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procedure CheckEG( $f_1$ )
   $S' := \{s \mid f_1 \in \text{label}(s)\};$ 
   $\text{SCC} := \{C \mid C \text{ is a nontrivial SCC of } S'\};$ 
   $T := \bigcup_{C \in \text{SCC}} \{s \mid s \in C\};$ 
  for all  $s \in T$  do  $\text{label}(s) := \text{label}(s) \cup \{EG f_1\};$ 
  while  $T \neq \emptyset$  do
    choose  $s \in T;$ 
     $T := T \setminus \{s\};$ 
    for all  $t$  such that  $t \in S' \text{ and } R(t, s)$  do
      if  $EG f_1 \notin \text{label}(t)$  then
         $\text{label}(t) := \text{label}(t) \cup \{EG f_1\};$ 
       $T := T \cup \{t\};$ 
    end if;
  end for all;
end while;
end procedure

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Figure 4.2
Procedure for labeling the states satisfying $EG f_1$.

is a path within C between any pair of states in C . Let s_1 and s_2 be states in C . Pick some instance of s_1 on π_1 . By the way in which π_1 was selected, we know that there is an instance of s_2 further along π_1 . The segment from s_1 to s_2 lies entirely within C . This segment is a finite path from s_1 to s_2 in C . Thus, either C is a strongly connected component or it is contained within one. In either case, both conditions (1) and (2) are satisfied.

Next, assume that Conditions (1) and (2) are satisfied. Let π_0 be the path from s to t . Let π_1 be a finite path of length at least 1 that leads from t back to t . The existence of π_1 is guaranteed because t is a state in a nontrivial strongly connected component. All the states on the infinite path $\pi = \pi_0 \pi_1^\omega$ satisfy f_1 . Since π is also a possible path starting at s in M , we see that $M, s \models EG f_1$. \square

The algorithm for the case of $g = EG f_1$ follows directly from the lemma. We construct the restricted Kripke structure $M' = (S', R', L')$ as described above. We partition the graph (S', R') into strongly connected components using the algorithm of Tarjan [2]. This algorithm has time complexity $O(|S'| + |R'|)$. Next, we find those states that belong to nontrivial components. We then work backward using the converse of R' and find all of those states that can be reached by a path in which each state is labeled with f_1 . The entire computation can be performed in time $O(|S'| + |R'|)$. In Figure 4.2 we give a procedure