

(a)

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CS-050 (BE)

Section - B

Assignment #1: CSM

Question #1(a)

$$t_a = 5 \text{ cycles}$$

$$t_m = 10 \text{ cycles}$$

$$\text{clock rate} = 250\text{MHz}$$

$$\# \text{ FP add} = N \quad \# \text{ FP mul} = 2N$$

$$\text{Total, } \# \text{ FP operations} = 3N$$

$$t_1 = N (t_a + 2t_m)$$

$$t_1 = N (5 + 2(10))$$

$$t_1 = 25N$$

$$\text{one cycle} = \frac{1}{250\text{MHz}} = 4\text{ n sec}$$

$$t_1 = 25N \times 4\text{ n}$$

$$// \quad t_1 = 100 N \text{ n sec} //$$

$$R_1 = \frac{\text{total}_1}{t_1} = \frac{3N}{100Nm} = 30 \text{ MFLOPS}$$

Question # 1(b)

$$s = 0$$

for (int i = 1; i <= N; i++)

if (x[i] != 0)

$$s = s + x[i] * x[i] * x[i]$$

Question # 1(c)

$$\# \text{ of FP add} = fN, \# \text{ of FP mul} = 2fN$$

$\therefore f$ = fraction of N for which $x[i]$ are non-zero

$$\text{total}_2 = \# \text{ FP operations} = 3fN$$

for Non-zero: $f = 0.7$

$$t_2 = N \{ t_{if} + f(t_a + 2t_m) \}$$

t_{if} = time required to execute each "if" test

$$t_2 = N \{ 3 + 0.7(5 + 2(10)) \}$$

$$\therefore t_2 = 20.5N \text{ cycles}$$

CPU Clock Rate = 250 MHz

Clock Period = 4 nsec

$$t_2 = 20.5 \text{ N} \times 4 \text{ nsec}$$

$$// \quad t_2 = 82 \text{ Nnsec} //$$

$$R_2 = \frac{\text{total}_2}{t_2} = \frac{3 \text{ fN}}{82 \text{ Nnsec}} = \frac{3(0.7)}{82 \text{ nsec}} = 25.60 \text{ MFlops}$$

Question #1 (d)

$$S_{B,A} = \frac{t_1}{t_2} = \frac{100 \text{ Nnsec}}{82 \text{ Nnsec}}$$

$$// \quad S_{B,A} = 1.22 //$$

Relative change of segment B over A

$$\Delta_{B,A} = 1.22 - 1$$

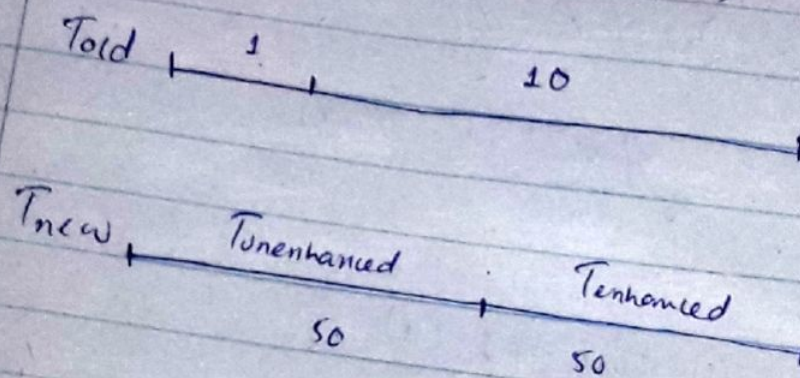
$$\Delta_{B,A} = 0.22$$

$$// \quad \Delta_{B,A} = 22\% //$$

Question #1 (e)

Execution rate of system A (R_1) is 20 MFlops whereas execution rate of system B (R_2) is 25.60 MFlops which shows that system B is slower than system A. On the other hand relative change is showing system B is actually 22% faster than system A. Therefore end-base metrics (execution time) are reliable.

Question # 2(a)



$$\text{Speed up} = \frac{T_{old}}{T_{new}}$$

$$\text{Speed up} = \frac{10+1}{1+1}$$

$$\text{Speed up} = \frac{11}{2}$$

$$\text{Speed up} = 5.5$$

Question # 2(b)

$$(1 - \alpha) = ?$$

Using Amdahl's law

$$\text{Speedup} = \frac{1}{\frac{1}{9} + \left(1 - \frac{1}{9}\right)\alpha}$$

$$5.5 = \frac{1}{\frac{1}{10} + \left(1 - \frac{1}{10}\right)\alpha}$$

$$\frac{1}{10} + \frac{9}{10} \alpha = \frac{1}{5.5}$$

$$\frac{9}{10} \alpha = \frac{1}{5.5} - \frac{1}{10}$$

$$\frac{9}{10} \alpha = \frac{9}{110}$$

$$\alpha = \frac{1}{11}$$

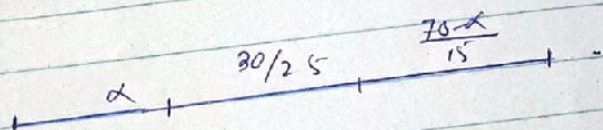
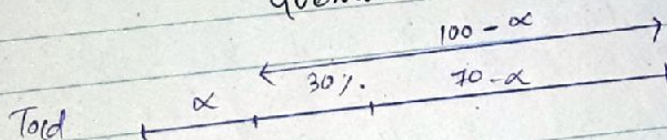
$$\alpha = 0.0909$$

$$\alpha = 0.91$$

$$1 - \alpha = 0.91$$

Therefore 91% of original execution time has been converted to fast mode.

Question # 3



$$\text{Speedup} = \frac{T_{old}}{T_{new}}$$

$$\text{Speedup} = \frac{\alpha + 100 - \alpha}{\frac{75\alpha + 90 + 350 - 5\alpha}{75}}$$

$$\text{Speedup} = \frac{100}{\frac{70\alpha + 440}{75}}$$

$$5 = \frac{100}{\frac{70\alpha + 440}{75}}$$

$$5 = \frac{7500}{70\alpha + 440}$$

$$70\alpha + 440 = \frac{7500}{5}$$

$$70\alpha = 1500 - 440$$

$$\alpha = \frac{1060}{70}$$

$$\alpha = 15.14$$

$$\alpha \approx 15\%$$

Hence enhancement 2 must be used as $70 - \alpha = 55\%$ of the time to achieve the overall speedup of 5.