Introduction to classification and regression trees, random forests and model-based recursive partitioning in R

Day 2: Stability and tree ensembles

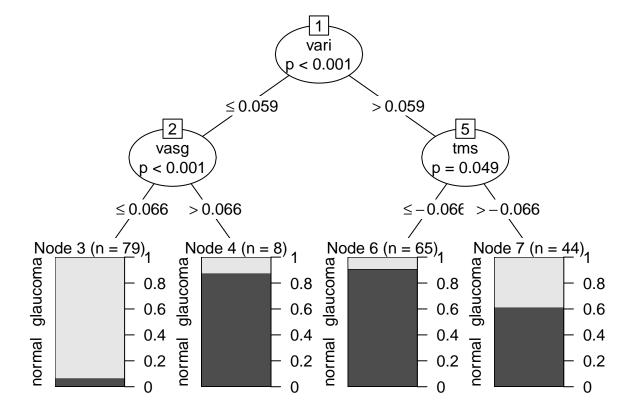
Exercise 1: Glaucoma data revisited (1)

- a) Use the stabletree() function from the stablelearner package to assess stability of the tree you fitted yesterday. Do not forget to set the random seed, as the stabletree() function uses bootstrap samples to assess stability.
- b) Is the first variable in the tree grown in Exercise 4 often selected? And how about the variables that appear further down the tree?
- c) Check whether there is multicollinearity in the data: Could that explain that the variables appearing in the tree are not selected in each of the bootstrap samples?

library(partykit)

```
## Loading required package: grid
```

```
data("GlaucomaM", package = "TH.data")
ct <- ctree(Class ~ ., data = GlaucomaM)
plot(ct)</pre>
```

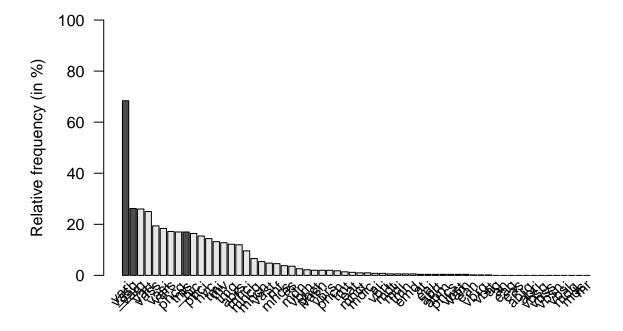


```
library("stablelearner")
set.seed(42)
```

```
ct_stab <- stabletree(ct)
summary(ct_stab)
##
## ctree(formula = Class ~ ., data = GlaucomaM)
##
## Sampler:
## B = 500
## Method = Bootstrap sampling
## Variable selection overview:
##
##
         freq * mean *
## vari 0.684 1 0.722 1
## vasg 0.262 1 0.262 1
## varg 0.260 0 0.260 0
## vart 0.250 0 0.250 0
## vass 0.194 0 0.196 0
## vasi 0.184 0 0.190 0
## vars 0.172 0 0.174 0
## phcg 0.170 0 0.172 0
## tms 0.170 1 0.170 1
## hic 0.164 0 0.166 0
## phci 0.154 0 0.156 0
## hvc 0.144 0 0.144 0
## tmi 0.132 0 0.132 0
       0.128 0 0.132 0
## mv
## tmg 0.122 0 0.130 0
## abrs 0.120 0 0.120 0
## mhci 0.096 0 0.096 0
## mhcg 0.066 0 0.066 0
## mhcn 0.054 0 0.054 0
## vast 0.048 0 0.050 0
## rnf 0.046 0 0.046 0
## mhcs 0.038 0 0.038 0
## as
       0.036 0 0.036 0
## mdn 0.026 0 0.026 0
## vbrn 0.022 0 0.022 0
## phct 0.020 0 0.020 0
## vasn 0.020 0 0.020 0
## vbrs 0.020 0 0.020 0
## phcn 0.018 0 0.018 0
## tmt 0.014 0 0.014 0
## eat 0.012 0 0.012 0
## mhct 0.010 0 0.010 0
## mdic 0.010 0 0.010 0
## ai
       0.008 0 0.008 0
## vbri 0.008 0 0.008 0
## mdt 0.006 0 0.006 0
## mdi 0.006 0 0.006 0
## tmn 0.006 0 0.006 0
## emd 0.006 0 0.006 0
## at
       0.004 0 0.004 0
```

```
## eai 0.004 0 0.004 0
## abrt 0.004 0 0.004 0
## abrn 0.004 0 0.004 0
## phcs 0.004 0 0.004 0
## vbst 0.004 0 0.004 0
## varn 0.004 0 0.004 0
## ean 0.002 0 0.002 0
## vbrg 0.002 0 0.002 0
## vbrt 0.002 0 0.002 0
        0.000 0 0.000 0
## an
        0.000 0 0.000 0
       0.000 0 0.000 0
## eag
## eas 0.000 0 0.000 0
## abrg 0.000 0 0.000 0
## abri 0.000 0 0.000 0
## vbsg 0.000 0 0.000 0
## vbss 0.000 0 0.000 0
## vbsn 0.000 0 0.000 0
## vbsi 0.000 0 0.000 0
## mdg 0.000 0 0.000 0
## mds 0.000 0 0.000 0
        0.000 0 0.000 0
## (* = original tree)
barplot(ct_stab)
```

Variable selection frequencies



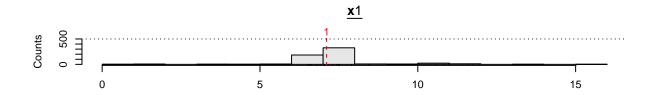
```
cor(GlaucomaM[,c("vari", "vasg", "varg", "vart", "vass", "vasi", "vars", "phcg")])
##
              vari
                                                                      vasi
                         vasg
                                    varg
                                               vart
                                                           vass
## vari
         1.0000000
                   0.4711082
                               0.9276727
                                          0.6121546
                                                     0.3281612
                                                                0.5348386
## vasg
         0.4711082
                    1.0000000
                               0.6181722
                                          0.5601590
                                                     0.9196471
                                                                0.8230907
## varg
         0.9276727
                    0.6181722
                               1.0000000
                                          0.7021653
                                                     0.4978143
                                                                0.5806854
        0.6121546
                    0.5601590
                               0.7021653
                                          1.0000000
                                                     0.5509784
                                                                0.5425974
## vart
## vass
        0.3281612
                   0.9196471
                               0.4978143
                                          0.5509784
                                                     1.0000000
                                                                0.6434028
        0.5348386
                   0.8230907
                               0.5806854
## vasi
                                          0.5425974
                                                     0.6434028
                                                                1.0000000
        0.8013808 0.6025811
                               0.9311459
                                          0.7353698
                                                     0.5734093
                                                                0.5288761
## phcg -0.5631943 -0.2728333 -0.5466596 -0.3827756 -0.1519453 -0.3363697
##
              vars
                         phcg
## vari 0.8013808 -0.5631943
        0.6025811 -0.2728333
## vasg
## varg 0.9311459 -0.5466596
## vart
        0.7353698 -0.3827756
        0.5734093 -0.1519453
## vass
## vasi
        0.5288761 -0.3363697
## vars 1.0000000 -0.4746608
## phcg -0.4746608 1.0000000
```

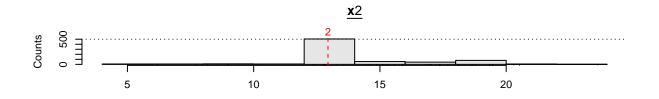
Exercise 2: Bootstrapping vs. subsampling

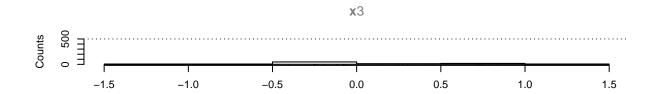
Below, the code for generating one of the datasets I used in the presentation sheets is provided. Using this data and the stabletree() function from the stablelearner package, evaluate the difference between subsampling and bootstrap sampling in terms of the selection with which noise variables are selected:

```
set.seed(12)
x1 <- rnorm(250, mean = 7, sd = 4)
x2 <- rnorm(250, mean = 14, sd = 4)
y_cont <- 8 + 5*(x1 > 7 & x2 > 13) + rnorm(250, 0, 1.5)
x3 <- rnorm(250)
ex_data <- data.frame(x1, x2, x3, y_cont)</pre>
```

- a) Fit a ctree which predicts y_cont from x1, x2 and x3.
- b) Use the stabletree() function to assess the tree's stability using bootstrap sampling (the default).
- c) Assess the tree's stability using subsamples instead of bootstrap samples. (Hint: Use ?stabletree and ?bootstrap to see how you can change the sampler used).
- d) Compare the selection frequencies you obtained with both sampling methods.

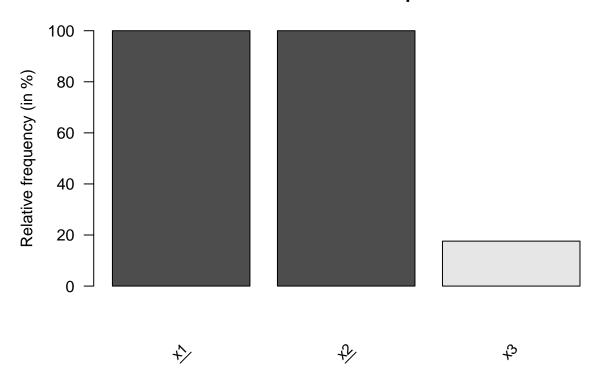


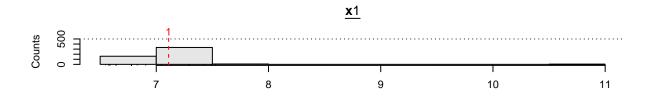


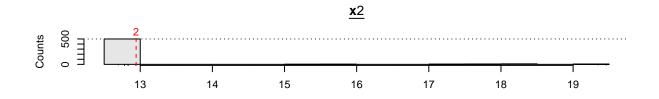


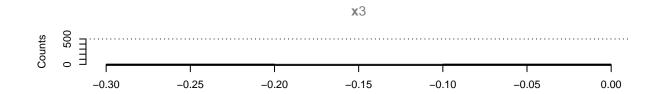
barplot(ct_stab)

Variable selection frequencies



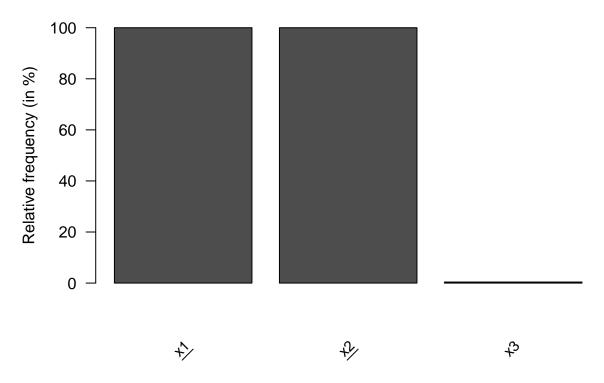






barplot(ct_stab)

Variable selection frequencies



dev.off() # note: normally not needed

null device
1