

$$\mathcal{L} = \frac{1}{2}(\sigma(wx + b) - t)^2$$

$$\frac{\partial \mathcal{L}}{\partial w} = \frac{\partial}{\partial w} \left[\frac{1}{2}(\sigma(wx + b) - t)^2 \right]$$

$$= \frac{1}{2} \frac{\partial}{\partial w} (\sigma(wx + b) - t)^2$$

$$= (\sigma(wx + b) - t) \frac{\partial}{\partial w} (\sigma(wx + b) - t)$$

$$= (\sigma(wx + b) - t) \sigma'(wx + b) \frac{\partial}{\partial w} (wx + b)$$

$$= (\sigma(wx + b) - t) \sigma'(wx + b) x$$

$$\frac{\partial \mathcal{L}}{\partial b} = \frac{\partial}{\partial b} \left[\frac{1}{2}(\sigma(wx + b) - t)^2 \right]$$

$$= \frac{1}{2} \frac{\partial}{\partial b} (\sigma(wx + b) - t)^2$$

$$= (\sigma(wx + b) - t) \frac{\partial}{\partial b} (\sigma(wx + b) - t)$$

$$= (\sigma(wx + b) - t) \sigma'(wx + b) \frac{\partial}{\partial b} (wx + b)$$

$$= (\sigma(wx + b) - t) \sigma'(wx + b)$$