# Appendix D

Replication scripts: Models fitted in main paper

## Introduction

In this Appendix, we present scripts for replicating the results from the main paper. In the Method section, packages used are listed and data preparation is shown. In the Results section, we show how each of the models in the main document were fit, and how the figures and tables can be replicated. In sections Appendix B and C, we show how results, tables and figures from the appendices can be replicated. Finally, the last section provides the references.

## Method

All analyses were performed in R (version 4.1.0, R Core Team, 2021). We fitted (penalized) logistic regression models using R package glmnet (version 4.1.3, Friedman et al., 2010); generalized additive models (GAMs) with smoothing splines using package mgcv (version 1.8.35, Wood, 2017); conditional inference trees using package partykit (version 1.2.15, Hothorn et al., 2006); gradient boosted tree ensembles using package gbm (version 2.1.8, Greenwell et al., 2020); random forests using package ranger (version 0.13.1, Wright & Ziegler, 2017); prediction rule ensembles using package pre (version 1.0.3, Fokkema, 2020); k nearest neighbours using package class (version 7.3.19, Venables & Ripley, 2002).

Appendix E shows our code and results for tuning the parameter settings using cross validation. All parameter settings employed here are based on those results, for most methods. We did not tune the parameters of the GAMs with smoothing splines, because we expected the defaults to work well out of the box. We simply employed the defaults of thin-plate regression splines and generalized cross validation method to fit the smoothing splines. This provides built-in regularization of the wigglyness, without the need for choosing an optimal value for penalty or tuning parameters. For smaller samples, restricted maximum likelihood (REML) would be preferred. For the analyses using the items as predictors, we set the number of basis functions of the thin-plate regression splines to four, instead of the default of eight, because the item responses have only five possible values; increasing the number of basis functions would yield an unidentified model. Furthermore, because of the larger number of predictors, and the benefit of penalization observed in the logistic regression, we also applied a penalty to the linear part of each smoothing spline function, so that some items can be completely eliminated from the model.

## Data preparation

```
data <- read.delim("data.csv", header = TRUE)</pre>
```

```
## Items should be scored 1-5, 0s are missings
data[, 1:48][sapply(data[, 1:48], function(x) x == 0)] \leftarrow NA
data <- data[complete.cases(data[ , 1:48]), ]</pre>
## Select only university students
data <- data[data$education >= 3, ]
# table(data$major)
psych_ids <- rowSums(sapply(c("psych", "psyhcology", "psycotherapy", "couns",</pre>
                                "behavior", "behaviour", "neuro"),
                              function(x) grepl(x, data$major, ignore.case = TRUE)))
anim_ids <- grepl("anim", data$major, ignore.case = TRUE) ## exclude animal psych
data$major <- factor(ifelse(psych_ids > 0, "psychology", "other"))
data$major[anim_ids > 0 & psych_ids > 0] <- "other"</pre>
set.seed(42)
test_ids <- sample(1:nrow(data), ceiling(nrow(data)/4))</pre>
train ids <- which(!1:nrow(data) %in% test ids)</pre>
train_y <- as.numeric(data$major)[train_ids] - 1</pre>
test_y <- as.numeric(data$major)[test_ids] - 1</pre>
data$Real <- rowSums(data[ , paste0("R", 1:8)])</pre>
data$Inve <- rowSums(data[ , paste0("I", 1:8)])</pre>
data$Arti <- rowSums(data[ , paste0("A", 1:8)])</pre>
data$Soci <- rowSums(data[ , paste0("S", 1:8)])</pre>
data$Ente <- rowSums(data[ , paste0("E", 1:8)])</pre>
data$Conv <- rowSums(data[ , paste0("C", 1:8)])</pre>
Sample size:
nrow(data)
## [1] 55593
Proportions of observations choosing psychology (not) as a major:
prop.table(table(data$major)) ## total dataset
##
##
        other psychology
    0.8057849 0.1942151
prop.table(table(data$major[train_ids])) ## train dataset
##
##
        other psychology
## 0.8053677 0.1946323
```

```
prop.table(table(data$major[test_ids])) ## test dataset

##

## other psychology
## 0.8070365 0.1929635
```

## Results

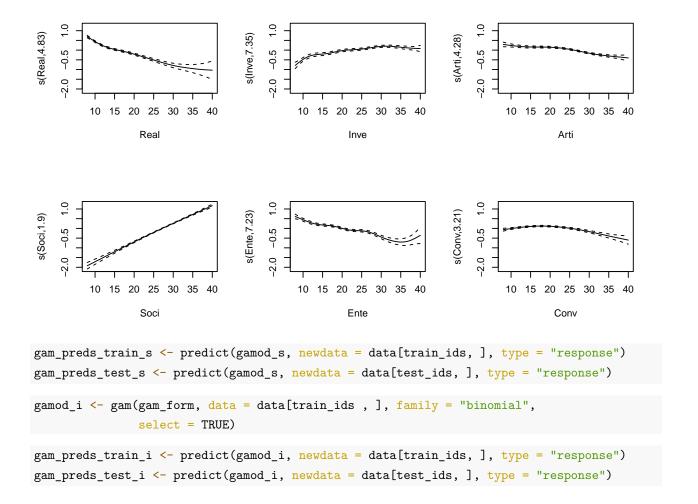
```
varnames_i <- pasteO(rep(c("R", "I", "A", "S", "E", "C"), each = 8), 1:8)
varnames_s <- c("R", "I", "A", "S", "E", "C")</pre>
```

## (Penalized) Logistic Regression

## Generalized Additive Model

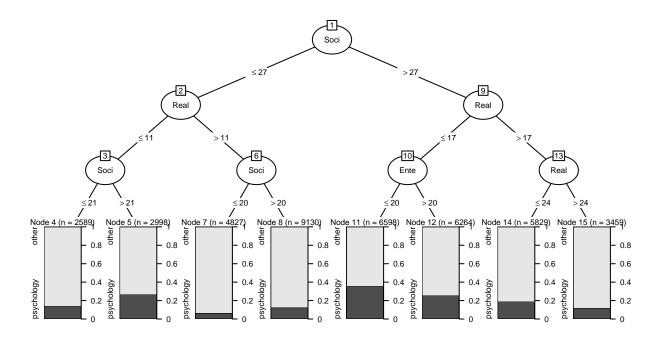
## Figure 1

```
par(mfrow = c(2, 3))
plot(gamod_s)
```



## **Decision Tree**

### Figure 2



```
ct_preds_train_s <- predict(ct_s, type = "prob")[ , "psychology"]
ct_preds_test_s <- predict(ct_s, newdata = data[test_ids , ], type = "prob")[ , "psychology"]
ct_form <- formula(paste("major ~", paste(varnames_i, collapse = "+")))
ct <- ctree(ct_form, data = data[train_ids , ], maxdepth = 9)
ct_preds_train_i <- predict(ct, type = "prob")[ , "psychology"]
ct_preds_test_i <- predict(ct, newdata = data[test_ids , ], type = "prob")[ , "psychology"]</pre>
```

#### Gradient boosted tree ensemble

```
gb_preds_train_i <- predict(gb_i, newdata = data[train_ids, ], type = "response")
gb_preds_test_i <- predict(gb_i, newdata = data[test_ids, ], type = "response")</pre>
```

#### Random Forest

## **Prediction Rule Ensembling**

#### Table 1

```
pr_preds_train_s <- predict(pr_s, type = "response")
pr_preds_test_s <- predict(pr_s, newdata = data[test_ids , ], type = "response")
imps <- pre::importance(pr_s, plot=FALSE)
varimps_pre <- imps$varimps
imps <- imps$baseimps[1:6, c("description", "coefficient")]
colnames(imps) <- c("Description", "Coefficient")
imps$Coefficient <- round(imps$Coefficient, digits = 3)
kable(imps, row.names = FALSE, align = c("l", "c"))</pre>
```

Description	Coefficient
Soci > 27 & Ente <= 31 & Conv <= 30	0.182
Soci > 23 & Ente $\leq$ 29 & Real $\leq$ 24	0.181
$\mathrm{Real} > 10 \ \& \ \mathrm{Soci} <= 35$	-0.175
$\mathrm{Real} <= 22 \ \& \ \mathrm{Soci} > 19 \ \& \ \mathrm{Inve} > 18$	0.138
Inve $> 10 \& \text{Real} \le 13$	0.120

Description	Coefficient
$Conv \le 23 \& Arti \le 29 \& Soci > 21$	0.112

```
pr_preds_train_i <- predict(pr_i, type = "response")
pr_preds_test_i <- predict(pr_i, newdata = data[test_ids , ], type = "response")</pre>
```

## k Nearest Neighbours

```
library("class")
## Model for training predictions
knn_mod <- knn(train = data[train_ids , varnames_s],</pre>
               test = data[train ids , varnames s],
               cl = as.factor(data[train_ids, "major"]),
               k = 300, use.all = TRUE, prob = TRUE)
## Need to obtain predicted probability for second class
knn_preds_train_s <- ifelse(</pre>
  knn_mod == "psychology", attr(knn_mod, "prob"), 1 - attr(knn_mod, "prob"))
## Model for testing predictions
knn_mod <- knn(train = data[train_ids , varnames_s],</pre>
               test = data[test_ids , varnames_s],
               cl = as.factor(data[train_ids, "major"]),
               k = 300, use.all = TRUE, prob = TRUE)
knn_preds_test_s <- ifelse(</pre>
  knn_mod == "psychology", attr(knn_mod, "prob"), 1 - attr(knn_mod, "prob"))
## Model for training predictions
knn_mod <- knn(train = data[train_ids , varnames_i],</pre>
               test = data[train_ids , varnames_i],
               cl = as.factor(data[train_ids, "major"]),
               k = 100, use.all = TRUE, prob = TRUE)
## Need to obtain predicted probability for second class
knn_preds_train_i <- ifelse(</pre>
  knn_mod == "psychology", attr(knn_mod, "prob"), 1 - attr(knn_mod, "prob"))
## Model for testing predictions
knn_mod <- knn(train = data[train_ids , varnames_i],</pre>
               test = data[test_ids , varnames_i],
               cl = as.factor(data[train_ids, "major"]),
               k = 100, use.all = TRUE, prob = TRUE)
knn_preds_test <- ifelse(</pre>
  knn_mod == "psychology", attr(knn_mod, "prob"), 1 - attr(knn_mod, "prob"))
```

## Model comparisons

## Figure 3

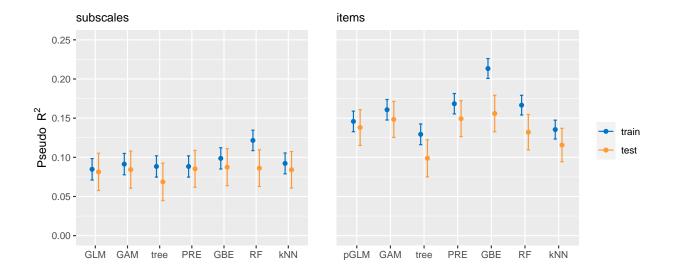
```
par(mfrow = c(2, 3))
par(mar = c(1, 4, 2, 1), mgp = c(1.5, .5, 0), tck = -0.05)
library("colorspace")
## Logistic regression
plot(coef(glmod s)[-1], xaxt = "n", ylab = "Estimated coefficient",
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     main = "Logistic Regression", cex.main = .7)
text(coef(glmod s)[-1], labels = varnames s, cex = 1,
     col = rep(qualitative_hcl(6)), font = 2)
abline(0, 0, col = "grey")
## Generalized additive model
sum <- summary(gamod_s)</pre>
plot(sqrt(sum$chi.sq), xaxt = "n", ylab = expression(sqrt(chi^2)),
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     main = "Generalized Additive Model", cex.main = .7)
text(sqrt(sum$chi.sq), labels = varnames_s, cex = 1,
     col = rep(qualitative_hcl(6)), font = 2)
## Conditional inference tree
ct6 <- cforest(major ~ Real + Inve + Arti + Soci + Ente + Conv,
               data = data[train_ids , ], ntree = 1L, mtry = 6,
               perturb = list(replace = FALSE, fraction = 1L),
               control = ctree_control(maxdepth = 6))
imps <- varimp(gettree(ct6), risk = "loglik")</pre>
imps <- imps[c("Real", "Inve", "Arti", "Soci", "Ente", "Conv")]</pre>
plot(sqrt(imps), xaxt = "n", ylab = expression(sqrt(Importance)),
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     main = "Tree", cex.main = .7)
text(sqrt(imps), labels = varnames_s, cex = 1,
     col = rep(qualitative_hcl(6)), font = 2)
## Gradient boosted ensemble
sum <- summary(gb_s, plotit = FALSE, method = permutation.test.gbm)</pre>
imps <- sum$rel.inf</pre>
names(imps) <- sum$var</pre>
imps <- imps[c("Real", "Inve", "Arti", "Soci", "Ente", "Conv")]</pre>
plot(sqrt(imps), xaxt = "n", ylab = expression(sqrt(Importance)),
col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
```

```
main = "Gradient Boosted Ensemble", cex.main = .7)
text(sqrt(imps), labels = varnames_s, cex = 1,
     col = rep(qualitative_hcl(6)), font = 2)
## Random forest
library("ranger")
load(file = "RF_subscales.Rda")
imps <- ranger::importance(rf_s)</pre>
plot(sqrt(imps), xaxt = "n", ylab = expression(sqrt(Importance)),
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     main = "Random Forest", cex.main = .7)
text(sqrt(imps), labels = varnames_s, cex = 1,
     col = rep(qualitative_hcl(6)), font = 2)
## Prediction rule ensemble
imps <- varimps_pre$imp</pre>
names(imps) <- varimps_pre$varname</pre>
imps <- imps[c("Real", "Inve", "Arti", "Soci", "Ente", "Conv")]</pre>
plot(imps, xaxt = "n", ylab = "Importance",
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     cex.main = .7, main = "Prediction Rule Ensemble")
text(imps, labels = varnames_s, cex = 1,
     col = rep(qualitative_hcl(6)), font = 2)
              Logistic Regression
                                                Generalized Additive Model
     0.10
   Estimated coefficient
     0.02
                                                                            0.15
                                      \stackrel{7}{\sim}
                                                                                                  Ē
     0.00
                                                                            0.10
                                                              Ē
                 Α
     -0.05
                           Ē
                                                                            0.05
            Gradient Boosted Ensemble
                                                   Random Forest
                                                                                    Prediction Rule Ensemble
                                         0.10
                                                                            0.30
                                                                          Importance
                                         0.08
                                                                                                  Ē
                                                                            0.20
                           Ē
                                         90.0
                                                              Ē
                 Α
```

Figure 5

```
ct_preds_train_s, pr_preds_train_s, gb_preds_train_s,
                           rf_preds_train_s, knn_preds_train_s)
preds_test <- data.frame(bm_preds_test = rep(mean(train_y), times = length(test_ids)),</pre>
                          glm_preds_test_s, gam_preds_test_s,
                          ct_preds_test_s, pr_preds_test_s, gb_preds_test_s,
                          rf_preds_test_s, knn_preds_test_s)
results <- data.frame(</pre>
  Brier_train = sapply(preds_train, function(x) mean((train_y - x)^2)),
  Brier_test = sapply(preds_test, function(x) mean((test_y - x)^2)))
results$R2_train <- 1 - results$Brier_train / results$Brier_train[1]</pre>
results$R2_test <- 1 - results$Brier_test / results$Brier_test[1]</pre>
tmp <- data.frame(</pre>
 R2 = c(results$R2_train[-1], results$R2_test[-1]),
  SE = c(sapply((preds_train[,-1] - train_y)^2,
                function(x) sd(x)/(sqrt(nrow(preds_train))*results$Brier_train[1])),
         sapply((preds_test[,-1] - test_y)^2,
                function(x) sd(x)/(sqrt(nrow(preds_test))*results$Brier_test[1]))),
  data = rep(c("train", "test"), each = nrow(results)-1),
  method = rep(c("GLM", "GAM", "tree", "PRE", "GBE", "RF", "kNN"), times = 2))
tmp$data <- factor(tmp$data, levels = c("train", "test"))</pre>
tmp$method <- factor(tmp$method, levels = c("GLM", "GAM", "tree", "PRE", "GBE", "RF", "kNN"))</pre>
## Plot results
library("ggplot2")
p_subscales \leftarrow ggplot(tmp, aes(x = method, y = R2)) +
  geom_point(aes(color = data, fill = data),
             stat = "identity", position = position_dodge(0.4)) +
  ggtitle("subscales") + xlab("") + ylab(expression("Pseudo "~R^2)) +
  theme(legend.position = "none", plot.title = element_text(size = 11)) +
  scale color manual(values = c("\#0073C2FF", "\#ff9933")) + vlim(0, 0.25) +
  scale_fill_manual(values = c("#0073C2FF", "#ff9933")) +
  geom_errorbar(aes(color=data, ymin = R2-1.96*SE, ymax = R2+1.96*SE),
                width = .2, position = position dodge(0.4))
## Gather results for prediction with items
preds_train <- data.frame(bm_preds_train = rep(mean(train_y), times = length(train_ids)),</pre>
                           glm_preds_train_i, gam_preds_train_i,
                           ct_preds_train_i, pr_preds_train_i, gb_preds_train_i,
                           rf_preds_train_i, knn_preds_train_i)
preds_test <- data.frame(bm_preds_test = rep(mean(train_y), times = length(test_ids)),</pre>
                           glm_preds_test_i, gam_preds_test_i,
                           ct_preds_test_i, pr_preds_test_i, gb_preds_test_i,
```

```
rf_preds_test_i, knn_preds_test_i)
results <- data.frame(</pre>
  Brier_train = sapply(preds_train, function(x) mean((train_y - x)^2)),
  Brier_test = sapply(preds_test, function(x) mean((test_y - x)^2)))
results$R2_train <- 1 - results$Brier_train / results$Brier_train[1]</pre>
results$R2_test <- 1 - results$Brier_test / results$Brier_test[1]</pre>
tmp <- data.frame(</pre>
 R2 = c(results$R2_train[-1], results$R2_test[-1]),
  SE = c(sapply((preds_train[,-1] - train_y)^2,
                function(x) sd(x)/(sqrt(nrow(preds train))*results$Brier train[1])),
          sapply((preds_test[,-1] - test_y)^2,
                function(x) sd(x)/(sqrt(nrow(preds_test))*results$Brier_test[1]))),
  data = rep(c("train", "test"), each = nrow(results)-1),
  method = rep(c("pGLM", "GAM", "tree", "PRE", "GBE", "RF", "kNN"), times = 2))
tmp$data <- factor(tmp$data, levels = c("train", "test"))</pre>
tmp$method <- factor(tmp$method, levels = c("pGLM", "GAM", "tree", "PRE", "GBE", "RF", "kNN"))
## Plot results
p_{items} \leftarrow ggplot(tmp, aes(x = method, y = R2)) +
  geom_point(aes(color = data, fill = data),
    stat = "identity", position = position_dodge(0.4)) + xlab("") + ylab(" ") +
  theme(axis.text.y=element_blank(), axis.ticks.y = element_blank(),
        plot.title = element_text(size = 11), legend.title = element_blank()) +
  ggtitle("items") + scale_color_manual(values = c("#0073C2FF", "#ff9933")) +
  scale_fill_manual(values = c("#0073C2FF", "#ff9933")) + ylim(0, .25) +
  geom_errorbar(aes(color=data, ymin = R2-1.96*SE, ymax = R2+1.96*SE),
                width = .2, position = position_dodge(0.4))
library("gridExtra")
grid.arrange(p_subscales, p_items, ncol = 2, widths = c(6.75, 8))
```



## Appendix B

##

```
data$age[data$age > 103] <- NA ## remove impossible ages</pre>
prop.table(table(data$gender)) ## 0=missing, 1=Male, 2=Female, 3=Other
##
##
## 0.001151224 0.320382062 0.673160290 0.005306423
prop.table(table(data$married)) ## 0=missing, 1,2,3=Never, currently, previously married
##
##
                                     2
                                                  3
## 0.005648193 0.582717249 0.328242764 0.083391794
prop.table(table(data$urban)) ## O=missing, 1=Rural, 2=Suburban, 3=Urban
##
##
## 0.007087223 0.217419459 0.372474952 0.403018366
prop.table(table(data$race)) ## 0=missing, 1=Asian, 2=Arab, 3=Black,
##
##
                                                                    5
## 0.01404853 0.19833432 0.01329304 0.07436188 0.60887162 0.09109060
## 4=Indigenous Australian/Native American/White, 5=Other
## (A coding mistake resulted in aggregating options in category 4)
prop.table(table(data$engnat)) ## 0=missing, 1=Yes, 2=No
```

```
## 0.002248485 0.659813286 0.337938230
```

Figure B1

```
par(mfrow = c(2, 3))
for (i in c("Real", "Inve", "Arti", "Soci" , "Ente", "Conv")) {
  dens <- density(data[ , i])
  plot(dens, main = "", xlab = i)
  polygon(dens, col="lightblue", border="black")
}</pre>
```

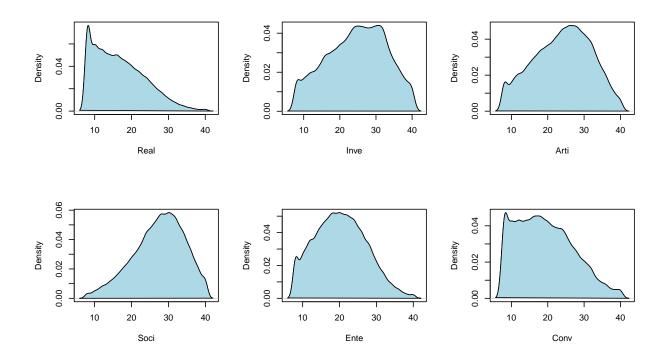


Table B1

	Real	Inve	$\operatorname{Arti}$	Soci	Ente	Conv
Real	1.000	0.332	0.182	0.049	0.305	0.460
Inve	0.332	1.000	0.329	0.141	0.016	0.065
Arti	0.182	0.329	1.000	0.290	0.253	-0.056
Soci	0.049	0.141	0.290	1.000	0.356	0.124
Ente	0.305	0.016	0.253	0.356	1.000	0.464

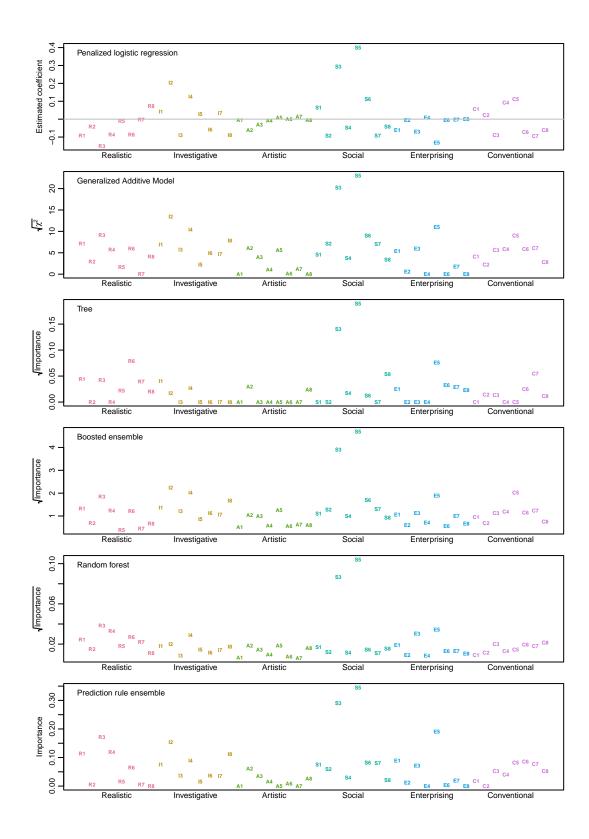
	Real	Inve	Arti	Soci	Ente	Conv
Conv	0.460	0.065	-0.056	0.124	0.464	1.000

## Appendix C

#### Figure C1

```
par(mar = c(1.5, 4, 0.2, 2), mgp = c(1.5, .5, 0), tck = -0.05)
par(mfrow = c(6, 1))
library("glmnet")
plot(coef(glmod_i)[-1], xaxt = "n", ylab = "Estimated coefficient",
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     main = " ", cex.main = .7)
text(coef(glmod_i)[-1], labels = varnames_i, cex = .5,
     col = rep(qualitative_hcl(6), each = 8), font = 2)
abline(0, 0, col = "grey")
legend("topleft", legend = "Penalized logistic regression", cex = .7, bty = "n")
axis(1, 4.5 + c(0:5)*8, tick = FALSE, padj = -1.5,
     labels = c("Realistic", "Investigative", "Artistic", "Social" ,
                              "Enterprising", "Conventional"),
     cex.axis = .7)
library("mgcv")
load(file = "GAM items.Rda")
sum <- summary(gamod i)</pre>
plot(sqrt(sum$chi.sq), xaxt = "n", ylab = expression(sqrt(chi^2)),
     main = " ", cex.main = .7,
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ")
text(sqrt(sum$chi.sq), labels = varnames_i, cex = .5,
     col = rep(qualitative_hcl(6), each = 8), font = 2)
legend("topleft", legend = "Generalized Additive Model", cex = .7, bty = "n")
axis(1, 4.5 + c(0:5)*8, tick = FALSE, padj = -1.5,
     labels = c("Realistic", "Investigative", "Artistic", "Social" ,
                             "Enterprising", "Conventional"),
     cex.axis = .7)
ct6 <- cforest(ct_form,</pre>
               data = data[train_ids , ], ntree = 1L, mtry = 6,
               perturb = list(replace = FALSE, fraction = 1L),
               control = ctree_control(maxdepth = 6))
imps <- varimp(gettree(ct6), risk = "loglik")</pre>
```

```
imp_names <- names(imps)</pre>
imps <- c(imps, rep(0, times = 48 - length(imps)))</pre>
names(imps) <- c(imp_names, varnames_i[!varnames_i %in% imp_names])</pre>
plot(sqrt(imps[varnames_i]), xaxt = "n", ylab = expression(sqrt(Importance)),
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     main = " ", cex.main = .7)
text(sqrt(imps[varnames_i]), labels = varnames_i, cex = .5,
     col = rep(qualitative_hcl(6), each = 8), font = 2)
legend("topleft", legend = "Tree", cex = .7, bty = "n")
axis(1, 4.5 + c(0:5)*8, tick = FALSE, padj = -1.5,
     labels = c("Realistic", "Investigative", "Artistic", "Social" ,
                              "Enterprising", "Conventional"),
     cex.axis = .7)
load(file = "gb_i_summary.Rda")
imps <- sum_i[match(varnames_i, sum_i$var), ]</pre>
plot(sqrt(imps$rel.inf), xaxt = "n", main = " ",
     ylab = expression(sqrt(Importance)), cex.main = .7,
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ")
text(sqrt(imps$rel.inf), labels = imps$var, cex = .5,
     col = rep(qualitative_hcl(6), each = 8), font = 2)
legend("topleft", legend = "Boosted ensemble", cex = .7, bty = "n")
axis(1, 4.5 + c(0:5)*8, tick = FALSE, padj = -1.5,
     labels = c("Realistic", "Investigative", "Artistic", "Social" ,
                              "Enterprising", "Conventional"),
     cex.axis = .7)
imps <- ranger::importance(rf_i)</pre>
plot(sqrt(imps), xaxt = "n", main = " ",
     col = "white", cex.lab = .7, cex.axis = .7, xlab = " ",
     ylab = expression(sqrt(Importance)), cex.main = .7)
text(sqrt(imps), labels = names(imps), cex = .5,
     col = rep(qualitative_hcl(6), each = 8), font = 2)
legend("topleft", legend = "Random forest", cex = .7, bty = "n")
axis(1, 4.5 + c(0:5)*8, tick = FALSE, padj = -1.5,
     labels = c("Realistic", "Investigative", "Artistic", "Social" ,
                              "Enterprising", "Conventional"),
     cex.axis = .7)
imps <- pre::importance(pr_i, cex.axis = .7, plot = FALSE)$varimps</pre>
zero_vars <- varnames_i[!varnames_i %in% imps[ , 1]]</pre>
imps <- rbind(imps, data.frame(varname = zero_vars,</pre>
                                imp = rep(0, times = length(zero_vars))))
```



# References

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