

for  $j$  in  $1 \dots J$

for  $i$  in  $1 \dots n_j$

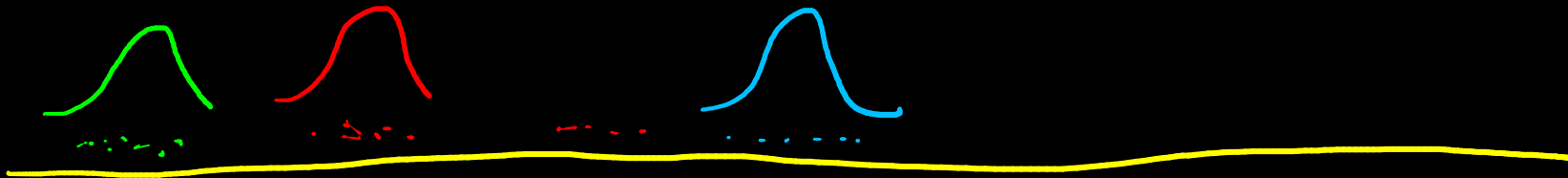
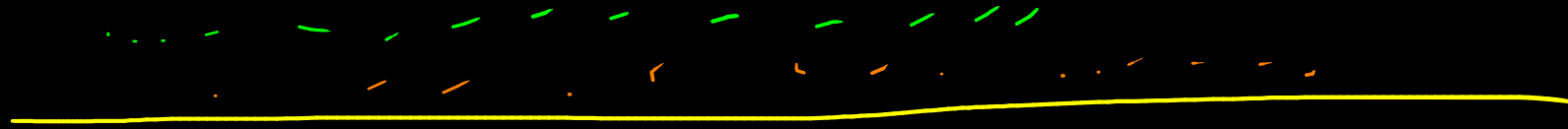
$$y_{ji} \sim N(\mu_j, \sigma^2)$$

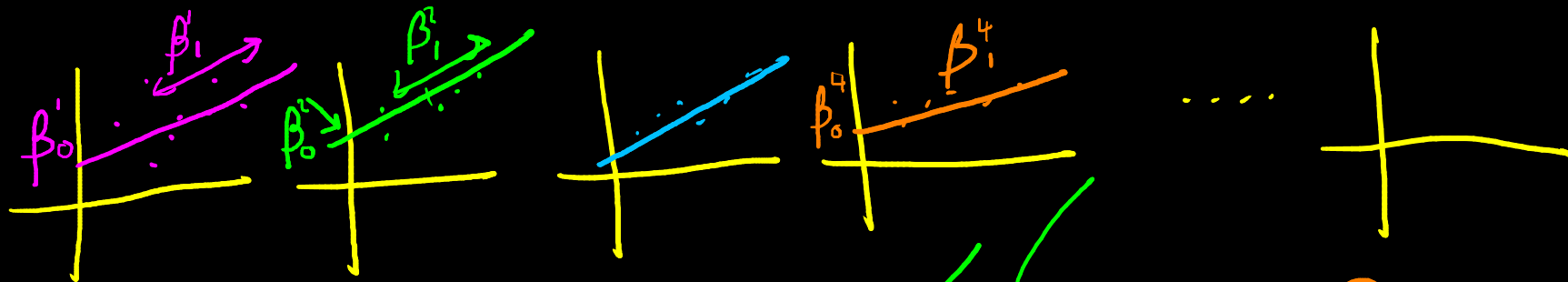
$$\mu_j \sim N(\theta, \tau^2)$$

$$n_j = 12$$

$$Z_j = \mu_j - \theta$$

$$\begin{cases} y_{ji} = \theta + Z_j + \varepsilon_{ji} \\ Z_j \sim N(0, \tau^2) ; \varepsilon_{ji} \sim N(0, \sigma^2) \end{cases}$$

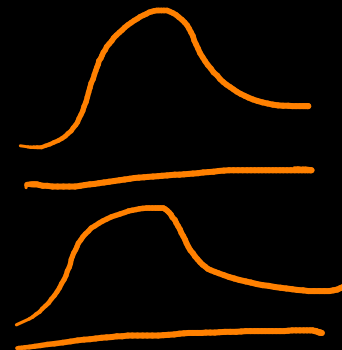




for  $j$  in  $1 \dots J$

$$\beta_0^j \sim N(b_0, \tau_0^2)$$

$$\beta_1^j \sim N(b_1, \tau_1^2)$$



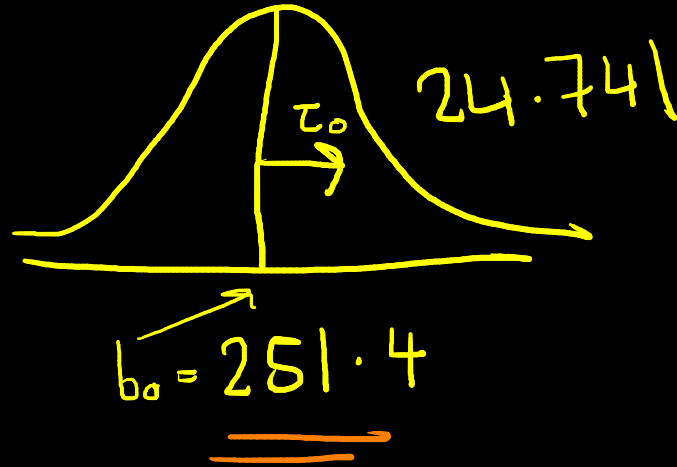
for  $i$  in  $1 \dots n$

$$y_i \sim N(\mu_i, \sigma^2)$$

$$\mu_i = \beta_0 + \beta_1 x_i$$

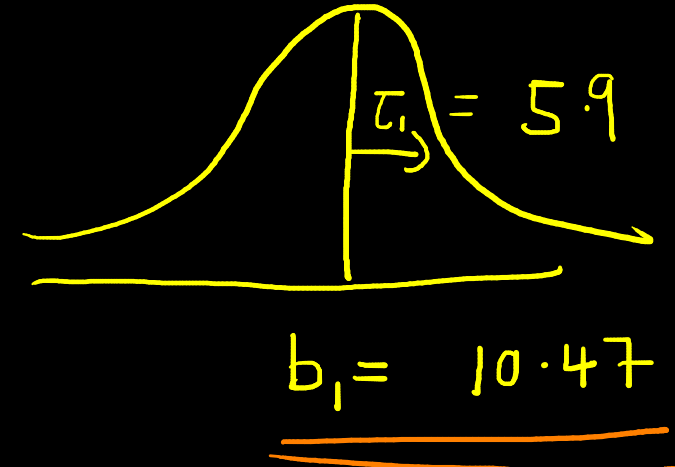
$$\begin{aligned}\mu &= \beta_0 + \beta_1 x \\ &= \beta_0 \times 1 + \beta_1 \times X\end{aligned}$$

intercepts



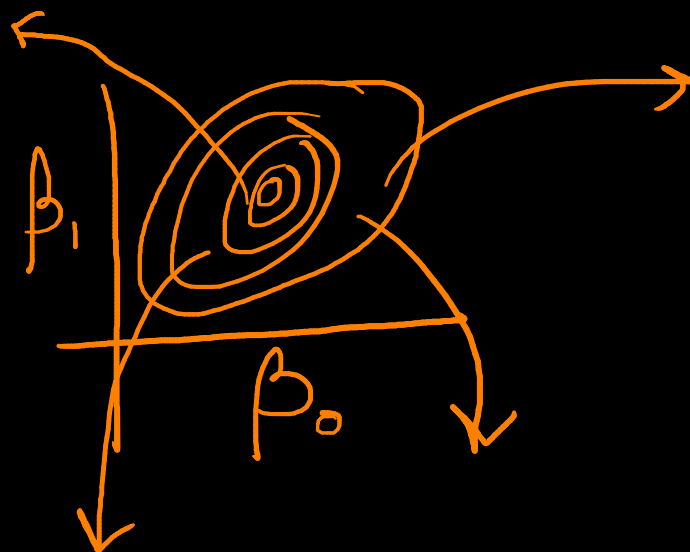
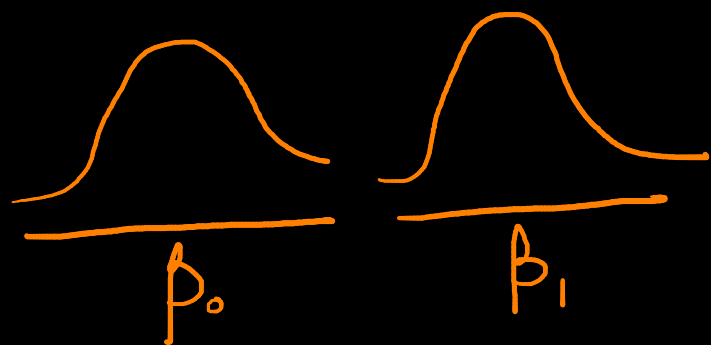
95%  $\approx$  (200, 300)  
interval  
over subject  
specific  
intercepts

slope



10-12, 10+12  
(-2, 22)





$$\begin{bmatrix} \beta_0 \\ \beta_1 \end{bmatrix} \sim N\left(\begin{bmatrix} b_0 \\ b_1 \end{bmatrix}, \Sigma\right)$$

$$\Sigma = \begin{bmatrix} \sigma_0^2 & \sigma_0 \sigma_1 \rho \\ \sigma_0 \sigma_1 \rho & \sigma_1^2 \end{bmatrix}$$

Annotations for the covariance matrix  $\Sigma$ :

- A green arrow points to the top-left element  $\sigma_0^2$ .
- A green arrow points to the bottom-right element  $\sigma_1^2$ .
- A green arrow points to the top-right element  $\sigma_0 \sigma_1 \rho$ .
- A green arrow points to the bottom-left element  $\sigma_0 \sigma_1 \rho$ .