# Pairs Trading on International ETFs

Dimitrios D. Thomakos<sup>♣</sup>, Tao Wang<sup>♠</sup> and Panagiotis Schizas<sup>\*</sup>

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#### **Abstract**

Pairs trading is a popular market-neutral trading strategy among finance practitioners that has been recently evaluated for U.S. stocks (Gatev, Goetzmann, and Rouwenhorst 2006). In this paper, we examine the pairs trading performance as well as the source of the profitability using international exchange traded funds (ETFs). Our results suggest that there are returns from pairs trading on international ETFs. Those returns could partially explained by economic factors.

#### JEL Classification:

**Keywords:** pairs trading, exchange traded funds, ETF, Fama-French, international asset pricing, long and short strategies, market neutral strategies.

<sup>\*</sup> Department of Economics, University of Peloponnese, 22 100, Greece. Email: <a href="mailto:thomakos@uop.gr">thomakos@gmail.com</a>. Tel.: +30-2710-230128, Fax: +30-2710-230139.

<sup>•</sup> Corresponding author. Department of Economics, Queens College City University of Nerw York, US. Email: <a href="mailto:twang2000@gmail.com">twang2000@gmail.com</a>. Tel: (718) 997-5445, Fax: (718) 997-5466.

<sup>\*</sup>Department of Economics, University of Peloponnese, 22 100, Greece. Email: <a href="mailto:pschizas@uop.gr">pschizas@uop.gr</a>, <a href="mailto:pschizas@gmail.com">pschizas@uop.gr</a>, <a href="mailto:pschizas@gmail.com">pschizas@uop.gr</a>,

### 1. Introduction

Investors and finance professionals are always on the lookout for successful trading strategies that account different aspects and assumptions about the markets. A family of strategies, that are relatively aggressive, is the one that uses assumptions and models about market timing: the ability to provide accurate signals of when to enter/exit the market and which way (long or short) to invest. However, market timing can also be casted in the context of market neutral strategies, where both a long and a short position are taken based on a timing signal. An example of such a strategy, much used in the industry but having received little attention in academia, is pairs trading. This particular strategy uses a number of underlying assumptions about the path that asset prices take; the most important ones are those of co-movement and mean reversion: prices of selected assets tend to move together and when they diverge this presents an investment opportunity that is exploited by taking a market neutral position. In a recent paper Gatev et al. (2006) report that the origins of pairs trading probably lies in the mid 1980s when Nunzio Tartaglia developed a high-end trading platform to implement it. In the early 1990s pairs trading strategy flourished as it was used by many individual and institutional investors, mostly hedge funds, in their attempt to reduce market exposure; according to Thomson Financial Database (2010), pair trading covers around 27% of the total hedge funds strategies. The pairs trading strategy exploits this a number of statistical tools, such as the concept of distance and of convergence/divergence of prices based on this distance. In this paper we examine in detail the performance of pairs trading using a large family of international exchange traded funds (ETFs), a liquid instrument of choice among professionals. Besides making a few methodological innovations in the application of the strategy we examine in sufficient detail the probable underlying causes of the profitability of the strategy and its variations.

Gatev, Goetzmann and Rouwenhorst (2006, hereafter GGR) and Engleberg, Gao and Jagannathan (2008, hereafter EGJ) replicate the "original" pairs trading methodology, as discussed above. The EGJ paper works some of the implications of pairs trading profitability, especially in examining the factors that may be responsible for the success of the method. These two papers provide a rather thorough treatment of pairs trading for the US securities markets. Our paper differs from their papers by concentrating on international ETFs, and for good reason: ETFs are very popular in the implementation

of trading strategies among industry practitioners; according to ETF landscape global handbook provided by Blackrock, at the beginning of June 2010, the global ETF industry has 2,218 ETFs with 4,478 listings, assets of \$1,0441.1bn from 131 providers on 42 exchanges around the world. This is the first time, to the best of our knowledge, that pairs trading is tested in this particular asset class.

There are a limited number of, neutral and non-neutral, strategies that use pairs and distances for formulating combinations of long/short positions. Jurek and Yang (2007) use the "Siamese twin formula" where a trading rule is formulated between two assets with common fundamentals and proposes a long position for an undervalued security and a short position for overvalued one. Here the fundamentals of a security take the place of price divergence. Nath (2003) applied an approach based on the (static) empirical distribution of returns. Now a record of the distance of pairs of different securities is being kept and a trade opens a trade when the difference exceeds the 15% percentile. At the same time positions that were already open are liquidated when the distance falls below the 5% percentile. There is also the literature that uses results on mean reversions but the strategies on this literature do not necessarily use pairs or are market neutral to be directly comparable to pairs trading.

While in pairs trading one usually focus the way that enters into a trade, it appears that is equally important to have a solid understanding of why and when to exit a trade. Since pairs trading requires to monitor convergence/divergence of prices one can have the situation that one stays into a trade "too long". According to GGR (2006) no convergence means to leave the pairs to trade within the next 6 months and if they do not converge within this horizon to liquidate the trade. An alternative, and simultaneously shorter perspective, applied by EGJ (2008) is called "cream-skimming strategy" and limits the trade only to the first 10 days after a trade is initiated. One of the contributions of our paper is that it examines in detail the profitability implications of different forms of exiting from a trade. Related to this issue is the issue of number of eligible pairs to trade, as pairs are ranked and then one has to make a decision of which pairs will he/she be considering for monitoring and actually trading.

Finally, as in the previous two papers who worked on pairs trading, we examine also in some detail the economic and other market factors that may explain profitability in pairs

trading. The significant difference in this exercise, compared to previous studies, is that we use a family of international assets and that there may be some factors that do not fall within the "traditional" set of variables that are usually used in assessing the causes of strategy profitability.

The rest of the paper is organized as follows. Next section discusses some of the previous studies related with pairs trading profitability. Section 3 describes data. Section 4 is the methodology. Empirical results are in section 5, and section 6 concludes.

# 2. Arbitrage, liquidity and short sale constraints

Trading strategies are implicitly grounded on the presence of a (possibly time-varying) arbitrage mechanism that could create profitable trading opportunities. Pairs trading assumes that such opportunities arises either when there is "extreme" divergence between pairs of assets within a larger family. Whether arbitrage opportunities exist is, of course, a matter of continuous investigation.

According to Shleifer and Vishny (1997) an arbitrage mechanism becomes ineffective when all arbitrageurs are fully invested and the profits have to be shared to a pool of participants. From such a pool of investors only a small incremental group of "specialists" could identify promptly abnormal returns and can utilize them. When the majority of investors realize these abnormalities, superior profits will diminish and investors will go long onto overpriced assets. It therefore becomes paramount to know when to enter a trade and when to exit from it, even when arbitrage opportunities exist and are acknowledged by investors. Risk aversion is a prime factor to be considered when taking trading positions. Empirical evidence shows that periods of high market volatility are considered significant by professionals in placing their trades: they tend to avoid extremely volatile arbitrage positions, even those positions which (ex post) are seen to terminate in excess returns. Thus, a high volatility environment will force investors to increase their redemptions and fund managers to exit the market, possibly with increased probability of having a loss. Extreme circumstances (such as the divergence that is used in pairs trading) do not reflect a direct consequence of fundamentals and macroeconomic risks but may simply reflect the arbitrageurs risk aversion. This is an important point to remember later when we discuss the factors of pairs trading profitability.

Jurek and Yang (2006) confirm Shleifer and Vishny's (1997) work, where arbitrageurs are reluctant to increase their allocation in a high volatility environment even when a mispricing opportunity has been detected. There is a trade-off between horizon and divergence risk, where after a crucial cut-off point any mispricing, even in the case of expanding divergence, leads to a smaller exposure to market positions. They argued that this trade-off creates a time-varying boundary, where outside the bounds even when the opportunity map increases rational arbitrageurs will diminish their exposure.

Kondor (2008) confirmed the vital role of arbitrage in the success of a trading strategy under three perspectives: (1) competition among investors leads the prices out of their long run "equilibrium" and the predictability of the direction of change diminishes (2) such competition can lead to substantial losses in the majority of cases when an extremely short horizon is considered (3) the absence of arbitrage from the market helps prices to converge to their "equilibrium".

Jacob and Levy (2003), on the question of optimal time to exit, argued that statistical arbitrage opportunities and accurate forecasting of the time series of price or return spreads should be considered as the unique factor which affects profitability of a pair trading strategy.

Do et al (2006), Jurek and Yang (2006) and Kondor (2008) all also discussed the issue of the "convergence time", i.e. the time to exit in pairs trading-like strategies. All agree that the decision of when to exit is among important factors that affect a strategies performance. Based on this we are lead to investigate several different timing intervals and to cross-compare results on the decision of when to exit a trade from a pairs trading strategy in an attempt to shed some light on whether there is an "optimal trading horizon".

Beyond these issues there are two other ones that greatly affect the implementation and profitability of any trading strategy: liquidity and trading constraints, especially short selling. There are studies that provide evidence that mean-reversals, both on a short and long run, are driven by the level of liquidity, see Conrad, Hemmed and Niden (1994), and Cooper (1994). Amihud and Mendelson (1986), Brennan and Subrahmanyam (1996) and

Brennan, Chordia, and Subrahmanyam (1998) argued that illiquid stocks give on average higher returns. Amihud (2002) and Jones (2000) model liquidity as an endogenous variable and show that there is a link between market liquidity and expected market returns. EWJ (2008), on the other hand, provide evidence that liquidity factors have limited power to explain pairs trading profits and this power further declines further as we shorten the time-to-exit from a trade. Llorente et al (2002) argued that short-term return reversals are driven by non-informational hedging trades where illiquid stocks are more vulnerable.

Chordia et al (2000) concentrate on aggregate spreads, depths and trading activity on US stocks, showing that on daily basis there is negative correlation between liquidity and trading activity. Liquidity collapses on bear markets and is positive correlated by long and short interest rates. Increasing market volatility has a direct negative effect in trading activity and spreads. Major macroeconomic announcements increase trading activity and depth just before their release. Knez et al (1997), under a different perspective, showed that the difference between quoted depth and order size is strongly correlated with conditional expected price, so the profits depends on the size of the positions.

Short sale constraints prohibit the application of market neutral strategies and cancel the hedging ability that arbitrageurs and investors have to reduce their market risk. However, EGJ (2008) on their pairs trading implementation argued that short-sale constraints are not correlated with the risk and return of pair trading. In our analysis we find that short selling might be important in that it appears as a strong driving force of pairs trading profitability in the group of ETFs that we consider.

## 3. Data

Our empirical analysis focuses on 22 international, passive ETFs. The ETFs come from both developed and developing economies. The primary listing exchange is the American Stock Exchange<sup>1</sup> The list of our series includes the following countries accompanied by their ticker: MSCI Australia (EWA), MSCI Belgium (EWK), MSCI Austria (EWO), MSCI Canada (EWC), MSCI France (EWQ), MSCI Germany (EWG), MSCI Hong–Kong (EWH), MSCI Italy (EWI), MSCI Japan (EWJ), MSCI Malaysia (EWM), MSCI

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<sup>&</sup>lt;sup>1</sup> The majority of the ETFs are provided by Barclays Global Investors - (Ishares).

Mexico (EWW), MSCI Netherlands (EWN), MSCI Singapore (EWS), MSCI Spain (EWP), MSCI Sweden (EWD), MSCI Switzerland (EWL), MSCI Japan (EWJ), MSCI S. Korea (EWY), MSCI EMU<sup>2</sup> (EZU), MSCI UK(EWU), MSCI BRAZIL (EWZ), MSCI TAIWAN (EWT) and S&P500 (SPY), the biggest ETF worldwide<sup>3</sup>.

The majority of the ETF records start on April, 01 1996<sup>4</sup>. Exceptions are MSCI S. Korea, which started on 10/05/2000, MSCI Taiwan, that started on 20/06/2000 and MSCI EMU that started on 25/07/2000. Our analysis is based on daily observations including open, high, low and close (dividend adjusted<sup>5</sup>) prices for each ETF series. All of the ETFs we use have futures contracts and some of them also have options<sup>6</sup>. Almost all of them can be traded, over the counter, to electronic platforms (ECN) at the AMEX trading hours.

An important part of our analysis, which has not been considered in the previous papers, is to examine whether there is differential behaviour of pairs trading in developed against developing economies. For this we split the ETFs into two respective groups and perform a separate analysis on both. We also use segmentation for our ETFs, based on market capitalisation. This split allows examining the potential effects of liquidity on the pairs trading strategy in cross-comparison with the level of financial development of the underlying market.

In addition to our full sample results we divided our sample into four different sub-periods. The first sub-period covers April 1st 1996 to December 31st of 1999. The second sub-period starts on January 1st 2000 and goes until December 31st of 2002. The third sub-period covers the period from January 1st 2003 until the end of 2005, and the last period is extended from January 1st of 2006 till the end of our dataset. The idea behind these sample splits is to examine if there are any patterns that lead the strategy

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<sup>&</sup>lt;sup>2</sup> EMU corresponds to the performance of publicly traded securities in the European Monetary Union markets.

<sup>&</sup>lt;sup>3</sup> We have selected all the international ETFs that have been launched before the 07/30/2000, which was our cut-off date in order to have a sufficient number of observations. The included ETFs are, naturally, a subsample of a broader group of international ETFs.

<sup>&</sup>lt;sup>4</sup> Note that it is the first time that we apply pair trading including the period of the recent great credit crunch.

<sup>&</sup>lt;sup>5</sup> Dividends may be responsible for some of the divergence of the prices. (NEEDS REFERENCE)

<sup>&</sup>lt;sup>6</sup> Options have the following ETFs: MSCI Australia, MSCI Brazil, MSCI Canada, MSCI Germany, MSCI Hong-Kong, MSCI Japan, MSCI UK, MSCI Taiwan, S&P500. The presence of options increases the liquidity of the respective ETFs.

only on specific periods and to check the relation of pairs trading to different conditions of capital markets. Furthermore, note that the first sub-period corresponds to a bull market while the second sub-period corresponds to a bear market. The third sub-period is related to a "recovery" period for the markets while the last sub-period covers both the rally of recent years and part of the start of the recent crisis.

Finally, two short comments on the suitability of our chosen dataset. First, the MSCI indices are free of survivor bias and are a very robust proxy of market performance for each country. In addition, when using such indices there is practically no bankruptcy risk, a factor that was discussed in GGR (2006) in connection with pairs trading performance. A characteristic example arises by the properties of "twin" stocks. A negative announcement on the first stock will have identical influence on both stocks but on different direction (positive for one and negative for the other): pairs trading between such "twin" stocks will be unsuccessful.

## 4. Methodology

In this section we describe the empirical methodology for implementing pairs trading. We start off with some preliminaries and terminology. To apply the methodology we have to first make a selection of pairs. This has to be done on a specific (rolling) time segment called the "formation period". During the formation period a specific rule is applied to find which pairs are eligible for trading. Then we have the actual trading period, whose length has to also be pre-selected as was done for the length of the formation period. During the trading period another rule is applied to monitor whether a trade should be terminated; all trades are exited at the end of the trading period. Then another formation period is considered and so on. Note that trading periods do not overlap while there is a partial overlap to the formation periods. To avoid the pitfalls of (excess) data mining we fix the formation period to 120 trading days throughout our analysis and experiment with different lengths for the trading period. Our approach relies on a shorter formation period when compared with GGR (2006) and EWJ (2008) but we have the advantage of non-overlapping trading periods. During the formation period we apply a rule similar, but not identical, to the one used in GGR (2006) and EWJ (2008). Our approach is as follows.

During the 120 days of each formation period we record the price of all ETFs in the group we are using. From these prices we compute normalized cumulative price indices which are comparable across the ETFs in the group. Divergence is based on these indices that are given as:

$$P_t^{\alpha} = \prod_{i=i+1}^{t+i} (1 + r_t^{\alpha}), \text{ for } t = 1, 2, \dots, 120$$
 (1)

where  $r_t^a = (P_t/P_{t-1}) - 1$  is the simple return of the *a*th ETF and the index *i* runs as a sequence of the form  $i = \{0, 20, 40, ...\}$  to create the partially overlapping rolling formation periods (note that these exclude the 20-day trading period) and similarly for other lengths of the trading period. Next, for each formation period we compute the average absolute distance among all pairs in the group we are considering as:

$$\Delta_{ab} = \frac{1}{120} \sum_{t=i+1}^{120+i} |P_t^a - P_t^b|, \text{ for all pairs } a, b$$
 (2)

and we rank the distances from largest to smallest to identify trading opportunities, where these distances are larger than a pre-specified threshold. The use of absolute distances allows us to have a bit more of trading opportunities and, as usual when compared to a sum-of-squares measure, is more robust to sudden large discrepancies that quickly disappear. Suppose now that we consider the top L pairs, i.e. the pairs that have the L largest  $\Delta_{ab}$  values during the formation period. For each of the 20 days of the trading period we compute the 120-day normalized cumulative price indices and compare them to a fraction of the  $\Delta_{ab}$  formation value for each pair; if the absolute difference of the price indices is greater than this fraction then a trade is initiated as:

$$T_{c+s}^{ab} = \begin{cases} 1, & \text{if } \left| P_{c+s}^{a} - P_{c+s}^{b} \right| > c\Delta_{ab} \\ 0, & \text{otherwise} \end{cases}, & \text{for } s = 1, 2, \dots, 20 \end{cases}$$
(3)

for some constant c (we experiment with c = 0.5, 1 and 2.) When a position is initialized we go long in the asset with the lowest price index and short in the asset with the highest one, say if  $P_{t+s}^{\alpha} > P_{t+s}^{b}$  then we go long on  $P_{t+s}^{b}$  and short on  $P_{t+s}^{a}$ . Then, we check that each day in the trading period the same sign is maintained otherwise the trade is terminated and the associated return of the trade is computed and stored. We thus have:

if 
$$T_{t+s}^{ab} = 1 \wedge sgn(P_{t+s+1}^a - P_{t+s+1}^b) = sgn(P_{t+s}^a - P_{t+s}^b)$$
 then  $T_{t+s+1}^{ab} = 1$ , (4) else  $T_{t+s+1}^{ab} = -1$ 

The above procedure is repeated for all L pairs and the strategy's return is then computed. Since we have both a long and a short position across L pairs we need to find the return for each long/short position and the total return across all L positions. First, we compute the return for a single pair as:

$$R_{t+s}^{ab} = R_{t+s}^{ab,Long} - R_{t+s}^{ab,short}$$

$$\tag{5}$$

and then we compute the return for the "portfolio" of L pairs as a weighted sum of the form:

$$R_{t+s}^{p} = \sum_{\forall a,b} W_{t+s}^{ab} R_{t+s}^{ab} \tag{6}$$

where the weights are computed based on the previously accumulated wealth as in:

$$W_{t+s}^{ab} = \frac{\omega_{t+s}^{ab}}{\sum_{\forall a,b} \omega_{t+s}^{ab}} \text{ and } \omega_{t+s}^{ab} = \left(1 + R_{t-1+s}^{ab}\right) \times ... \times \left(1 + R_{t-20+s}^{ab}\right)$$

The above describe our basic methodology for pairs trading. An important issue that we do not put into equation format is whether a trade is executed on the signal day or the following day (a one-day delay); we experiment with both scenarios as do GGR (2006) and EWJ (2008). Other variations and robustness checks are presented and discussed in the results section that follows.

# 5. Empirical results

## Choice of trading horizon

The pairs trading methodology relies on certain user-defined conditions, such as the choice of c and the choice of the trading horizon. We therefore start our discussion with empirical results on the choice of a 20-day trading horizon. In Figure 1 we present the mean return of the pairs trading strategy for three different values of c and a sequence of trading horizons k=1, 2, 3, 4, 5, 10, 20, ..., 120 days for L=5 (using the first five pairs).

Within the maximum horizon of 120 business days, the optimal trading period roughly corresponds to 20 days, irrespective of the choice of c. We can see a rather clear peak at the 20-day trading horizon. While it is possible to let the pairs trading strategy run until the price indices have converged we can clearly see that there is an increasing risk associated with this approach.

## Properties of trading

Using the 20-day horizon we next compute some summary measures for the actual trading activity and report them in Table 1 (PROXY THIS -- THE AVERAGE NUMBER OF TRADING DAYS IS WRONG). In Panel A of the table we report some statistics on the time and duration of pairs trading across different values of L. The interesting results are that (a) there is, on average, one-round trip per pair across all L combinations and (b) almost all pairs open for trading with the 20-day horizon. However, not all pairs convergence and the trade is terminated within the 20-days. As we can see from Panel B of Table 1 to have about 50% of the pairs to converge we require a trading horizon of about 40 days. This is an interesting result of practical significance that can partially explain the success of the pairs trading method: if one waits long enough for all the trades to converge will essentially gain nothing from this strategy; there appears to be an issue of underlying "timing" at work here, a horizon after which you will not be making much of a profit. Taking any profits that may arise using the signals of the strategy appears to be a suitable way to go.

## Stochastic dominance

Before embarking on a detailed analysis of our results it is interesting to ask whether there is any "utilitarian" point in the whole exercise. By this we mean, does it matter to even consider a strategy if this strategy does not provide sufficient "utility" to us compared to the naive buy-and-hold benchmark? Here we briefly discuss some results on our application of tests of stochastic dominance of various orders that are based in the notion of "utility". Jarrow (1986) examined the existence of arbitrage opportunities incorporating first order stochastic dominance and argued that stochastic dominance implies the presence of arbitrage opportunities. Fong et al (2005) provide evidence of stochastic dominance for international momentum strategies. They strongly argued that the non-parametric nature of stochastic dominance tests allows to more easily deciding between profits and losses, and the knowledge of the utility function is adequate for the

investors to decide, without the need to be aware of the distribution of the returns. In contrast, simple ranking is sensitive to outliers. Their major outcome was that traditional asset pricing model fails to explain momentum profits with respect to non-satiated and risk averse investors. However, asset pricing models that integrate behavioural biases of investors could be an optimal alternative solution to this problem. Here we examine stochastic dominance of orders one through three, in an approach similar to Cho, Linton and Whang (2007), which allows for a rather complete testing procedure with boostrap-based p-values, based on the results of Linton, Maasoumi and Whang (2005). For space considerations we do not present here the details of the test statistics and the procedure but they are available on the above two references and on request.

The results on the stochastic dominance of pairs trading against the buy-and-hold of the S&P500 ETF are given in Table 2 and are rather clear: pairs trading, irrespective of the trade opening day (event day or next day) stochastically dominate the buy-and-hold approach for all orders of dominance examined. This is important to begin with since it says that it does make sense to work with pairs trading because it is more "useful" to do so on utilitarian grounds.

## Profitability of pairs trading: baseline results

Pairs trading is a profitable strategy. The extent of the profitability results that we obtain of course varies, depending on the number of pairs L used, the groupings based on market origin or capitalization and sub-samples in time. But it will be seen that the profitability results are robust across all these categories.

Before discussing the results let us overview the exact methodological parameters on which they are based. The backtesting starts on September, 23 1996 with the first 19 available ETFs. At June, 20 2000 we add the latest ETF. The number of pairs used in constructing the portfolio returns are set to L = 2, 5, 10 and 20. The formation period is 120 and the trading period is 20 days; results based on a 60-day trading period are also available but not discussed here. The threshold parameter is set to c = 0.5 throughout. Finally, a trade is initiated at the closing prices of the day *after* a signal is given (one-day waiting) and, for comparison, we also provide results when a trade is initiated at the closing prices of the signal ("event" in the tables) day.

Table 3 presents the baseline results of our application of pairs trading. Panel A has the results based on the event day and Panel B has the results with one-day waiting. We present various summary measures and we discuss them in turn. Terminal wealth of the portfolio is affected by the size of L: using half or more of our universe of pairs results in deterioration of performance based on terminal wealth, especially when one uses the (more realistic) one-day waiting approach. Therefore, a smaller size of pairs, in our case that of about 10% to 25%, appears to be best suited for the strategy at hand. Note that terminal wealth is cut in half or more when the one-day waiting approach is used although the other performance measures appear to be quite similar. The strategy's skewness is always positive, a rather significant result when compared to the mildly negative skewness that most equity indices have. Next, note the difference in the risk of the L=2 portfolio vs. the portfolios with L=5 or more pairs: as expected, a larger Lleads to a smaller standard deviation of the strategy but also to a smaller Sharpe ratio (for Panel B; in Panel A the Sharpe ratios are becoming larger with L but the practicality of the event-day strategy is rather limited). The use of L = 5 pairs appears to be giving the best overall performance throughout in Table 1; the annualized Sharpe ratio for the L =5 pairs portfolio for the one-day waiting period is about 1,86 (using 252 trading days per year).

The results of the table also reveal that the timing abilities of this strategy are rather good: the mean positive excess return of the strategy is always larger than the mean negative excess return of the strategy. This implies that the successful trades are on average larger (they are slightly over 50%) than the negative ones but, more importantly, they tend to be more accurate in their timing. This is important for making an investor using this strategy accept the inherent risks. Finally, it's also important to note that the strategy is almost unrelated to the returns of the S&P500 index (especially for L = 2 or L = 5); this reflects on either the international composition of our ETF group (which, nevertheless, includes the ETF for the S&P500) or on the timing ability of the strategy to correctly identify disequilibria in the price paths.

The evolution the strategy's wealth (cumulative return), corresponding to Panel B of Table 3, is given in Figure 2. There we plot the pairs trading performance, the S&P500

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<sup>&</sup>lt;sup>7</sup> Goetzmann et al (2002) argued that evaluation results based on the Sharpe ratio can be misleading if the strategy's return distribution exhibits negative skewness but this problem disappears when we observe positive skewness.

and also the long and the short components of the strategy, all for L=2, 5, 10 and 20 pairs. There are some interesting features in the plots: first, the strategy's performance during the boom years before 2000 is below that of S&P500 but it sharply picks up and outperforms the S&P500 after we go into the bear market; second, the strategy's performance increases almost monotonically for all pairs except for L=2, when we can see a large drawdown period after 2002; third, the apparent success of the strategy's timing ability shows through the domination of the short component – this makes sense since the strategy's performance starts going over the S&P500 when the bear market started; finally, this figure leaves open the question as to whether the strategy would perform equally well if it was implemented from a different starting point. We return to this question later in our discussion.

Before continuing we give a very brief comparison of performance of pairs trading between this paper and GGR (2006). For the top L=5 eligible our asset selection and implementation gave an average *monthly* excess of 1.49% versus a 0.78% for GGR; for L=20 the numbers are much more similar, being 0.93% and 0.81% respectively.

#### Results based on market capitalization

Are the results we have seen so far affected by market size? After all our grouping is one that includes data on ETFs from different markets. We repeat our analysis by splitting the ETFs into "small" and "large" capitalization groups and examining the new results. In the context of their analysis, GGR (2006) argued that an examination of different levels of capitalization provides a robustness check against short-selling – and we have seen that the short component was pretty strong in driving the previous results. In the context of pairs trading and contrarian strategies, Avramov et al (2006) claim that large mean reversals are positively linked to illiquid stocks and higher turnover. Put differently, a low level of liquidity is more vulnerable to non-informational trades and Llorente et al (2002) argued that short-term reversals are correlated to non-information driven hedging trades.<sup>8</sup>

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<sup>&</sup>lt;sup>8</sup> In the context of more "traditional" approaches that rely on market capitalization there is some evidence that across countries small capitalization might outperform large capitalization; see Bondt et al (1989), Conrad et al (1989), Rouwenhorst (1998), Zarowin (1990), Richards (1997), Chan (1988) and Ball et all (1989) and Knez et al (1996).

For the size split we consider "large" capitalization to correspond to ETFs with market cap between 384 millions to 65 billions while "small" capitalization to correspond to ETFs with market cap from 330 millions down to 59 millions. Accordingly, we have in the "large" cap category the ETFs for: Australia, Brazil Canada, EMU, Hong Kong, Japan, Singapore and South Korea, Taiwan, UK, S&P500; and on the "small" cap category the ETFs from Austria, Belgium, France, Germany, Italy, Malaysia, Mexico, the Netherlands, Spain, Sweden and Switzerland Table 5 has the related results.

The most striking result from this split is that performance of the trading strategy is greatly reduced for both groups, in terms of terminal wealth, mean return and Sharpe ratio – although the strategy's performance remains unrelated to the S&P500. However, we can also see that there are differences between the "large" and "small" ETFs. First, the performance appears to be slightly better for the "small" cap group in terms of terminal wealth and Sharpe ratio – now for L=5 the annualized Sharpe ratio for the "small" cap group is 1.03 and for the "large" cap group is 0.87. Due to the diminished size of the universe of ETFs in each group we also see that better performance is for L=2 rather than L=5 but with a lower Sharpe ratio. Second, the performance of the "small" cap group might be driven by the timing ability of the strategy in the smaller markets since we can see that the percentage of observations with positive returns is larger for this group than for the "large" cap group. Overall, the results here indicate that a blend large and small ETFs is better than either group alone – the strategy needs a larger, more diverse universe to be able to provide market timing results.

EGJ (2008) split their sample into two portfolios based on average market capitalization and level of liquidity, however they do not find anything conclusive in terms of the interaction of market capitalization and profitability for their data. This suggests that the type of exposure (domestic vs. international) may also be a significant factor behind pairs trading performance.

### Results based on type of market (developed vs. emerging)

Splitting the ETFs into "small" and "large" cap groups is useful but it mixes markets that are mature with markets that are still developing. Since emerging markets are always seen as potential opportunities it is of interest to separately analyze the performance of the strategy in developed and emerging markets. Bekaert et al (1998) claim that to threat

emerging markets as identical to developed markets could lead to wrong assumptions and wrong conclusions. Due to the pronounced heterogeneity of this new split we have to make some changes in the way we run our backtesting. First, due to differences in inception dates the backtesting starts on June of 2000. Second, there are only five ETFs classified as "emerging" markets: Brazil, Malaysia, Mexico, Taiwan and South Korea; this limits the number of pairs to be considered to a max of L = 10.

#### Results based on long and short components separately

As we already discussed in the baseline results (see Figure 2), the short component in the pairs trading appear to be dominating the long component. In Table 6 we present more detailed results that document that indeed this is the cases (here we are again using all ETFs as in the baseline results). The better performance of the short component is evident across all L pairs but note that its effect diminishes as L increases. While there is a differences in terminal wealth, mean return and Sharpe ratio, its interesting to note that the differences in the standard deviations of the short and long components are rather small. Another interesting result in the table is that we can now see a pronounced, positive correlation of both the short and long component with the S&P500: this probably supports the timing ability of the strategy, since we require a positive correlation even when the S&P500 is falling so as to effect the short side of the trade. See that the correlation with the S&P500 is larger for the short component, thus supporting what we saw in Figure 2 (the strategy picking up in terms of performance when the S&P500 started falling in 2000).

### Results based on sub-samples: sensitivity analysis

Does it matter when this (or any other trading strategy) starts? It should matter otherwise we would have a "universal" winner. To examine the sensitivity of our results so far we break the full sample into four sub-samples covering different periods of interest: first sub-sample goes from April 1, 1996 until the end of 1999; the second sub-sample goes from January, 1 2000 and ends on 2002; the third sub-sample starts in 2003 and ends in 2005 while the last sub-sample spans 2006 to March 2009. As we already noted in passing, the first period is one of a bull market, the second period has the bear market that followed, the third period can be thought of as the "recovery" period for global

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<sup>&</sup>lt;sup>9</sup> We followed the MCSI classification for this.

<sup>&</sup>lt;sup>10</sup> GGR (2006) argued about the necessity of examining separately these two components of the strategy.

markets while the fourth and last period has a structural break in it (first going into a small uptrend and then getting into the subprime crisis and the ensued global financial turmoil).

If pairs trading is a "true" market-neutral strategy we would expect to maintain its profitability even in bear markets where a significant downturn is occurring. We can examine whether this is the case by looking at the results in Table 8. The performance details during the second sub-sample immediately stand out: performance is increasing with L as does the positive correlation of the strategy with the S&P500. The annualized Sharpe ratio for L = 5 (for comparability with the baseline results) is now 2.06 (compared to 1.86 in the baseline case), a value that falls in the range of practitioners' interest. Then, note that the strategy's performance is (obviously) best during trending markets, i.e. in the first or the second subsample, irrespective of the trend direction. During the "recovery" period of the third sub-sample the performance is worse among all four sub-samples considered. During the second and third sub-samples there appears to be increased "risk aversion", and that a higher L gives better performance. On the fourth sub-period that contains both a positive trend and a break components we can see that performance has the same characteristics as in the first sub-sample although all measures are now smaller in magnitude; note that here we have, as in the second subsample, increased correlation with the S&P500.

#### Pairs Trading Profitability and Economic Fundamentals

Our discussion so far shows that, in GGR (2006) and EWJ (2008), pairs trading is a viable and profitable trading strategy that exploits price divergence among co-moving assets. However, where does its profitability come from? This question has been addressed in these two studies but here we have a different family of assets that we are working with. We therefore have to use not just the literature standards, such as the Fama and French factors, but also other economic and market variables that are suitable to the international aspect of our dataset.

We cannot possibly review the literature that relates to factors here in any degree of detail. We briefly go over some references that are related to the work that we discuss in this section. We can split the work on factors on three major categories, according to the purpose that the asset pricing model has been constructed.

- (1) Firm-Level Characteristics (Idiosyncratic), as in Cavaglia, Brightman and Aked (2000), Carrieri, Errunza and Sarkissian (2005), Hou, Karolyi and Kho (2006) and Engelberg (2008).
- (2) Market level characteristics (local and global markets), as in Fama and French (FF) (1992, 1996, 1998), Rouwenhorst (1998) and Griffin (2002).
- (3) Macro-economic or country characteristics, as in Chan, Chen and Hsieh (1985), Liew and Vasalou (2000), Vasalou (2003), Brennan, Wang and Xia (2004) and Petkova (2006).

Financial practitioners have also employed several risk models including explanatory factors, the most popular being (according to Hou et al. [2006]) the BARRA Integrated Global Equity Market Model (Stefek, 2002; Senechal, 2003), Northfield's Global Equity Risk Model (Northfield, 2005), ITG's Global Equity Risk Model (ITG, 2003) and Salomon Smith Barney's Global Equity Risk Management (GRAM, Miller et al., 2002).

### Pairs trading against the FF-type factors

Table 9 has the results of a regression of compounded monthly returns from our backtesting on the three FF factors and a momentum factor. For both the 20 and the 60-day trading horizon we can see that there are significant excess returns that cannot be explained by any factor except the HML one, which is based on book-to-market. The estimates are negative and significant for all choices of *L* pairs. Our results reveal a different source of pairs trading profitability compared to GGR (2006) and EWJ (2008), which was expected due to the different composition of the universe of assets that we considered here.

Performing the same analysis but in sub-samples, and adding two more momentum indicators, we can see a variety of interesting results at Table 10. First, note that the significant excess returns now only appear in the first and second sub-sample of the bull/bear markets that goes until 2000 and 2002; this is in accordance of our earlier result that pairs trading appeared to worked strongly in trending markets. During these two sub-samples no factor appears to be statistically significant, except the short-term reversal indicator for the second sub-sample – which again validates the timing ability of

<sup>&</sup>lt;sup>11</sup> The conversion to monthly returns was done for conformability with the earlier literature; results are available for a daily frequency as well. In addition, all the estimations have been conducted with the long and short term reversal factors, as they are presenting in Ken French's website. However, their explanatory power was low and we dropped them; results are available as well.

the strategy. Second, for the third and fourth sub-samples it is difficult to discuss the explanatory ability of the factors since the excess returns are statistically zero. The significant coefficients appeared scattered with no discernible pattern.

In Tables 11 and 12 we present results similar to Table 9 but using the ETF splits to emerging vs. developed markets and "small" vs. "large" capitalization – as we have done for the presentation of baseline results in Tables 5 and 6. For the split based on market development, in Table 11, we can see that excess returns are significant in both types of markets but profitability is explained by different factors. In the case of emerging markets the market and momentum factors loads negatively and significantly while in the case of developed markets the book-to-market factor leads negatively and significantly. These results are intuitive since the emerging markets could not possibly be explained by structural factors like book-to-market but rather by the leading U.S. market and the underlying momentum. Note that the  $R^2$  values from the emerging markets regressions are the highest so far, up to 17% for the top L=5, 10 pairs. Turning next to the split based on capitalization, in Table 12, we can see that for the "large" cap portfolio we have significance excess returns and negative and significant the size factor – that was to be expected. For the "small" capitalization portfolio the excess returns are significant but not as significant as in the "large" cap case; no factor appears to be overall significant

Finally, in Tables 13 and 14 we present results from a regression based on FF-type international factors, constructed from international indices that were weighted based on the MCSI EAFE index. The results of the full sample in Table  $12^{12}$  show that we have excess returns that are significant and cannot be explained by any of these factors, maybe except the book-to-market factor for L=2 – but then again this choice of L was not the most successful one in backtesting. On the other hand in Table 14, where we have the sub-samples that were discussed before, we can see some more interesting results. For the first sub-period the excess returns remain significant while there is some (limited) explanatory power to the earnings to price variable; for the second sub-period (the bear market after 2000) no factor has any explanatory value – this is important for the strategy has a very good performance even during downturns and its interesting to know that this performance is unrelated to these international factors. However, the most interesting of

<sup>&</sup>lt;sup>12</sup> We perform the estimations with the earnings-to-price variable and dividend yield as they represented in Ken French's website; Results are available on request.

all results in Table 14 are those for the last period, that is after 2006. Note here the magnitude of the R<sup>2</sup> values, which ranges from 37% to 59% indicating that these international factors can explain a large percentage of variation for pairs trading during this period that includes the onset of the financial crisis. Two variables account for this percentage of explanatory power, earnings-to-price and dividend yield, especially the last one.

## 5. Conclusion

In this paper, we examine the pairs trading performance as well as the source of the profitability using international exchange traded funds (ETFs). Our results suggest that there are returns from pairs trading on international ETFs.

While it is clearly interesting to examine the potential factors that explain pairs trading profitability, it is also of interest to consider whether there are economic or financial variables that can explain the generation of signals in pairs trading. Currently, we are exploring the topic in this direction.

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Table 1
Summary of Trading Statistics

The table represents the trading statistics of the excess return portfolios. Due to different inception dates of dataset, I initiate the calculations with the first 19 ETFs and we add each separate ETF by its own inception date. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. On Panel A, we open the trade when the divergence between the pairs exceed 0.5 standard deviations, and if does not converge within the next 20 business days we stop the trade. The implementation of the strategy takes place the next business day of the divergence. Panel B, represents pairs that convergence according to different trading periods.

Panel A: Trading Statistics													
Pairs Portfolio	Top 2	Top 5	Тор10	Top 20									
Average Number of Trading Days per pair	19,115	19,070	19,056	18,951									
Standard Deviation Average Number of Trading days	1,416	1,506	1,645	1,813									
Average Number of Round-Trips per pair	0,952	0,920	0,857	0,805									
Standard Deviation of Average Number of Round-Trips	1,064	1,042	1,021	0,997									
Average Number Pairs Open in 20days	1,913	4,772	9,537	18,969									
Standard Deviation of Average Number Pairs Open	0,099	0,161	0,281	0,472									
Panel B: Pairs that Convergence within N trading days													
Trading Horizon	Тор 2	Top 5	Тор10	Top 20									
5 Days	26,8%	26,9%	25,6%	25,5%									
10 Days	33,5%	33,2%	31,9%	31,6%									
20 Days	42,7%	41,3%	40,4%	40,9%									
40 Days	57,7%	53,3%	52,1%	51,8%									
60 Days	69,2%	65,4%	61,5%	60,7%									
120 Days	80,8%	74,6%	72,3%	72,1%									

Table 2
Summary Statistics for Stochastic Dominance Test

The table represents stochastic dominance test of the excess return portfolios. For definitions of pair trading refer to table 1. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). One day waiting estimations represents the implementation of the strategy the next business day. We implement three order stochastic dominance test. Stochastic dominance test examines the order of dominance between two assets according to their distribution. The test refers to the null hypothesis that pair profitability stochastically dominates S&P500 profitability

	Panel A: Event Day													
Pairs Portfolio	Тор 2	Top 5	Тор10	Тор 20										
1st Order	0,0000	0,0000	0,0000	0,0000										
2nd Order	0,0005	0,0000	0,0000	0,0000										
3rd Order	0,0042	0,0037	0,0096	0,0101										
	Panel B: One	Day Waiting	7											
Pairs Portfolio	<i>Top 2</i>	Top 5	Top10	Top 20										
1st Order	0,0000	0,0000	0,0000	0,0000										
2nd Order	0,0008	0,0000	0,0000	0,0000										
3rd Order	0,0043	0,0042	0,0050	0,0056										

Table 3
Summary Statistics of Daily Estimations of Baseline results

The table represents the summary statistics in percentage basis of the excess return portfolios. Due to different inception dates of the dataset, we initiate the calculations with the first 19 ETFs and we add each separate ETF by its own inception date. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. We open the trade when the divergence between the pairs exceed 0.5 standard deviations and if does not converge within the next 20 business days we stop the trade. One day waiting estimations represents the implementation of the strategy the next business day.

Pā	nnel A: Event day	/		
Pairs Portfolio	Top 2	<i>Top 5</i>	Top10	Top20
Terminal Wealth	10 204	20.041	12 706	9.065
	18,284	20,041	13,786	8,965
Mean Standard Davistion	0,097	0,098	0,085	0,071
Standard Deviation	0,887	0,667	0,551	0,454
Sharpe Ratio	0,109	0,147	0,155	0,156
Maximum	9,420	8,860	7,070	4,720
Minimum	-7,450	-7,780	-6,030	-4,080
Skewness	1,050	1,340	1,740	1,400
Kurtosis	13,700	26,800	28,600	16,700
Correlation with S&P500	0,065	0,069	0,101	0,146
Observations with Excess return>0	52,55%	54,14%	55,41%	55,73%
Mean of Excess Return >0	0,660	0,502	0,406	0,344
Mean of Excess Return <0	-0,543	-0,380	-0,317	-0,273
Mean of top ten excess return	5,778	4,729	4,099	3,347
Mean of bottom ten excess return	-3,504	-2,644	-0,020	-1,629
Panei	l B: One day wai	iting		
Pairs Portfolio	Тор 2	<i>Top 5</i>	Top10	Top20
Terminal Wealth	10,994	9,769	5,502	4,183
Mean	0,080	0,075	0,056	0,047
Standard Deviation	0,869	0,637	0,534	0,448
Sharpe Ratio	0,092	0,117	0,104	0,104
Maximum	6,150	6,300	7,060	4,650
Minimum	-7,440	-7,760	-6,860	-4,440
Skewness	0,637	0,470	0,822	0,938
Kurtosis	10,200	17,600	27,000	15,700

Correlation with S&P500	0,049	0,070	0,086	0,128
Observations with Excess return>0	51,91%	53,50%	53,18%	53,50%
Mean of Excess Return >0	0,647	0,476	0,387	0,330
Mean of Excess Return <0	-0,552	-0,389	-0,323	-0,279
Mean of top ten excess return	5,204	4,035	3,657	3,038
Mean of bottom ten excess return	-3,582	-2,798	-2,329	-1,957

Table 4
Summary Statistics of Relative Comparison between Two Trading Horizons

The table represents the summary statistics in percentage basis of the excess return portfolios. Due to different inception dates of our dataset, we initiate the calculations with the first 19 ETFs and we add each separate ETF by its own inception date. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. We open the trade when the divergence between the pairs exceed 0.5 standard deviations, and if does not converge within the selected trading horizons we stop the trade. The selected trading horizons are 20 and 60 business days respectively. The implementation of the strategy occurs one day after the divergence.

Trading Horizon		20 (	days					
Pairs Portfolio	<i>Top 2</i>	Top 5	Тор10	Top20	Тор 2	Top 5	Top10	Top20
Tarminal Waalth	10.004	0.760	E E02	4 102	E 744	2 261	2 471	2 200
Terminal Wealth	10,994	9,769	5,502	4,183	5,744	3,361	2,471	2,298
Mean	0,080	0,075	0,056	0,047	0,059	0,040	0,030	0,028
Standard Deviation	0,869	0,637	0,534	0,448	0,814	0,590	0,468	0,432
Sharpe Ratio	0,092	0,117	0,104	0,104	0,072	0,068	0,064	0,064
Maximum	6,150	6,300	7,060	4,650	6,820	3,110	2,580	3,090
Minimum	-7,440	-7,760	-6,860	-4,440	-3,250	-3,340	-2,360	-3,130
Skewness	0,637	0,470	0,822	0,938	53,500	15,400	6,350	24,800
Kurtosis	10,200	17,600	27,000	15,700	7,340	5,310	4,790	7,740
Correlation with S&P500	0,049	0,070	0,086	0,128	0,028	0,064	0,051	0,134
Observations with Excess return>0	51,91%	53,50%	53,18%	53,50%	50,96%	52,87%	51,91%	51,59%
Mean of Excess Return >0	0,647	0,476	0,387	0,330	0,624	0,447	0,361	0,327
Mean of Excess Return <0	-0,552	-0,389	-0,323	-0,279	-0,543	-0,419	-0,329	-0,294
Mean of top ten excess return	5,204	4,035	3,657	3,038	4,231	2,564	1,882	2,177
Mean of bottom ten excess return	-3,582	-2,798	-2,329	-1,957	-2,933	-2,270	-1,711	-1,949

Table 5
Summary Statistics of Daily Estimations between Large vs. Small Capitalization Portfolios

The table represents the summary statistics in percentage basis of the excess return distribution including the segmentation of the data set into two portfolios according to their capitalization: The first portfolio includes the first 50% of the sample with the larger capitalization and the supplementary 50% included in the second portfolio. Due to different inception dates of the our dataset, we initiate the calculations with the first 19 ETFs and we add each separate ETF by its own inception date. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. We open the trade when the divergence between the pairs exceed 0.5 standard deviations, and if does not converge within the next 20 business days we stop the trade. The implementation of the strategy occurs the next business day after the event of divergence occurs

	Large	Capitaliz	zation Po	ortfolio	Small Capitalization Portfolio					
Pairs Portfolio	<i>Top 2</i>	Top 5	Top10	Top 20	Top 2	Top 5	Top10	Top 20		
Terminal Wealth	4,352	3,511	2,301	2,000	4,766	3,197	2,038	1,873		
Mean	0,052	0,043	0,029	0,024	0,053	0,039	0,024	0,021		
Standard Deviation	1,010	0,785	0,667	0,647	0,829	0,595	0,517	0,447		
Sharpe Ratio	0,051	0,055	0,043	0,037	0,064	0,065	0,046	0,047		
Maximum	8,300	7,940	6,260	4,790	4,400	2,940	3,340	2,620		
Minimum	-5,810	-5,050	-4,740	-4,190	-7,200	-2,660	-2,320	-1,980		
Skewness	0,385	0,934	0,679	0,525	0,009	0,020	0,133	0,183		
Kurtosis	7,260	12,100	11,000	8,700	7,180	4,690	5,280	5,340		
Correlation with S&P500	-0,022	0,037	0,066	0,112	0,094	0,110	0,135	0,178		
Observations with Excess return>0	50,32%	50,32%	50,96%	51,27%	50,96%	53,18%	51,59%	51,91%		
Mean of Excess Return >0	0,767	0,579	0,485	0,466	0,628	0,448	0,393	0,338		
Mean of Excess Return <0	-0,693	-0,504	-0,444	-0,440	-0,565	-0,427	-0,369	-0,320		
Mean of top ten excess return	5,004	5,078	3,966	3,690	3,590	2,327	2,307	2,061		
Mean of bottom ten excess return	-4,222	-3,128	-2,943	-2,698	-3,614	-2,225	-1,944	-1,698		

Table 6
Summary Statistics of Daily Estimations of Developed vs. Emerging Countries

The table represents the summary statistics in percentage basis of the excess return distribution including the segmentation of the data set into two different subsets: Developed and Emerging markets. Due to different inception dates of the dataset, we initiate the calculations for developed markets by its own inception date and we add additional ETFs based on developed markets by the inception date. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). For emerging markets, we initiate the calculations, at June, 20 2000 where the last ETF on emerging market incepted (2.050 observations). The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. We open the trade when the divergence between the pairs exceed 0.5 standard deviations, and if does not converge within the next 20 business days we stop the trade. The implementation of the strategy occurs the next business day that the event of divergence occurs

	Emer	ging Cou	ıntries	Developed Countries						
Pairs Portfolio	Top 2	Top 5	Top 10	Top 2	Top 5	Top 10	Top 20			
Mean	0,063	0,050	0,764	0,069	0,056	0,049	0,047			
Standard Deviation	1,320	1,060	0,709	0,842	0,603	0,486	0,415			
Sharpe Ratio	0,048	0,048	1,078	0,082	0,093	0,100	0,113			
Maximum	6,890	8,050	4,960	6,050	3,500	2,580	3,050			
Minimum	-5,710	-4,620	0,001	-4,480	-2,900	-1,900	-2,020			
Skewness	0,225	0,813	1,880	0,386	0,385	0,206	0,341			
Kurtosis	6,050	9,070	8,190	7,710	5,670	4,900	6,060			
Correlation with S&P500	0,075	0,077	0,061	0,066	0,087	0,107	0,129			
Observations with Excess return>0	51,71%	49,76%	50,73%	52,55%	52,23%	52,55%	53,18%			
Mean of Excess Return >0	0,983	0,811	0,764	0,625	0,472	0,388	0,327			
Mean of Excess Return <0	-0,939	-0,694	-0,726	-0,565	-0,399	-0,329	-0,274			
Mean of top ten excess return	5,886	5,589	4,168	4,516	2,849	2,149	1,920			
Mean of bottom ten excess return	-5,079	-3,741	-3,489	-3,571	-2,281	-1,695	-1,681			

Table 7
Summary Statistics of baseline results according to Long and Short decomposition

The table represents the summary statistics in percentage basis of the excess return portfolios decomposed into long and short components. Due to different inception dates of the dataset, we initiate the calculations with the first 19 ETFs and we add each separate ETF by its own inception date. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. We open the trade when the divergence between the pairs exceed 0.5 standard deviations and if does not converge within the next 20 business days we stop the trade. One day waiting estimations represents the implementation of the strategy the next business day

Pairs Portfolio	То	p 2	To	p 5	То	p10	То	p20
	Long	Short	Long	Short	Long	Short	Long	Short
Terminal Wealth	0,940	10,722	1,506	6,424	1,438	3,810	1,249	3,464
Mean	0,005	0,082	0,016	0,062	0,013	0,044	0,008	0,041
Standard Deviation	1,160	1,150	0,751	0,781	0,519	0,560	0,437	0,472
Sharpe Ratio	0,004	0,072	0,021	0,080	0,025	0,079	0,018	0,086
Maximum	16,000	8,670	7,810	5,700	3,640	6,010	3,400	4,200
Minimum	-8,860	-9,160	-6,700	-7,610	-3,940	-4,570	-3,890	-4,060
Skewness	0,709	0,389	0,174	0,323	-0,246	0,911	-0,248	0,650
Kurtosis	21,700	12,100	16,700	14,500	9,960	15,700	12,900	15,700
Correlation with S&P500	0,364	0,379	0,380	0,439	0,441	0,531	0,437	0,503
Observations with Excess return>0	49,04%	51,27%	50,00%	53,18%	50,96%	52,23%	50,64%	53,18%
Mean of Excess Return >0	0,742	0,797	0,502	0,535	0,361	0,395	0,292	0,325
Mean of Excess Return <0	-0,755	-0,722	-0,473	-0,476	-0,352	-0,339	-0,286	-0,282
Mean of top ten excess return	7,319	6,834	4,710	4,915	2,623	3,707	2,468	3,033
Mean of bottom ten excess return	-6,316	-6,171	-4,639	-4,535	-2,883	-2,748	-2,553	-2,603

Table 8
Summary Statistics of Daily Estimations of Subsamples Portfolios

The table represents the summary statistics in percentage basis of the excess return portfolios. Due to different inception dates of the our dataset, we initiate the calculations with the first 19 ETFs and we add each separate ETF by its own inception date. The sample period is from April, 01 1996 to March, 11 2009 (3.140 observations). The sample period has been divided into 4 subsamples: The first period is from April, 01 1996 to December, 31 1999 (827 observations), the second period is from January, 1 2000 to December 31 2002 (631 observations). The third period is from January 1 2003 to December, 31 2005 (635 observations) and the last period is from January 1 2006, to March 11 2009 (681 observations). The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. We open the trade when the divergence between the pairs exceed 0.5 standard deviations, and if does not converge within the next 20 business days we stop the trade. One day waiting estimations represents the implementation of the strategy the next business day.

Sample Range:		1996:04	1-1999:1	12	2000:01-2002:12				2003:01-2005:12				2006:01-2009:03			
Pair Portfolio	Top 2	Top 5	Top10	Top20	Top 2	Top 5	Top10	Top20	Top 2	Top 5	Top10	Top20	Top 2	Top 5	Top10	Top20
Mean	0,133	0,093	0,077	0,044	0,061	0,087	0,081	0,083	-0,002	0,018	0,019	0,023	0,033	0,031	0,032	0,022
Standard Deviation	1,070	0,682	0,524	0,465	0,923	0,669	0,564	0,494	0,513	0,367	0,284	0,261	0,524	0,434	0,389	0,333
Sharpe ratio	0,124	0,137	0,146	0,094	0,066	0,130	0,144	0,167	-0,004	0,050	0,066	0,089	0,062	0,070	0,083	0,065
Maximum	6,050	3,230	2,340	3,560	4,220	3,760	2,450	1,730	2,070	1,360	1,210	1,030	4,790	3,580	3,140	2,300
Minimum	-3,740	-2,470	-1,480	-2,540	-3,350	-2,340	-1,510	-1,520	-3,200	-1,980	-0,961	-0,817	-1,940	-1,820	-1,330	-1,300
Skewness	0,457	0,231	0,189	0,445	0,351	0,264	0,337	0,154	-0,550	0,090	0,187	0,297	1,390	1,610	1,350	0,988
Kurtosis	5,540	3,910	3,470	7,910	5,510	4,710	3,880	3,630	6,510	5,200	4,630	3,650	15,000	15,300	12,600	9,650
Correlation with S&P500	0,050	0,014	0,007	0,042	0,203	0,185	0,201	0,253	0,045	0,047	0,053	0,057	0,183	0,155	0,210	0,190
Observations with Excess return>0	52,36%	54,66%	54,17%	53,81%	51,35%	55,31%	55,63%	54,99%	49,13%	51,34%	49,92%	52,28%	50,37%	51,84%	52,13%	52,72%
Mean of Excess Return >0	0,896	0,575	0,454	0,368	0,718	0,547	0,464	0,426	0,378	0,283	0,220	0,199	0,381	0,310	0,282	0,240
Mean of Excess Return <0	-0,749	-0,490	-0,369	-0,334	-0,648	-0,482	-0,398	-0,337	-0,379	-0,262	-0,201	-0,176	-0,329	-0,271	-0,241	-0,223
Mean of top ten excess return	3,851	2,201	1,562	1,605	3,267	2,146	1,840	1,527	1,345	1,150	0,889	0,737	2,069	1,920	1,736	1,339
Mean of bottom ten excess return	-2,867	-1,755	-1,320	-1,233	-2,602	-1,656	-1,253	-1,238	-1,731	-1,031	-0,812	-0,556	2,069	-1,198	-1,045	-0,923

Table 9
Profitability of Pair Trading Strategies

The table represents the results of monthly excess log returns from pair trading portfolios where the independent variables are 6 risk factors as represented by Fama and French. The implementation of the strategy occurs the next business day of the divergence and the trading horizon is constant 20 days. Daily returns are compounded to calculate monthly returns. The independent variables are: Value weighted market excess return (MARKET), a size portfolio based on small equities minus big equities (SMB), a book-to market portfolio of high minus low stocks (HML), a portfolio of year long winners minus year long losers (MOMENTUM). The corresponding p-values are reported for each separate variable and statistics are corrected for autocorrelation and heteroscedasticity using the Newey-West estimator with 4 lags. The sample period is from September 1996 to February 2009. The p-values and R<sup>2</sup> from each time-series regression are reported in nominal form.

Trading Horizon		20	days				60	days	
Monthly Pairs Portfolio	Top 2	<i>Top 5</i>	Тор 10	Top 20	_	Top 2	Top 5	Тор 10	Top 20
Intercept	0,016	0,016	0,012	0,009		0,012	0,009	0,007	0,006
Market	0,000 -0,049	0,000 0,004	0,000 -0,014	0,000 -0,019		0,004 -0,068	0,001 -0,005	0,000 -0,012	0,000 0,010
HML	0,454 -0,206	0,949 -0,183	0,763 -0,188	0,660 -0,107		0,540 -0,248	0,941 -0,108	0,727 -0,097	0,805 -0,091
TIME	0,005	0,008	0,001	0,047		0,023	0,103	0,041	0,035
SMB	-0,031 0,817	-0,031 0,708	0,048 0,429	0,038 0,500		-0,031 0,778	0,054 0,335	0,021 0,568	-0,013 0,724
Momentum	0,076	0,074	0,025	0,059		0,042	0,012	-0,001	-0,006
	0,211	0,157	0,527	0,130		0,410	0,739	0,950	0,821
<i>Observations</i> R <sup>2</sup>	150 0,039	150 0,062	150 0,115	150 0,086		150 0,049	150 0,046	150 0,050	150 0,047

 $Table\ 11$  Regression of Monthly Returns of the Subsamples Estimations

is constant 20days. Daily returns are compounded to calculate monthly returns. The independent variables are: the value weighted market excess return (MARKET), a size portfolio based on small equities minus big equities (SMB), a book-to-market portfolio of high minus low stocks (HML), a portfolio of year long winners minus a year long using Newey-West estimator with 3 lags. The p-values and R<sup>2</sup> are reported in nominal form. The sample period has been divided into 4 subsamples. losers(LONG TERM REVERSAL). The corresponding p-values are reported for each separate variable and statistics are corrected for autocorrelation and heteroscedasticity losers (MOMENTUM), a portfolio of last month losers minus last month winners (SHORT TERM REVERSAL) and finally a portfolio of 4 year long winners minus 4 year long variables are 6 risk factors as represented by Fama and French. The implementation of the strategy occurs the next business day of the divergence and the trading horizon The table represents the results of monthly excess return from pair trading portfolios segment by regions of emerging and developed markets where the independent

Period:		1996:04	1996:04-1999:12	,		2000:01	2000:01-2002:12	,		2003:01	2003:01-2005:12			2006:01-2009:02	N <sub>3</sub>	20.600
Pair Portfolio	Top 2	Top 5	Tap10 Tap20		Top 2	Top 5		Тор10 Тор20	Tap 2	Top 5	Top10 Top20 Top2 Top5 Top10 Top20	Top20	Top 2	Top 5		Tap10
Intercept	0.024	0.017	0.017	0,011	0.010	0.016	0.019	0.024	-0.005	0.002	0.003	0.003	0.004	0.004		0.006
	0.081	0.078	0.003	0.016	0.205	0.068	0.003	0.000	0.263	0.347	0.221	0.307	0.338	0.126	_	0.009
Market	0.024	0.018	0.030	0.041	0.101	0.204	0.129	0.256	0.574	0.302	0.214	0.092	-0.167	-0.127	T	-0.077
	0.924	0.919	0.795	0.715	0.593	0.150	0.262	0.055	0.041	0.049	0.114	0.414	0.341	0.422	_	0.262
IME	-0.180	-0.215	0.006	0.047	0.020	0.210	0.019	0.031	-0.051	-0.181	-0.053	0.121	-0.089		Ь	-0.126
	0.733	0.506	0.979	0.827	0.921	0.247	0.876	0.789	0.821	0.462	0.718	0.390		0.198	0	0.138
SMB	-0.473	-0.057	0.144	0.148	0.016	0.085	-0.009	-0.071	-0.815	-0.325	-0.291	-0.082	-0.106		6	-0.245
	0.250	0.833	0.410	0.311	0.945	0.539	0.936	0.436	0.062	0.216	0.093	0.527	0.650	0.561	0	0.067
Long Term Reversal	0.282	-0.006	-0.201	-0.333	0.225	-0.042	-0.041	-0.271	-0.536	-0.078	0.029	0.096	0.222	0.242	0	0.070
	0.677	0.989	0.397	0.089	0.412	0.803	0.798	0.066	0.063	0.640	0.843	0.524	0.266	0.181	0	0.413
Short Term Reversal	-0.030	0.041	-0.054	-0.069	0.057	0.028	-0.013	-0.067	0.160	0.125	0.172	0.043	0.102	0.114	0	0.078
	0.919	0.845	0.685	0.519	0.540	0.698	0.799	0.130	0.581	0.508	0.189	0.684	0.514	0.439	0	0.186
Momentum	-0.125	-0.047	-0.059	-0.032	-0.129	-0.023	0.002	0.104	0.238	0.096	0.052	-0.013	0.143	0.155	0	0.030
	0.674	0.742	0.571	0.726	0.209	0.605	0.975	0.072	0.279	0.565	0.711	0.895	0.248	0.190	0	0.656
Observations	40	40	40	40	31	31	31	31	31	31	31	31	33	ಜ		8 8
R <sub>2</sub>	0.053	0.044	0.064	0.125	0.138	0.129	0.079	0.320	0.315	0.143	0.182	0.120	0.192	0.230	0	0.289

Table 11

Profitability of Pair Trading between Developed and Emerging Countries

The table represents the results of monthly excess return from pair trading portfolios segment by regions of emerging and developed markets where the independent variables are 6 risk factors as represented by Fama and French. The implementation of the strategy occurs the next business day of the divergence and the trading horizon is constant 20days. Daily returns are compounded to calculate monthly returns. The independent variables are: Value weighted market excess return (MARKET), a size portfolio based on small equities minus big equities (SMB), a book-to-market portfolio of high minus low stocks (HML), a portfolio of year long winners minus a year long losers (MOMENTUM). The corresponding p-values are reported for each separate variable and statistic are corrected for autocorrelation and heteroscedasticity using Newey-West estimator with 4 lags for developed and 3 lags for emerging markets. The sample period extended from September 1996 to February 2009. The p-values are estimated for a rolling window of and R<sup>2</sup> from each time-series regression are reported in nominal form.

	Eme	rging ma	arkets		evelope	ed marke	ts
Monthly Pairs Portfolio	<i>Top 2</i>	<i>Top 5</i>	Top 10	Top 2	Top 5	Тор 10	Top 20
Intercept	0,012	0,010	0,005	0,014	0,013	0,010	0,010
	0,037	0,025	0,146	0,000	0,000	0,000	0,000
Market	-0,345	-0,494	-0,419	-0,025	-0,015	-0,017	-0,022
	0,155	0,027	0,014	0,709	0,808	0,721	0,602
HML	-0,099	-0,184	0,006	-0,173	-0,250	-0,130	-0,075
	0,727	0,502	0,976	0,020	0,002	0,026	0,253
SMB	-0,011	0,024	0,028	-0,191	-0,096	0,045	-0,031
	0,953	0,911	0,877	0,088	0,136	0,424	0,546
Momentum	-0,214	-0,242	-0,276	0,063	-0,010	0,005	0,042
	0,118	0,002	0,002	0,269	0,784	0,824	0,175
Observations	98	98	98	150	150	150	150
$R^2$	0,060	0,166	0,170	0,046	0,088	0,075	0,037

Table 12
Profitability according to Market Capitalization

The table represents the results of monthly excess return from pair trading portfolios segment by regions of emerging and developed markets where the independent variables are 6 risk factors as represented by Fama and French. The implementation of the strategy occurs the next business day of the divergence and the trading horizon is constant 20days. Daily returns are compounded to calculate monthly returns. The independent variables are: the value weighted market excess return (MARKET), a size portfolio based on small equities minus big equities (SMB), a book-to-market portfolio of high minus low stocks (HML), a portfolio of year long winners minus a year long losers (MOMENTUM). The corresponding p-values are reported for each separate variable, and statistics are corrected for autocorrelation and heteroscedasticity using Newey-West estimator with 4 lags. The sample period extended from September 1996 to February 2009. The p-values and R<sup>2</sup> from each time-series regression are reported in nominal form.

	Larg	e Capital	ization Po	rtfolio	Sm	all Capita	alization Po	ortfolio
Monthly Pairs Portfolio	<i>Top 2</i>	Top 5	Тор 10	Top 20	Top 2	Top 5	Тор 10	Top 20
Intercept	0,013	0,009	0,005	0,005	0,010	0,008	0,005	0,005
·	0,000	0,000	0,001	0,001	0,018	0,016	0,033	0,055
Market	-0,005	0,043	0,081	0,021	0,000	-0,133	-0,061	-0,030
	0,943	0,405	0,044	0,527	0,999	0,175	0,265	0,584
HML	-0,276	-0,072	0,051	0,015	-0,068	-0,071	-0,011	-0,059
	0,000	0,250	0,237	0,711	0,490	0,559	0,897	0,526
SMB	-0,193	-0,175	-0,085	-0,066	0,250	0,027	0,032	0,036
	0,027	0,006	0,069	0,122	0,037	0,791	0,712	0,659
Momentum	-0,060	-0,014	-0,018	-0,055	0,027	0,065	0,072	-0,003
	0,096	0,775	0,571	0,063	0,789	0,323	0,196	0,952
Observations	150	150	150	150	150	150	150	150
R <sup>2</sup>	0,074	0,070	0,070	0,059	0,056	0,049	0,037	0,012

Table 13
Profitability of Pair Trading Strategy against to International Factors

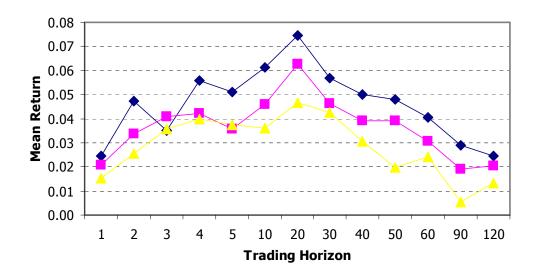
The table represents the results of monthly excess log returns from pair trading portfolios where the independent variables are 4 risk factors as represented by Fama and French constructed from international indices where the weighted is according to the weights of MSCI EAFE. The implementation of the strategy occurs the next business day of the divergence and the trading horizon is divided into two periods of 20 and 60 days. Daily returns are compounded to calculate monthly returns. The table reports loadings on 5 factors market excess return (MKT), bookto-market (B/M), cash earnings to price (CE/P). The corresponding p-values are reported for each separate regression and statistics are corrected for autocorrelation and heteroscedasticity using the Newey-West estimator with 4 lags. The sample period is from September 1996 to December 2007. The p-values and R<sup>2</sup> from each time-series regression are reported in nominal form.

Trading Horizon		20	days				6	0 days	
Monthly Pairs Portfolio	<i>Top 2</i>	Top 5	Тор 10	Top 20		Top 2	<i>Top 5</i>	Top 10	Top 20
Intercept	0,018	0,016	0,012	0,010	•	0,013	0,007	0,006	0,006
	0,000	0,000	0,000	0,000		0,009	0,010	0,001	0,000
Market	0,011	0,052	0,023	-0,011		0,102	0,117	0,036	0,041
	0,869	0,294	0,618	0,842		0,354	0,119	0,328	0,384
B/M	0,068	0,174	0,142	0,081		0,034	-0,131	-0,101	-0,122
	0,825	0,403	0,314	0,476		0,868	0,300	0,234	0,075
CE/P	-0,200	-0,184	-0,199	-0,124		-0,362	0,030	-0,016	0,014
	0,406	0,233	0,109	0,237		0,068	0,816	0,843	0,858
Observations	126	126	126	126		126	126	126	126
Observations R <sup>2</sup>	136 0,009	136 0,015	136 0,021	136 0,010		136 0,068	136 0,048	136 0,041	136 0,047

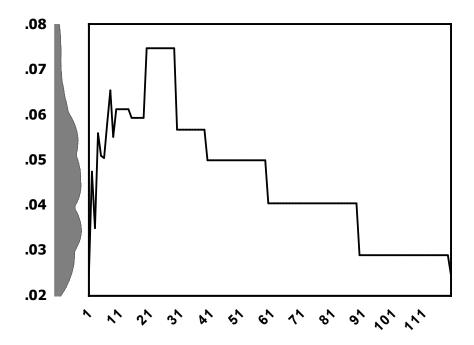
Regression of monthly returns of the subsamples International evidence

sample period has been divided into 4 subsamples: The first period is from April, 01 1996 to December, 31 1999, the second period is from January, 1 2000 to December 31 French constructed on international indices. The sample period is from April, 01 1996 to December, 2007. Daily returns are compounded to calculate monthly returns. The book-to-market (B/M), cash earnings to price (CE/P), earnings-price (E/P), dividend yield (D/P) sorted by size next business day. International indices where the weighted is according to the weights of MSCI EAFE. The table reports loadings on 5 factors market excess return (MKT), deviations, and if does not converge within the next 20 business days we stop the trade. One day waiting estimations represents the implementation of the strategy the 2002. The third period extends from January 1 2003 to December, 31 2005 and the last period extended from January 1 2006, to December 2007. The "top n" represents the "n" best eligible ranked pairs according to the historical distance of their mean price. We open the trade when the divergence between the pairs exceed 0.5 standard The table represents the returns on monthly excess log returns form pair trading portfolios where the independent variables are 4 risk factors as represented by Fama and

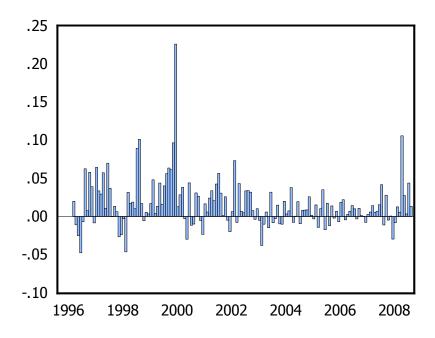
Observations R <sup>2</sup>	D/P	E/P	CE/Þ	в/М	Market	Intercept	Pair Portfolio	Period:
40 0.049	0.441 -0.108 0.873	0.240 0.383	0.599 -0.694	0.744 0.418	0.024 0.073	0.027	Тор 2	
40 0.114	0.371 -0.225 0.493	0.071 0.202	0.095 -0.592	0.647 0.521	0.023	0.019	Top 5	1996:04
40 0.064	0.727 0.014 0.963	0.131 0.048	0.387 -0.347	0.647 0.262	0.010	0.016	Тор 5 Тор10 Тор20	1996:04-1999:12
40 0.167	0.385 0.189 0.373	0.027	0.793 -0.416	0.123 0.047	0.075	0.008	Top20	2
31 0.077	0.377 -0.225 0.707	0.432 0.884	0.408 -0.819	0.453	0.078 0.142	0.011	Top 2	
31 0.137	0.235 0.006 0.984	0.327 0.804	0.802 -0.648	0.150 0.107	0.069	0.016	Top 2 Top 5 Top 10 Top 20	2000:01
31 0.111	0.892 0.272 0.267	0.890	0.450 -0.072	0.067	0.004	0.017	Top10	2000:01-2002:12
31 0.103	0.943 0.212 0.502	0.489	0.996 -0.232	0.084	0.000	0.020	Top20	
31 0.212	0.862 0.329 0.598	0.791	0.018	0.537	0.161 -0.147	0.010	Tap 2	
31 0.076	0.565 0.261 0.430	0.577 0.158	0.238 -0.166	0.704 -0.294	0.165 0.052	0.005	Tap 5	2003:01
31 0.199	0.276 0.497 0.101	0.253 0.196	0.273 -0.222	0.646 -0.183	0.263	0.003	Top10	-2005:12
31 0.189	0.630 0.446 0.024	0.404	0.781 -0.120	0.703	0.154 0.029	0.003	Top20	
34 0.377	0.247 0.523 0.010	0.306	0.170 0.484	0.780 0.382	0.198 -0.058	0.004	Tap 2	
34 0.589	0.052 0.547 0.013	0.130 -0.839	0.385	0.333	0.144 -0.166	0.004	Tap 5	2006:01
34 0.310	0.517 0.290 0.093	0.695 -0.113	0.561 -0.062	0.491 0.214	0.005	0.009	Top10 Top20 Top2 Top5 Top10 Top20	2006:01-2007:12
34 0.477	0.013 0.360 0.032	0.178 -0.341	0.622 0.157	0.900 0.149	0.650 -0.016	0.001	Top20	



**Figure 1:** The lines plot the distribution of mean returns of the best 5 eligible pairs according to different measures of standard deviations on the identification of the opportunities. During the formation period (120 days), the strategy is evaluating two price absolute differences according to three different scales of distance. For different k trading horizons, where k=1,...,120, we consider three scales of deviations, 0.5, 1.0 and 2.0 standard deviations. Blue line corresponds to the distribution of mean returns for 0.5 standard deviations, magenta corresponds to empirical distribution of 1.0 standard deviation, and gold corresponds to empirical distribution of 2.0 standards deviations. The execution of the strategy occurs one day after the divergence

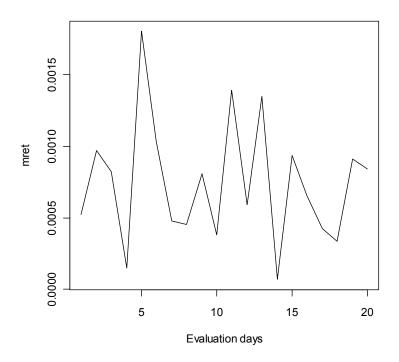


**Figure 2:** Distribution of Mean Returns according to different Time Exit Strategies. The testing period is between 1day and 120days. The mean returns are represented also from Kernel density on the left. The execution of the strategy occurs the next business after the divergence and the evidence have been applied to top 5 pairs. The grey bar on the left side of the plot represents Kernel Density.

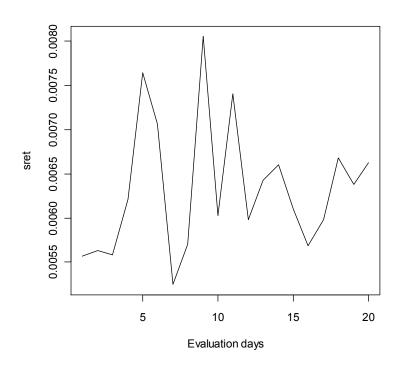


**Figure 3:** The line plots the distribution of the monthly Excess Return of Pair Trading Strategy for the top 5 eligible pairs. The trading period is extended from September 1996 to March 2009. The execution horizon is 20days. The strategy is implemented the next business day of the divergence day.

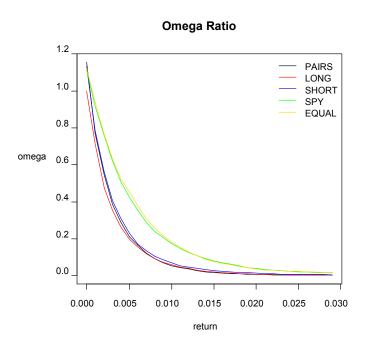
Panel A: Mean return distribution during the 20days execution period.



Panel B: Distribution of standard deviation during the 20 days execution period.

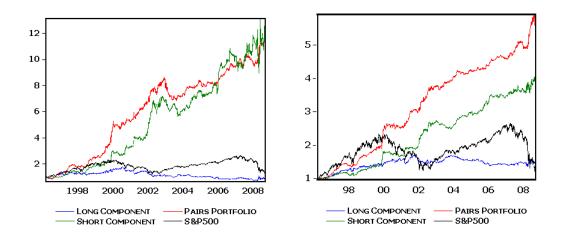


**Figure 4:** Panel A and Panel B plots the distribution of mean returns and standard deviation of top 5 eligible pairs of pairs trading strategy. The execution horizon is 20 days. The implementation of the strategy occurs one day after the divergence.



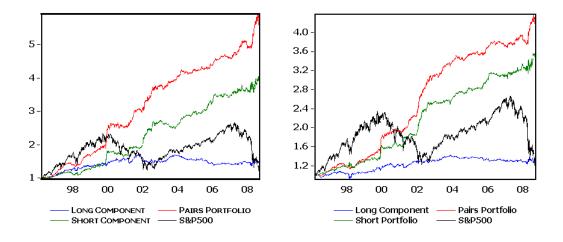
**Figure 5:** The plot exhibits the daily Omega Ratio produce with the best 2 eligible pairs. We set as r threshold 0 and we are considering the positive returns. In the plot, we are representing pairs trading strategy, and long and short component separately. For the relative comparison, we represent S&P500 and equally weighted portfolio.

Panel B: Top5 Pairs Portfolio



Panel C: Top10 Pairs Portfolio

Panel D: Top20 Pairs Portfolio



**Figure 6:** Presents daily terminal wealth of baseline results for different number of eligible pairs in the respective panels (A:2pairs, B:5pairs, C:10pairs, D:20pairs). In the figures, we represent in align with the terminal wealth, long and short component and S&P500 for the relative comparison.