

Hoja de trabajo #3

Ejercicio #1

Realizar $[s(s(0)))] \oplus [s(s(s(0)))]$ paso por paso:

Empezamos con $[s(s(0)))] \oplus [s(s(s(0)))]$

$$\rightarrow s[s(s(0) \oplus s(s(s(0))))]$$

$$\rightarrow s[s[s(0) \oplus s(s(s(0)))]]$$

$$\rightarrow s[s[s[0 \oplus s(s(s(0)))]]]$$

$$\rightarrow s[s[s[s(s(s(0)))]]]$$

$$\rightarrow s(s(s(s(s(s(0))))))$$

Ejercicio #2

Definicion de multiplicacion para numeros unarios (\otimes):

$$n \otimes m = \begin{cases} 0 & \text{si } n = 0 \\ 0 & \text{si } m = 0 \\ n \oplus (n \otimes i) & \text{si } m = s(i) \end{cases}$$

Ejercicio #3

Verificacion de la definicion de la multiplicacion del problema #2:

$s(s(s(0))) \otimes 0$:

$$s(s(s(0))) \otimes 0 = 0 \text{ Por la segunda propiedad: } n \otimes m = 0 \text{ si } m = 0$$

$s(s(s(0))) \otimes s(0)$:

$$s(s(s(0))) \otimes s(0)$$

$$\rightarrow s(s(s(0))) \oplus [s(s(s(0))) \otimes 0]$$

Por la definicion sabemos que el resultado del lado derecho de la *suma* es 0

$$\rightarrow s(s(s(0))) \oplus 0$$

$$\rightarrow s(s(s(0)))$$

$$s(s(s(0))) \otimes s(s(0)):$$

$$\begin{aligned}
& s(s(s(0))) \otimes s(s(0)) \\
& \rightarrow s(s(s(0))) \oplus [s(s(s(0))) \oplus s(0)] \\
& \rightarrow s(s(s(0))) \oplus [s(s(s(0))) \oplus [s(s(s(0))) \otimes 0]] \\
& \rightarrow s(s(s(0))) \oplus [s(s(s(0))) \oplus 0] \\
& \rightarrow s(s(s(0))) \oplus s(s(s(0))) \\
& \rightarrow s[s(s(s(0))) \oplus s(s(s(0)))] \\
& \rightarrow s[s[s(0) \oplus s(s(s(0)))] \\
& \rightarrow s[s[s[0 \oplus s(s(s(0)))] \\
& \rightarrow s[s[s[s(s(s(0)))] \\
& \rightarrow s(s(s(s(s(s(0))))))
\end{aligned}$$

Ejercicio #4

$$a \oplus s(s(0)) = s(s(a)):$$

Tomamos la parte derecha de la igualdad y la modificamos de la siguiente forma:

$$\begin{aligned}
& \rightarrow a \oplus s(s(0)) \\
& \rightarrow s(s(0)) \oplus a \\
& \rightarrow s[s(0) + a] \\
& \rightarrow s[s[0 + a]]
\end{aligned}$$

Por definicion de la suma sabemos que $0 + a = a$

$$\begin{aligned}
& \rightarrow s[s(a)] \\
& \rightarrow s(s(a)) = s(s(a))
\end{aligned}$$

$$a \otimes b = b \otimes a:$$

No pude :’(

$$a \otimes (b \otimes c) = (a \otimes b) \otimes c$$

Esta tampoco :’(

$$(a \oplus b) \otimes c = (a \otimes c) \oplus (b \otimes c)$$

Esta menos :’(