

## 1. Types of statistics:

- Descriptive: displaying data in an informative way
- inferential: generalization the population by examination of sample

## 2. Types of data:

- Qualitative: data not expressed in terms of numbers (Bar chart - pie chart)
- Quantitative: data expressed in terms of numbers (Histogram - frequency polygon)
  - ↳ • discrete: certain values
  - continuous: within a specific range

- frequency: عدد مرات حدوث الحدث
- Relative frequency: frequency  $\div$  number of observations
- Percentage frequency = relative frequency  $\times 100$
- angle frequency (pie chart) = relative frequency  $\times 360$
- How to create a frequency table from raw data?

↳ 1) Range = largest value - smallest value

2) get the number of classes ( $k$ ):  $2^k > n$ , where  $n$  = sample size

3) class width  $R = \frac{\text{Range}}{k}$   $\rightarrow$  متوسط المدى

• midpoint classes:  $\frac{\text{class} + \text{class}}{2}$

4) Set the class limits.

- population mean ( $\mu$ ) =  $\frac{\sum x}{N}$  • central tendency: mean, mode, median

- Sample mean ( $\bar{x}$ ) =  $\frac{\sum x}{n}$

- median (second quartile) = • in the middle • 50% of the data before & 50% of the data after

↳ (1) arrange ascendingly (2) Median location:  $\frac{n+1}{2}$ , when  $n$  is odd sample space number

(3) Median value

$\frac{n}{2}, \frac{n}{2} + 1$ , where  $n$  is even sample space #

- mode: is the value that occurs most frequently in a data set.

- Range: Largest value - smallest value

• dispersion cannot be less than zero

- Standard deviation  $(s)$  =  $\sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}}$  •  $s^2 \rightarrow$  variance • Variation في data لا في mean value  
↳ كل في تقارب في data لا في mean value  
↳ يقيس بُعد كل observation عن mean value

=  $\sqrt{\frac{1}{n-1} [\sum x_i^2 - \frac{(\sum x_i)^2}{n}]}$

- IQR =  $Q_3 - Q_1$

- lower bound =  $Q_1 - 1.5(IQR)$

- upper bound =  $Q_3 + 1.5(IQR)$

- Coefficient of variation:

•  $\frac{s}{\bar{x}} \times 100\%$

•  $\frac{Q_3 - Q_1}{Q_3 + Q_1} \times 100\%$  (extreme value)

- Commenting on box-plot:

- 1) measure of center tendency
- 2) IQR
- 3) Symmetric or not (-ve skewed or +ve skewed)
- 4) extreme value or not

$$0 \leq p(A) \leq 1$$

$$p(A \cup B) = p(A) + p(B) - p(A \cap B) \quad (\text{general})$$

$$p(A \cup B) = p(A) + p(B) \quad (\text{disjoint}) \rightarrow \text{لا يمكن حدوث نفس الوقت}$$

$$p(A \cup B) = p(A) + p(B) - p(A) \cdot p(B) \quad (\text{independent}) \rightarrow \text{يمكن حدوث نفس الوقت}$$

$$p(A \cap B) = p(A) \cdot p(B) \quad \uparrow$$

$$\bullet p(A|B) = \frac{p(A \cap B)}{p(B)} \quad \text{where } p(B) \neq 0 \quad (\text{conditional probability})$$

$$\bullet p(I) p(B|I) + p(II) p(B|II) + \dots \quad (\text{total probability rule})$$

$$\bullet p(D) = p(D \cap I) + p(D \cap II)$$

$$= p(I) \cdot p(D|I) + p(II) \cdot p(D|II)$$

$$\text{Bay's rule: } p(II|D) = \frac{p(II \cap D)}{p(D)} \quad \leftarrow$$

• probability distribution:

$$\text{i) } p(x) \geq 0 \quad \text{ii) } \sum p(x) = 1 \xrightarrow{\neq 1} C[x] = 1 \quad C = \frac{1}{x}$$

$$\bullet \text{Expected value} = E(x) = \sum x p(x) = 1, \quad E(x^2) = \sum x^2 p(x)$$

$$S^2 = E(x^2) - (E(x))^2 \quad \text{variance}$$

$$\bullet E(ax+b) = 0$$

$$a E(x) + b$$

$$\bullet V(ax+b) = a^2 V(x)$$