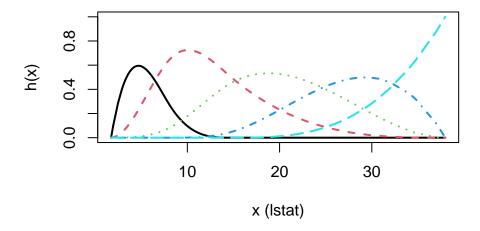
## Answers to exercises Session 5

# Exercise 1: Cubic and natural splines



```
attr(bs_x, "degree")
```

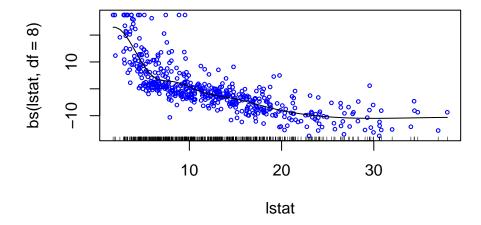
#### ## [1] 3

With df = 5, we obtain a design matrix of 5 columns. With a cubic spline, we use up 3 df for the first three expansions. Thus, with 5 df, we have 2 df 'left' to spend on the knots. Each knot introduces one additional basis function. Thus, with 5 df for a cubic spline, we can use 2 knots. Note that the knots are placed based on the univariate distribution of the predicton.

```
d)
library("gam")
mod_df5 <- gam(medv ~ bs(lstat, df = 5), data = Boston)</pre>
summary(mod_df5)
##
## Call: gam(formula = medv ~ bs(lstat, df = 5), data = Boston)
## Deviance Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                            Max
## -15.1774 -3.1790 -0.7981
                                2.0964
                                        26.6755
##
## (Dispersion Parameter for gaussian family taken to be 27.109)
##
      Null Deviance: 42716.3 on 505 degrees of freedom
##
## Residual Deviance: 13554.52 on 500 degrees of freedom
## AIC: 3113.663
## Number of Local Scoring Iterations: 2
##
## Anova for Parametric Effects
                      Df Sum Sq Mean Sq F value
                                                   Pr(>F)
                       5 29162 5832.4 215.14 < 2.2e-16 ***
## bs(lstat, df = 5)
                     500
## Residuals
                         13554
                                   27.1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(mod_df5, residuals = TRUE, col = "blue", cex = .5)
```

```
10 20 30 lstat
```

```
mod_df8 <- gam(medv ~ bs(lstat, df = 8), data = Boston)</pre>
summary(mod_df8)
##
## Call: gam(formula = medv ~ bs(lstat, df = 8), data = Boston)
## Deviance Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -14.9627 -3.1253 -0.6612
                                2.0831 26.0972
## (Dispersion Parameter for gaussian family taken to be 26.7118)
       Null Deviance: 42716.3 on 505 degrees of freedom
##
## Residual Deviance: 13275.77 on 497 degrees of freedom
## AIC: 3109.148
##
## Number of Local Scoring Iterations: 2
##
## Anova for Parametric Effects
##
                      Df Sum Sq Mean Sq F value
                                                   Pr(>F)
## bs(lstat, df = 8)
                       8 29441 3680.1 137.77 < 2.2e-16 ***
## Residuals
                          13276
                                   26.7
                     497
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
plot(mod_df8, residuals = TRUE, col = "blue", cex = .5)
```



```
BIC(mod_df5)
```

## [1] 3143.249

BIC(mod\_df8)

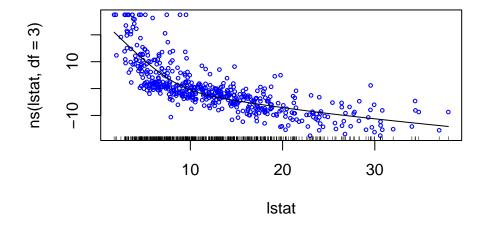
#### ## [1] 3151.414

The 5 df cubic spline fits best according to BIC, the plots suggest similar: 8 df yields a slightly too wiggly function. Note that models with different (number of location of) knots are not nested, so we cannot use stattistical testing to compare the model fit.

```
e)
mod_ns3 <- gam(medv ~ ns(lstat, df = 3), data = Boston)
summary(mod_ns3)
```

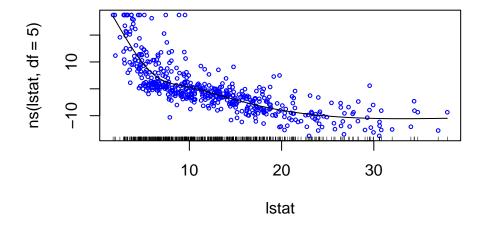
```
##
## Call: gam(formula = medv ~ ns(lstat, df = 3), data = Boston)
## Deviance Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
  -13.7595
            -3.3628
                     -0.6468
                                2.3062
                                        27.2857
##
##
##
   (Dispersion Parameter for gaussian family taken to be 28.4261)
##
      Null Deviance: 42716.3 on 505 degrees of freedom
##
## Residual Deviance: 14269.9 on 502 degrees of freedom
  AIC: 3135.688
##
##
## Number of Local Scoring Iterations: 2
##
## Anova for Parametric Effects
##
                      Df Sum Sq Mean Sq F value
                                                   Pr(>F)
## ns(lstat, df = 3)
                       3
                         28446
                                 9482.1 333.57 < 2.2e-16 ***
## Residuals
                     502
                         14270
                                   28.4
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
plot(mod_ns3, residuals = TRUE, col = "blue", cex = .5)
```



plot(mod\_ns5, residuals = TRUE, col = "blue", cex = .5)

```
mod_ns5 <- gam(medv ~ ns(lstat, df = 5), data = Boston)</pre>
summary(mod_ns5)
##
## Call: gam(formula = medv ~ ns(lstat, df = 5), data = Boston)
## Deviance Residuals:
        Min
                  1Q
                       Median
## -13.9811 -3.0266 -0.7252
                                 2.1416 26.5111
## (Dispersion Parameter for gaussian family taken to be 26.9021)
##
##
       Null Deviance: 42716.3 on 505 degrees of freedom
## Residual Deviance: 13451.03 on 500 degrees of freedom
## AIC: 3109.785
## Number of Local Scoring Iterations: 2
##
## Anova for Parametric Effects
##
                      {\tt Df \; Sum \; Sq \; Mean \; Sq \; F \; value}
                                                    Pr(>F)
## ns(1stat, df = 5)
                                 5853.1 217.57 < 2.2e-16 ***
                       5 29265
## Residuals
                     500 13451
                                    26.9
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```



BIC(mod\_ns3)

## [1] 3156.82

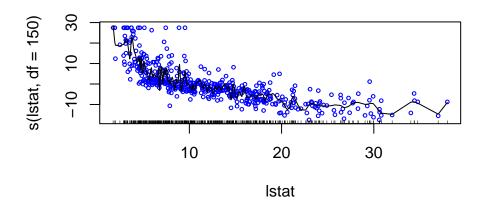
BIC(mod\_ns5)

## [1] 3139.37

The lowest BIC value was obtained for the natural spline with  $5~\rm{df}$ . Visually, both the  $3~\rm{and}~5~\rm{df}$  natural splines seem to provide a good fit to the data.

### Exercise 2: Smoothing spline

```
mod_sc <- gam(medv ~ s(lstat, df = 150), data = Boston) # complex fit</pre>
summary(mod_sc)
##
## Call: gam(formula = medv ~ s(lstat, df = 150), data = Boston)
## Deviance Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
  -14.0712 -2.7340
                     -0.4702
                                2.0649
                                        21.9654
##
  (Dispersion Parameter for gaussian family taken to be 27.6915)
##
##
##
      Null Deviance: 42716.3 on 505 degrees of freedom
## Residual Deviance: 10772.01 on 389 degrees of freedom
## AIC: 3219.4
##
## Number of Local Scoring Iterations: NA
##
## Anova for Parametric Effects
##
                       Df Sum Sq Mean Sq F value
## s(lstat, df = 150)
                          23244 23243.9 839.39 < 2.2e-16 ***
                        1
## Residuals
                           10772
                                    27.7
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Anova for Nonparametric Effects
##
                      Npar Df Npar F
                                         Pr(F)
## (Intercept)
## s(lstat, df = 150)
                          115 2.7321 2.103e-13 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(mod_sc, residuals = TRUE, cex = .5, col = "blue")
```

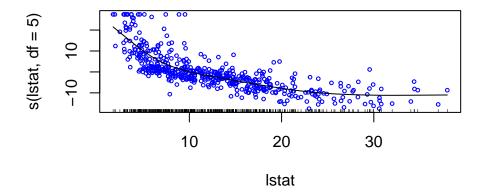


The results present both a parametric and non-parametric effect of lstat. The parametric effect represent the linear slope, thus using only 1 df. The non-parametric effects represent the non-linear effects. The

non-linear part of the smoothing spline for lstat took up 115 degrees of freedom. Note that this is less than the requested degrees of freedom, because by default the knots are placed at a subset of the observations, for computational considerations. In addition, > 115 knots would be rarely needed to approximate a curve.

```
mod_ss <- gam(medv ~ s(lstat, df = 5), data = Boston) # more simple fit
summary(mod_ss)</pre>
```

```
##
## Call: gam(formula = medv ~ s(lstat, df = 5), data = Boston)
## Deviance Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                       26.8386
##
  -13.6332
            -3.2159
                     -0.6577
                                2.2051
##
  (Dispersion Parameter for gaussian family taken to be 27.6492)
##
##
       Null Deviance: 42716.3 on 505 degrees of freedom
##
## Residual Deviance: 13824.6 on 499.9999 degrees of freedom
##
  AIC: 3123.646
##
## Number of Local Scoring Iterations: NA
##
## Anova for Parametric Effects
##
                     Df Sum Sq Mean Sq F value
                                                  Pr(>F)
                      1 23244 23243.9 840.67 < 2.2e-16 ***
## s(lstat, df = 5)
## Residuals
                    500
                        13825
                                  27.6
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Anova for Nonparametric Effects
                    Npar Df Npar F
                                       Pr(F)
##
## (Intercept)
## s(1stat, df = 5)
                          4 51.065 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(mod_ss, residuals = TRUE, col = "blue", cex = .5)
```



With 5 df, the flexibility is much lower, and we obtain a much smoother fit.

BIC(mod\_ss)

## [1] 3136.326

BIC(mod\_sc)

## [1] 3232.079

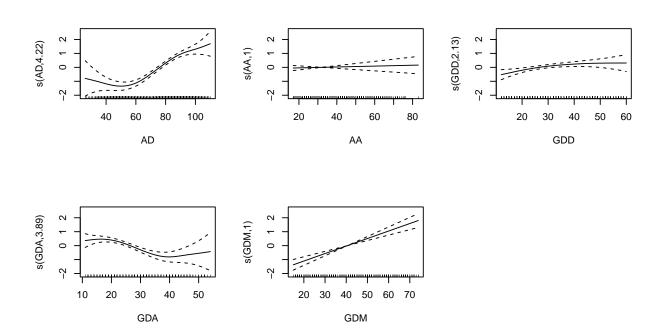
BIC(mod\_ns5)

## [1] 3139.37

According to the BIC, the more heavily penalized smoothing spline (i.e., with df = 5) has better fit than the less reularized smoothing spline. This is in accordance with what we can conclude from the visual inspection of the fitted smoothing splines. The smoothing spline with 5 df also outperforms the natural spline with 5 df from the previous exercise. Thus, the non-parametric smoothing spline approach appears to improve on the parametric natural and cubic spline approaches.

### Exercise 3: Multiple predictors, binary outcome

```
detach("package:gam", unload=TRUE)
library("mgcv")
MASQ <- read.table("MASQ.txt")</pre>
set.seed(1)
train <- sample(1:nrow(MASQ), size = nrow(MASQ)*.8)</pre>
summary(MASQ)
##
      D DEPDYS
                          AD
                                                         GDD
                                           AA
                           : 26.00
##
   Min. :0.0000
                                           :17.00
                                                    Min.
                                                           :12.00
                    \mathtt{Min}.
                                   {	t Min.}
   1st Qu.:0.0000
                    1st Qu.: 64.00
##
                                   1st Qu.:22.00
                                                    1st Qu.:20.00
                    Median: 77.00 Median: 28.00
  Median :0.0000
                                                    Median :29.00
                    Mean : 75.05
  Mean :0.4643
                                   Mean :32.01
                                                    Mean
                                                           :30.64
   3rd Qu.:1.0000
                    3rd Qu.: 88.00 3rd Qu.:39.00
                                                    3rd Qu.:40.00
##
##
  Max.
          :1.0000
                    Max.
                         :110.00 Max. :83.00
                                                    Max.
                                                           :60.00
##
        GDA
                       GDM
                                   leeftijd
                                                geslacht
## Min.
          :11.0
                 Min. :15.0 Min. :17.0
                                               Length:3597
##
  1st Qu.:19.0
                 1st Qu.:31.0
                                1st Qu.:28.0
                                               Class : character
## Median :24.0
                  Median:40.0
                                Median:38.0
                                               Mode :character
## Mean :25.4
                  Mean :40.6
                                Mean :38.8
## 3rd Qu.:31.0
                  3rd Qu.:50.0
                                3rd Qu.:48.0
##
   Max.
         :54.0
                  Max. :75.0
                               Max.
                                      :91.0
       D_TOT
##
  Min.
          :0.000
  1st Qu.:1.000
##
## Median :2.000
## Mean :2.127
## 3rd Qu.:4.000
## Max.
          :7.000
GAM \leftarrow gam(D DEPDYS \sim s(AD) + s(AA) + s(GDD) + s(GDA) + s(GDM),
          data = MASQ[train, ], method = "REML", family = "binomial")
summary(GAM)
##
## Family: binomial
## Link function: logit
## Formula:
## D_DEPDYS \sim s(AD) + s(AA) + s(GDD) + s(GDA) + s(GDM)
## Parametric coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -0.25204
                          0.04854 -5.192 2.08e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
           edf Ref.df Chi.sq p-value
## s(AD) 4.221 5.213 156.700 < 2e-16 ***
## s(AA) 1.001 1.002
                        0.272
                                0.6026
## s(GDD) 2.132 2.725
                       9.315
                                0.0216 *
## s(GDA) 3.891 4.847 34.126 3.71e-06 ***
## s(GDM) 1.001 1.001 51.882 < 2e-16 ***
```



We compute the mean squared error and misclassification rate using predicted probabilities, for both training and test observations:

```
## Training data
GAM_preds_train <- predict(GAM, newdata = MASQ[train, ], type = "response")
mean((MASQ[train, "D_DEPDYS"] - GAM_preds_train)^2) ## Brier score

## [1] 0.1669075
tab_train <- prop.table(table(MASQ[train, "D_DEPDYS"], GAM_preds_train > .5)) ## confusion matrix
1 - sum(diag(tab_train)) ## MCR

## [1] 0.2440042
## Test data
GAM_preds_test <- predict(GAM, newdata = MASQ[-train, ], type = "response")
mean((MASQ[-train, "D_DEPDYS"] - GAM_preds_test)^2) ## Brier score

## [1] 0.1690516
tab_test <- prop.table(table(MASQ[-train, "D_DEPDYS"], GAM_preds_test > .5)) ## confusion matrix
```

#### ## [1] 0.244444

1 - sum(diag(tab\_test)) ## MCR

The Brier score and confusion matrices are quite similar between training and test data, indicating little

overfitting.

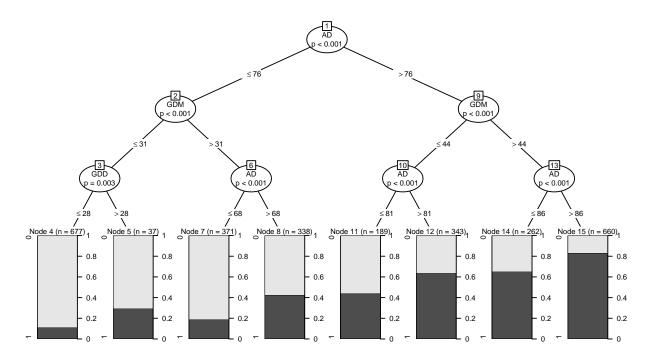
### Exercise 4: Fit an SVM

```
library("e1071")
## Warning: package 'e1071' was built under R version 4.1.1
cost <- c(.001, .01, .1, 1, 5, 10, 100)
set.seed(42)
names (MASQ)
## [1] "D DEPDYS" "AD"
                               "AA"
                                           "GDD"
                                                      "GDA"
                                                                  "GDM"
                                                                              "leeftijd"
## [8] "geslacht" "D_TOT"
MASQ <- MASQ[ , -9]
names (MASQ)
## [1] "D_DEPDYS" "AD"
                               "AA"
                                           "GDD"
                                                      "GDA"
                                                                  "GDM"
                                                                              "leeftijd"
## [8] "geslacht"
MASQ$D_DEPDYS <- factor(MASQ$D_DEPDYS)</pre>
tune.out <- tune(svm, D_DEPDYS ~ ., data = MASQ[train, ], kernel = "linear",</pre>
                  ranges = list(cost = cost))
tune.out$best.parameters
     cost
## 3 0.1
svmfit <- svm(D_DEPDYS ~ ., data = MASQ[train,], kernel = "linear",</pre>
            cost = 0.1)
tab_train <- table(MASQ[train, "D_DEPDYS"],</pre>
                    predict(svmfit, newdata = MASQ[train, ]))
1 - sum(diag(prop.table(tab_train))) ## misclassification rate
## [1] 0.2415711
tab_test <- table(MASQ[-train, "D_DEPDYS"],</pre>
                    predict(svmfit, newdata = MASQ[-train, ]))
1 - sum(diag(prop.table(tab_test))) ## misclassification rate
## [1] 0.2486111
Radial basis kernel
Perhaps we can further improve predictions by using a non-linear kernel. We try the radial basis kernel:
gamma \leftarrow c(0.5, 1, 2, 3, 4)
tune.out <- tune(svm, D_DEPDYS ~ ., data = MASQ[train, ],</pre>
                  kernel = "radial", ranges = list(
                   cost = cost, gamma = gamma))
tune.out$best.parameters
     cost gamma
## 4
        1 0.5
rbkfit <- svm(D_DEPDYS ~ ., data = MASQ[train, ],</pre>
              kernel = "radial", gamma = 0.5,
```

The radial basis kernel did not improve performance on test data.

### Exercise 5: Fit a ctree to MASQ data

```
library("partykit")
MASQ$geslacht <- factor(MASQ$geslacht)
ct <- ctree(D_DEPDYS ~ . , data = MASQ[train, ])
plot(ct, gp = gpar(cex = .5))</pre>
```



The conditional inference tree indicates a positive effect of the AD, GDM and GDD subscales on the probability of having a depressive / dysthymic disorder.

```
y_train <- as.numeric(MASQ[train, "D_DEPDYS"]) - 1
## Training data
ct_preds_train <- predict(ct, newdata = MASQ[train, ], type = "prob")[ , 2]
mean((y_train - ct_preds_train)^2) ## Brier score

## [1] 0.1705674
tab_train <- prop.table(table(MASQ[train, "D_DEPDYS"], ct_preds_train > .5)) ## confusion matrix
1 - sum(diag(tab_train)) ## MCR

## [1] 0.2457421
## Test data
y_test <- as.numeric(MASQ[-train, "D_DEPDYS"]) - 1
ct_preds_test <- predict(ct, newdata = MASQ[-train, ], type = "prob")[ , 2]
mean((y_test - ct_preds_test)^2) ## Brier score

## [1] 0.1738697
tab_test <- prop.table(table(MASQ[-train, "D_DEPDYS"], ct_preds_test > .5)) ## confusion matrix
1 - sum(diag(tab_test)) ## MCR
```

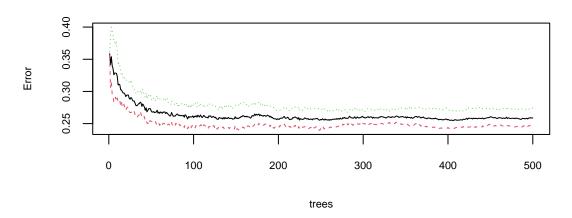
## [1] 0.2388889

The conditional inference tree yields slightly lower test error than the pruned CART tree. Thus, the conditional inference tree provided best predictive accuracy of the single trees.

## Exercise 6: Fit a random forest to the MASQ data

We fit the ensembles:

#### **Bagging**

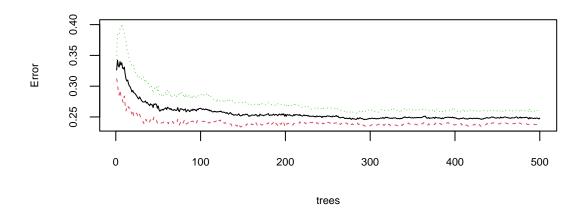


For these data, the out-of-bag (OOB) error decreases fast with the first 100 trees. After 200-300 trees, the OOB error stabilizes.

Note that for binary classification, three curves are provided: The black curve shows the misclassification error, the green and red curves show the classification error in each of the classes (comparable to sensitivity and specificity).

```
plot(rf.ens, cex.lab = .7, cex.axis = .7, cex.main = .7, main = "Random forest")
```

#### Random forest



The OOB error plotted against the number of trees shows a very similar pattern as with the bagged ensemble. Compute train MCR:

```
tab <- prop.table(table(MASQ[train, "D_DEPDYS"],</pre>
                        predict(bag.ens, newdata = MASQ[train,])))
1 - sum(diag(tab)) ## misclassification rate for bagging
## [1] 0
tab <- prop.table(table(MASQ[train, "D_DEPDYS"],</pre>
                        predict(rf.ens, newdata = MASQ[train,])))
1 - sum(diag(tab)) ## misclassification rate for RF
## [1] 0
Compute test MCR:
tab <- prop.table(table(MASQ[-train, "D_DEPDYS"],</pre>
predict(bag.ens, newdata = MASQ[-train,])))
1 - sum(diag(tab)) ## misclassification rate for bagging
## [1] 0.2388889
tab <- prop.table(table(MASQ[-train, "D_DEPDYS"],</pre>
predict(rf.ens, newdata = MASQ[-train,])))
1 - sum(diag(tab)) ## misclassification rate for RF
## [1] 0.2388889
We compute train SEL:
mean(((as.numeric(MASQ[train, "D_DEPDYS"]) - 1) -
        predict(bag.ens, newdata = MASQ[train,], type = "prob")[ , 2])^2)
## [1] 0.02466598
mean(((as.numeric(MASQ[train, "D_DEPDYS"]) - 1) -
        predict(rf.ens, newdata = MASQ[train,], type = "prob")[ , 2])^2)
```

## [1] 0.02431729

We compute test SEL:

## [1] 0.1723298

Note that the predict method returns predicted probabilities for both classes, for objects of class randomForest. Therefore, we selected the second column of the returned probabilities ([ , 2]).

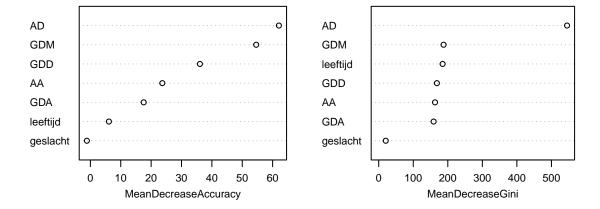
Test MCRs are identical for the bagged ensemble and random forest. Test SEL is lower for the random forest.

#### Interpretation

We inspect variable importances:

```
importance(bag.ens)
##
                                1 MeanDecreaseAccuracy MeanDecreaseGini
## AD
            26.008074 46.6261372
                                             62.061330
                                                               545.20309
            11.210061 19.5952066
                                             23.683674
                                                               163.04057
##
  GDD
            24.875687 18.2097877
                                             36.050773
##
                                                               168.41636
## GDA
            18.096720 3.1288186
                                             17.552676
                                                               158.92755
## GDM
            24.393229 39.5161589
                                             54.590675
                                                               187.79771
## leeftijd 2.752565 5.6442541
                                              6.098998
                                                               185.04514
## geslacht -1.634730 -0.1247933
                                                                20.31331
                                             -1.150591
varImpPlot(bag.ens, cex = .7, cex.main = .7)
```

## bag.ens

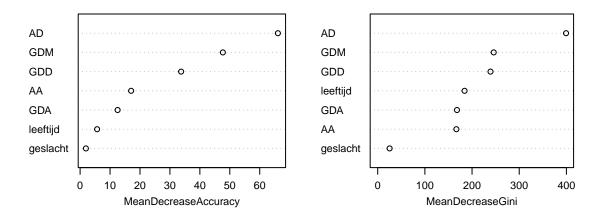


According to the reduction in MSE for the out-of-bag observations (left panel) if the values of each predictor variable are permuted, the AD (anhedonic depression), GDM (general distress mixed), and GDD (general distress depression) are the most important predictors of a depressive disorder diagnosis.

According to the improvement in node purity (i.e., training error; right panel), AD, leeftijd (age) and GDM are the most important predictors of a depressive disorder diagnosis.

```
importance(rf.ens)
##
                               1 MeanDecreaseAccuracy MeanDecreaseGini
                                            66.064052
## AD
            33.630440 48.266024
                                                              399.27306
## AA
             6.599139 15.579649
                                            17.047234
                                                              166.79307
## GDD
            22.394085 16.774428
                                            33.745150
                                                              239.10990
## GDA
            13.584839
                      1.184124
                                            12.532481
                                                              168.00515
## GDM
            21.001515 36.662315
                                                              245.91414
                                            47.677333
## leeftijd 1.773007
                       5.834744
                                             5.682049
                                                              184.13887
## geslacht 1.344184
                       1.423987
                                             1.931168
                                                               25.26403
varImpPlot(rf.ens, cex = .7, cex.main = .7)
```

### rf.ens

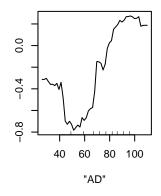


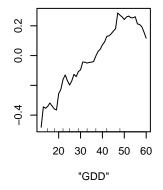
The AD, GDM and GDD scales appear most important in the random forest.

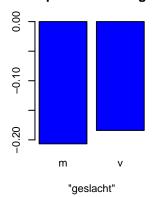
We request partial dependence plots for the bagged ensemble:

```
par(mfrow = c(1, 3))
partialPlot(bag.ens, x.var = "AD", pred.data = MASQ[train,], which.class = "1")
partialPlot(bag.ens, x.var = "GDD", pred.data = MASQ[train,], which.class = "1")
partialPlot(bag.ens, x.var = "geslacht", pred.data = MASQ[train,], which.class = "1")
```

### Partial Dependence on "AD Partial Dependence on "GDI Partial Dependence on "geslace



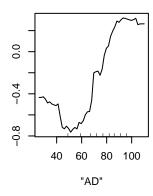


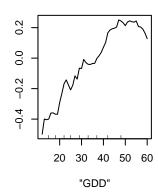


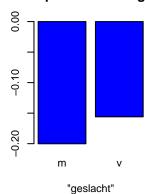
Note that we have to specify the appropriate class label for these plots if we perform classification, otherwise we get partial dependence plots for the effect on the probability of belonging to the first ("0", non-depressed) class.

```
par(mfrow = c(1, 3))
partialPlot(rf.ens, x.var = "AD", pred.data = MASQ[train,], which.class = "1")
partialPlot(rf.ens, x.var = "GDD", pred.data = MASQ[train,], which.class = "1")
partialPlot(rf.ens, x.var = "geslacht", pred.data = MASQ[train,], which.class = "1")
```

### Partial Dependence on "AD Partial Dependence on "GDI Partial Dependence on "geslace





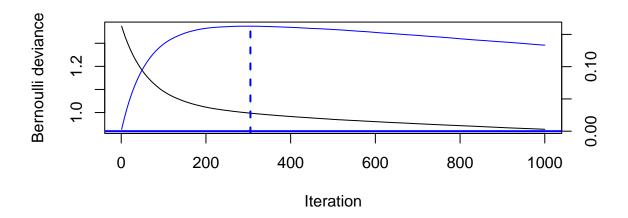


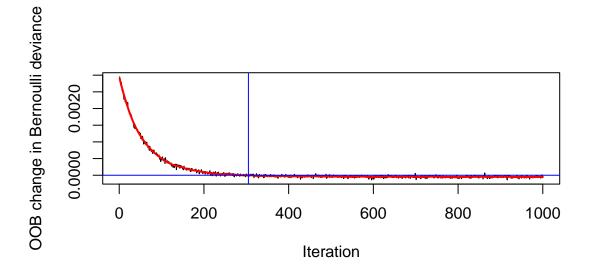
## Exercise 7: Fit a gradient boosted ensemble to the MASQ data

The n.trees argument controls the number of generated trees, which defaults to 100. The bag.fraction argument controls the fraction of training set observations randomly generated to fit each tree in the ensemble. Tree depth is controlled by argument interaction.depth, which defaults to 1 (trees with a single split, i.e., 2 terminal nodes, i.e., main effects only). The learning rate is controlled by the shrinkage argument, which defaults to 0.001.

```
gbm.perf(boost.ens, method = "00B", oobag.curve = TRUE)
```

## OOB generally underestimates the optimal number of iterations although predictive performance is rea





```
## [1] 305
## attr(,"smoother")
## Call:
## loess(formula = object$oobag.improve ~ x, enp.target = min(max(4,
## length(x)/10), 50))
##
## Number of Observations: 1000
## Equivalent Number of Parameters: 40
## Residual Standard Error: 3.229e-05
```

The black curve in the first plot represents training error, which decreases as a function of the number of iterations (fitted trees). The blue curve represents the estimated cumulative improvement in the deviance as estimated based on OOB observations (we requested this through specifying oobag.curve = TRUE).

In the first plot, the vertical blue dotted line indicates at which iteration the OOB error starts increasing (instead of decreasing). In the second plot, we see that this is where the OOB change in deviance becomes negative instead of positive. Thus, this appears the optimal number of iterations (according to the OOB deviance).

We also obtained a warning that OOB generally underestimates the number of required iterations, so the initial value of 1000 might not be bad, also because the second plot indicates no big risk of overfitting (i.e., although the OOB change in deviance becomes negative, but it remains very close to 0).

```
test_y <- MASQ$D_DEPDYS[-train]
train_y <- MASQ$D_DEPDYS[train]
test_N <- length(test_y)
train_N <- nrow(MASQ)-test_N
preds_test <- predict(boost.ens, newdata = MASQ[-train,], type = "response")

## Using 1000 trees...
preds_train <- predict(boost.ens, newdata = MASQ[train,], type = "response")

## Using 1000 trees...
tab_test <- table(true = test_y, predicted = preds_test > .5)
1 - sum(diag(tab_test)) / test_N ## misclassification rate
```

## [1] 0.2375

```
mean((test_y - preds_test)^2) ## brier score

## [1] 0.1675675

tab_train <- table(true = train_y, predicted = preds_train > .5)
1 - sum(diag(tab_train)) / train_N ## misclassification rate

## [1] 0.2210636

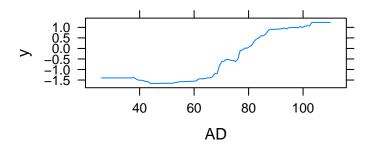
mean((train_y - preds_train)^2) ## brier score
```

## [1] 0.1502326

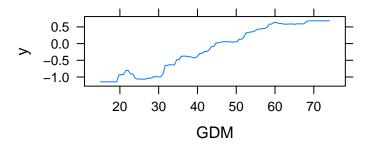
This seems to be the lowest test error we obtained thus far.

## Interpretation

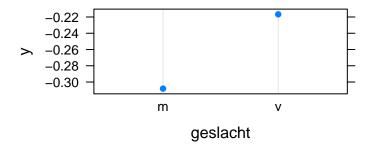
```
plot(boost.ens, i.var = "AD")
```



plot(boost.ens, i.var = "GDM")



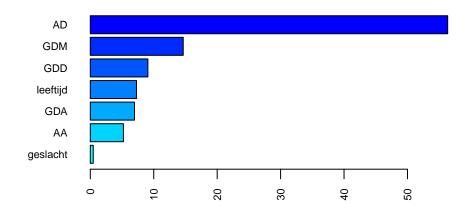
plot(boost.ens, i.var = "geslacht")



The partial dependence plot suggest that the higher the AD and GDM scale scores, the higher the probability of having depression or dysthymia. Men appear to have a slightly lower probability of having a diagnosis, compared to women.

We request a summary of the model in order to obtain variable importances:

```
summary(boost.ens, cex.lab = .7, cex.axis = .7, cex.sub = .7, cex = .7, las = 2)
```



Relative influence

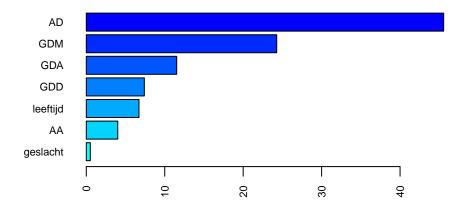
```
##
                         rel.inf
                  var
## AD
                   AD 56.3372131
## GDM
                  GDM 14.6522092
## GDD
                  GDD
                       9.0783275
## leeftijd leeftijd
                       7.2809713
## GDA
                  GDA
                       6.9666723
## AA
                       5.2209153
                   AA
## geslacht geslacht
                       0.4636913
```

Through the various cex arguments, we set the size of text and plotting symbols. Through the las argument, we specify the orientation of the axis labels (see ?par for more explanation).

Like with the bagged and random forest ensembles, again we find that the AD variable is the strongest predictor of depressive disorder, followed by GDM and GDD.

Function gbm() return importances based on training error, by default (see ?summary.gbm). We can obtain permutation importances (but note: these are computed using both in-bag and OOB observations, see also ?summary.gbm) through specifying the method argument:

```
summary(boost.ens, cex.lab = .7, cex.axis = .7, cex.sub = .7, cex = .7,
    method = permutation.test.gbm, las = 2)
```



Relative influence

```
##
                 rel.inf
          var
           AD 45.5601747
## 1
## 2
          GDM 24.2750184
## 3
          GDA 11.5252439
## 4
          GDD 7.3987442
## 5 leeftijd
              6.7159431
## 6
           AA
               4.0113324
## 7 geslacht 0.5135434
```

### Tuning parameters

```
shrinkage n.trees interaction.depth n.minobsinnode
##
## 1
         0.100
                     10
                                          1
## 2
         0.010
                     10
                                          1
                                                          10
## 3
         0.001
                     10
                                          1
                                                          10
         0.100
                    100
                                                          10
## 4
                                          1
## 5
         0.010
                    100
                                          1
                                                          10
## 6
         0.001
                    100
                                          1
                                                          10
```

# tail(grid, 6)

```
##
       shrinkage n.trees interaction.depth n.minobsinnode
## 31
           0.100
                      100
## 32
           0.010
                      100
                                             4
                                                             10
## 33
           0.001
                      100
                                             4
                                                             10
## 34
           0.100
                     1000
                                             4
                                                             10
## 35
           0.010
                                             4
                                                             10
                     1000
## 36
           0.001
                     1000
                                             4
                                                             10
```

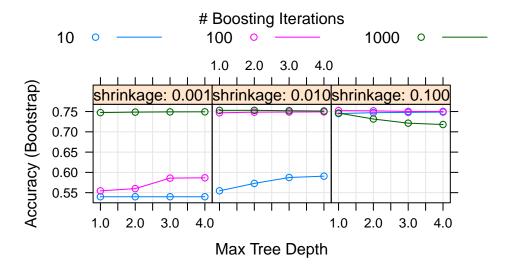
Above, we created a grid of tuning parameters that predictive accuracy will be assessed over. As the train() function from package caret employs sub sampling to assess performance of the models, we have to set the random seed to allow for future replication of our results. Note that running the following code fits repeatedly fits boosted models for each set of parameter values, so it will take some time to run.

Note that train() requires a factor as the response for classification task, (unlike function gbm()), so I set the response to be a factor:

Check out ?train and ?trainControl (which explains the arguments passed to argument trControl) to see what we did with this code. The default of bootstrap sampling with 25 repeats was used, (see method and number arguments of in ?trainControl). Note that these predictive accuracies are estimated on test observations (i.e., 'OOB' observations).

We plot the results:

plot(gbmFit)



Note that the highest accuracies are close to what we have obtained with the models we fitted before. The plot suggests that with higher values of shrinkage, we need less boosting iterations, which is as expected. Note that several combinations of parameter settings appear to yield similar accuracy.

Increasing tree depth to values > 1 seems not to make much different, only seems beneficial when there are

less trees, suggesting mostly main effects of the predictor variables.

The best accuracy is obtained with:

```
gbmFit$bestTune
```

```
## n.trees interaction.depth shrinkage n.minobsinnode
## 18 1000 2 0.01 10
```

These optimal settings differ, but not by much, from our original parameter settings.

We refit the ensemble using the parameter values that can be expected to optimize predictive accuracy:

```
set.seed(42)
boost.ens2 <- gbm(D_DEPDYS ~ ., data = MASQ[-train,], n.trees = 1000,
                  shrinkage = .01, interaction.depth = 2,
                  distribution = "bernoulli")
preds_test <- predict(boost.ens2, newdata = MASQ[-train,], type = "response")</pre>
## Using 1000 trees...
preds_train <- predict(boost.ens2, newdata = MASQ[train,], type = "response")</pre>
## Using 1000 trees...
tab_test <- table(true = test_y, predicted = preds_test > .5)
1 - sum(diag(tab test)) / test N
## [1] 0.1875
mean((test_y - preds_test)^2)
## [1] 0.135182
tab_train <- table(true = train_y, predicted = preds_train > .5)
1 - sum(diag(tab_train)) / train_N
## [1] 0.2502607
mean((train_y - preds_train)^2)
```

#### ## [1] 0.1759091

Both MCR and SEL improved compared to the earlier boosted ensemble. The boosted ensemble with tuned parameters also outperformed the random forest and bagged ensemble fitted to these data previously. All fitted tree ensembles require all variables for making a prediction (because all variables have non-zero importances).

The CART tree requires only the AD scale for prediction. The ctree requires only the variables AD and GDD, and in some cases also GDD for prediction. They thus require substantially less information for prediction, but at a cost to predictive accuracy.