Fitting a prediction rule ensemble using R package pre

Load package and data

First, we have to get the package from GitHub and install. Also, we have to get the example dataset, which is from a paper by Carillo et al. (2001) on predicting depression based on personality scales:

```
library(devtools)
install_github("marjoleinF/pre")
```

```
library(pre)
library(foreign)
car_data <- read.spss("https://github.com/marjoleinF/misc/raw/master/data Carillo et al.sav", to.data.frame = TRUE
)</pre>
```

```
## Warning in read.spss("https://github.com/marjoleinF/misc/raw/master/data
## Carillo et al.sav", : C:\Users\fokkemam\AppData\Local\Temp\RtmpQPP7Xs
## \file257460ff4264: Unrecognized record type 7, subtype 18 encountered in
## system file
```

```
names(car_data)
```

```
"n4"
## [1] "n1"
## [8] "e1"
              "n2" "n3"
"e2" "e3"
                                          "n5"
                                                   "e6"
                                                            "ntot"
                                 "e4"
                                          "e5"
                                                            "etot"
## [15] "open1" "open2" "open3"
                                 "open4"
                                                   "opentot" "altot"
                                          "open6"
## [22] "contot" "bdi"
                                 "edad"
                        "sexo"
                                          "open5"
```

Fit the ensemble

To fit the prediction rule ensemble, we have to regress depression (bdi) on all other variables.

```
set.seed(42)
car_pre <- pre(formula = bdi ~ ., data = car_data)</pre>
```

Note we have to set the seed to be able to reproduce our results later. Above, defaut settings are used. Alternatively, we can generate the initial ensemble like a bagged ensemble or random forest:

```
pre_bag <- pre(formula = bdi ~ ., data = car_data, maxdepth = Inf, learnrate = 0, mtry = Inf, sampfrac = 1)
pre_rf <- pre(formula = bdi ~ ., data = car_data, maxdepth = Inf, learnrate = 0, mtry = ncol(car_data)/3, sampfrac = 1)</pre>
```

Inspect the ensemble

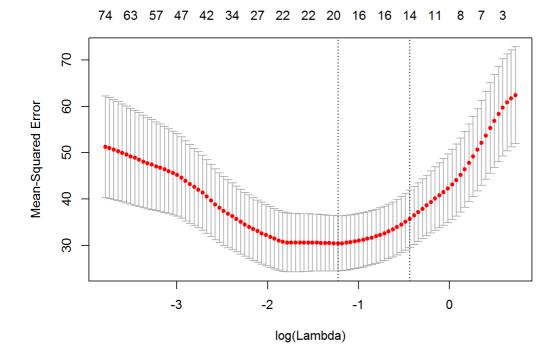
We can check out the resulting prediction rule ensemble using the function:

```
print (car_pre)
```

```
##
## Final ensemble with cv error within 1se of minimum:
    lambda = 0.64585
    number of terms = 14
    mean cv error (se) = 35.71728 (6.164456)
##
           rule coefficient
                                           description
##
                  8.20331296
    (Intercept)
##
        rule112
                  2.83654289
                                n4 > 15 & open4 <= 13
##
        rule136 -1.37288781
                                 n2 <= 16 & open4 > 10
##
         rule24
                 -1.19069321 ntot <= 109 & etot > 101
##
        rule123 -1.14486626
                               ntot <= 109 & e6 > 15
##
         rule54
                  1.03135600
                                               n6 > 19
##
         rule22 -1.00553016
                                              n3 <= 22
##
          rule2
                 0.87187489
                                               n3 > 17
##
        rule150 -0.40073882
                                n2 <= 16 & open5 > 11
                 0.37436067
                              open4 <= 13 & ntot > 82
##
         rule88
        rule121 -0.30189699
                                   n2 <= 16 & e6 > 14
##
         rule53 -0.27360995
                                 n6 <= 19 & open4 > 12
##
         rule41 -0.21459613
                                ntot <= 109 & n4 <= 14
##
                 0.17546398
                                     2 <= n3 <= 30.225
##
            n3
                 0.03072938
                                               n1 > 20
##
         rule59
```

We may be willing to trade some predictive accuracy in order to have a smaller ensemble, of only four rules, for example:

```
plot(car_pre$glmnet.fit)
```



Note that predictive accuracy will be much compromised in this case. To illustrate, we will use a very small ensemble here. Then we should get the value of the penalty parameter that gives us the desired number of terms:

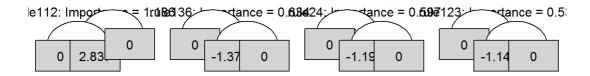
```
head(data.frame(number_of_nonzero_terms = car_pre$glmnet.fit$nzero, lambda = car_pre$glmnet.fit$lambda))
##
      number_of_nonzero_terms
                                lambda
## s0
                            0 2.066247
## s1
                             1 1.972333
## s2
                             3 1.882687
## s3
                             3 1.797116
## s4
                             4 1.715434
                             5 1.637465
## s5
```

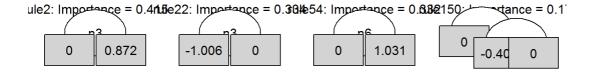
```
print(car_pre, penalty.par.val = 1.72)
```

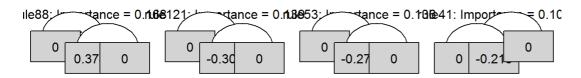
```
## Final ensemble with lambda = 1.715434
##
    number of terms = 4
    mean cv error (se) = 58.34011 (10.3031)
           rule coefficient
                                           description
##
    (Intercept)
                 8.52339118
                 -0.74435122 ntot <= 109 & etot > 101
##
         rule24
                 0.69482844
##
          rule2
                                              n3 > 17
                 -0.57775956
                                ntot <= 109 & e6 > 15
##
        rule123
##
        rule112
                 0.01523659
                                n4 > 15 & open4 <= 13
```

The smaller ensemble will give lower predictive accuracy on new observations, as the plot of the cross-validated mean squared error above indicates. Let's continue with the ensemble selected by default, and plot it:

```
plot(car_pre)
```







Linear effect of n3 rule59: Importance = 0.015
Importance = 0.07

We can generate predictions for new observations (though note that these observations are in fact not new, but were already used for training the ensemble):

```
head(coef(car_pre))
```

```
##
           rule coefficient
                                       description
      (Intercept) 8.203313
## 1
                                              <NA>
        rule112 2.836543 n4 > 15 & open4 <= 13
## 34
         rule136 -1.372888 n2 <= 16 & open4 > 10
## 54
         rule24 -1.190693 ntot <= 109 & etot > 101
## 84
## 42
         rule123 -1.144866 ntot <= 109 & e6 > 15
                                           n6 > 19
## 107
         rule54 1.031356
```

```
predict(car_pre, newdata = car_data[1:10,])
```

```
## 1 2 3 4 5 6 7

## 5.105917 14.348409 4.579525 4.267730 4.930453 8.416082 18.787560

## 8 9 10

## 7.519413 2.298494 4.298459
```

To obtain an estimate of future prediction error through k-fold cross validation:

```
set.seed(42)
cv_car1 <- cvpre(car_pre)
cv_car2 <- cvpre(car_pre, penalty.par.val = 1.72)
cv_car1$accuracy</pre>
```

```
## $MSE
## [1] 43.77261
##
## $MAE
## [1] 5.182656
```

```
cv_car2$accuracy
```

```
## $MSE
## [1] 56.26237
##
## $MAE
## [1] 5.753458
```

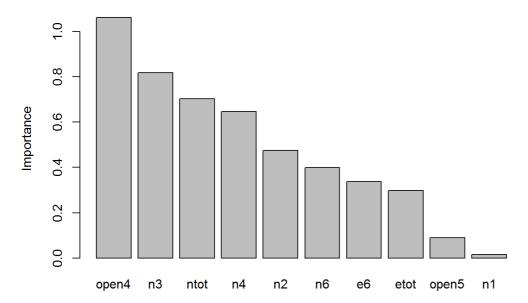
```
var(car_data$bdi)
```

```
## [1] 61.46774
```

We can get an estimate of the importance of variables and base learners using the function.

```
importance(car_pre, round = 4,)
```

Variable importances



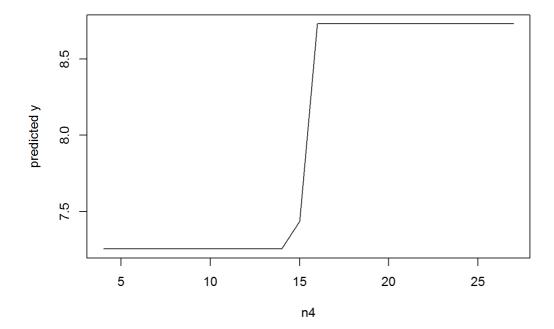
```
## $varimps
##
     varname
                imp
## 18
       open4 1.0622
##
  3
          n3 0.8189
##
  7
        ntot 0.7029
##
  4
          n4 0.6469
##
  2
          n2 0.4759
## 6
          n6 0.3997
          e6 0.3362
## 14
        etot 0.2986
## 25
       open5 0.0891
##
  1
          n1 0.0147
##
## $baseimps
\#\,\#
         rule
                            description
                                          imp coefficient
## 35 rule112
                 n4 > 15 \& open4 \le 13 1.1864
                                                  2.8365 0.4183
                 n2 <= 16 & open4 > 10 0.6341
                                                   -1.3729 0.4619
## 55 rule136
## 85
       rule24 ntot <= 109 & etot > 101 0.5972
                                                   -1.1907 0.5015
                 ntot <= 109 & e6 > 15 0.5330
                                                   -1.1449 0.4656
## 43
      rule123
                               n3 > 17 0.4147
## 81
                                                   0.8719 0.4756
        rule2
                               n3 <= 22 0.3340
                                                   -1.0055 0.3322
## 83
       rule22
## 108 rule54
                               n6 > 19 0.3318
                                                   1.0314 0.3218
                n2 <= 16 & open5 > 11 0.1783
                                                   -0.4007 0.4448
## 65 rule150
## 131 rule88 open4 <= 13 & ntot > 82 0.1682
                                                   0.3744 0.4494
                   n2 <= 16 & e6 > 14 0.1394
                                                   -0.3019 0.4619
## 41 rule121
                 n6 <= 19 & open4 > 12 0.1356
                                                   -0.2736 0.4957
## 107
       rule53
                ntot <= 109 & n4 <= 14 0.1073
## 97
                                                   -0.2146 0.5002
        rule41
## 13
                      2 <= n3 <= 30.225 0.0702
                                                   0.1755 0.4000
           n3
## 111 rule59
                                n1 > 20 0.0147
                                                   0.0307 0.4785
```

Note that predictive accuracy would have been much better if we would have gone with the default .

We can assess the effect of a single variable on the predictions of the ensemble using the function:

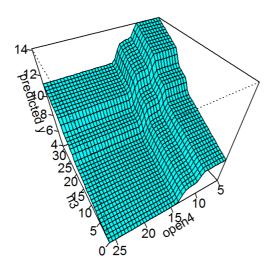
```
singleplot(car_pre, "n4")
```

partial dependence on n4



We can assess the effect of pairs of variables on the predictions of the ensemble using the function:

```
pairplot(car_pre, c("n3", "open4"), nticks = 6, theta = 240)
```



 $\ensuremath{\mbox{\#\#}}$ NOTE: function pairplot uses package 'akima', which has an ACM license.

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