

# CHAPTER 17

## Representation Learning and Generative Learning Using Autoencoders and GANs

Chapter 17 presents **autoencoders** and **GANs** as key tools for unsupervised representation learning and generative modeling, showing how to learn compact latent spaces and synthesize realistic data such as images.

### Autoencoder fundamentals and uses

An **autoencoder** consists of an encoder that maps inputs to a latent **coding**, and a decoder that reconstructs the inputs from this coding; it is trained to minimize reconstruction loss (e.g., MSE) on unlabeled data. Main uses:

- **Dimensionality reduction & visualization:** undercomplete autoencoders (bottleneck smaller than input) learn compressed representations similar to PCA, but can be nonlinear and scale to large datasets.
- **Feature learning & unsupervised pretraining:** stacked autoencoders can pretrain deep nets when labeled data is scarce, by reusing encoder layers as initialization for supervised models.
- **Generative modeling & denoising:** certain variants (e.g., VAEs) can generate realistic new samples; denoising autoencoders learn robust representations by reconstructing clean inputs from noisy versions.

A **linear** undercomplete autoencoder with MSE essentially performs PCA on the data.

### Stacked, tied, denoising, and sparse autoencoders

**Stacked autoencoders** add multiple hidden layers (symmetrical around the bottleneck) to capture more complex structure, often with nonlinear activations like ReLU or SELU.

Techniques:

- **Weight tying:** decoder weights set to the transpose of encoder weights, reducing parameters and encouraging symmetric mappings; implemented by sharing variables or using DenseTranspose-style layers.
- **Greedy layer-wise training:** train shallow autoencoders one at a time on successively encoded data, then stack them; used historically to stabilize deep training before modern methods.
- **Denoising autoencoders:** corrupt inputs with noise (e.g., masking, Gaussian) and train to reconstruct the original clean input, forcing the model to learn robust structure and act as a regularizer.

- **Sparse autoencoders:** use large hidden layers but enforce sparsity via L1 regularization or KL-divergence penalties on average activations, encouraging each neuron to specialize on rare patterns.

These variants help avoid trivial identity mappings and encourage meaningful latent representations.

### Variational autoencoders (VAEs)

**VAEs** are probabilistic autoencoders that learn a smooth latent **distribution** rather than point codings, making them powerful generative models. Key ideas:

- Encoder outputs parameters of a Gaussian distribution per input (mean  $\mu$  and log-variance  $\log \sigma^2$ ), defining  $q_\phi(z | x)$ .
- Latent sample via **reparameterization trick**:  $z = \mu + \sigma \odot \epsilon$  with  $\epsilon \sim \mathcal{N}(0, I)$  so gradients can flow through randomness.
- Decoder defines  $p_\theta(x | z)$ ; training minimizes **reconstruction loss** plus a **KL divergence** term that pushes  $q_\phi(z | x)$  towards a unit Gaussian prior  $p(z)$ .

Loss per example:

- For continuous data:  $\text{MSE}(x, \hat{x}) + \beta \text{KL}(q_\phi(z | x) || \mathcal{N}(0, I))$  with optional scaling  $\beta$ .

After training, sampling  $z \sim \mathcal{N}(0, I)$  and decoding produces new data points (e.g., novel Fashion-MNIST images), and interpolating between two latent codes yields smooth transitions between samples.

### Generative adversarial networks (GANs)

A **GAN** consists of a **generator**  $G$  that maps random noise  $z$  to fake samples  $G(z)$ , and a **discriminator**  $D$  that tries to distinguish real samples from fake; they are trained in an adversarial min-max game. Basic training:

- Update  $D$  to maximize  $\log D(x) + \log (1 - D(G(z)))$ .
- Update  $G$  to maximize  $\log D(G(z))$  (or equivalently minimize  $\log (1 - D(G(z)))$ ).

Applications include **image synthesis**, super-resolution, inpainting, style transfer, data augmentation, and more.

Training challenges and remedies:

- **Mode collapse:** generator produces limited variety; mitigations include minibatch discrimination, feature matching, and architectural tweaks.
- **Training instability/oscillation:** addressed by improved losses (e.g., Wasserstein GANs with gradient penalty), careful architecture (DCGAN guidelines), and learning-rate/batch-size tuning.

- **Overpowerful discriminator:** can be tempered by label smoothing, noisy labels, or updating  $G$  more frequently than  $D$ .

**DCGAN** adds convolutional structure and practical rules (strided convs, transposed convs, BatchNorm, ReLU in  $G$  and LeakyReLU in  $D$ ) to generate convincing medium-resolution images (e.g., faces, bedrooms).

### Advanced GAN variants: Progressive GAN, StyleGAN

To generate **high-resolution, coherent images**, the chapter reviews more advanced designs:

- **Progressive Growing of GANs:** start with very low-res images (e.g.,  $4 \times 4$ ), then progressively add layers to  $G$  and  $D$  to reach higher resolutions ( $8 \times 8 \rightarrow 16 \times 16 \rightarrow \dots \rightarrow 1024 \times 1024$ ), smoothly fading in new layers; stabilizes training and improves global structure.
- **StyleGAN:** refines the generator with:
  - A **mapping network** that converts latent code  $z$  into a **style vector**  $w$ , then applies per-layer affine transforms (AdaIN) to control feature scales and biases, giving fine-grained control over attributes like pose, hairstyle, or lighting.
  - Per-layer **noise inputs** added to features to model stochastic local detail (e.g., hair strands, freckles) separately from global style, improving realism.
  - **Style mixing regularization**, combining styles from different  $w$  vectors at different depths to encourage disentangled and local controls in latent space.

These models enable **semantic arithmetic in latent space** (e.g., “woman with glasses”  $\approx$  “woman” + “man with glasses” – “man”), and produce faces so realistic that they underpin sites like “this person does not exist.”