



Symbols

General color codina

Best to Worst: Links and TBDs:

Symbols

Recommendations differ depending on organization

☼ Parameter set

Encryption / Ciphertext

Signing / Signature

Not yet standardized by NIST

Implementation Code

6 Implementation size

Key / Key Generation

▲ Decryption

Verification

CPU Cycles

Implementation complexity

Security categories of parameter sets











NIST Security Categories V, IV, III, II, I

Higher is more secure.

Implementation complexity and size









Low/Medium/High implementation complexity

Low/Medium/High implementation size

Lower is better, * can be P. P. ?. A. or A.

Rating scales for parameter sizes and performance

 $[5^n, 5^{n+1}]$ CPU kilo cycles for signing

Best to Worst: n < 2, $n \in \{3, 4\}$, $n \in \{5, 6\}$, $n \in \{7, 8\}$, n > 9

 $[5^n, 5^{n+1}]$ CPU kilo cycles for key generation

 $[5^n, 5^{n+1}]$ CPU kilo cycles for signature verification

 $[5^n, 5^{n+1}]$ CPU kilo cycles for encryption / key encapsulation

 $[5^n, 5^{n+1}]$ CPU kilo cycles for decryption / key decapsulation

 $[2^n, 2^{n+1}]$ KB of signature size

 $[2^n, 2^{n+1}]$ KB of ciphertext size $[2^{n-5}, 2^{n-4}]$ KB of signature algorithm public key size

 $[2^n, 2^{n+1}]$ KB of encryption algorithm public key size

How To Interpret The Cheat Sheets

The goal of this series of cheat sheets is to make it as easy as possible to figure out which algorithm to pick for a given use case. Algorithm ID cards break down algorithm parameter sets, their important values and performance characteristics. The cheat sheets are intended to help users primarily in technical roles, such as engineers, architects or software developers working with post-quantum cryptography.

The focus is to avoid giving specific numbers measured in bits, bytes or cycles as this makes makes comparing numbers across algorithms difficult. Instead, this complexity is simplified by only providing a colorcoded number indicating the order of magnitude of each metric. Furthermore, an "Algorithm Overall Usability Score" is assigned to each algorithm. This score aims to make it visible at first glance how good of an overall package the algorithm offers (refer to the appendix for the definition of the score).

This approach prioritizes easy interpretation and comparability of metrics and in general quick informational gain over absolute precision of data – remember this is a cheat sheet, not a standard! This document is not intended to replace the study of algorithm specifications. It just aims to point you in the right direction quickly. If you are looking for the original and precise data, you can find it θ here.

The approach of focusing on orders of magnitude walks a fine line between treating too many things as "equal" and not simplifying things enough to be easy to read and compare. "In the same order of magnitude" usually refers to "equal up to a factor of at most 10", which is a very coarse way of comparing numbers. Treating metrics that differ by a factor of e.g. 9.9 as "equal" because 9.9 < 10 paints a distorted picture. In cryptography, factors of 5 or even 2 can make a significant difference in security or performance, both in theory and in practice. In order to still tease out the differences in metrics without throwing too many things together that actually differ significantly, this cheat sheet applies different scaling and "orders of magnitude" (i.e., not regarding base 10) for different metrics.

It turns out that for metrics measured in (kilo) CPU cycle counts, i.e. algorithm performance, "up to a factor of 5" is a scale that is granular enough to work out the differences between algorithms while maintaining easy comparability. Those cycle counts heavily depend on the CPU used during measurement, hence the numbers need to be taken with a grain of salt, even if given exactly and not in terms of orders of magnitude.

For signature and ciphertext sizes as well as key sizes, measuring numbers in kilobytes "up to a factor of 2" is well suited to work out the differences between algorithms while allowing for quick comparison. Specifically for signature public key sizes only, we offset the corresponding color coding by 5 orders of magnitude. This is because SLH-DSA has extremely small public keys compared to all other signature alagrithms, which would extend the scale into negative numbers (e.g., for SLH-DSA-SHA2-128s, the public key has $32=2^5$ bytes, which corresponds to an order of magnitude of -5 when measuring in orders of magnitude of base 2 and in kilobytes). This phenomenon of algorithm metrics spanning a very large range of orders of (base 2) magnitudes does not occur to this extent for encryption algorithms, making an offset unnecessary.

All values thus have a lower bound of 0. We do not limit the upper end of scales, but don't distinguish values greater than 10 anymore in terms of color coding. Please refer to the definitions on the left for symbol explanations, color coding and interpretation of numeric values.



ALGORITHM CHOICE GUIDANCE: RULES OF THUMB

The following orders of preference should be considered as general rules of thumb applicable to most use cases. They should however not be considered to be universal truths. Unstandardized algorithms are listed for the sake of completeness. All information is valid at the time of writing (02 February 2025) only. Note that cryptography may become obsolete in the future.



SECURITY CATEGORY CHOICES

• As a baseline, first consider using parameters.



- Use IV or V for more security if possible (i.e., if a decrease in performance is not a concern and if no constraints apply).
- Use or in if and only if in or higher is not an option due to constraints (e.g. performance, memory, etc.).
- Comparing post-quantum security categories of algorithms to their traditional security level in bits is a complex subject and like comparing apples and oranges to some degree.

Pure vs. Pre-Hashing

C. McEliece

C. McEliece

#0*

Frodo-KEM (1)

- First, consider using pure (i.e., without pre-hashing) as this is the general recommendation.
- Pre-Hashing may be considered if one or more of the following apply:
 - The message M is too large to be sent to the cryptographic module (CM) for hashing without significantly impacting performance. This may be the case e.g. in CMS related use cases such as S/MIME or code signing, or in cases of very narrow communication channels to the CM (e.g. between APDUs exchanged between smartcard and smartcard reader).
 - The hash needs to be signed with different algorithms and would be computed repeatedly without pre-hashing.
 - The specific hash function is not supported in a CM.

PURE PQC VS PQ/T HYBRID

This topic depends on too many factors (e.g. cost of migration, security considerations, risk profile, GRC requirements) to give general advice. Those aspects will differ greatly between different organizations. The main reasons to adopt PQ/T hybrids are to still have traditional algorithms in place in case a new algorithm turns out to be insecure, and that PQ/T might help to avoid a big bang migration as systems could simply ignore the PQC component if they do not support it yet. Consider recommendations from different government agencies: BSI and ANSSI recommend PQ/T hybrid strategies, whereas NIST is more reserved towards PQ/T. If using PQ/T hybrids, preferably use ECC (e.g. secp256r1, brainpoolP256r1, Curve25519) instead of RSA for the traditional component to keep key sizes as small as possible.



SIGNATURE ALGORITHMS

ID Cards



ML-DSA (Module-Lattice-Based Digital Signature Algorithm)



PARAMETER	OID	SECURITY	PER	FORMAN	ICE	SIGNATURE	PUBLIC KEY	Pre-Hashing
SET		CATEGORY	P		8	SIZE	SIZE	PRE-HASHING
ML-DSA-44	2.16.840.1.101.3.4.3.17		38	3	20		5	SHA512
IVIL DO/ (44	2.16.840.1.101.3.4.3.32		-0		-0		50	011/1012
ML-DSA-65	2.16.840.1.101.3.4.3.18		30	30	30		_	SHA512
IVIL-D3A-03	2.16.840.1.101.3.4.3.33	III	30	30	30		50	311/1012
ML-DSA-87	2.16.840.1.101.3.4.3.19			42	- 0			SHA512
IVIL-DSA-07	2.16.840.1.101.3.4.3.34	V ⊚	40	4 0	3 0	20	60	3HA312

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
HASHING
NAMING

CRYSTALS-DILITHIUM $\mbox{\it \emph{O}}$ FIPS 204 Signature Lattice Yes Standardized NIST, BSI, ANSSI Pure, Pre-Hashing by $k \times l$ matrix A(e.g. $6 \times 5 \rightarrow$ ML-DSA-65)

IMPLEMENTATION	P	•	8
Complexity	6 ₹ %	6 ₹₩	6 ?
Size	6 ?	\$ ₹	\$?\$

/ Pros / Use If:

- You need a general-purpose signature algorithm with decent specs in all categories
- \bullet Usually the best option for a signature algorithm in most protocols (e.g. TLS, SSH, S/MIME, etc.).
- Good choice for X.509 certificates, including CA certificates.

/ Cons / Don't Use If:

You don't want a lattice-based algorithm



SLH-DSA (STATELESS HASH-BASED DIGITAL SIGNATURE STANDARD)



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
HASHING
NAMING

SPHINCS+

FIPS 205
Signature
Hash (stateless)
Yes
Standardized
NIST, BSI, ANSSI
Pure, Pre-Hashing
based on various characteristics
(*s=small signatures, *f=fast)

IMPLEMENTATION	P		0
COMPLEXITY	6 ²	6 ⁷ 6	6 ?
Size	6 [?] ∅	5 ⁷ ⊕	6 [?] ⊕

PARAMETER	OID	SECURITY	PER	FORMAI	NCE	SIGNATURE	PUBLIC KEY	
SET	(Pure, Pre-hash)	CATEGORY	P		8	SIZE	SIZE	Pre-Hashing
SI H-DSA-SHA2-128s	2.16.840.1.101.3.4.3.20			98	50	2		SHA-256
	2.16.840.1.101.3.4.3.35				-0			
SLH-DSA-SHA2-128F	2.16.840.1.101.3.4.3.21		58	78	50	40	0	SHA-256
	2.16.840.1.101.3.4.3.36					-0		
SLH-DSA-SHA2-192s	2.16.840.1.101.3.4.3.22	III		98	50	40	0	SHA-512
	2.16.840.1.101.3.4.3.37					-0		
SI H-DSA-SHA2-192F	2.16.840.1.101.3.4.3.23	III	52	78	60	5	10	SHA-512
	2.16.840.1.101.3.4.3.38							
SI H-DSA-SHA2-256s	2.16.840.1.101.3.4.3.24	V	73	92	50	4	0	SHA-512
	2.16.840.1.101.3.4.3.39				-0	40		
SLH-DSA-SHA2-256F	2.16.840.1.101.3.4.3.25	V	62		60	5	10	SHA-512
	2.16.840.1.101.3.4.3.40							
SI H-DSA-SHAKE-128s	2.16.840.1.101.3.4.3.26			9	50	20	0	SHAKE128
	2.16.840.1.101.3.4.3.41							OT 17 (TCL 120
SLH-DSA-SHAKE-128F	2.16.840.1.101.3.4.3.27		52	78	50	4	0	SHAKE128
	2.16.840.1.101.3.4.3.42					40		0117 (KL 120
SI H-DSA-SHAKE-192s	2.16.840.1.101.3.4.3.28			92	50	4		SHAKE256
	2.16.840.1.101.3.4.3.43	III				40	0	01 17 (RL200
SLH-DSA-SHAKE-192F	2.16.840.1.101.3.4.3.29		58	78	60	-		SHAKE256
OLIT DO/ CON/ (NE 172)	2.16.840.1.101.3.4.3.44	III	-0		0	5	100	01 17 (TCL200
SLH-DSA-SHAKE-256s	2.16.840.1.101.3.4.3.30	- A	R	98	50			SHAKE256
3E11-D3/ (311) (RE 2003	2.16.840.1.101.3.4.3.45	V			30	40	0	01 17 (TCL200
SLH-DSA-SHAKE-256F	2.16.840.1.101.3.4.3.31	V	68		60	_		SHAKE256
3LI I-D3A-3I IARL-230F	2.16.840.1.101.3.4.3.46	V®	° 0		0	5	10	JI IANLESO

/ Pros / Use If:

- Alternative to ML-DSA and Falcon that is not based on lattices
- Very small public keys
- Generally good for use in most protocols, even if ML-DSA is the preferred option.
- Use as a more conservative choice in use cases with less frequent algorithm execution, i.e. where latency or message size are not a big concern. For example, S/MIME, document or code signing, creation of CAs.

- Poor key generation and signing performance compared to other algorithms
- High complexity of the algorithm and the implementation
- Possible interoperability issues due to the many variants that may not all be supported everywhere



FALCON (FAST-FOURIER LATTICE-BASED COMPACT SIGNATURES OVER NTRU)



Algorithm	Overall	Usability	Score
AIGOIIIIIII	Overdii	O3GDIIII y	SCOIL

Falcon

Lattice

Yes

TBD TBD

TRD

Signature

Pending

Project Page

PREVIOUS NAME SPECIFICATION TYPE **FAMILY** SUITABLE FOR GENERAL USE STANDARDIZATION STATUS RECOMMENDED BY HASHING NAMING

IMPLEMENTATION	P	•	0
Complexity	6 ₹\$	676	670
Size	67%	6 ?₽	\$ [?] \$

PARAMETER SET	OID	SECURITY CATEGORY	PER	FORMAN	(CE	SIGNATURE SIZE	PUBLIC KEY SIZE	Pre-Hashing
Falcon-512 Falcon-1024	TBD TBD	l _o		40	20 30	00	40	TBD TBD

/ Pros / Use If:

- Generally good for use in most protocols (e.g. TLS, SSH, S/MIME, etc.). Exceptions may apply in cases of repeated generation of ephemeral keys (poor performance).
- Falcon has smaller signature sizes than ML-DSA:











• Falcon has smaller public key sizes than ML-DSA:















/ Cons / Don't Use If:





- The algorithm is not yet standardized
- The algorithm requires expensive floating point arithmetic
- Key generation and signing are slower than for ML-DSA
- Less suitable in applications involving the creation of lots of ephemeral keys/certificates (key generation is slow).



NUMBER OF

XMSS / XMSS-MT (eXtended Merkle Signature Scheme / eXtended Merkle Signature Scheme Multi Tree)

PARAMETER

NUMERIC

SECURITY



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
HASHING
NAMING

XMSS/XMSSMT SP 800-208, PRFC 8391 Signature Merkle Trees (stateful hash trees) No	
Standardized NIST, BSI, ANSSI TBD	
XMSS-[Hashfamily]_[h]_[n] XMSSMT-[Hashfamily]_[h]/[d]_[n] where h is the tree height, d is the number of layers, and n is the message length in bits	

	SET	IDENTIFIER	CATEGORY	٩		0	SIZE	SIGNATURES	LAYE
×	(MSS-SHA2_10_256	0x00000001	V	?	?	?0	?	210	1
X	(MSS-SHA2_16_256	0x00000002	V	? <u>?</u> ?	78	₹ <u></u>	?	216	1
X	(MSS-SHA2_20_256	0x00000003	V	?	?8	?	?	2 ²⁰	1
XMS	SSMT-SHA2_20/2_256	0x00000001	V	??	?8	?	?	2 ²⁰	2
XMS	SSMT-SHA2_20/4_256	0x00000002	V	?	78	₹	?	2 ²⁰	4
XMS	SSMT-SHA2_40/2_256	0x00000003	V	78	78	₹	?	2 ⁴⁰	2
XMS	SSMT-SHA2_40/4_256	0x00000004	V	? <u>?</u> ?	78	₹	?	2 ⁴⁰	4
XMS	SSMT-SHA2_40/8_256	0x00000005	V	? 8	70	₹	?	2 ⁴⁰	8
XMS	SSMT-SHA2_60/3_256	0x00000006	V	? 8	70	₹ <u>?</u>	?	2 ⁶⁰	3
XMS	SSMT-SHA2_60/6_256	0x00000007	V	· ??	₹	₹	?	2 ⁶⁰	6
XMS	SMT-SHA2_60/12_256	0x00000008	V	?6	?	?0	?0	2 ⁶⁰	12

PERFORMANCE

SIGNATURE

Махімим

NOTE:

₱ SP 800-208 defines further parameter sets not listed in ₱ RFC 8391 using other hash functions (SHA256/192, SHAKE256/256, SHAKE256/192). Furthermore, ₱ RFC 8391 lists optional parameter sets that are not approved in ₱ SP 800-208. All of those variants are omitted here as they are not likely to be widely used, in particular not after ML-DSA and SLH-DSA have been standardized in the meantime.

/ Pros / Use If:

IMPLEMENTATION

COMPLEXITY

Size

- You can predict the maximum number of signatures that are going to be required
- Firmware signing use cases
- You want a signature scheme where the security only relies on the security of the hash function used without assuming the hardness of another mathematical problem.
- Cf. SP 800-208, Section 1.1 for additional explanations

- You require an algorithm for general use
- You cannot predict the maximum number of signatures that are going to be required, or the number of required signatures exceeds the maximum number of signatures enabled through the approved parameter sets
- Your application does not allow for the careful state management and tracking of signatures performed that is required with this algorithm



LMS/HSS (Leighton-Micali Signature / Hierarchical Signature System)



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
HASHING
NAMING

LMS, LMS/HSS

S P 800-208, RFC 8554
Signature
Merkle Trees (stateful hash trees)
No
Standardized
NIST, BSI, ANSSI
TBD
LMS_SHA256_M32_[h]
where h is the tree height

IMPLEMENTATION	P		0
Complexity	6 ₹∯	6 ₹	6 ₹₩
Size	6 ₹	8 ?	8 ?

PARAMETER SET	NUMERIC IDENTIFIER	SECURITY CATEGORY	PER	FORMAN	O O	Signature Size	MAXIMUM SIGNATURES
LMS SHA256 M32 H5	0x00000005			? <u>?</u> ?	?0	?,	 2 ⁵
LMS_SHA256_M32_H10	0x00000006	V	78	?	70	?	2 ¹⁰
LMS_SHA256_M32_H15	0x00000007	V	??	? 8	? <u>@</u>	?	2 ¹⁵
LMS_SHA256_M32_H20	0x00000008	V	· ??	?	79	?	2 ²⁰
LMS_SHA256_M32_H25	0x00000009	Vo	?6	76	? 0	?	2 ²⁵

NOTE

♦ SP 800-208 defines further parameter sets not listed in ♠ RFC 8554 using other hash functions (SHA256/192, SHAKE256/256, SHAKE256/192). Those variants are omitted here as they are not likely to be widely used, in particular not after ML-DSA and SLH-DSA have been standardized in the meantime. Similar to XMSS multi-tree variants, a comparable structure exists with Hierarchical Signature System (HSS) variants of LMS that involves a number of LMS instances.

/ Pros / Use If:

- You can predict the maximum number of signatures that are going to be required
- Firmware signing use cases
- You want a signature scheme where the security only relies on the security of the hash function used without assuming the hardness of another mathematical problem.
- Cf. SP 800-208, Section 1.1 for additional explanations

- You require an algorithm for general use
- You cannot predict the maximum number of signatures that are going to be required, or the number of required signatures exceeds the maximum number of signatures enabled through the approved parameter sets
- Your application does not allow for the careful state management and tracking of signatures performed that is required with this algorithm
- Rather difficult to set up correctly and configure and fine tune all necessary parameters



ENCRYPTION / KEM ALGORITHMS

ID Cards



ML-KEM (Module-Lattice-Based Key-Encapsulation Mechanism Standard)



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
NAMING

CRYSTALS-KYBER
FIPS 203
Encryption/KEM
Lattice
Yes
Standardized
NIST, BSI, ANSSI
TBD

	_	
Complexity	6 ₹\$	6 ⁷
Size	6 ₹\$6	6 [?]

PARAMETER SET	OID	SECURITY CATEGORY	PER	FORMAN	CE CE	CIPHERTEXT SIZE	PUBLIC KEY SIZE	
ML-KEM-512	2.16.840.1.101.3.4.4.7		20	20	2 <u>0</u>	<u>о</u>	•	
ML-KEM-768	2.16.840.1.101.3.4.4.2	III	20	20	30	o _O	00	
ML-KEM-1024	2.16.840.1.101.3.4.4.3	V	30	3 <mark>0</mark>	3 <mark>0</mark>	<u>о</u>	0	

/ Pros / Use If:

IMPLEMENTATION

- Currently the only post-quantum encryption/key encapsulation algorithm standardized by NIST
- Need a general-purpose encryption / key-encapsulation algorithm with decent specs in all categories
- Usually the best choice in most protocols involving an encryption/KEM component (e.g. TLS, S/MIME, etc.)

/ Cons / Don't Use If:

• You don't want a lattice-based algorithm



BIKE (BIT FLIPPING KEY ENCAPSULATION)



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
NAMING

BIKE

Project Page
Encryption/KEM
Codes
Yes
4th round candidate
TBD
after security categories I, III and V

IMPLEMENTATION	P		8	
Complexity	6 ₹₩	6 ₹₩	6 ₹ 6	
Size	670	6? D	5 ?∯	

PARAMETER SET	OID	SECURITY CATEGORY	PER	FORMAN	ICE	CIPHERTEXT SIZE	PUBLIC KEY SIZE
BIKE-L1	TBD		30	20	4 <u>C</u>	<u></u>	•
BIKE-L3	TBD	III _®	42	3 0	5 <u>O</u>	10	100
BIKE-L5	TBD	Vo	n/g	n/g	n/e	2 ₀	20

Note:

No data available for BIKE-L5 for cycle counts. The algorithm overall usability score is computed over BIKE-L1 and BIKE-L3 only.

/ Pros / Use If:

• Possible alternative to ML-KEM not based on lattices.

- Not yet standardized. Note that NIST intends to standardize at most one of the algorithms HQC and BIKE.
- Metrics not as good as the ones of ML-KEM.



HQC (HAMMING-QUASI-CYCLIC)



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
NAMING

HQC

Project Page
Encryption/KEM
Codes
Yes
4th round candidate
TBD
128, 192 and 256 bits of security

in reference to security categories

IMPLEMENTATION	P	•	•	
Complexity	676	6 ₹₩	6 ₹ 0	
Size		₹	₹	

I, III and V

PARAMETER SET	OID	SECURITY CATEGORY	PER	FORMAN	CE	CIPHERTEXT SIZE	PUBLIC KEY SIZE
HQC-128	TBD		20	3 <mark>0</mark>	3 <mark>0</mark>	20	100
HQC-192	TBD	III	38	30	4 <mark>0</mark>	3 _O	20
HQC-256	TBD	V	30	40	40	30	20

/ Pros / Use If:

Possible alternative to ML-KEM not based on lattices.

- Not yet standardized. Note that NIST intends to standardize at most one of the algorithms HQC and BIKE.
- Metrics not as good as the ones of ML-KEM.



FRODOKEM



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
NAMING

FrodoKEM

Project Page
Encryption/KEM
Lattice
Yes
Disregarded by NIST
BSI, ANSSI
FrodoKEM-[n]-[AES | SHAKE]
where n is a matrix dimension

IMPLEMENTATION	P	•	0	
Complexity	6 ₹	6 ₹ 0	6 [?] ₽	
Size	6 ?	\$? (\$?∯	

PARAMETER	OID	SECURITY	PER	PERFORMANCE		CIPHERTEXT	PUBLIC KEY
SET		CATEGORY	₽	<u></u>	<u>_</u>	Size	Size
Frodokem-640-AES	TBD		42	4 <mark>0</mark>	4 <mark>0</mark>	3 ⊖	30
Frodokem-640-SHAKE	TBD		50	50	50	3 ₀	30
Frodokem-976-AES	TBD	III	48	40	40	3 ₀	30
Frodokem-976-SHAKE	TBD	III	63	60	60	3 ₀	30
Frodokem-1344-Aes	TBD	V	50	50	50	40	40
Frodokem-1344-Shake	TBD	V	60	60	6 <u>0</u>	40	40

NOTE

There are also ephemeral versions of FrodoKEM (eFrodoKEM-640, etc.), but BSI only recommends FrodoKEM-976 and FrodoKEM-1344 versions for long-term protection. The algorithm score also only includes the non-ephemeral versions listed above.

/ Pros / Use If:

• More conservative than ML-KEM since it is based on unstructured grids

/ Cons / Don't Use If:

• Not standardized by NIST because ML-KEM is more efficient.



CLASSIC McELIECE



Algorithm Overall Usability Score

PREVIOUS NAME
SPECIFICATION
TYPE
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
NAMING

Classic McEliece \uptheta Project Page Encryption/KEM Codes No / With Limitations 4th round candidate (NIST) BSI mceliece[n][deg(F(y))][[f]] where n, F(y) are parameters non-f versions: $(\mu, \nu) = (0, 0)$ f versions: $(\mu, \nu) = (32, 64)$

IMPLEMENTATION	,		•
Complexity	6 ₹ ₽	6 ₹ 0	6 ?∯
Size	676	6 [?]	6 [?]

PARAMETER SET	OID	SECURITY CATEGORY	PER	FORMAN	CE ICE	CIPHERTEXT SIZE	PUBLIC KEY Size
MCELIECE348864	TBD		60	20	3 O	<u>о</u>	8
MCELIECE348864F	TBD		62	n/3	n/e	<u></u>	6
мсецесе460896	TBD	III _®	Ř	20	3 0	<u></u>	9,
MCELIECE460896F	TBD	III	R	n/S	n/e	<u></u>	9,
MCELIECE6688128	TBD	V®	R	3 <u>0</u>	3 O	<u></u>	10,
MCELIECE6688128F	TBD	V®	8	n/S	n/e	<u>о</u>	10,
MCELIECE6960119	TBD	V®	7 8	30	3 O	<u></u>	10,
MCELIECE6960119F	TBD	V®	R	n/e	n/e	0 0	10,
MCELIECE8192128	TBD	V®		30	30	0 0	10,
MCELIECE8192128F	TBD	V		n/B	n/e	6	10,

Note:

No data available for the f versions for encryption/decryption cycle counts. The algorithm overall usability score is computed over non-f versions only. Non-f and f versions are interoperable, with f versions offering faster key generation and non-f versions having simpler key generation.

/ Pros / Use If:

- Possible alternative to ML-KEM not based on lattices.
- Considered safe and recommended by BSI even though not standardized by NIST.
- Use cases that allow for pre-sharing of keys where the large public key size is not a concern.

- Not yet standardized by NIST.
- Not suitable for general use due to the very large public keys and poor performance of key generation.
- Due to aforementioned point, likely not suitable for embedded devices.



NTRU (Number Theory Research Unit / Number Theorists 'R' Us)



PREVIOUS NAME
SPECIFICATION
Түре
FAMILY
SUITABLE FOR GENERAL USE
STANDARDIZATION STATUS
RECOMMENDED BY
Naming

NTRU

Project Page
Encryption/KEM
Lattice
Yes
Not Standardized
n/a
author initials and a prime number

IMPLEMENTATION	P		0	
Complexity	676	6 ⁷	6 [?] #	
Size	6 [?] ₽	5 ?	\$? ()	

Parameter Set	OID	SECURITY CATEGORY	Per P	FORMAN	ICE	CIPHERTEXT SIZE	PUBLIC KEY SIZE
NTRUHPS2048509	N/A		50	40	<mark>4</mark> 0	○	0
ntruhrss701	N/A	III	68	40	50	o _O	0
NTRUHPS2048677	N/A	III	68	40	5 <u>0</u>	o _O	0
NTRUHPS4096821	N/A	V	60	40	50	○	00

/ Pros / Use If:

• The intellectual property rights of ML-KEM have been unclear for a while, with NTRU being a possible backup alternative without such issues. This topic is now considered sufficiently clear and resolved by NIST. In case legal concerns about ML-KEM still apply in some exceptional cases, NTRU might be an option. However, ML-KEM is usually the better option in terms of technical aspects.

- Not standardized
- Performance not as good as ML-KEM, especially for key generation. Similarly, BIKE and HQC offer better metrics.







Overview: Hash Algorithms and Extendable Output Functions (XOF)

FAMILY	VARIANT	OUTPUT SIZE [BITS]	ROUNDS	Construction	TRADITIONAL	PRE-QUANTUM SE			-QUANTUM SECURITY		SECURITY (PERFORMANCE
					Collision	Pre-Image	2nd Pre-Image	Collision	Pre-Image	2nd Pre-Image	Collission	Preimage	
	SHA-224	224	64	Merkle-Damgård construction	112	224	224	74	112	112	<1 _®	III	7.62
	SHA-512/224	224	80	Merkle-Damgård construction	112	224	224	TBD	TBD	TBD	<1 _®	III	≈ SHA-384
SHA-2	SHA-256	256	64	Merkle-Damgård construction	128	256	256	85	128	128	110	V	7.63
	SHA-512/256	256	80	Merkle-Damgård construction	128	256	256	TBD	TBD	TBD		Vo	≈ SHA-384
	SHA-384	384	80	Merkle-Damgård construction	192	384	384	128	192	192	IV	V	5.12
	SHA-512	512	80	Merkle-Damgård construction	256	512	512	170	256	256	V	Vo	5.06
	SHA3-224	224	24	Keccak sponge construction	112	224	224	74	112	112	<1 _®	III	8.12
	SHA3-256	256	24	Keccak sponge construction	128	256	256	85	128	128		V	8.59
SHA-3	SHA3-384	384	24	Keccak sponge construction	192	384	384	128	192	192	IV	V	11.06
0 0	SHA3-512	512	24	Keccak sponge construction	256	512	512	170	256	256	Vo	Vo	15.88
	SHAKE128	d (ARBITRARY)	24	Keccak sponge construction	$\min\left(\frac{d}{2}; 128\right)$	$\min\left(\tfrac{d}{2};128\right)$	$\min\left(\tfrac{d}{2};128\right)$	$\min\left(\frac{d}{3}; 128\right)$	$\min\left(\frac{d}{2};128\right)$	$\min\left(\tfrac{d}{2};128\right)$	110		7.08
	SHAKE256	d (ARBITRARY)	24	Keccak sponge construction	$\min\left(\frac{d}{2}; 256\right)$	$\min\left(\tfrac{d}{2};256\right)$	$\min\left(\tfrac{d}{2};256\right)$	$\min\left(\frac{d}{3}; 256\right)$	$\min\left(\tfrac{d}{2};256\right)$	$\min\left(\tfrac{d}{2};256\right)$	Vo	Vo	8.59

NOTES & TAKEAWAYS

- ullet SHAKE128 and SHAKE256 are exendable output functions and allow for an arbitrary output size d.
- SHA-512/224 and SHA-512/256 denotes the truncation of the SHA-512 hash to 224 resp. 256 bits.
- Security against collision attacks is specified using values according to Brassard et al. (Source)
- Performance is measured in median cycles/byte on a Skylake CPU (Source).
- Hash functions other than SHA-3 and SHA-3 variants (e.g. SHA-1, RipeMD-160, MD5, etc.) should generally be avoided as they are less secure. They are therefore not part of the above overview.







TRADITIONAL VS. POST-QUANTUM SECURITY LEVEL COMPARISON

TRADITIONAL PRE-QUANTUM SECURITY		ATTACK IN TERMS	ALGORITHM	NIST SECURITY CATEGORIES	Post-Quantum Security					
SECURITY [BITS]	Classical Attack Complexity	OF BIT SIZE N	Examples	DEFINED THROUGH ATTACK	Classical Attack Improvement	QUANTUM ATTACK COMPLEXITY	SECURITY [BITS]	Signature Parameter Sets	Encryption/KEM Parameter Sets	
\overline{n}	$\mathcal{O}\left(2^{n}\right)$	$n ext{-BIT}$ KEY SPACE EXHAUSTIVE KEY SEARCH	AES		Grover	$\mathcal{O}\left(2^{\frac{n}{2}}\right)$	$\frac{n}{2}$			
n	$\mathcal{O}\left(2^{n}\right)$	$n ext{-BIT}$ hash pre-image attack	SHA-2, SHA-3		Grover	$\mathcal{O}\left(2^{\frac{n}{2}}\right)$	$\frac{n}{2}$			
n	$\mathcal{O}\left(2^{n}\right)$	n-bit hash 2nd-pre-image attack	SHA-2, SHA-3		Grover	$\mathcal{O}\left(2^{\frac{n}{2}}\right)$	$\frac{n}{2}$			
$\frac{n}{2}$	$\mathcal{O}\left(2^{\frac{n}{2}}\right)$	n-bit hash collision attack	SHA-2, SHA-3		Brassard et al.	$\mathcal{O}\left(2^{\frac{n}{3}}\right)$	$\frac{n}{3}$			
-	2128	128-bit key space exhaustive key search	AES-128	Category 1	Grover	2^{64}	64	Falcon-512.	ML-KEM-512,	
128		128-bit hash pre-image attack	N/A		Grover	264	64	SLH-DSA 128 variants	BIKE-L1, HQC-128,	
		128-bit hash 2nd-pre-image attack	N/A		Grover	2^{64}	64		FrodoKEM-640	
		256-bit hash collision attack	SHA-256, SHA3-256	Category 2	Brassard et al.	$\frac{2^{85}}{2^{85}}$	85	MLA-DSA-44		
		192-bit key space exhaustive key search	AES-192	Category 3	Grover	2^{96}	96	ML-DSA-65,	ML-KEM-768,	
192	2192	192-bit hash pre-image attack	N/A		Grover	2^{96}	96	LMS/XMSS/SLH-DSA 192 VARIANTS	BIKE-L3, HQC-192,	
	-	192-bit hash 2nd-pre-image attack	N/A		Grover	296	96		FrodoKEM-976	
		384-bit hash collision attack	SHA-384, SHA3-384	Category 4	Brassard et al.	2^{128}	128			
		256-bit key space exhaustive key search	AES-256	Category 5	Grover	2^{128}	128		ML-KEM-1024,	
256	2^{256}	256-bit hash pre-image attack	SHA-256, SHA3-256		Grover	2^{128}	128	ML-DSA-85,	BIKE-L5, HQC-256,	
200		256-bit hash 2nd-pre-image attack	SHA-256, SHA3-256		Grover	2^{128}	128	LMS/XMSS/SLH-DSA 256 VARIANTS	FrodoKEM-1344	
		512-bit hash collision attack	SHA-512, SHA3-512		Brassard et al.	2^{170}	170			
		384-bit key space exhaustive key search	N/A		Grover	2^{192}	192			
384	2384	384-bit hash pre-image attack	SHA-384, SHA3-384		Grover	2^{192}	192			
004	4	384-bit hash 2nd-pre-image attack	SHA-384, SHA3-384		Grover	2^{192}	192			
		768-bit hash collision attack	N/A		Brassard et al.	2^{256}	256			
		512-BIT KEY SPACE EXHAUSTIVE KEY SEARCH	N/A		Grover	2^{256}	256			
512	2512	512-bit hash pre-image attack	SHA-512, SHA3-512		Grover	2^{256}	256			
012	4	512-bit hash 2nd-pre-image attack	SHA-512, SHA3-512		Grover	2^{256}	256			
		1024-bit hash collision attack	N/A		Brassard et al.	2^{341}	341			

NOTES & TAKEAWAYS

- The above is still a simplified view. It does not dive into the specific assumptions made in the new algorithms' security proofs and the possible attacks on those algorithms (e.g., is a collision attack on a hash function enough, or would a pre-image be required to break the signature scheme using that hash function). It is also not including considering practical considerations and predictions about quantum computers, such as runtime or quantum circuit depth. Cf. NIST PQC Evaluation Criteria, 4.A.5 for further details.
- A pre-quantum security level can have different post-quantum security levels equivalents. It all depends on the specific attack in question, resp. the security assumption a new post-quantum algorithm is based on or must be secure against. For hashing, the often cited "SHA-256 offers 128 bits of security" is not wrong, but only part of the picture: it offers 256 bits of security against pre-image and 2nd-preimage-attacks. The *n* bits of security against 2nd-preimage attacks is still a slightly simplified and harmonized view to avoid different formulas for different hash functions. Cf. ## NIST: Hash Functions for details.
- The fact that the exact level of post-quantum security still depends on so many assumptions about CRQCs, comparing pre-quantum and post-quantum security levels remains an apples and oranges comparison to some degree. Such comparisons should be taken with a grain of salt, especially when done only on a rather superficial level.
- The lines marked with colors , and are the ones used by NIST to define categories I, II, III, IV and V. The lines marked in lighter colors , and have the same post-quantum security as the defining lines of categories I, III and V, respectively. They therefore fulfill the "comparable to or greater than" clause in NIST's category definitions. Note that categories IV and V are differentiated despite having 128 bits of post-quantum security again highlighting the fact that a precise categorization is difficult and requires a detailed analysis of many aspects.



ALGORITHM OVERALL USABILITY SCORE

We try to measure an algorithm's overall usability for a general use case (i.e., a use case without any special characteristics and constraints) by calculating a single number between 0 (worst) and 10 (best) for the algorithm. This calculation is taking into account all parameter sets, performance metrics, public key size, signature/ciphertext size, the number of security categories provided, whether or not it is suitable for general use, and the complexity and size of its implementation. There are many possible ways to define a formula for this purpose and weigh in different individual metrics into overall usability. Here, we define an algorithm's overall score as

$$\mathsf{score}_{\textit{algorithm}} = \mathsf{max}\left\{\mathsf{0}, \ \mathsf{avg}\left\{\mathsf{score}_{\textit{parameterSet}} \mid \textit{parameterSet} \ \text{is a parameter set of} \ \textit{algorithm}\right\} - \frac{1}{8} \cdot \left(\mathsf{5} - \mathsf{categories}_{\textit{algorithm}}\right) - \frac{1}{4} \cdot \mathsf{impl}_{\textit{algorithm}} - \mathsf{generality}_{\textit{algorithm}}\right\} - \frac{1}{8} \cdot \left(\mathsf{5} - \mathsf{categories}_{\textit{algorithm}}\right) - \frac{1}{4} \cdot \mathsf{impl}_{\textit{algorithm}} - \mathsf{generality}_{\textit{algorithm}} - \mathsf{generality}_{\textit{algor$$

where score parameterSet is a score for an individual algorithm parameter set. It aims to express the various performance and size metrics of the specific variant. Depending on the type of algorithm, score parameterSet is defined as

$$score_{\textit{signature-parameterSet}} = 10 - avg\left\{ \begin{array}{cccc} \textbf{n} & \textbf{n} & \textbf{n} & \textbf{n} & \textbf{n} \\ \textbf{n} & \textbf{n} & \textbf{n} & \textbf{n} & \textbf{n} \end{array} \right\}$$

respectively

$$score_{encryption-parameterSet} = 10 - avg \left\{ \begin{array}{ccc} \mathbf{n_0^o}, & \mathbf{n_0^o}, & \mathbf{n_0^o}, & \mathbf{n_0^o}, \end{array} \right.$$





Furthermore, $1 \le$ categories algorithm ≤ 5 denotes the number of different NIST security categories offered by algorithm. By assigning numeric values of $0 = 10^{-5}$ and $0 = 10^{-5}$ and















 $impl_{signature-algorithm} = avg \left\{ \begin{array}{ccc} & & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ \end{array} \right.$

respectively

to take into account the implementation size and complexity (here, complexity doesn't mean running time, but difficulty of implementing the algorithm correctly). Finally, we define

$$\text{generality}_{\textit{algorithm}} = \begin{cases} 0 & \text{if } \textit{algorithm} \text{ is a general purpose algorithm} \\ 2 & \text{else} \end{cases}$$

to take into account if the algorithm is suitable for general use (i.e., algorithms not suitable for general use are penalized by subtracting two usability points). TBD: In the algorithm scores given in ID cards, we currently use implagorithm = 0 in the respective computations because the necessary values for implementation complexity and size are still TBD. This will be corrected later.

Example: ML-DSA Overall Usability Score

We calculate

 $score_{ML-DSA-44} = 10 - avg \left\{ 32, 32, 29, 12, 53 \right\} = 10 - 2.8 = 7.2$







Similarly, we obtain $score_{ML-DSA-65} = 7.0$ and $score_{ML-DSA-67} = 6.2$. Furthermore, categories $_{ML-DSA} = 3$ since ML-DSA offers the three security categories $_{ML-DSA}$, and $_{NL-DSA} = 0$ since ML-DSA is a general purpose signature algorithm. This results in an overall usability score of 6.55:





ML-DSA Overall Usability Score

$$score_{ML-DSA} = \max \left\{ 0, \text{ avg } \{score_{ML-DSA-44}, \text{ score}_{ML-DSA-65}, \text{ score}_{ML-DSA-87} \} - \frac{1}{8} \cdot (5 - \text{categories}_{ML-DSA}) - \frac{1}{4} \cdot \text{impl}_{ML-DSA} - \text{generality}_{ML-DSA} \right\}$$

$$= \max \left\{ 0, \text{ avg } \{7.2, 7.0, 6.2\} - \frac{1}{8} \cdot (5-3) - 0 - 0 \right\}$$

$$= \max \left\{ 0, 6.8 - 0.25 \right\}$$

$$= \max \left\{ 0, 6.55 \right\}$$

$$= 6.55$$

TBD: We use $impl_{MI-DSA} = 0$ because the necessary values to compute it are still TBD, cf. ML-DSA ID card. This will be corrected later.



ALGORITHM IMPLEMENTATION COMPLEXITY AND SIZE TBD

Size

In some contexts, algorithm implementation size can be important. For example, on smartcards or embedded devices with little storage or memory capacity and limited computational resources, an algorithms "footprint" may be a relevant factor. Developers may have to determine it is even possible to fit an algorithms implementation on a particular device and execute it. For that reason, this cheat sheet aims to include indicators for algorithms' implementation size for key generation, signature generation and verification resp. encryption and decryption.

However, it is difficult to define a useful way to measure an implementation's size: possible metrics could be lines of source code or the size of a compiled binary measured in bytes. However, those measurements would depend on factors such as programming language, compiler, and platform architecture. They are thus not ideal.

Complexity

Similarly, some developers may be concerned with an algorithm's implementation complexity. Here, "complexity" refers not to running time or space complexity, but rather to the level of difficulty of implementing an algorithm correctly without introducing vulnerabilities by mistake. The question of how difficult it is to implement a particular algorithm compared to another has repeatedly come up in exchanges on cryptography mailing lists or forums. It is also not specific to PQC (e.g. it is often claimed that ECDSA is harder to implement without vulnerabilities than RSA). Therefore, this cheat sheet also aims to include indicators about that complexity/difficulty.

However, as with an algorithm's size, there is no obvious and objective way to measure this complexity.

To complete this part of the cheat sheets in a useful manner, suggestions and contributions from the cryptography community for how to do so are welcome and necessary!

General considerations for developers implementing cryptographic algorithms

For implementations of cryptography, unlike other algorithms, getting the correct outputs is not sufficient. For a secure implementation, it is crucial that no sensitive and confidential information leaks in any way, not even through side channel attacks. Such a leak could occur in many different ways and places in an implementation (e.g. leaked nonces, biased bits in (pseudo-)random numbers, prime numbers, execution times of certain parts of the code, etc.). Compilers, code generation tools or even an IDE applying code formatting rules may try to optimize code to make it more performant - but introduce a vulnerability while doing so.



Developers should be aware of the possible pitfalls of implementing cryptography on their own. Caution is advised, and if possible, it is recommended to use well-known cryptographic libraries and products developed by experts instead of using self-developed implementations.



Sources and References

TBD