

SUPPORTING DOCUMENT FOR LAB #2

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1 Device space and Logic Space

1.1 Device space

Device space is a one for working with GUI-framework, for examples, Java Swing. This space has the following features and it is illustrated in Figure 1.

1. It is discrete, the coordinate is represented by **integer value**.
2. Its origin is always at the **left-top corner** of the GUI-component, for example JPanel.
3. The y-axis is **upside down**, so the y-coordinate is increased from the left-top corner down to the bottom of the screen.

Students can verify the above features with the application accompanied with this tutorial (source of the app. included).

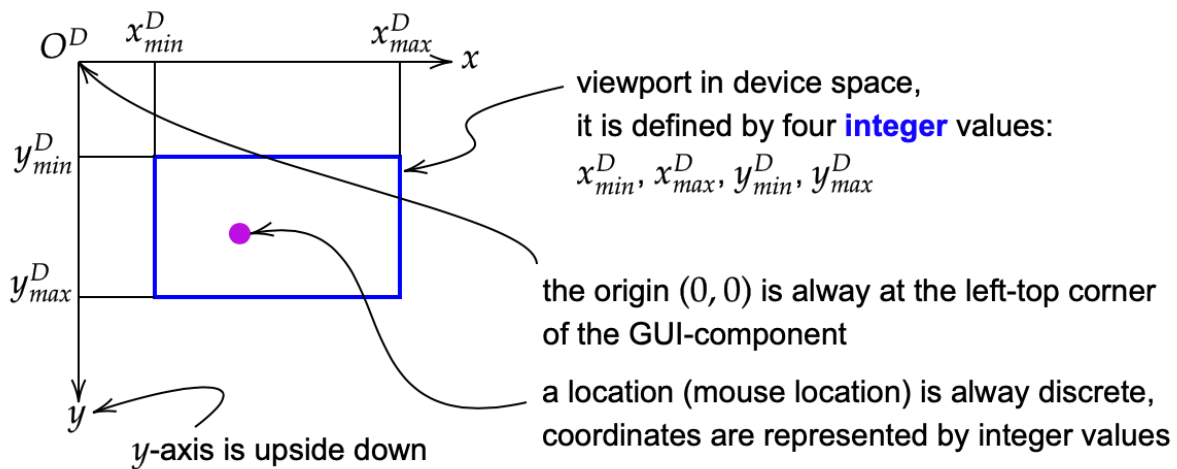


Figure 1: Device space is **discrete**. Note that $x_{min}^D \leq x_{max}^D$ and $y_{min}^D \leq y_{max}^D$. x_{min}^D is on the left of x_{max}^D and y_{min}^D is **upper** than y_{max}^D .

1.2 Logic space

Logic space is the one that all students have studied and used in mathematics, as shown in Figure 2. Some main features are as follows.

1. It is **continuous**, the coordinate is represented by **floating value**.
2. The y-axis is **upright**.

To create a drawing, the logic space is more general; you can specify your objects in a continuous space instead of a discrete one. It is also easier and more natural for drawing than the device space. For example, if you want to draw a graph, e.g. $\sin x$, you immediately think about and imagine about the logic space, the one with upright y-axis.

1.3 Viewport

Because the logic space is infinitive, so you need to show only an area inside that space. That area is usually **rectangular** and called a **viewport**. A viewport for the logical space is specified by **four floating values**: $x_{min}^L, x_{max}^L, y_{min}^L$ and y_{max}^L .

The logic space is natural for logically thinking about the drawing, but if you want to show your drawing, you need the device space; it means that you need to show your drawing on a specific GUI component. Moreover, you need show your drawing on a specific area on the device space. That area is called a viewport on the device space. That viewport is specified by **four integer values**: $x_{min}^D, x_{max}^D, y_{min}^D$ and y_{max}^D .

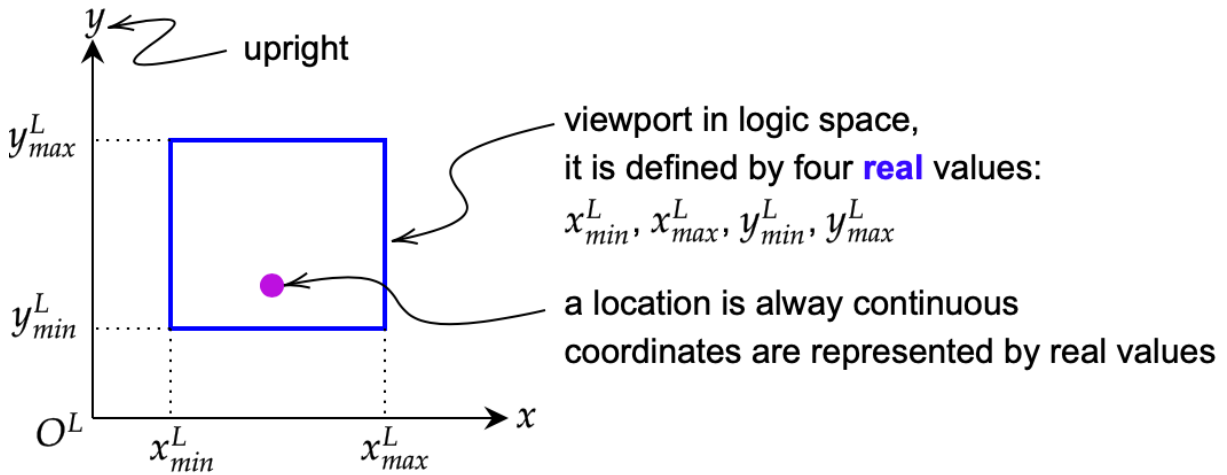


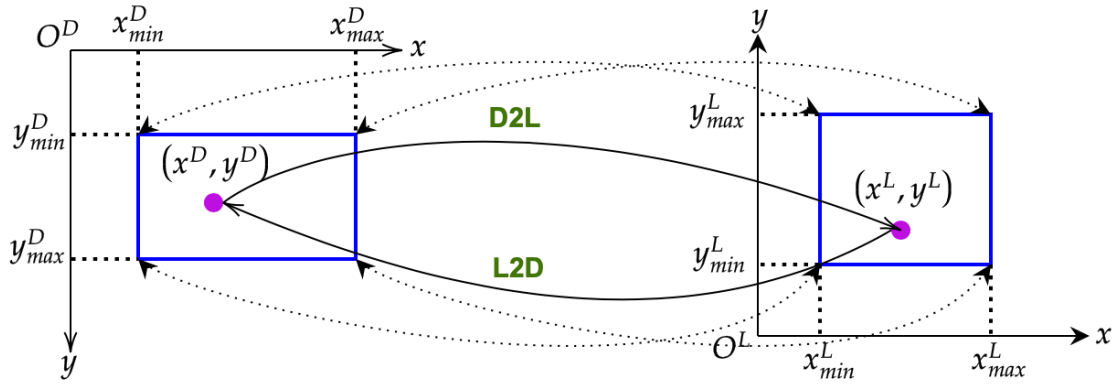
Figure 2: Logic space is **continuous**. Note that $x_{min}^D \leq x_{max}^D$ and $y_{min}^D \leq y_{max}^D$. x_{min}^D on the left of x_{max}^D and y_{min}^D is **lower** than y_{max}^D

2 Conversion between logic and device space

Logically, Programming API in graphic frameworks support users the following steps to create drawing.

1. Support API for users to create drawings on the logic space. Users make drawings by using the space as studied in mathematics. The device space is hidden from users; it means the conversion from the logic space to/from the device space is **automated by frameworks**.
2. The frameworks convert the drawings to the device space and perform actual drawing tasks on GUI-components. Therefore, if you are a provider of your graphic framework, as in this tutorial, you need to answer **where is on the device space to which a given point on the logic space convert?**; this task is called **Logic2Device** or **L2D** conversion.
3. The end users use mouse pointer to interact with the drawings, we can catch the mouse position in the device space. In order to change the graph, we need to answer **where is on the logic space to which a given device point convert?**; this task is called **Device2Logic** or **D2L** conversion.

The above explanation means that we need to solve a problem or develop an algorithm to determine (x^D, y^D) from (x^L, y^L) and vice versa. Where, (x^D, y^D) is a point in the viewport of the device space; and (x^L, y^L) is a point in the viewport of the logic space, as shown in Figure 3.



D2L: where is (x^D, y^D) on logic space?

L2D: where is (x^L, y^L) on device space?

Figure 3: Conversion between space. We map the viewport on the logic device to the viewport on the device space and vice versa.

2.1 Scaling for matching two viewports

We have:

- The viewport on the device space, it is specified by: $x_{min}^D, x_{max}^D, y_{min}^D$ and y_{max}^D
- The viewport on the logic space, it is specified by: $x_{min}^L, x_{max}^L, y_{min}^L$ and y_{max}^L

We can compute the width and the height of the two viewports.

- The width of the viewport on the device space: $W^D = x_{max}^D - x_{min}^D$
- The height of the viewport on the device space: $H^D = y_{max}^D - y_{min}^D$
- The width of the viewport on the logic space: $W^L = x_{max}^L - x_{min}^L$
- The height of the viewport on the logic space: $H^L = y_{max}^L - y_{min}^L$

Viewport mapping, what does it means? We can think as you need to **resize a viewport** to match with the size of another viewport.

It means that W^D units (pixels) on the device space will be mapped to (corresponds to) W^L units on the logic space. So, **1 unit on the device will be mapped to $\frac{W^L}{W^D}$ units on the logic space**, this factor named as $sxD2L$; so, $sxD2L = \frac{W^L}{W^D}$. Moreover, in order to convert d units from device space to logic space, just multiply it with $sxD2L$; so d units are mapped to $d \times sxD2L$

In similar way, we have the following results

1. to convert 1 units on x-axis from device to logic, use factor $sxD2L$: $sxD2L = \frac{W^L}{W^D}$
2. to convert 1 units on y-axis from device to logic, use factor $syD2L$: $syD2L = \frac{H^L}{H^D}$
3. to convert 1 units on x-axis from logic to device, use factor $sxL2D$: $sxL2D = \frac{W^D}{W^L}$
4. to convert 1 units on y-axis from logic to device, use factor $syL2D$: $syL2D = \frac{H^D}{H^L}$

2.2 The coordinates of the origin of the logic space on the device space

When we perform the conversion, we map the viewport on the logic space to the viewport on the device space and vice versa, see Figure 3. Therefore, we need to map four corners of the two viewport coresponding (**left-bottom to left-bottom** , **left-top to left-top** , **right-top to right-top** , and **right-bottom to right-bottom**).

We come to a question. Where is the location on the device space to which the origin of the logic space map? To answer this question, we try the following reasoning and combination with looking at Figure 3.

- The left-bottom of the viewport on the logic space is mapped to the left-bottom of the viewport on the device. It means $(x_{min}^L, y_{min}^L) \rightarrow (x_{min}^D, y_{max}^D)$; **please note that y_{max}^D instead of y_{min}^D** .
- On the logic space, the origin is displaced from the **left-bottom** of the viewport a vector \vec{t}^L **from the left-bottom to the origin**, so $\vec{t}^L = [-x_{min}^L, -y_{min}^L]$ (L denotes the logic space).
- Conversion of \vec{t}^L to the device by the following two steps:
 - scaling: to convert x_{min}^L and y_{min}^L to the device space; hence, we obtain \vec{t}^D ; their coordinates are computed according to Equation (1) and (2)

$$\vec{t}_x^D = -sxL2D \times x_{min}^L \quad (\text{after scaling}) \quad (1)$$

$$\vec{t}_y^D = -syL2D \times y_{min}^L \quad (\text{after scaling}) \quad (2)$$

- flipping: because y-axis on the device space is upside down (instead of upright as in the logic space), we need to do the reflection about the x-axis (also called flipping). The reflection is simple, just change the sign of y-coordinate; thereby, we obtain the coordinates of \vec{t}^D Equation (3) and (4).

$$\vec{t}_x^D = -sxL2D \times x_{min}^L \quad (\text{after scaling and then reflection}) \quad (3)$$

$$\vec{t}_y^D = syL2D \times y_{min}^L \quad (\text{after scaling and then reflection}) \quad (4)$$

- Let O^{LinD} be the point on the device space which is mapped from the origin of the logic space. The coordinates of O^{LinD} is obtained by translating the **left-bottom** of the viewport on the device space by vector \vec{t}^D obtained above; this translation is performed by Equation (5) and (6).

$$O_x^{\text{LinD}} = x_{min}^D - sxL2D \times x_{min}^L \quad (5)$$

$$O_y^{\text{LinD}} = y_{max}^D + syL2D \times y_{min}^L \quad (6)$$

2.3 Conversion from device to logic

Let $P(x^D, y^D)$ be the point in the device space; x^D and y^D are integer, they are the coordinates of pixel P on the device space. Now, we would like to know where is P on the logic space. Please note that P is still there on the device, but we actually want to know its coordinates in the logic space. What all we do is to change the system for measuring the coordinates. The changing is called conversion, it consists of three steps as follows:

1. **Scaling**: this step is to convert the unit of the device space (pixel) to the unit used in the logic space (metric). As explained in Section 2.1, we can use factor $sxD2L$ and $syD2L$ to convert for x- and y-coordinate. Thereby, after the scaling, the coordinates of P in the scaled system are $(x^{\text{scaled}}, y^{\text{scaled}})$ and computed according to Equation (7) and (8).

$$x^{\text{scaled}} = sxD2L \times x^D \quad (7)$$

$$y^{\text{scaled}} = syD2L \times y^D \quad (8)$$

2. **Reflection:** this step is to convert a coordinate measured by an upside down axis (y-axis of the device) to an upright axis (as in y-axis of the logic space). We do this task by changing the sign of the y-coordinate. Thereby, after the reflection, the coordinates of p in the reflected system are (x^{ref}, y^{ref}) , see Equation (9) and (10). The reflected system is denoted as $O^{ref}xy$.

$$x^{ref} = \text{sxD2L} \times x^D \quad (9)$$

$$y^{ref} = -\text{syD2L} \times y^D \quad (10)$$

In Section 2.2, the location of the origin of the logical space on the device space is O^{LinD} . We change its coordinates to $O^{ref}xy$ by the two above steps (scaling and then reflection), we obtain O^{LinRef} ; the x- and the y-coordinate of O^{LinRef} are computed using Equation (11) and (12).

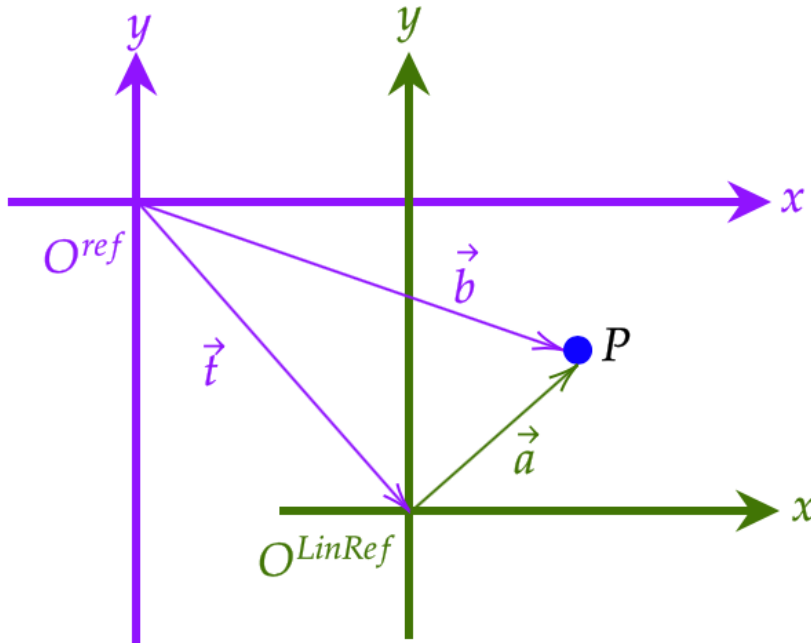
$$O_x^{LinRef} = \text{sxD2L} \times O_x^{LinD} \quad (11)$$

$$O_y^{LinRef} = -\text{syD2L} \times O_y^{LinD} \quad (12)$$

3. **Translation:** As shown in Figure 4, the coordinates of P in the logic space is represented by vector \vec{a} . Using the **rule of vector addition**, we can infer $\vec{a} = \vec{b} - \vec{t}$ (see Equation (13) and (14)); where, \vec{b} represents for the coordinates of P in the reflected system, see Equation (9) and (10). and \vec{t} represents for the coordinates of the origin of the logic space in the reflected system, see Equation (11) and (12).

$$x^L = \text{sxD2L} \times x^D - O_x^{LinRef} = \text{sxD2L} \times x^D - \text{sxD2L} \times O_x^{LinD} \quad (13)$$

$$y^L = -\text{syD2L} \times y^D - O_y^{LinRef} = -\text{syD2L} \times y^D + \text{syD2L} \times O_y^{LinD} \quad (14)$$



$$\vec{b} = \overrightarrow{O^{ref}P}$$

$$\vec{t} = \overrightarrow{O^{ref}O^L}$$

$$\vec{a} = \overrightarrow{O^L P}$$

$$\vec{t} + \vec{a} = \vec{b}$$

$$\vec{a} = \vec{b} - \vec{t}$$

Figure 4: Conversion from $O^{ref}xy$ system to O^Lxy ($\equiv O^{LinRef}xy$) system. \vec{b} and \vec{t} is the representation of point P and O^L in $O^{ref}xy$ respectively. \vec{a} is the representation of point P in the logical space.

2.4 Conversion from logic to device

$$x^D = \text{sxL2D} \times x^L + O_x^{LinD} \quad (15)$$

$$y^D = -\text{syL2D} \times y^L + O_y^{LinD} \quad (16)$$

Using Equation (13) and (14), we can obtain Equation (15) and (16) for converting from the logic to the device space. Please using $\text{sxL2D} = 1/\text{sxD2L}$ and $\text{syD2L} = 1/\text{syL2D}$ for transformation of equations.

3 Implementation

3.1 Data fields and constructors

In order to do the mapping, we need to maintain the viewport of the logic space and of the device space. Table 1 shows the relation between data fields used in Class `SpaceMapping` (see Figure 5) and their notation used in mathematical equations in previous sections.

As shown in Figure 5, Class `SpaceMapping` has a default constructor, it initializes the objects with default values for 8 data fields. Those data fields will be updated to actual values by methods `updateDevViewPort` and `updateLogViewPort` later.

Table 1: Data fields and their notation in mathematical equations

Index	Data fields	Notation
1	<code>minDevX</code>	x_{min}^D
2	<code>maxDevX</code>	x_{max}^D
3	<code>minDevY</code>	y_{min}^D
4	<code>maxDevY</code>	y_{max}^D
5	<code>minLogX</code>	x_{min}^L
6	<code>maxLogX</code>	x_{max}^L
7	<code>minLogY</code>	y_{min}^L
8	<code>maxLogY</code>	y_{max}^L

```

1 public class SpaceMapping {
2     private int minDevX, maxDevX;
3     private int minDevY, maxDevY;
4     private double minLogX, maxLogX;
5     private double minLogY, maxLogY;
6
7
8     public SpaceMapping() {
9         this.minDevX = 0;
10        this.maxDevX = 800;
11        this.minDevY = 0;
12        this.maxDevY = 600;
13
14        this.minLogX = 0;
15        this.maxLogX = 1.0;
16        this.minLogY = 0;
17        this.maxLogY = 1.0;
18    }
19    //here: has more code (later)
20 }

```

Figure 5: Class `SpaceMapping`: data fields and constructors

3.2 Supporting methods

Some methods for supporting the conversion are shown in Figure 6, 7, and 8. Figure 6 contains methods for computing the width (prefixed with letter **w**) and the height (prefixed with letter **h**) of the viewports. Letter **D** and **L** denote for **Device** and **Logic** respectively.

Figure 7 contains methods for scaling units between space; they are **sxL2D** , **syL2D** , **sxD2L** , and **syD2L** . Method **oLinD** is to determine the coordinates of the origin of the logic space in the device space, see Equation (5) and (6).

Method **step** returns the distance in the logic space that corresponds to 5 pixels in the device space. This method helps to rasterize the logic space (it is continuous) to grid of cells that corresponds to n ($n=5$) pixels in the device space.

Figure 8 contains method for updating the viewports. Parameters of these methods can the limits (min and max on x- and y-axis) or the object of Class **Viewport** . This class is defined in Figure 11.

```
21 public class SpaceMapping {
22     //data fields and constructors
23     public double wL() {
24         return this.maxLogX - this.minLogX;
25     }
26     public double hL() {
27         return this.maxLogY - this.minLogY;
28     }
29     public double wD() {
30         return this.maxDevX - this.minDevX;
31     }
32     public double hD() {
33         return this.maxDevY - this.minDevY;
34     }
35     //here: has more code (later)
36 }
```

Figure 6: Class SpaceMapping: Supporting methods - PART 1

3.3 Conversion between Logic and Device

The conversion the coordinates from the device space to the logic space programed as in Figure 9, the code follows Equation (13) and (14).

Similarly, The conversion the coordinates from the logic space to the device space programed as in Figure 10, the code follows Equation (15) and (16).

```

37 public class SpaceMapping {
38     //data fields and constructors
39
40     public double sxD2D() {
41         double wL = this.maxLogX - this.minLogX;
42         double wD = this.maxDevX - this.minDevX;
43         return wD/wL;
44     }
45     public double syD2D() {
46         double hL = this.maxLogY - this.minLogY;
47         double hD = this.maxDevY - this.minDevY;
48         return hD/hL;
49     }
50     public double sxD2L() {
51         double wL = this.maxLogX - this.minLogX;
52         double wD = this.maxDevX - this.minDevX;
53         return wL/wD;
54     }
55     public double syD2L() {
56         double hL = this.maxLogY - this.minLogY;
57         double hD = this.maxDevY - this.minDevY;
58         return hL/hD;
59     }
60     public Point2D oLinD() {
61         return new Point2D(
62             this.minDevX - this.minLogX*this.sxD2D(),
63             this.maxDevY + this.minLogY*this.syD2D()
64         );
65     }
66     public double step() {
67         return 5.0*Math.min(this.sxD2L(), this.syD2L());
68     }
69     //here: has more code (later)
70 }

```

Figure 7: Class SpaceMapping: Supporting methods - PART II


```

71 public class SpaceMapping {
72     //data fields and constructors
73
74     public void updateDevViewPort(int minDevX, int maxDevX, int minDevY,
75         int maxDevY){
76         this.minDevX = minDevX;
77         this.maxDevX = maxDevX;
78         this.minDevY = minDevY;
79         this.maxDevY = maxDevY;
80     }
81     public void updateLogViewPort(double minLogX, double maxLogX, double
82         minLogY, double maxLogY){
83         this.minLogX = minLogX;
84         this.maxLogX = maxLogX;
85         this.minLogY = minLogY;
86         this.maxLogY = maxLogY;
87     }
88     public void updateLogViewPort(Viewport vp){
89         this.minLogX = vp.getxMin();
90         this.maxLogX = vp.getxMax();
91         this.minLogY = vp.getyMin();
92         this.maxLogY = vp.getyMax();
93     }
94     //here: has more code (later)
95 }

```

Figure 8: Class SpaceMapping: Supporting methods - PART III

```

94 public class SpaceMapping {
95     //data fields and constructors
96     //Supporting methods
97
98     public Point2D device2Logic(Point2D devPoint){
99         return device2Logic((int)devPoint.getX(), (int)devPoint.getY());
100     }
101     public Point2D device2Logic(int devX, int devY){
102         double txD2L = this.oLinD().getX() * sxD2L();
103         double tyD2L = - this.oLinD().getY() * syD2L(); // "-" means
104             flipped
105         double logX = sxD2L()*devX - txD2L;
106         double logY = -syD2L()*devY - tyD2L;
107         return new Point2D(logX, logY);
108     }
109     //here: has more code (later)
110 }

```

Figure 9: Class SpaceMapping: Device to Logic conversion

```

110 public class SpaceMapping {
111     //data fields and constructors
112     //Supporting methods
113     public Point2D logic2Device(Point2D logPoint){
114         return logic2Device(logPoint.getX(), logPoint.getY());
115     }
116     public Point2D logic2Device(double logX, double logY){
117         double txL2D = this.oLinD().getX();
118         double tyL2D = -this.oLinD().getY();
119         double devX = sxL2D()*logX + txL2D;
120         double devY = -syL2D()*logY - tyL2D;
121         return new Point2D(devX, devY);
122     }
123 }

```

Figure 10: Class SpaceMapping: Logic to Device Conversion

```

1 public class Viewport {
2     //Setter and Getter
3     public double getYMin() { return yMin; }
4     public void setYMin(double yMin) { this.yMin = yMin; }
5     public double getYMax() { return yMax; }
6     public void setYMax(double yMax) { this.yMax = yMax; }
7     public double getXMin() { return xMin; }
8     public void setXMin(double xMin) { this.xMin = xMin; }
9     public double getXMax() { return xMax; }
10    public void setXMax(double xMax) { this.xMax = xMax; }
11    //Data fields
12    private double xMin, xMax;
13    private double yMin, yMax;
14
15    //Constructors
16    public Viewport(double xMin, double xMax, double yMin, double yMax){
17        this.xMin = xMin; this.xMax = xMax;
18        this.yMin = yMin; this.yMax = yMax;
19    }
20    public Viewport clone(){
21        return new Viewport(this.xMin, this.xMax, this.yMin, this.yMax);
22    }
23    public void combine(Viewport vp){
24        this.xMin = Math.min(this.xMin, vp.xMin);
25        this.xMax = Math.max(this.xMax, vp.xMax);
26        this.yMin = Math.min(this.yMin, vp.yMin);
27        this.yMax = Math.max(this.yMax, vp.yMax);
28    }
29    public void addPoint(Point2D point){
30        this.xMin = Math.min(this.xMin, point.getX());
31        this.xMax = Math.max(this.xMax, point.getX());
32        this.yMin = Math.min(this.yMin, point.getY());
33        this.yMax = Math.max(this.yMax, point.getY());
34    }
35 }

```

Figure 11: Class Viewport