

I certify that every answer in this assignment is the result of my own work; that I have neither copied off the Internet nor from any one else's work; and I have not shared my answers or attempts at answers with anyone else.

1: Compute the worst-case time requirement of the following algorithm as a function of n , the length of the input array A . Assume a constant cost of 2 for the loop control statements and 1 for every other executable statement (and, of course, zero for comments).

Insert entries in a table with 3 columns: Line, Cost, and # Times.

Next, use those entries to obtain a closed-form expression (a polynomial in n) for $T(n)$. Hint: see the slides for INSERTIONSORT. Repeat the above for best-case.

Line#	Cost	Worst Case	Best Case
1	c_1	1	1
2	c_2	n	1
3	c_3	$n-1$	1
4	c_4	$\frac{n(n+1)}{2} - 1$	$n-1$
5	c_5	0	0
6	c_6	0	0
7	c_7	$\frac{n(n+1)}{2} - 2$	$n-1$
8	c_8	$\frac{n(n+1)}{2} - 2$	0
9	c_9	$\frac{n(n+1)}{2} - 2$	0
10	c_{10}	$\frac{n(n+1)}{2} - 2$	0
11	c_{11}	$\frac{n(n+1)}{2} - 2$	0
12	c_{12}	$\frac{n(n+1)}{2} - 1$	1
13	c_{13}	1	1

Best Case: $T(n) = (n-1)(c_4 + c_7) + c_1 + c_2 + c_3 + c_{12} + c_{13}$

Worst Case: $T(n) =$

$$\left(\frac{n(n+1)}{2} - 1\right)(c_4 + c_{12}) + \left(\frac{n(n+1)}{2} - 2\right)(c_7 + c_8 + c_9 + c_{10} + c_{11}) + c_2n + c_3(n-1) + c_1$$

2: For each of the following statements, answer if it is true or false as per the definition of the three asymptotic notations $O()/\Omega()/\Theta()$. If true, then provide appropriate corresponding constant(s) $c/c_1, c_2$ when n_0 is chosen as 2. If false, then correct the RHS (right hand side) by replacing the function family but retaining the asymptotic notation (i.e., do not change $O()$ to something else like $\Theta()$). Provide as tight a bound as possible and provide appropriate constant(s) $c/c_1, c_2$ when n_0 is chosen as 2.

- **TRUE/FALSE** $2n \lg n + 100n + 10 = O(n^2)$
This statement is False. The RHS should be $O(n \lg n)$ where $n_0 = 2$ and $c = 5$
- **TRUE/FALSE** $2n \lg n + n + 10 = \Omega(n^2)$ This statement is true when corresponding to $n_0 = 2$ and $c = 4$
- **TRUE/FALSE** $10n \lg n + n^2 + n + 10 = \Theta(n^2)$ This is true for $n_0 = 2$ and for constant values $c_1 = 2$ and $c_2 = 10$