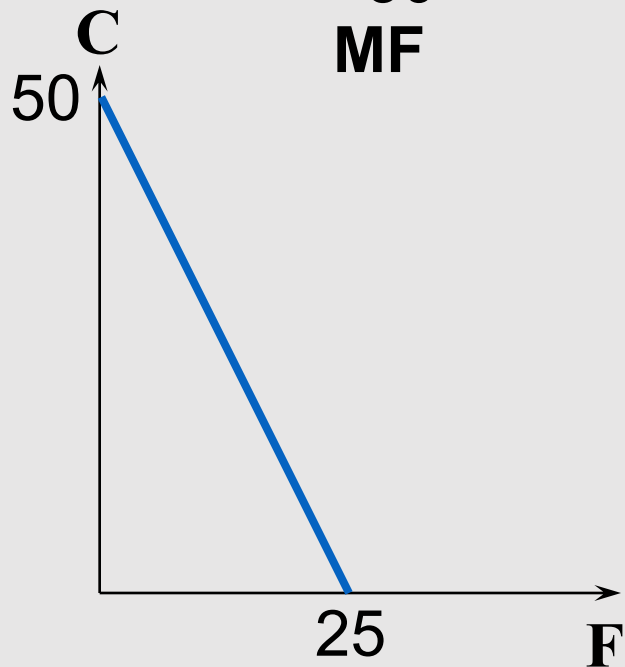
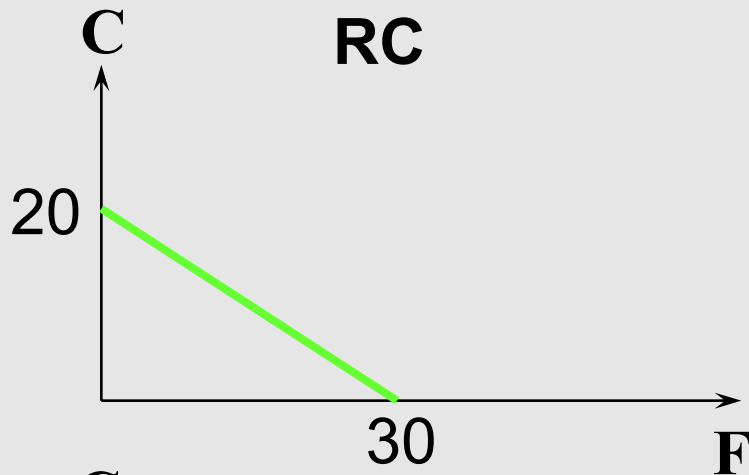
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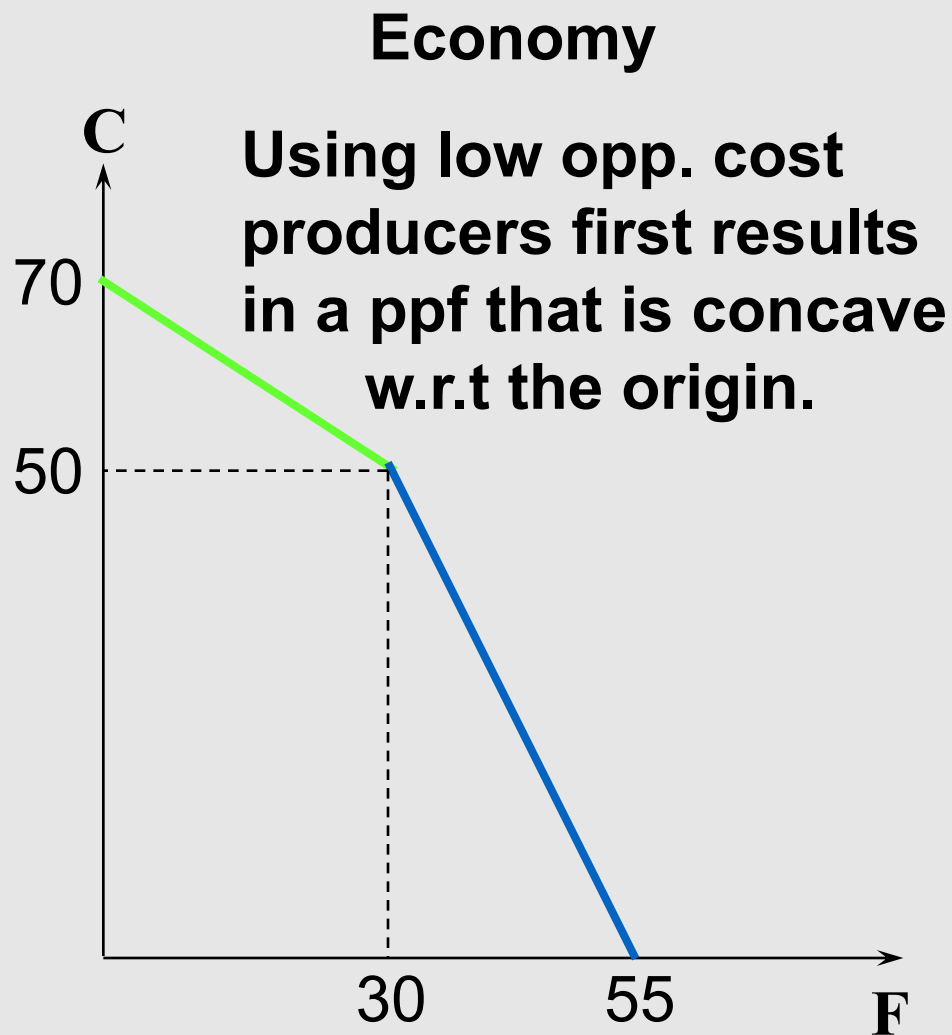
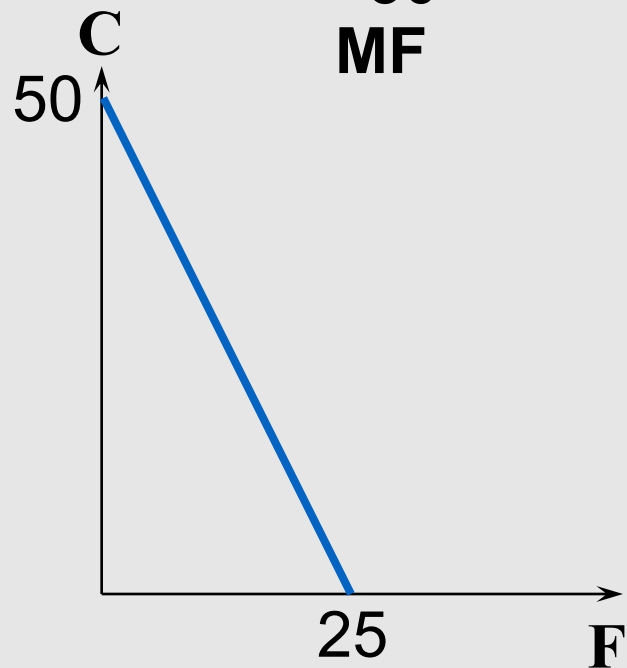
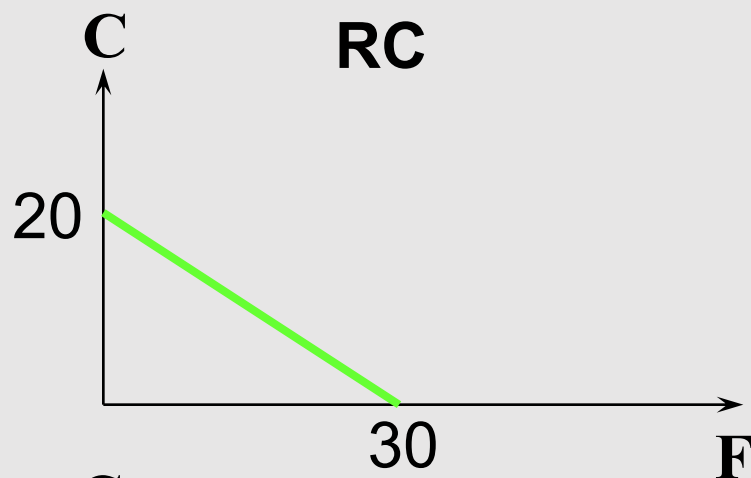
MRPT = -2 coconuts/fish so opp. cost of one more coconut is $1/2$ foregone fish.

MF has the comparative opp. cost advantage in producing coconuts.

Comparative Advantage



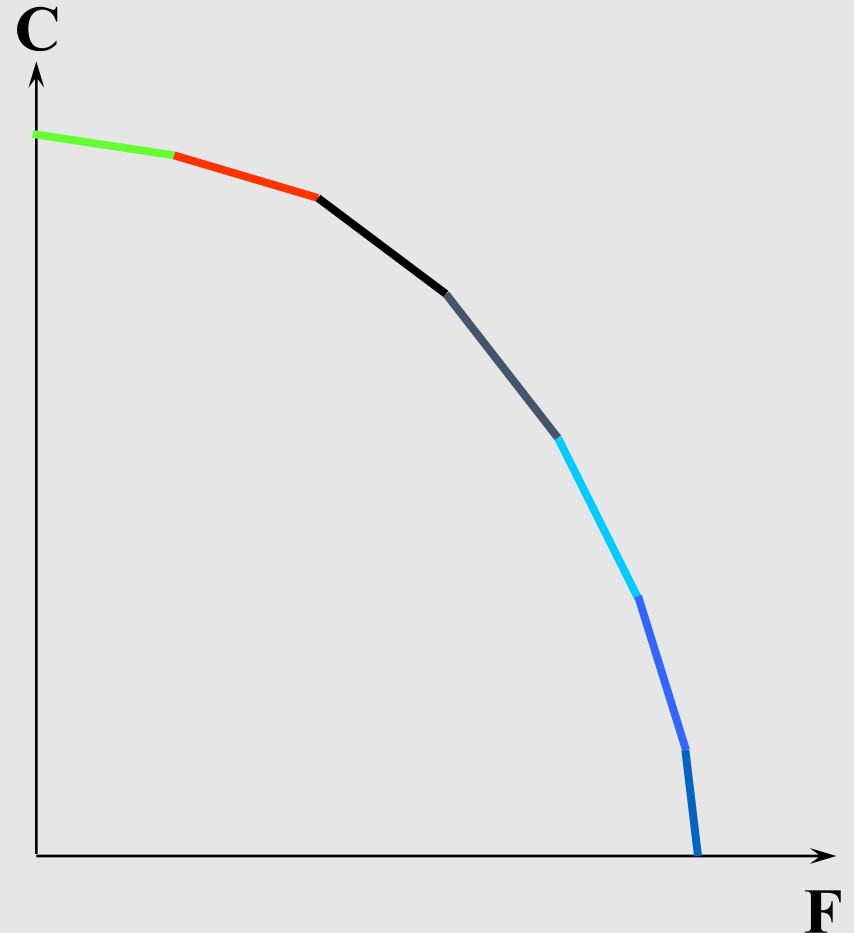
Comparative Advantage



Comparative Advantage

Economy

More producers with
different opp. costs
“smooth out” the ppf.

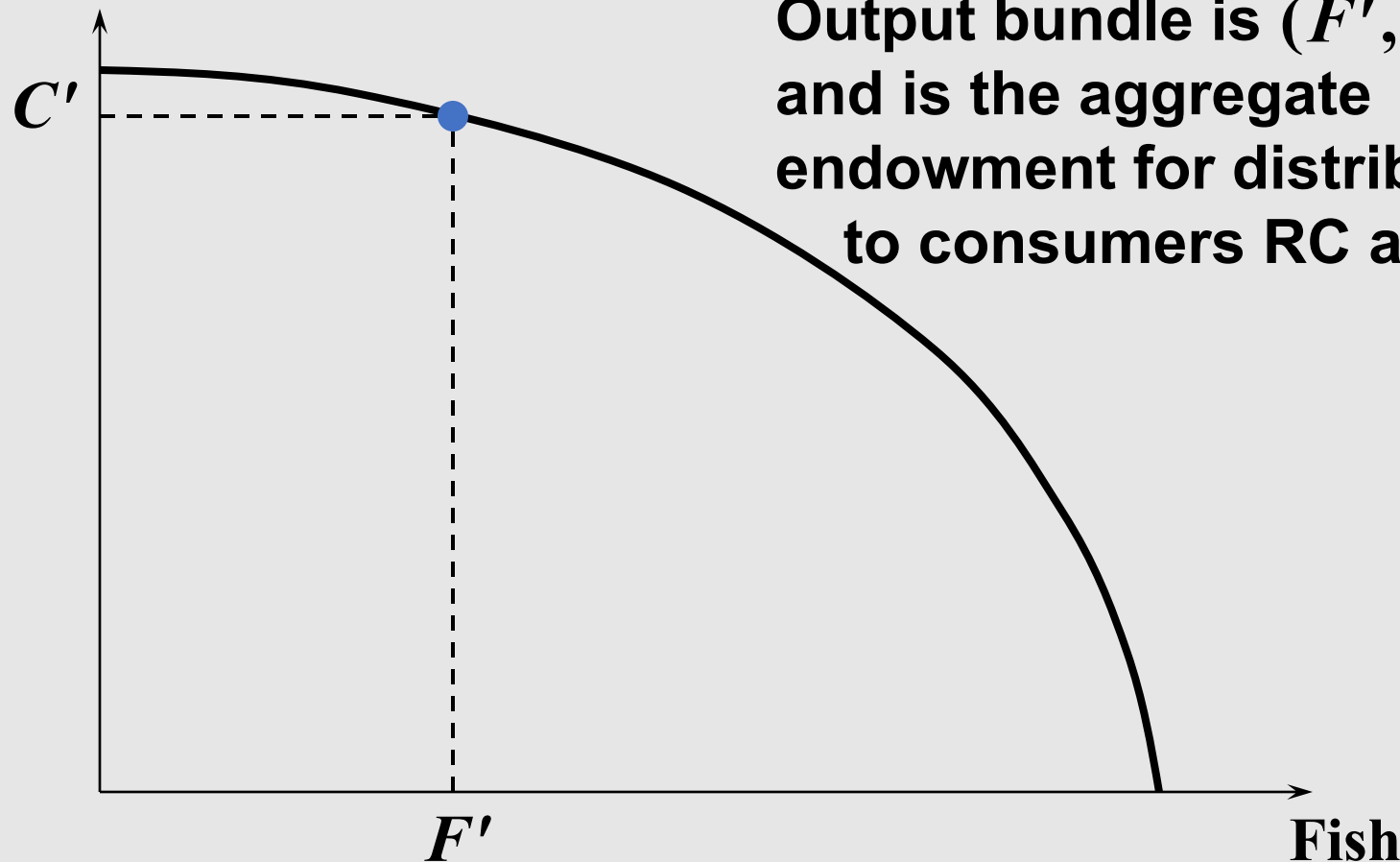


Coordinating Production & Consumption

- The ppf contains many technically efficient output bundles.
- Which are Pareto efficient for consumers?

Coordinating Production & Consumption

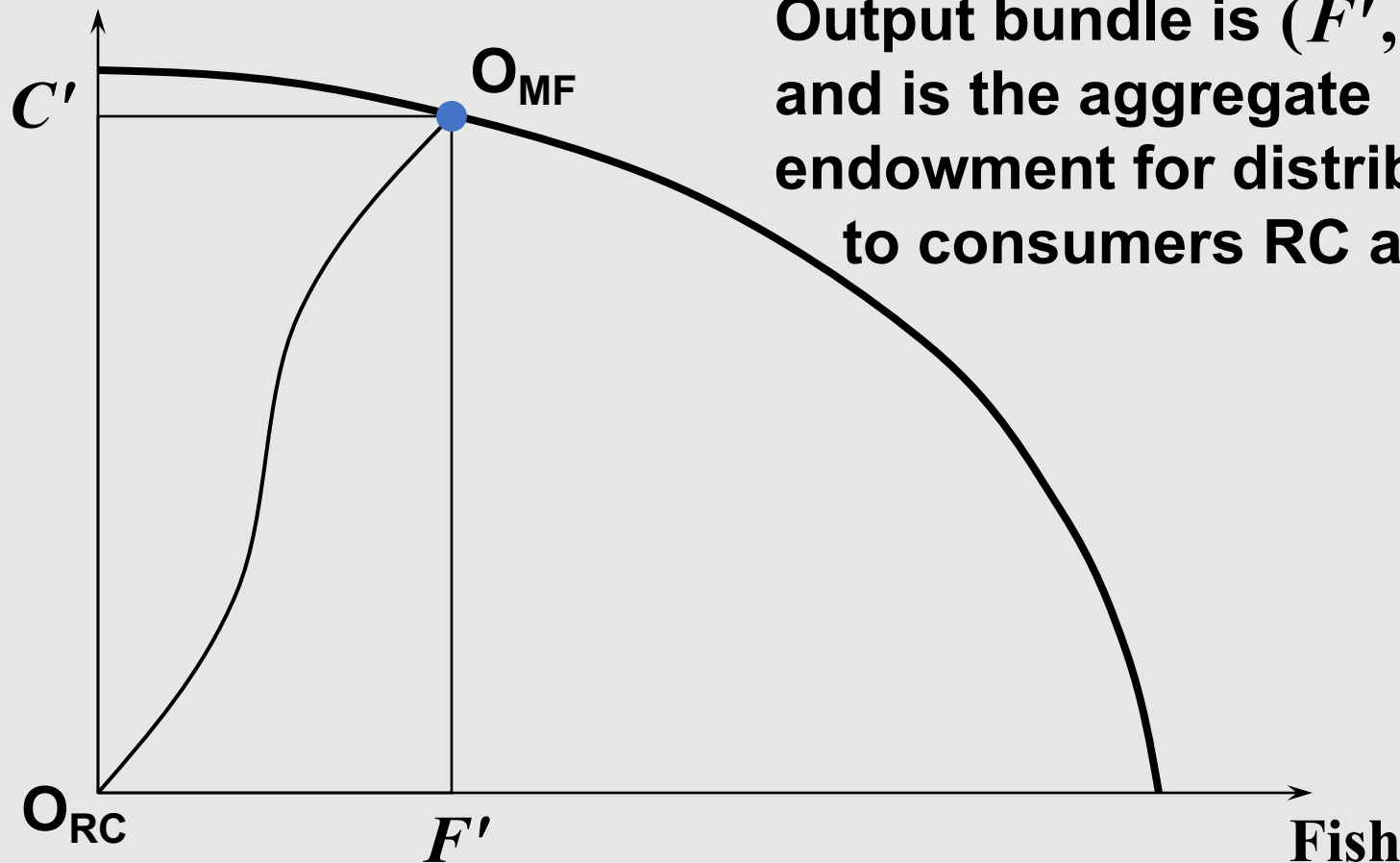
Coconuts



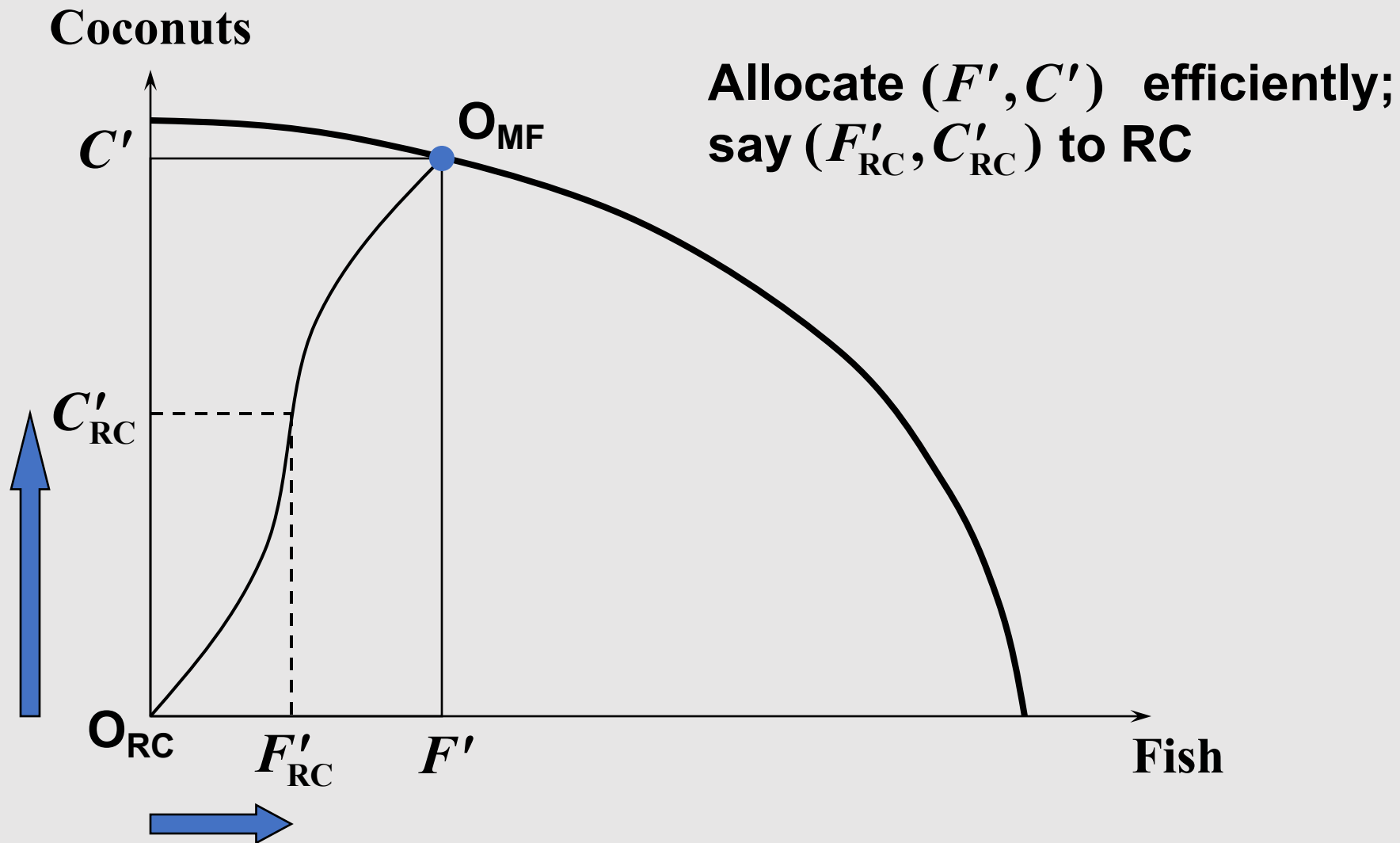
**Output bundle is (F', C')
and is the aggregate
endowment for distribution
to consumers RC and MF.**

Coordinating Production & Consumption

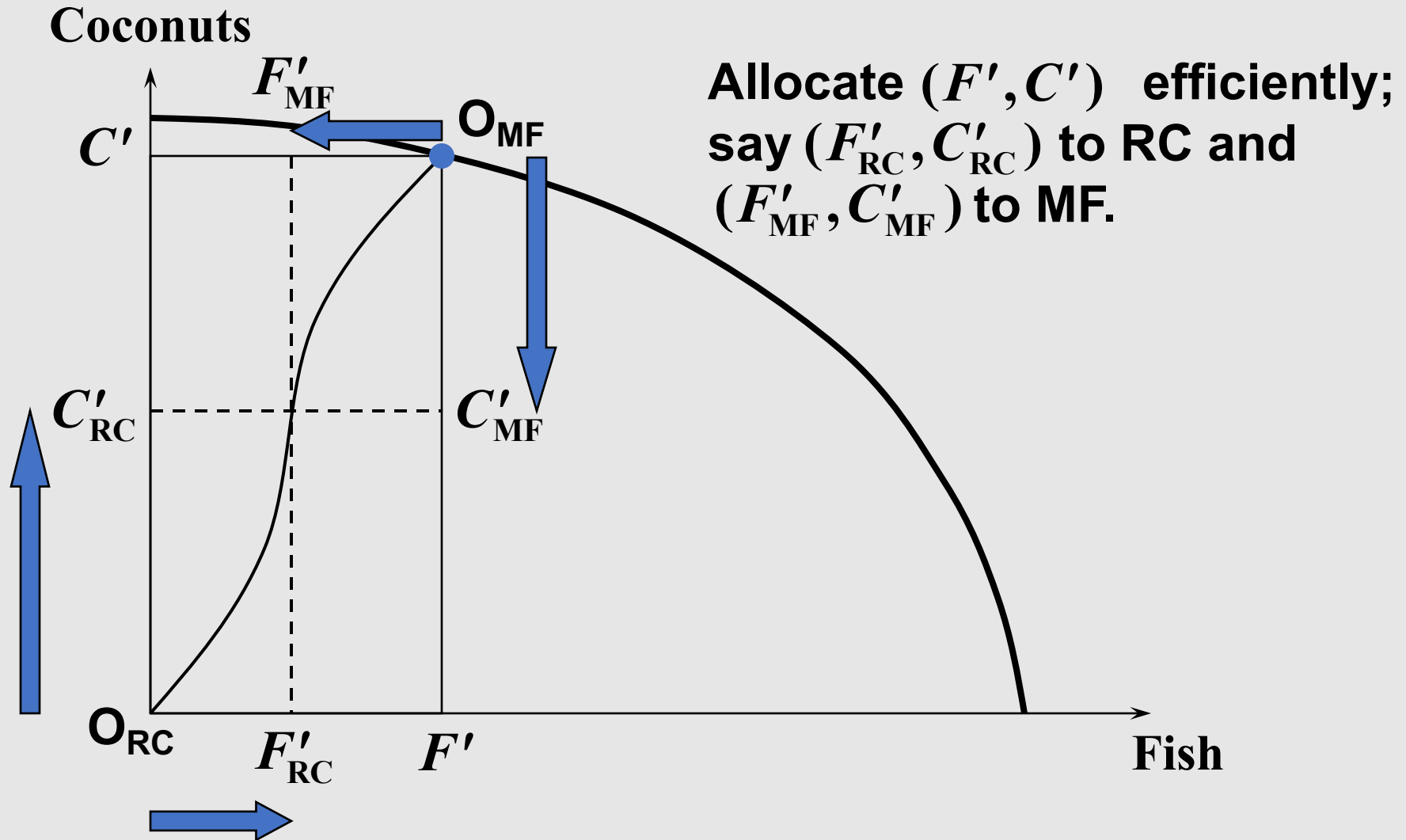
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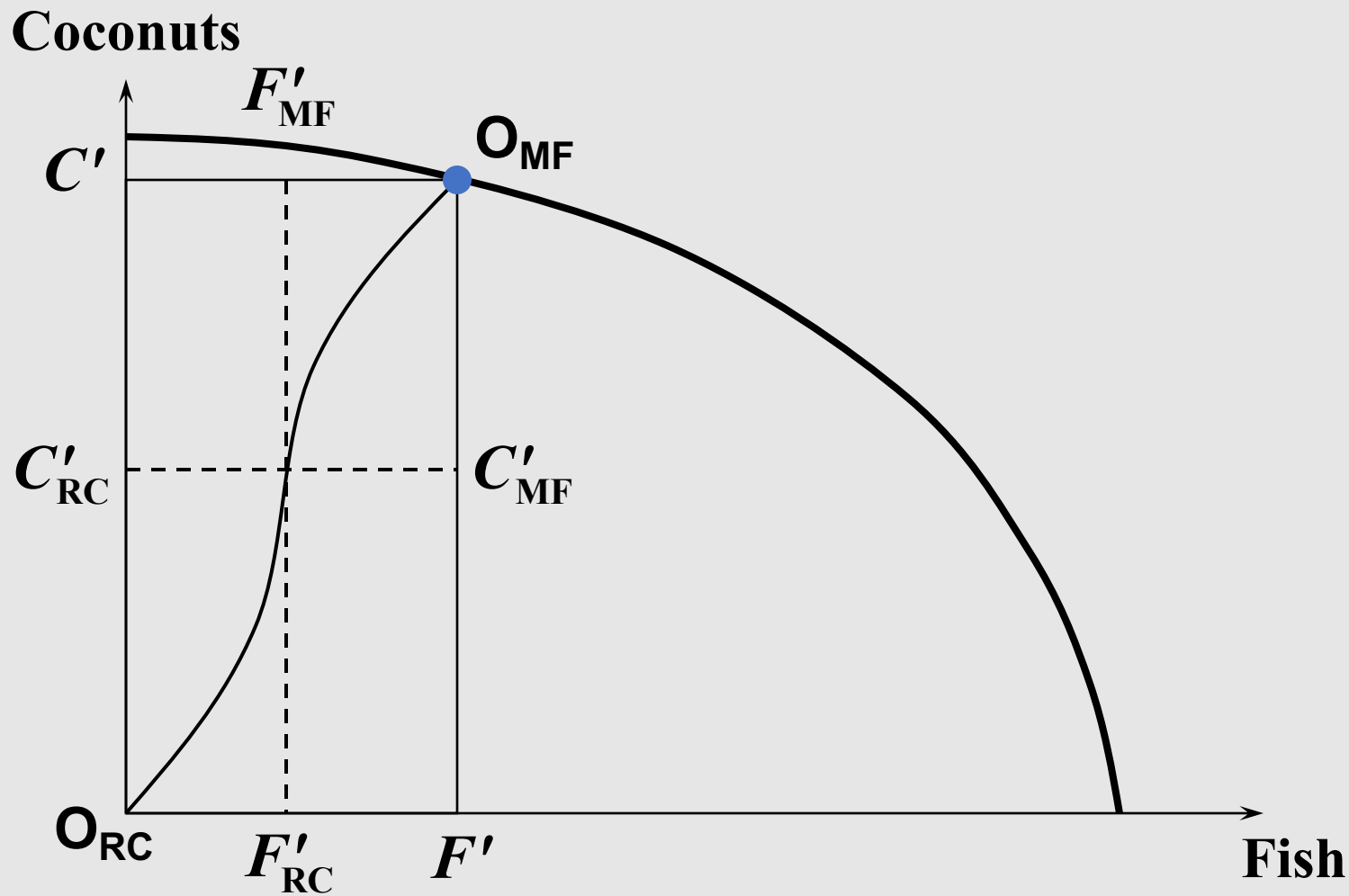
Coordinating Production & Consumption



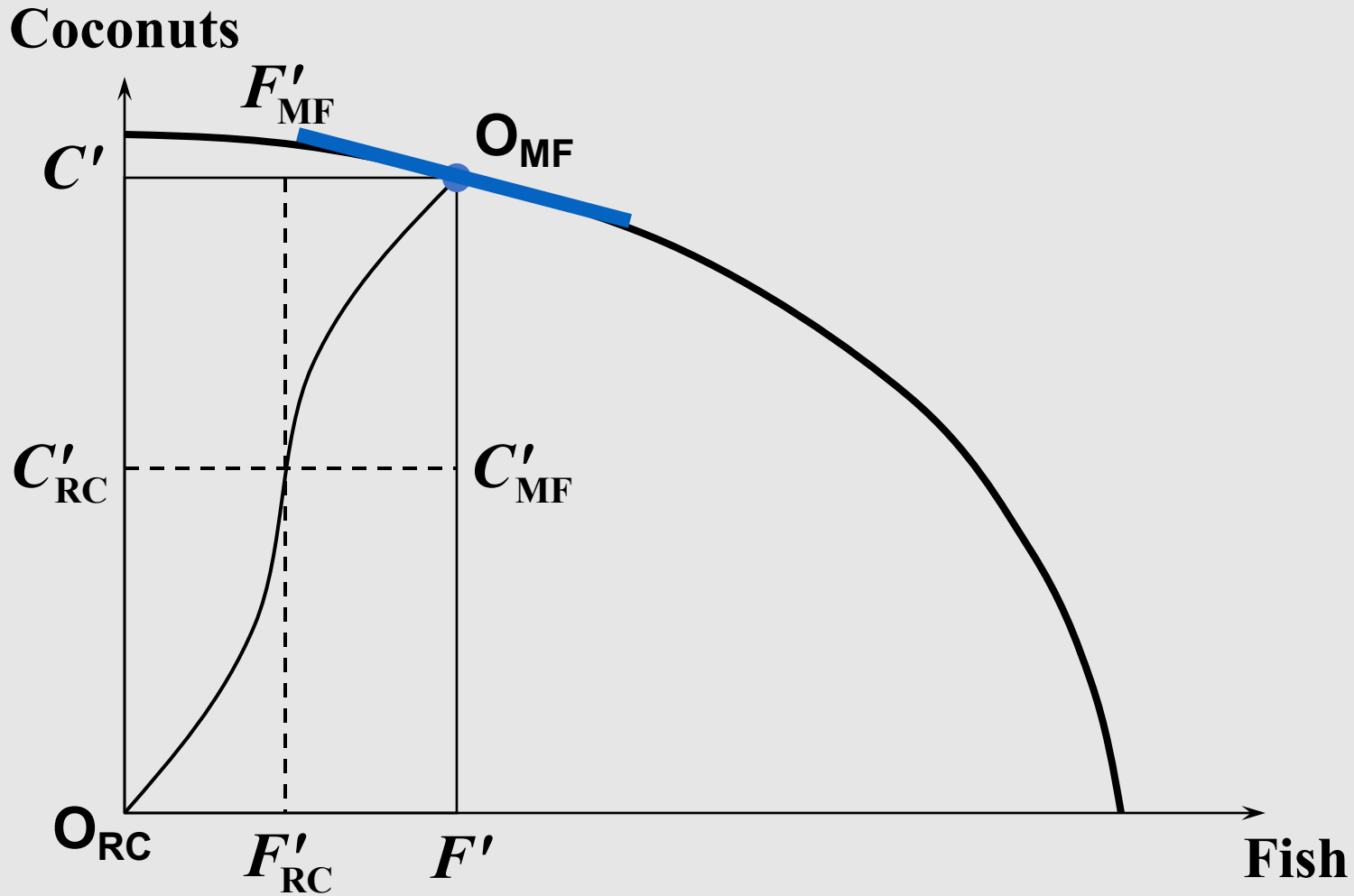
Coordinating Production & Consumption



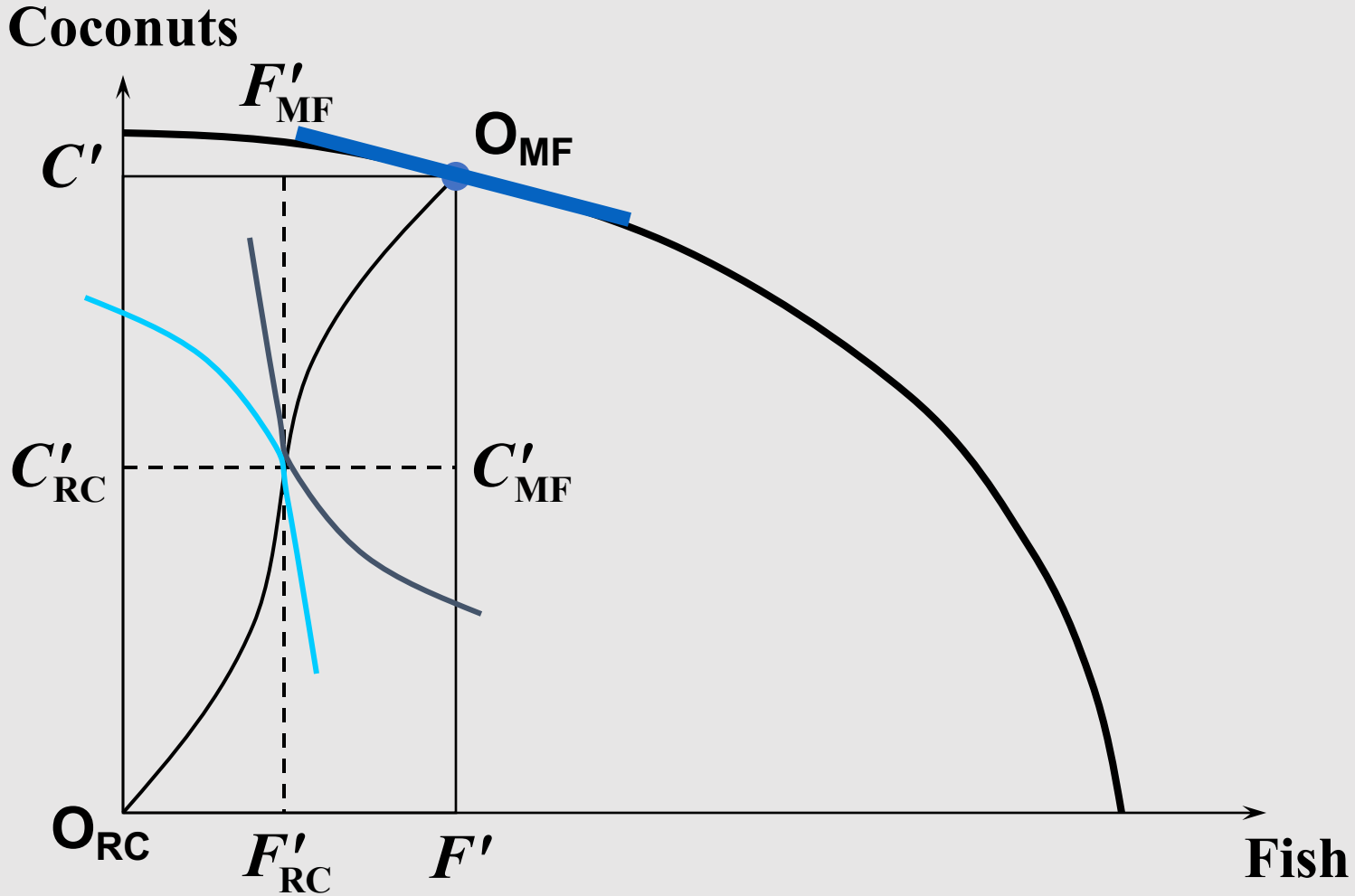
Coordinating Production & Consumption



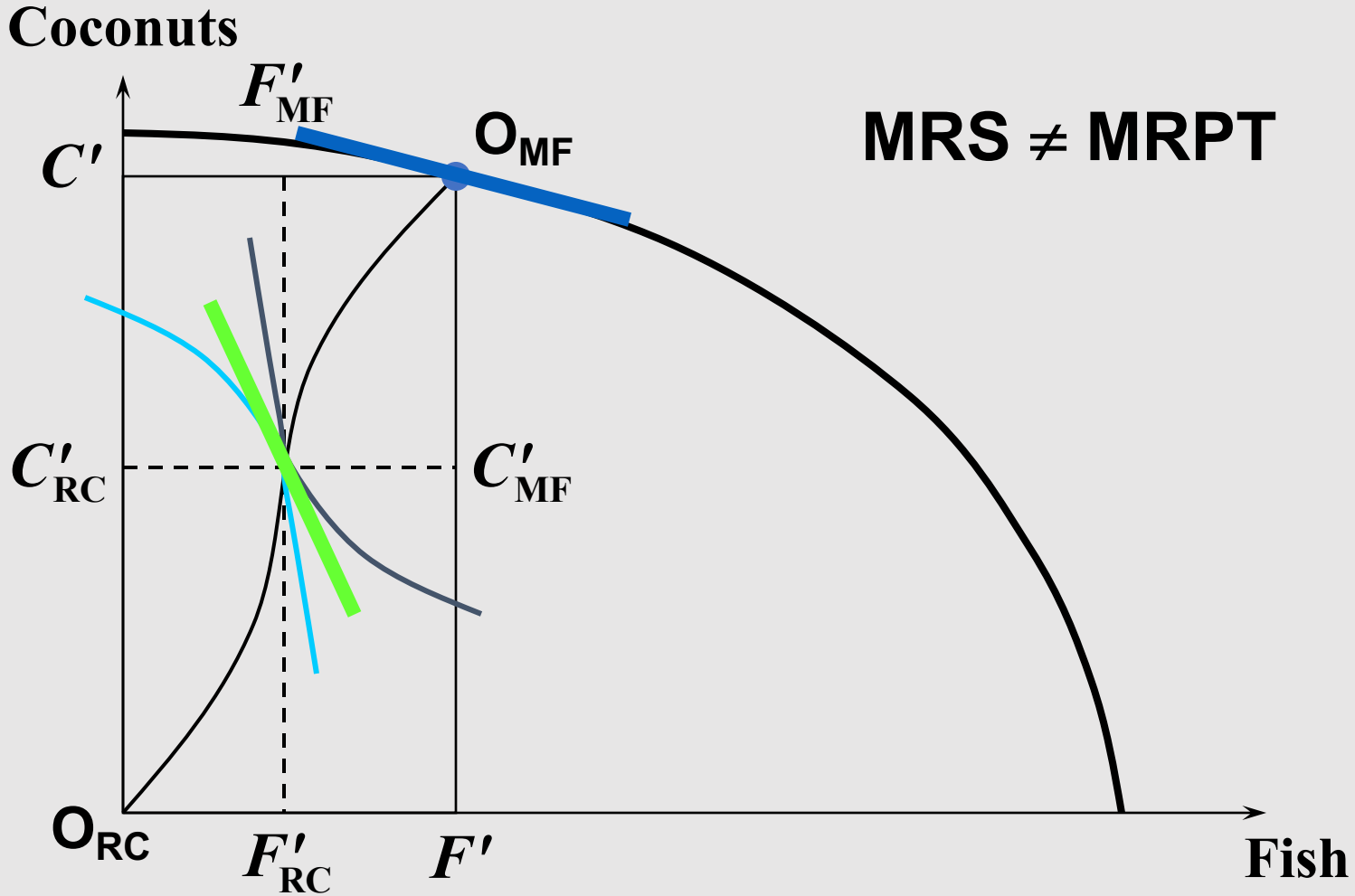
Coordinating Production & Consumption



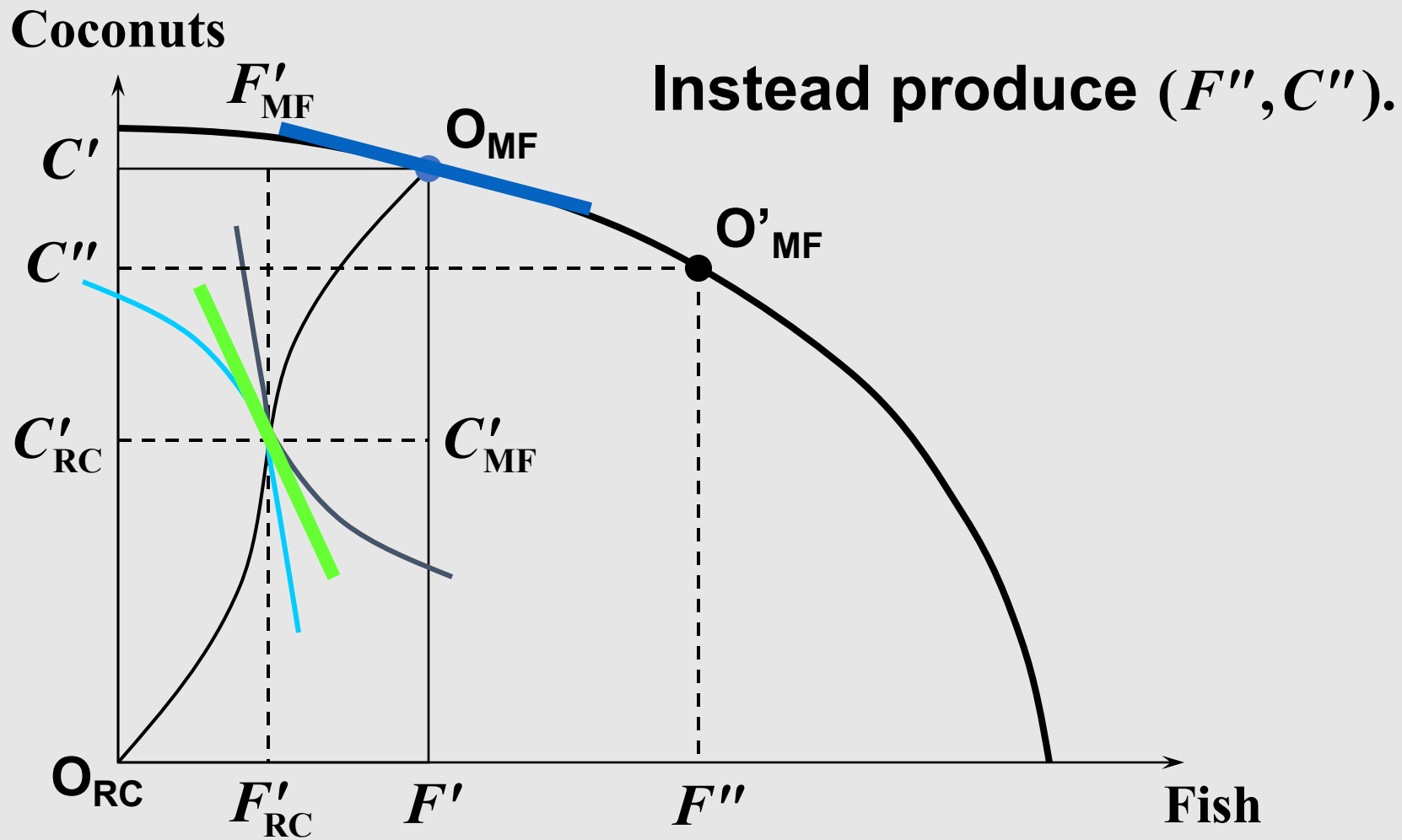
Coordinating Production & Consumption



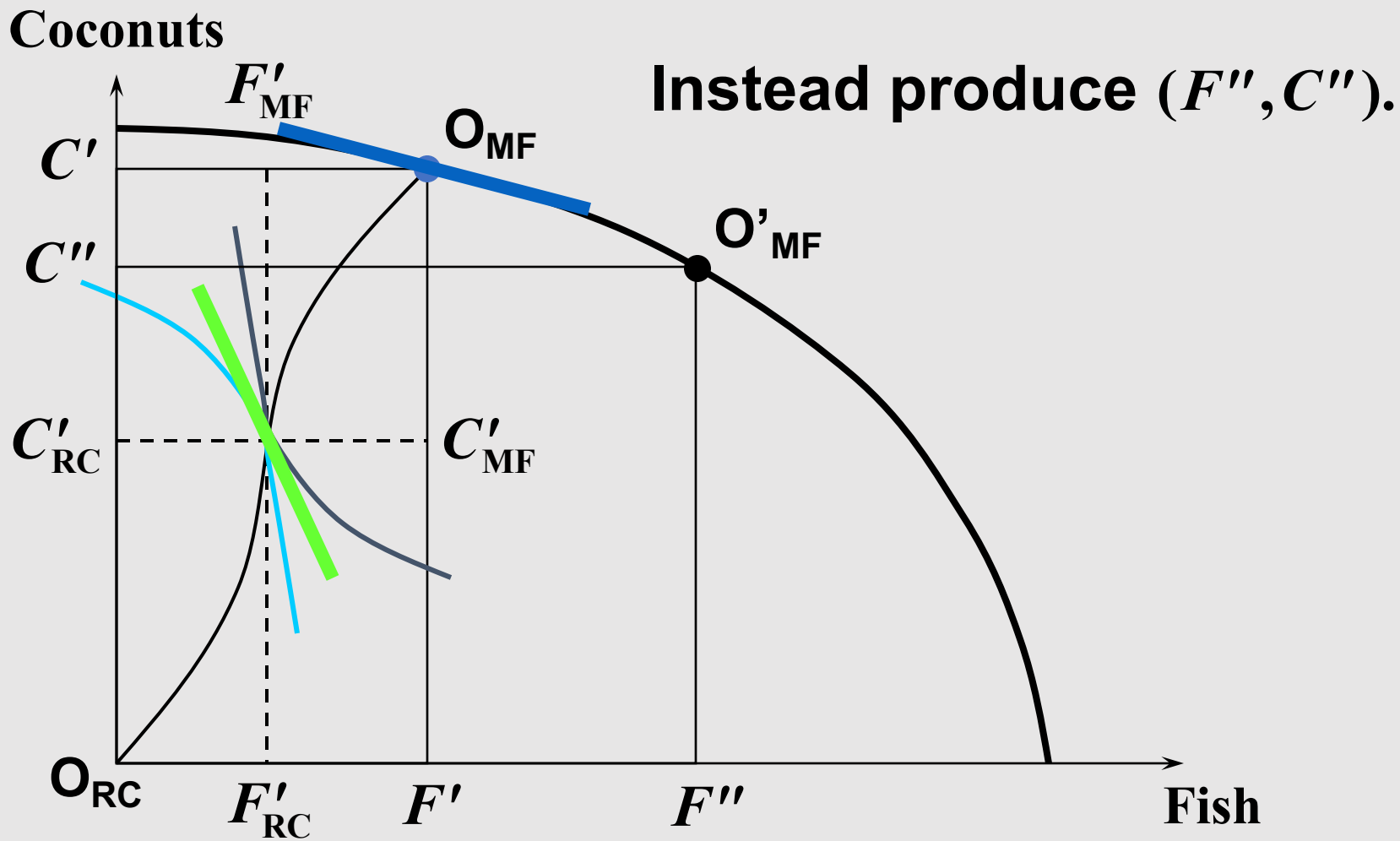
Coordinating Production & Consumption



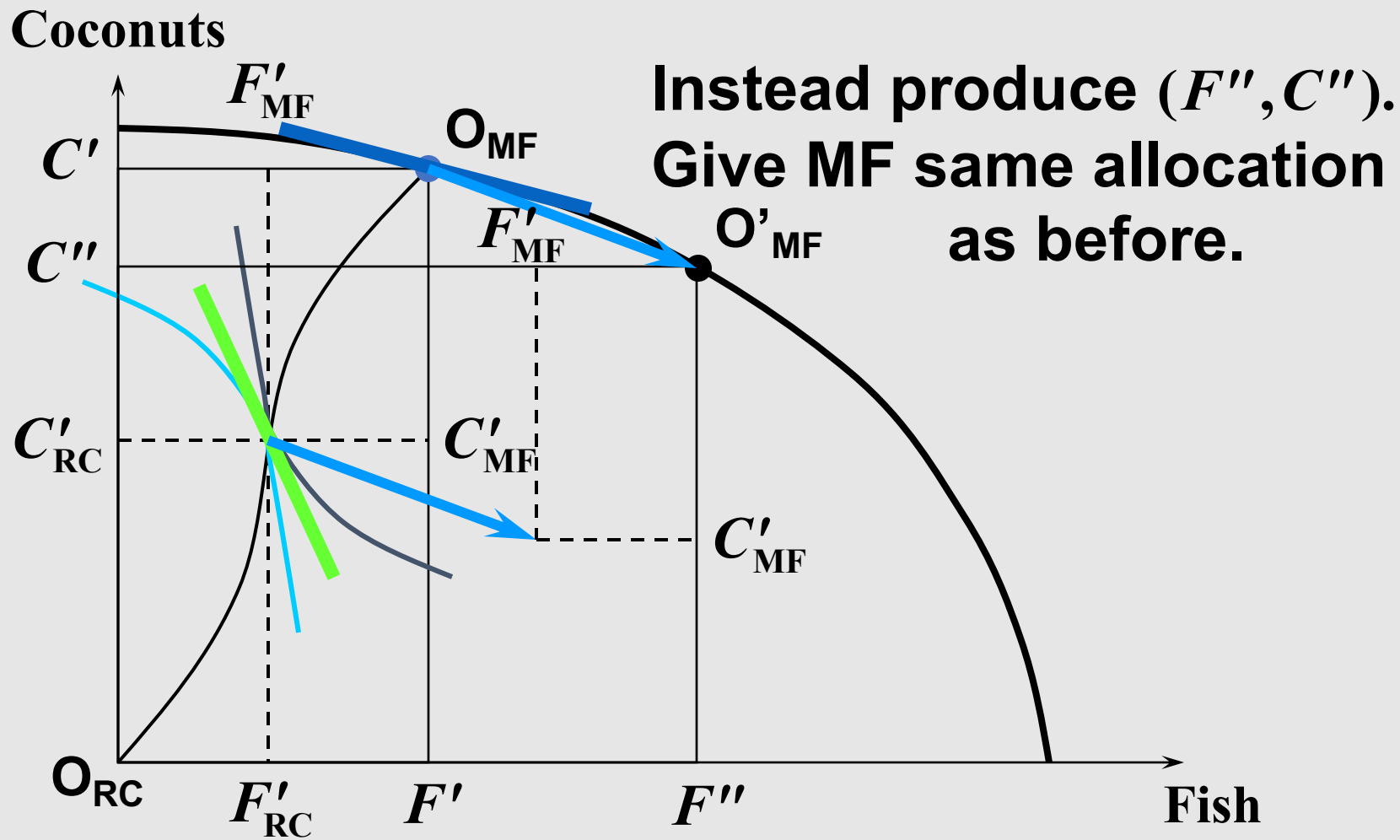
Coordinating Production & Consumption



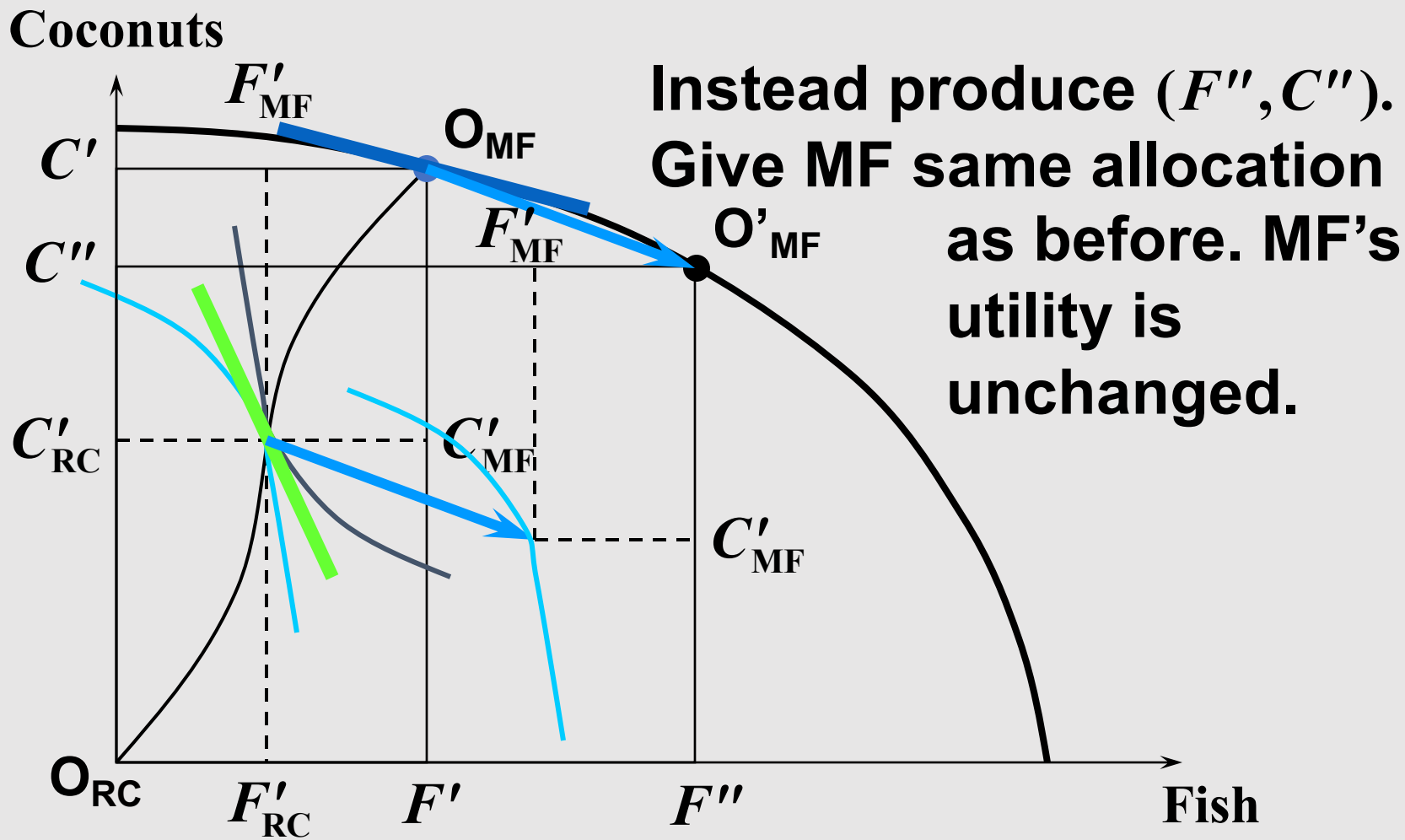
Coordinating Production & Consumption



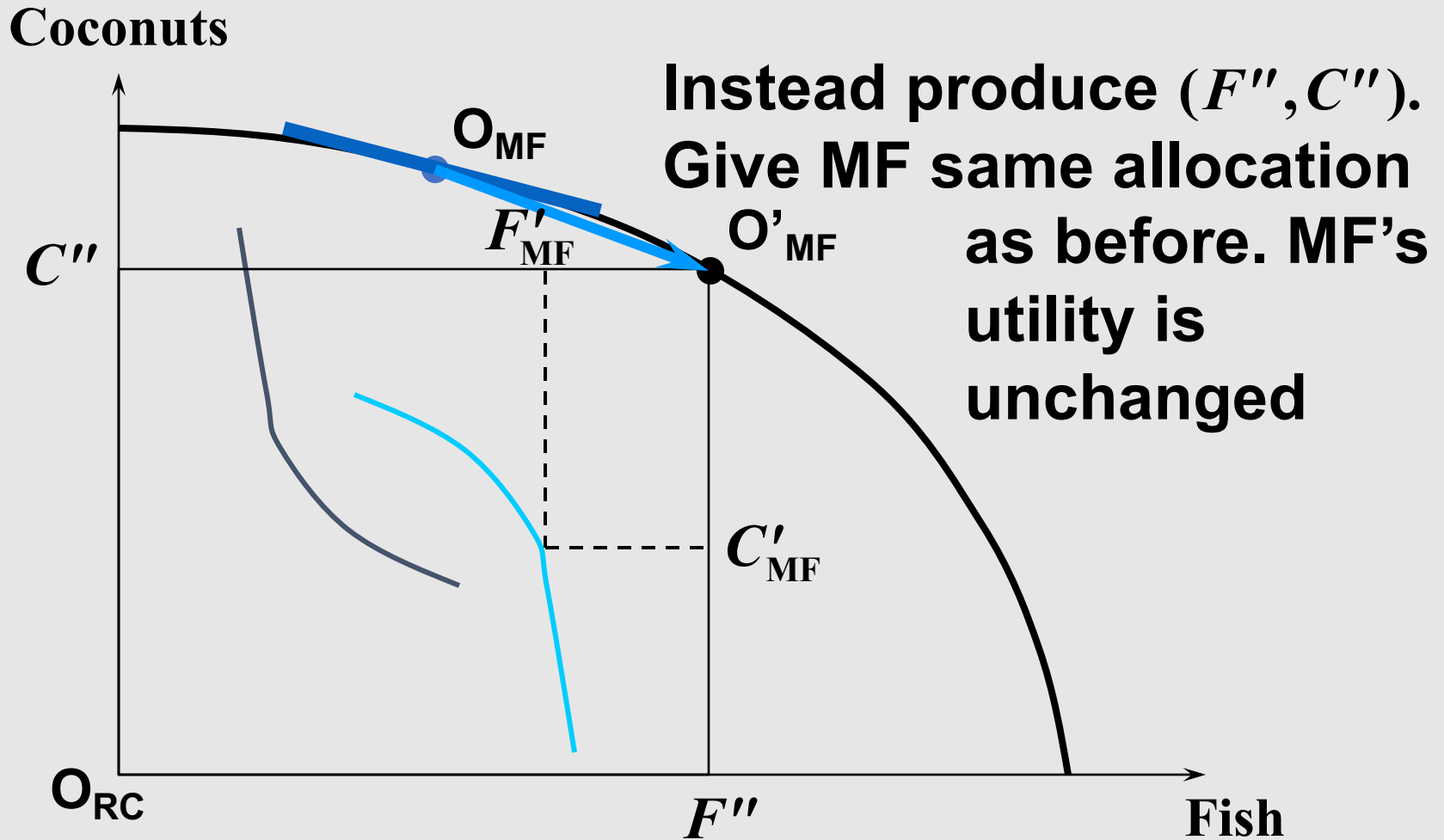
Coordinating Production & Consumption



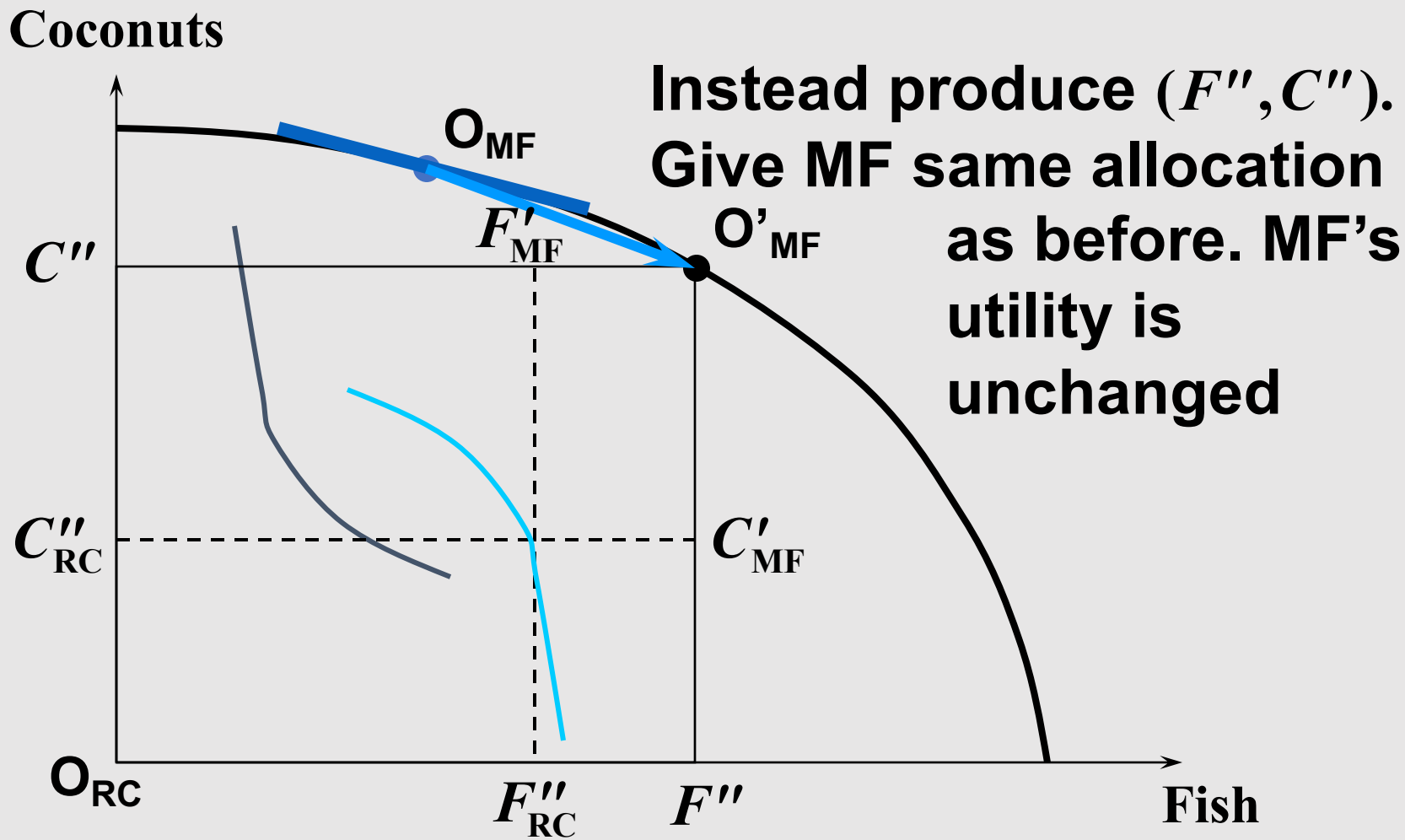
Coordinating Production & Consumption



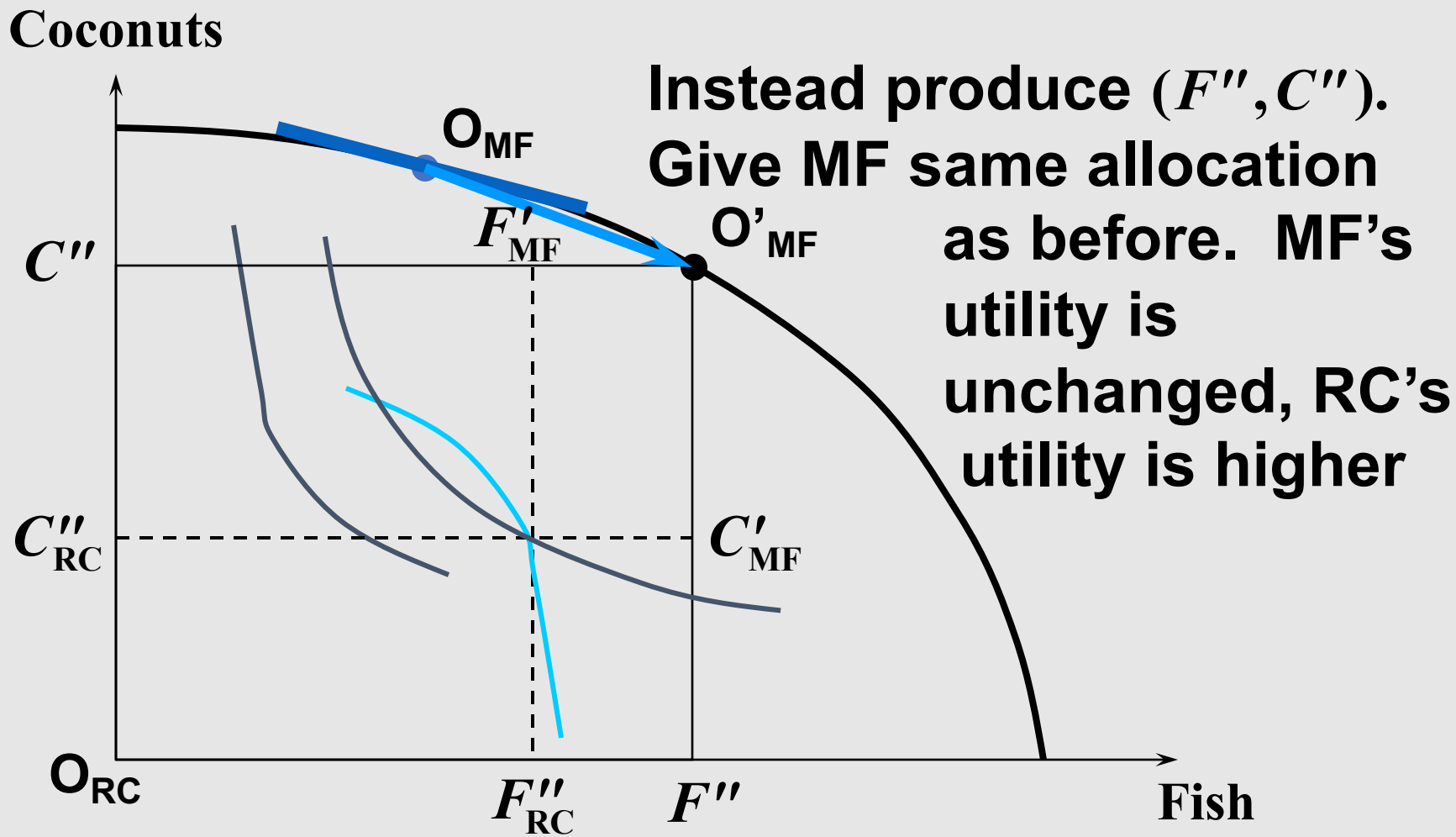
Coordinating Production & Consumption



Coordinating Production & Consumption

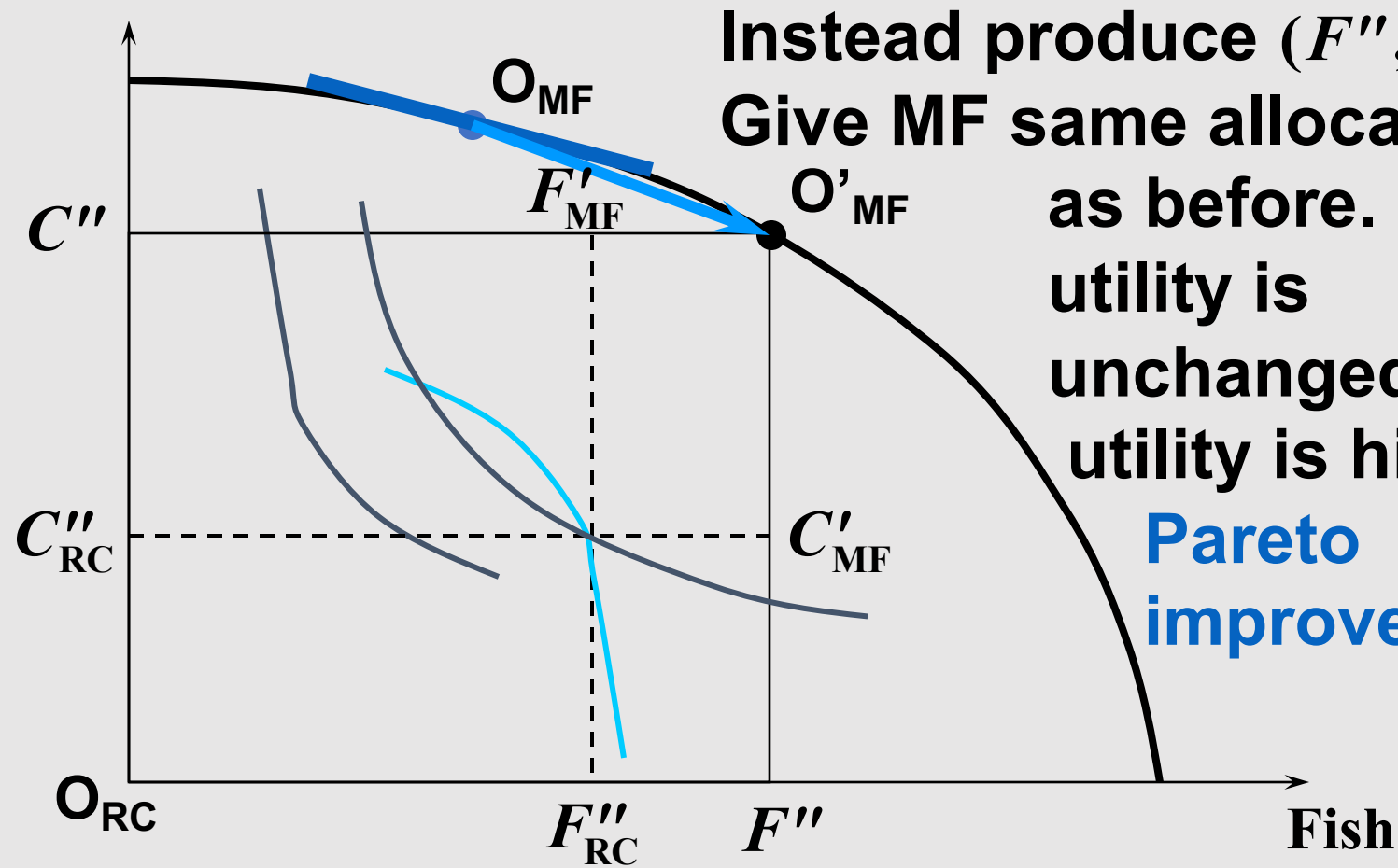


Coordinating Production & Consumption



Coordinating Production & Consumption

Coconuts

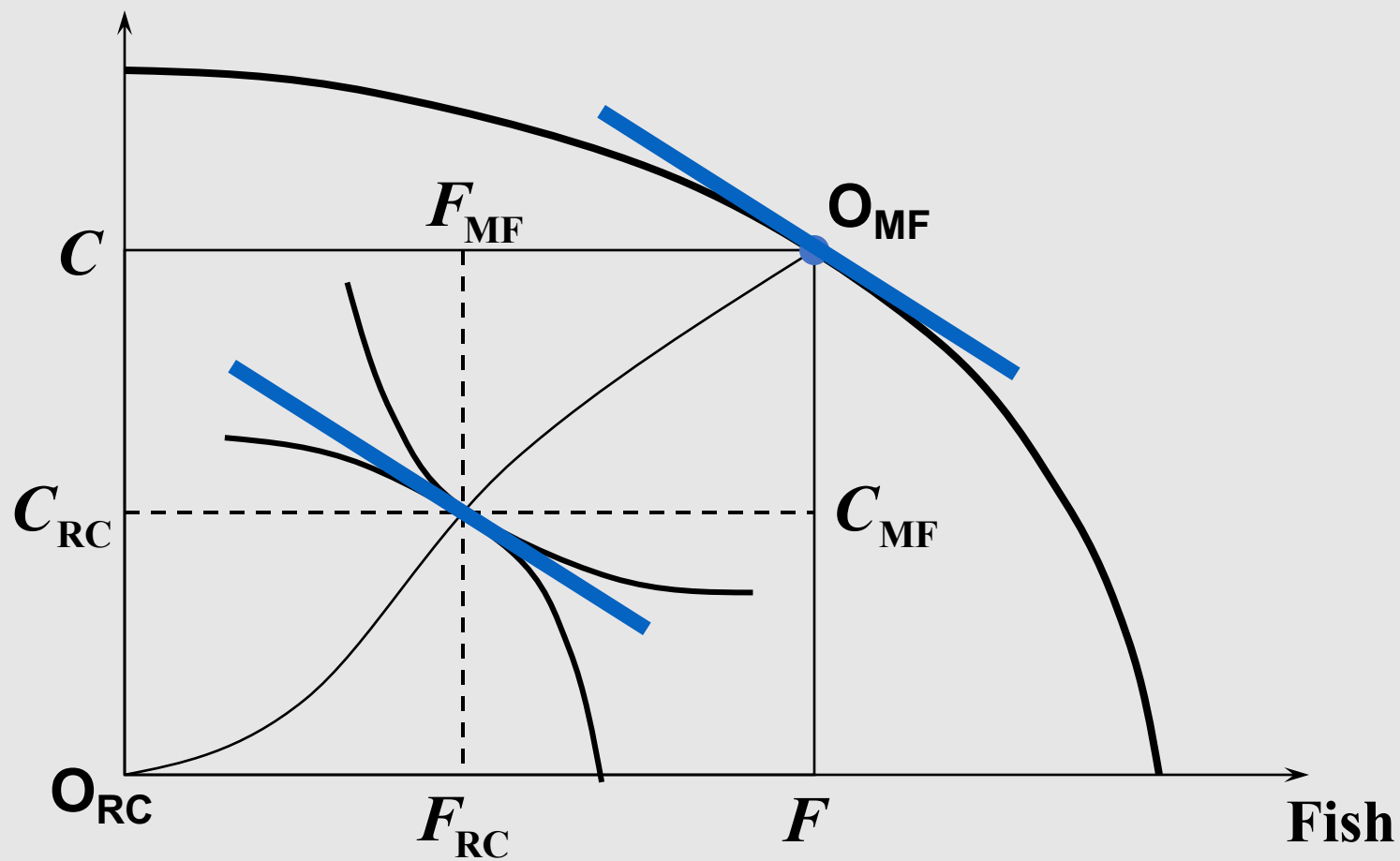


Coordinating Production & Consumption

- $MRS \neq MRPT \Rightarrow$ inefficient coordination of production and consumption.
- Hence, $MRS = MRPT$ is necessary for a Pareto optimal economic state.

Coordinating Production & Consumption

Coconuts



Decentralized Coordination of Production & Consumption

- RC and MF jointly run a firm producing coconuts and fish.
- RC and MF are also consumers who can sell labor.
- Price of coconut = p_C .
- Price of fish = p_F .
- RC's wage rate = w_{RC} .
- MF's wage rate = w_{MF} .

Decentralized Coordination of Production & Consumption

- L_{RC} , L_{MF} are amounts of labor purchased from RC and MF.
- F irm's profit-maximization problem is choose C , F , L_{RC} and L_{MF} to

$$\max \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}.$$

Decentralized Coordination of Production & Consumption

$$\max \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}.$$

Isoprofit line equation is

$$\text{constant } \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}$$

Decentralized Coordination of Production & Consumption

$$\max \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}.$$

Isoprofit line equation is

$$\text{constant } \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}$$

which rearranges to

$$C = \frac{\pi + w_{RC} L_{RC} + w_{MF} L_{MF}}{p_C} - \frac{p_F}{p_C} F.$$

Decentralized Coordination of Production & Consumption

$$\max \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}.$$

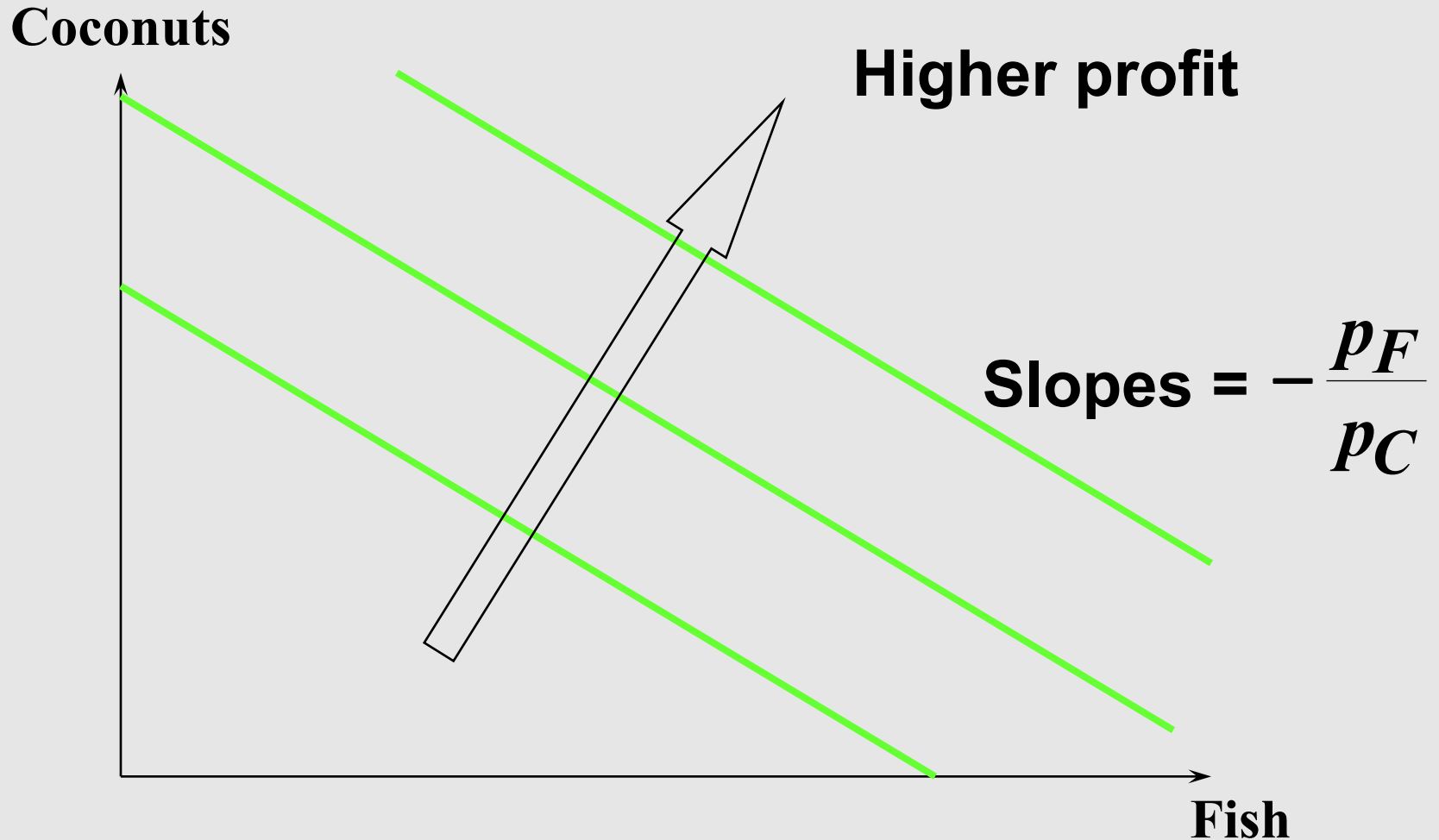
Isoprofit line equation is

$$\text{constant } \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}$$

which rearranges to

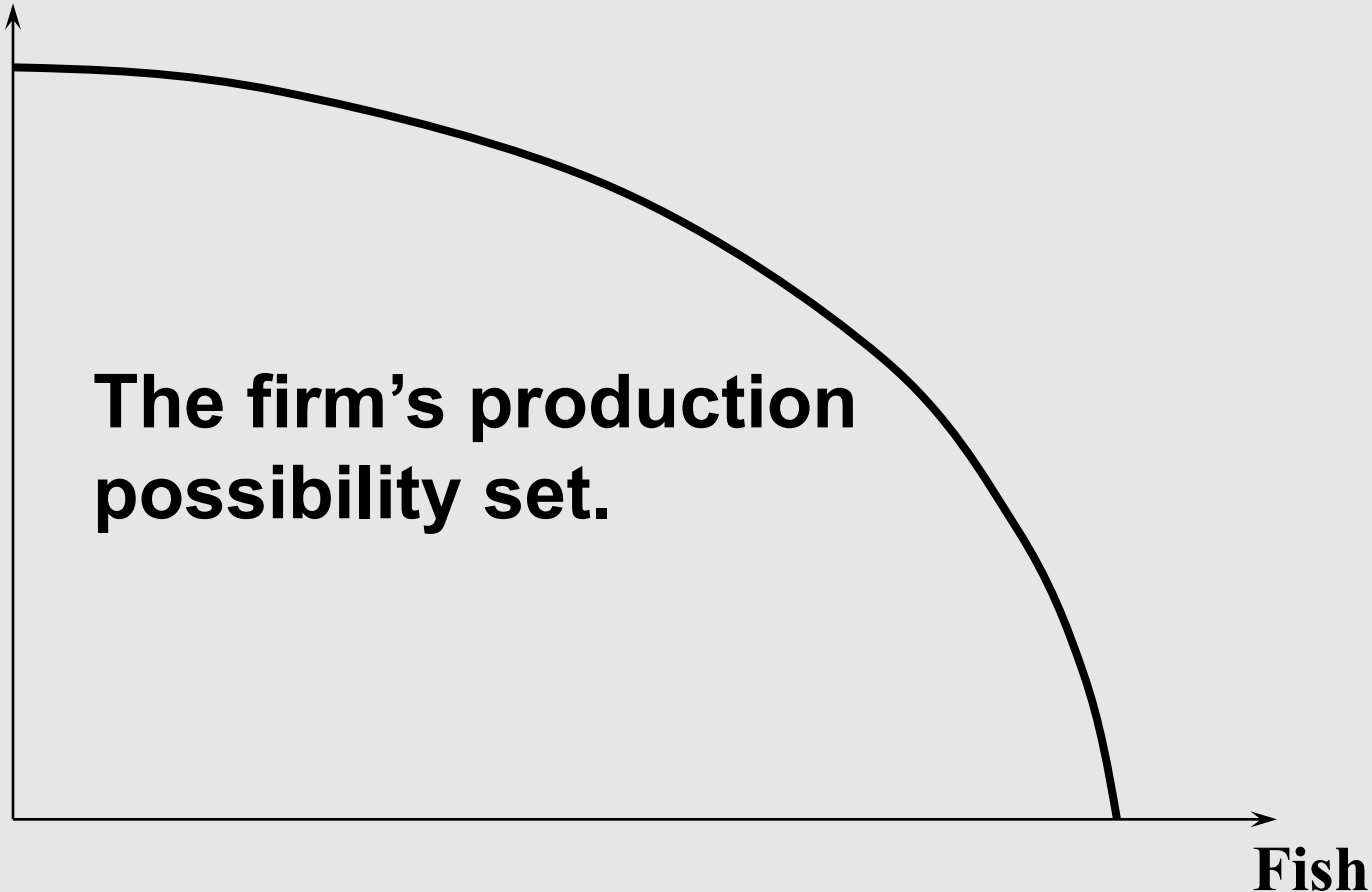
$$C = \underbrace{\frac{\pi + w_{RC} L_{RC} + w_{MF} L_{MF}}{p_C}}_{\text{Intercept}} - \underbrace{\frac{p_F}{p_C} F}_{\text{Slope}}.$$

Decentralized Coordination of Production & Consumption



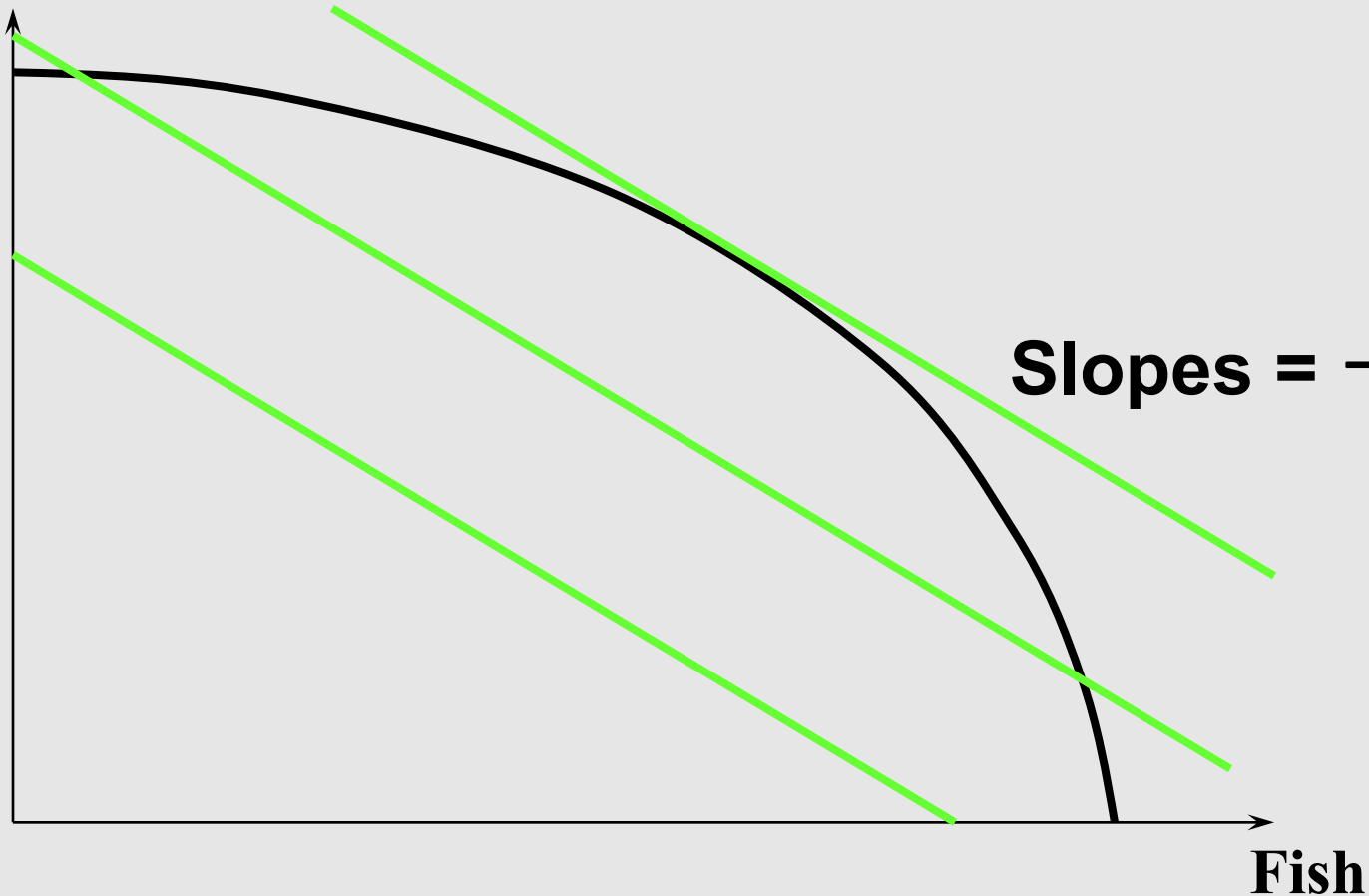
Decentralized Coordination of Production & Consumption

Coconuts

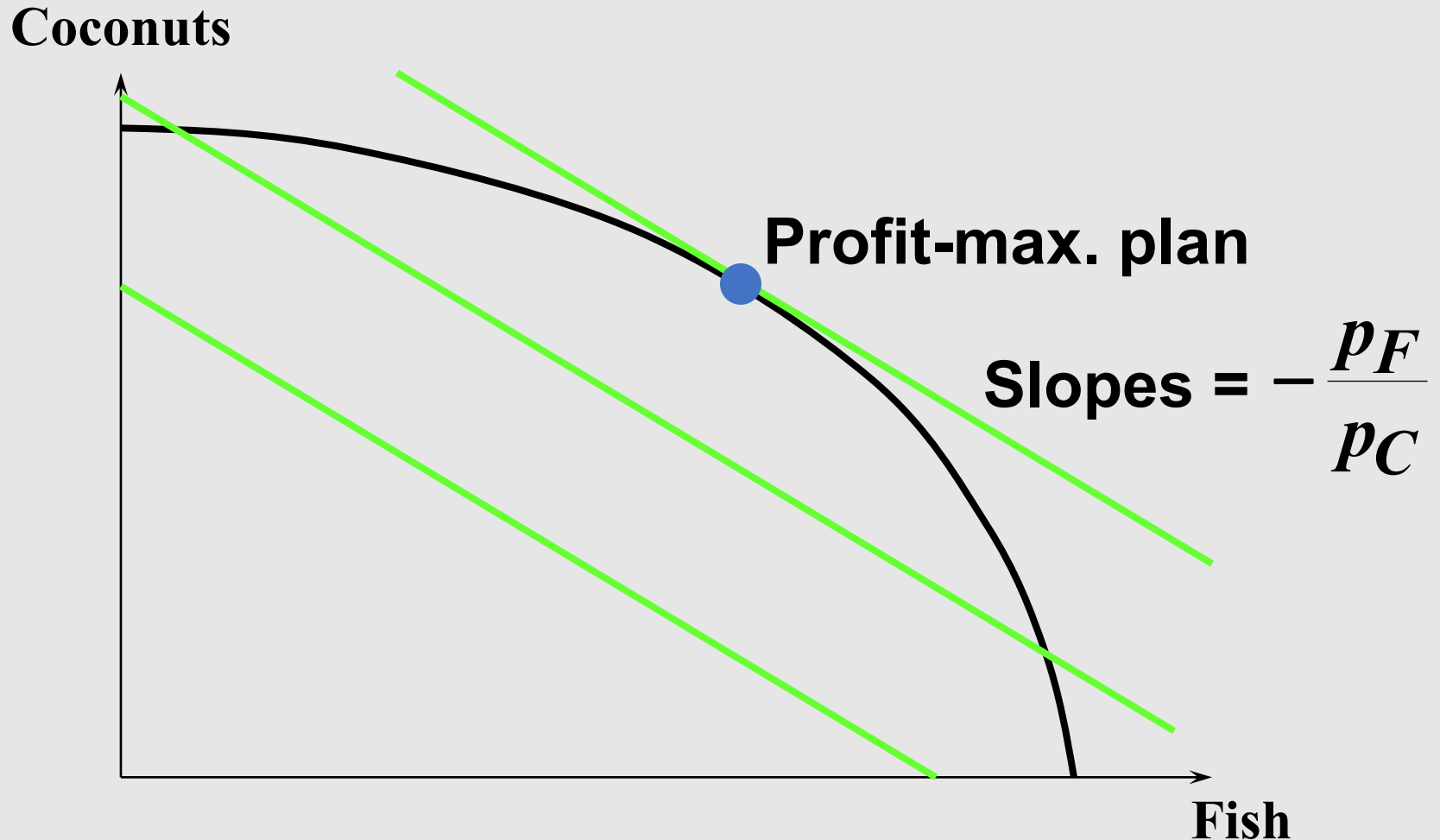


Decentralized Coordination of Production & Consumption

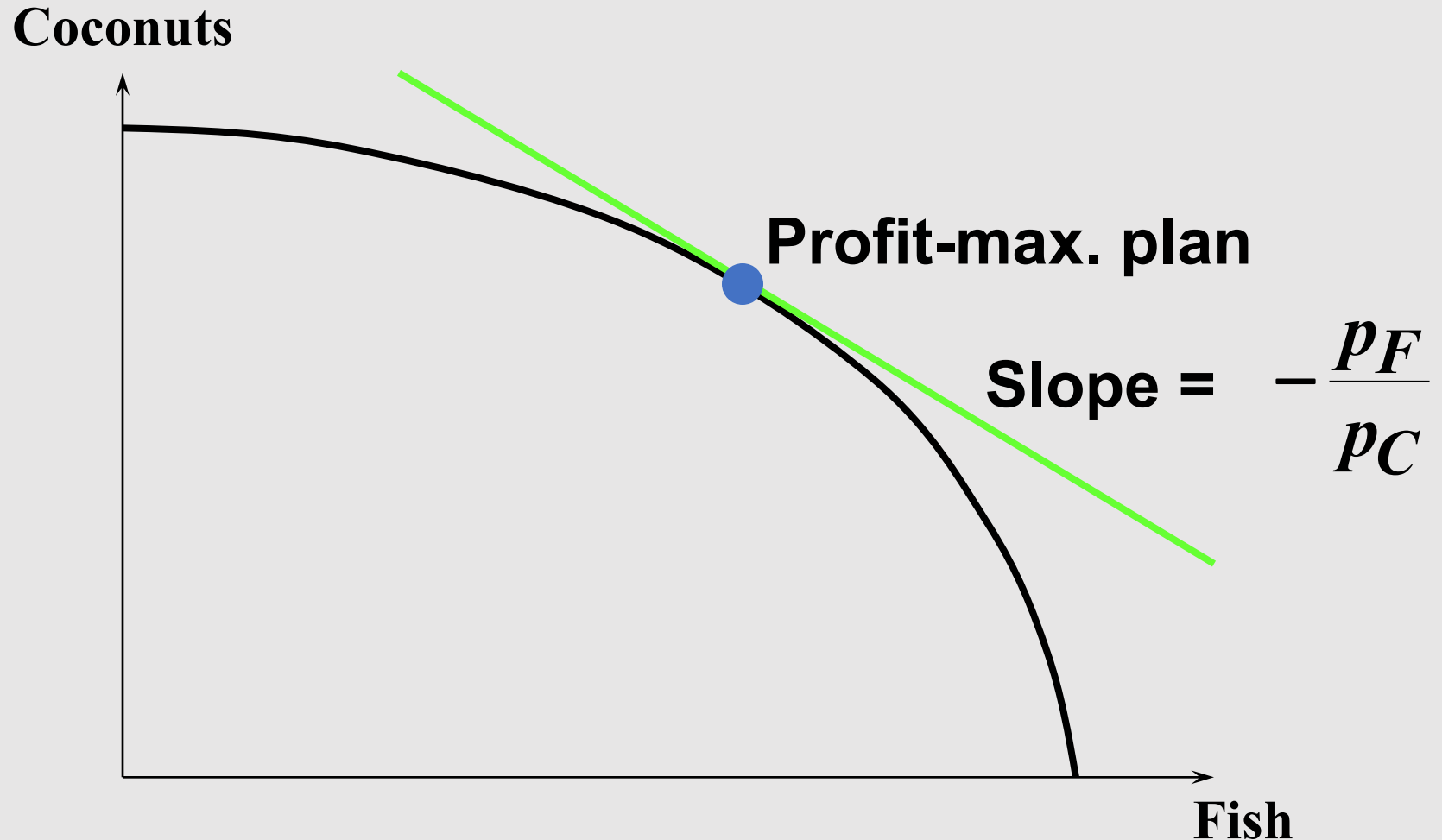
Coconuts



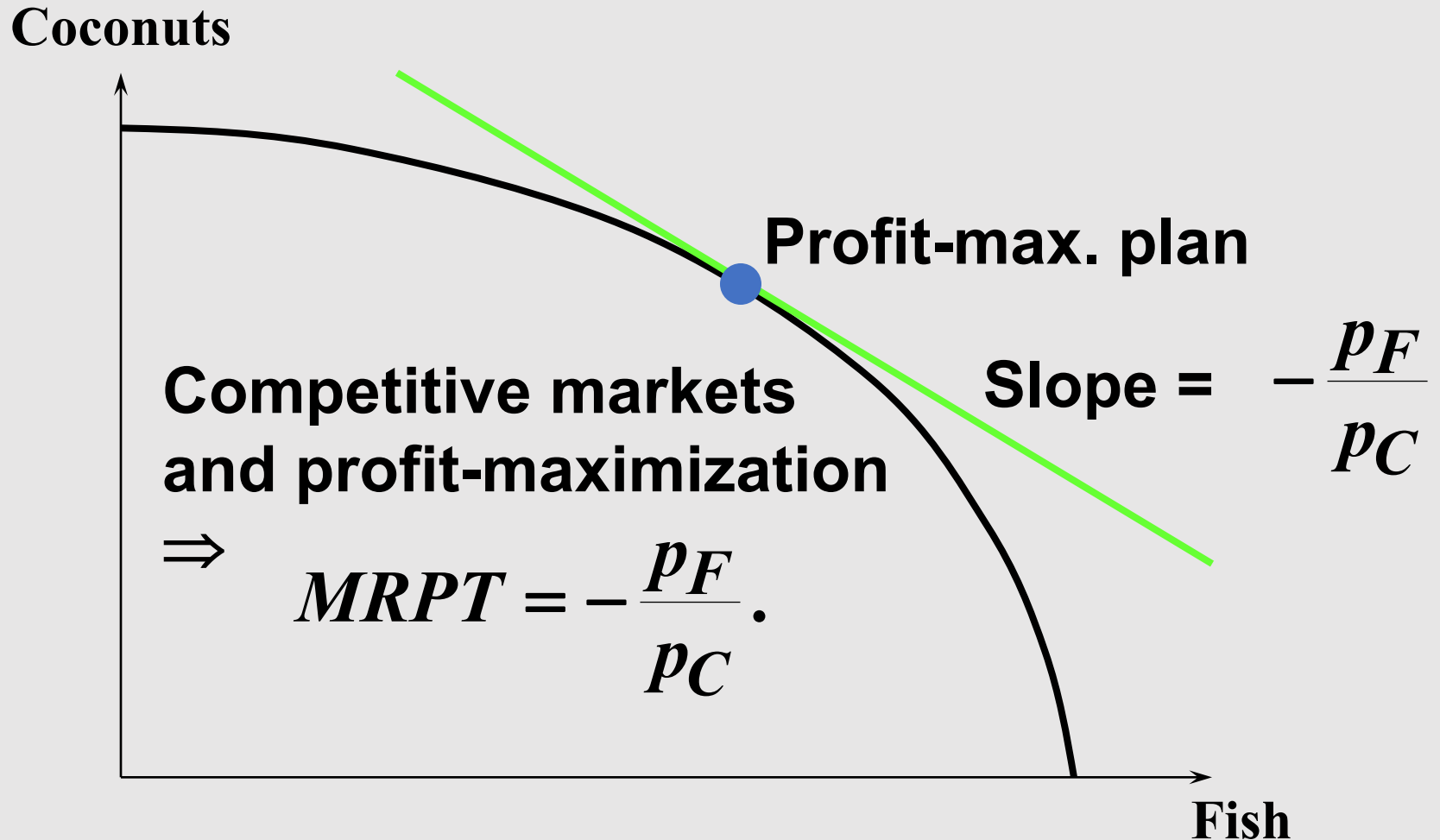
Decentralized Coordination of Production & Consumption



Decentralized Coordination of Production & Consumption



Decentralized Coordination of Production & Consumption



Decentralized Coordination of Production & Consumption

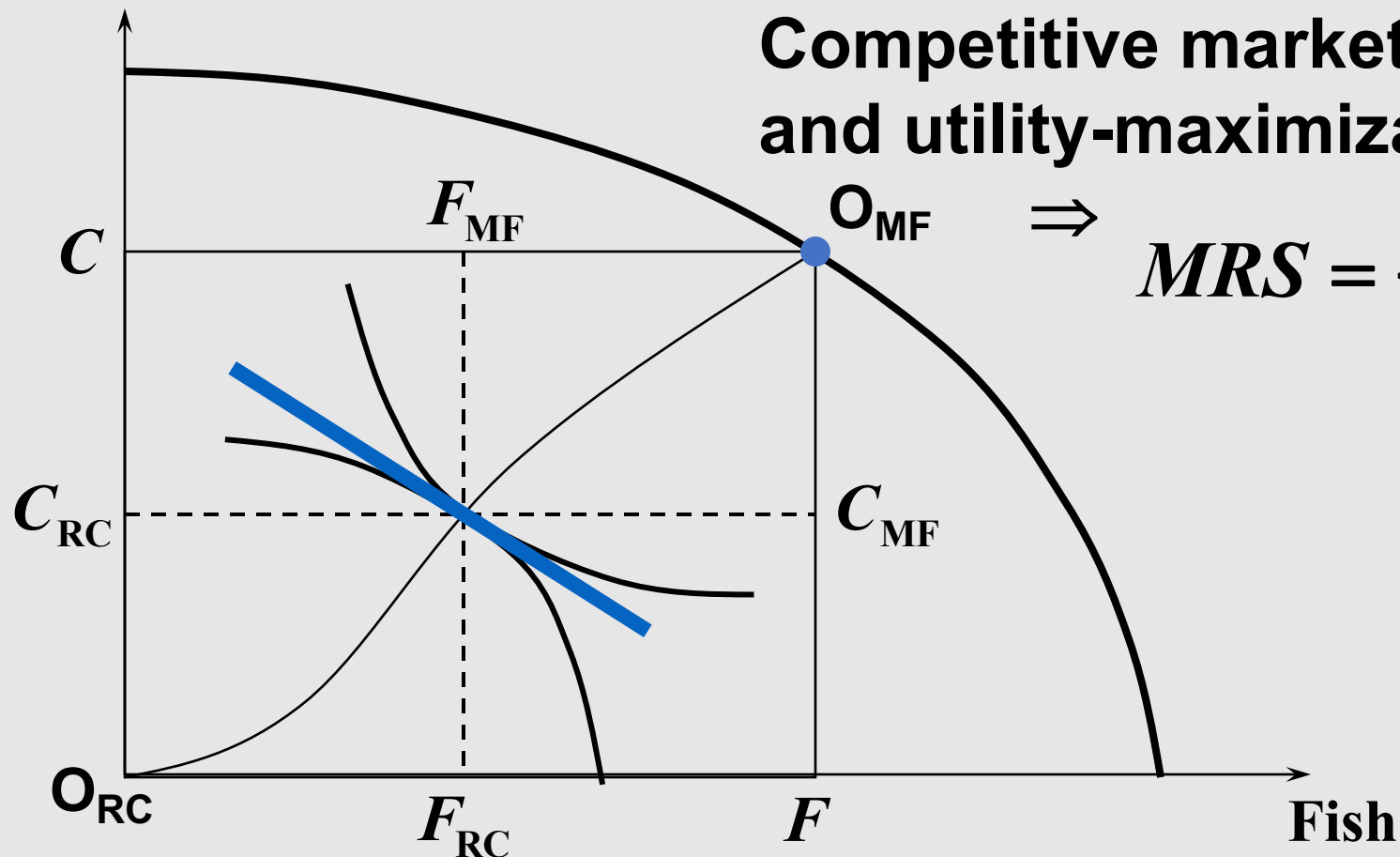
→ So competitive markets, profit-maximization, and utility maximization all together cause

$$MRPT = -\frac{p_F}{p_C} = MRS,$$

→ the condition necessary for a Pareto optimal economic state.

Decentralized Coordination of Production & Consumption

Coconuts



Decentralized Coordination of Production & Consumption

