Ensemble Kalman Filter adapted to particle simulations

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ABSTRACT

Data assimilation methods refer to a sequential estimation of the state of a system based on the incorporation of online observations. The complete way determines the state’s posterior distribution given the observations until now.

In the case of linear Gaussian models and observations, one can update the mean and covariance of the system’s state analytically using the Kalman Filter formula [1].

However, in general, one must estimate the state’s distribution. A popular filter is the Ensemble Kalman Filter (EnKF), a Monte-Carlo version of the Kalman Filter, which is suitable for non-linear problems and high-dimensional states [2]. The EnKF method uses a set of realizations (in our case, simulations) to estimate the empirical distribution of the system’s state. Then, the approximated Kalman Filter formula is applied to update the members of the realizations’ set.

This method has been extensively applied to problems discretized on fixed Eulerian grids (for instance, in Geociences [3]). The EnKF filter requires adaptations for more specific Eulerian discretization methods, such as for problems using members having different mesh resolutions [4] or moving mesh simulations [5]. In this work, we adapt the EnKF method to particle-based simulations. Specifically, we focus on the case of members with different particle discretizations (number of particles, positions, and weights).

We propose and test different filters involving hybrid particle-mesh or purely Lagrangian approaches, with a criterion to adapt the particle discretization of the updated members. These developments are illustrated with 2D vortex simulations. The proposed schemes can be applied to other methods, such as the SPH or MPM.

**REFERENCES**

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